

Applications of DSP

Project 2

**UNIVERSITY OF CENTRAL FLORIDA
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Project 2

Question 1:

Part 1 a

Given,

- I. $H(j\omega)$ is a 4th order low pass Chebyshev function
- II. $A_p=0.5$ dB
- III. $f_l=2$ kHz
- IV. $f_s=10$ kHz

obtain $H_D(z)$.

Solution: Using low pass Chebyshev prototype that is available in MATLAB (`cheb1ap`) in the impulse invariant method we obtain the following output in the console window:

```
-----Answer to question 1-----
1a) _____ Hd(z) when f1=2KHz fs=10KHz _____

ans =

-9.095e-17 s^3 + 0.09261 s^2 + 0.2321 s + 0.04396
-----
s^4 - 1.479 s^3 + 1.46 s^2 - 0.8131 s + 0.2221

Continuous-time transfer function.

poles(1)

z1 =

1.0e+15 *

1.0183
-0.0000
-0.0000

p1 =

0.2323 + 0.7679i
0.2323 - 0.7679i
0.5071 + 0.2965i
0.5071 - 0.2965i
```

Part 1 b:

Poles of $H_D(z)$

In Impulse invariant method, the transfer function in the analog domain is given by:

$$H_A(s) = \sum_{i=1}^N \left(\frac{A_i}{s - p_i} \right)$$

$$H_A(s) \leftrightarrow h_A(t)$$

Now, $h_D(t) = h_A(nT)$, where, T is the sampling period.

$$H_D(z) = \sum_{i=1}^N A_i * \frac{z}{z - e^{p_i T}}$$

We also know that, If our poles are inside the unit circle then our system is stable. From the console of the MATLAB we get The Magnitude of the poles:

```
_____1b_____
the magnitude of each pole

p1_1 =
    0.8022

p1_2 =
    0.8022

p1_3 =
    0.5874

p1_4 =
    0.5874
```

Also we get the Angles of the poles:

the angle of each pole

A1_1 =

73.1702

A1_2 =

-73.1702

A1_3 =

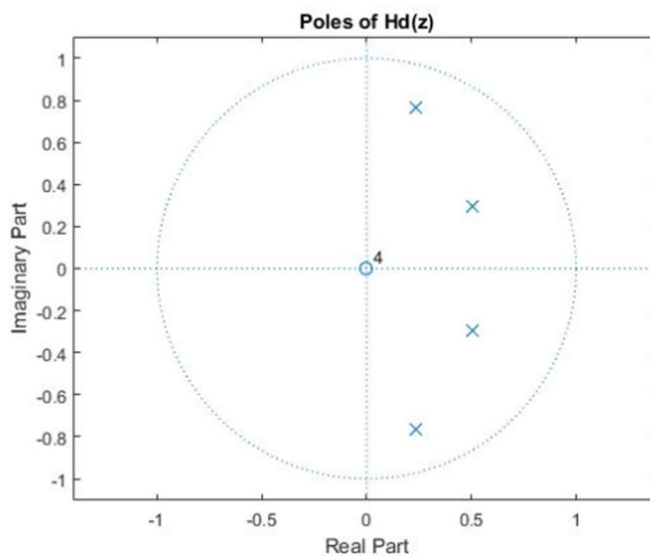
30.3081

A1_4 =

-30.3081

Here, $|Z_p|$ max is 0.8022.

Pole Zero locations are mapped below :

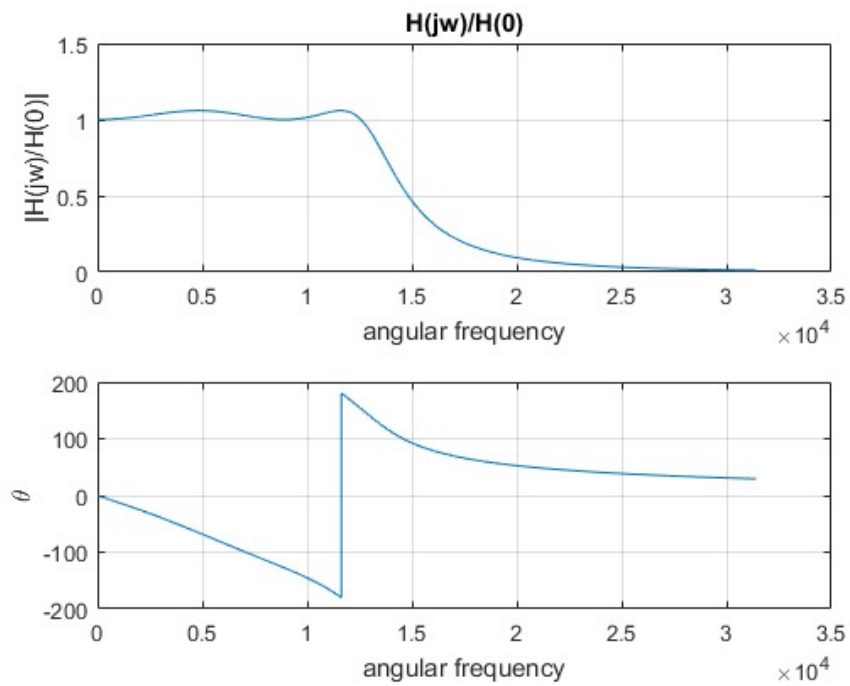


As all the poles are inside the unit circle, the system is stable.

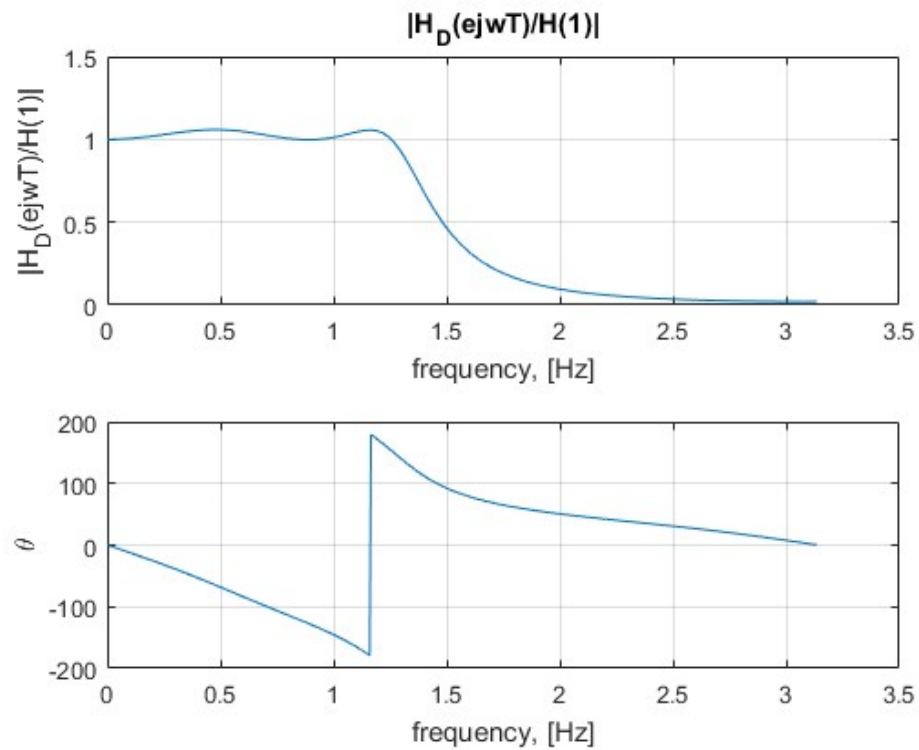
Part 1 c:

Here we need to plot The magnitude and phase of $\frac{H(jw)}{H(0)}$.

The Analog filter response is as given below:



The digital filter response is as given below:



Question 2:

Here, we repeat question 1 for $f_1=2\text{kHz}$ and $f_s=20\text{kHz}$. Then we compare $|Z_p|_{\max}$ in (2) and (1) as well as the approximation accuracy of $\frac{Hde^{j\omega t}}{Hd(1)}$ relative to $\frac{H(j\omega)}{H(0)}$, $|\omega| \leq \frac{\omega_s}{2}$

Console output:

```
-----Answer to question 2-----
2a Hd(z) when f1=2KHz fs=20KHz
ans =

-4.547e-17 s^3 + 0.007521 s^2 + 0.02436 s + 0.005167
-----
s^4 - 2.918 s^3 + 3.518 s^2 - 2.032 s + 0.4713

Continuous-time transfer function.

poles(2)

z3 =

1.0e+14 *

1.6538
-0.0000
-0.0000

p3 =

0.7192 + 0.5338i
0.7192 - 0.5338i
0.7398 + 0.2004i
0.7398 - 0.2004i
```

Part 2 b:

The Magnitude of the poles found from the console window:

$\frac{2b}{\text{the magnitude of each pole}}$

p2_1 =
0.8957

p2_2 =
0.8957

p2_3 =
0.7664

p2_4 =
0.7664

The Angle of the poles found from the console window:

the angle of each pole

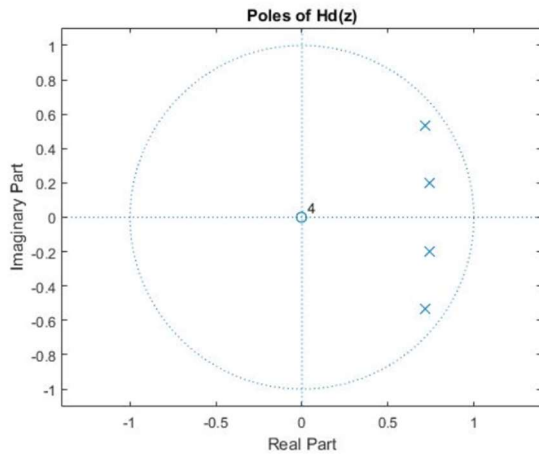
A2_1 =
36.5851

A2_2 =
-36.5851

A2_3 =
15.1541

A2_4 =
-15.1541

The pole-zero plot is as follows:



As all the poles are inside the unit circle and hence system is stable.

Part 2 c:

$|Z_p|_{\max}$ value from the console window:

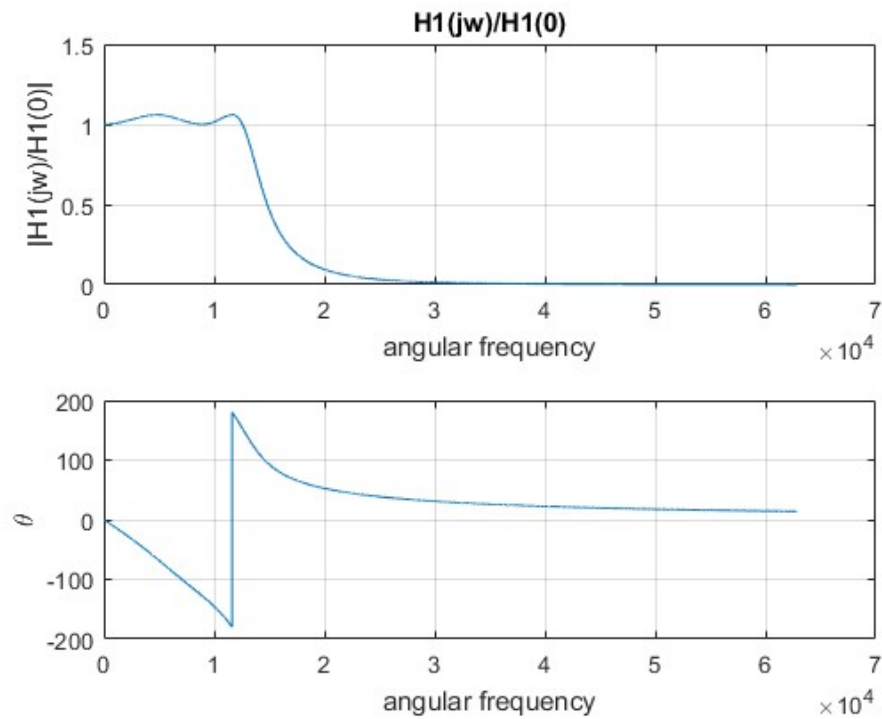
```
zp1max =  
0.8022
```

```
zp2max =  
0.8957
```

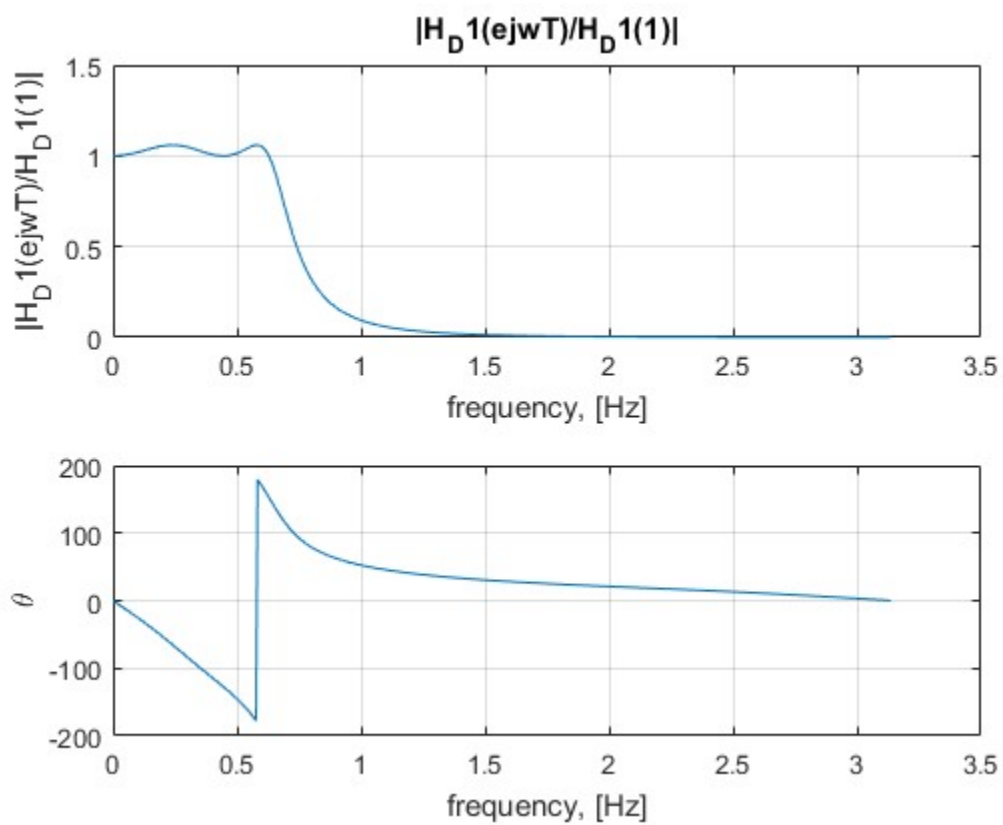
Now comparing the $|Z_p|_{\max}$ in both the questions, we see that we have $P1 = 0.8022$ and $P2 = 0.8957$. So the $|Z_p|_{\max}$ in part 2 is larger.

Coming to the part where we have to compare the approximation accuracy of $H_D(e^{j\omega t})/H_D(1)$ relative to $H(j\omega)/H(0)$.

The Analog filter response is:



The Digital filter response is:



Question 3:

Here, we repeat question 1 with $f_1=3\text{KHz}$ and $f_s=15\text{KHz}$.

The MATLAB console output showing the poles and zeros for this question is as follows:

```
-----Answer to question 3-----
3a _____ Hd(z) when f1=3KHz fs=15KHz _____

ans =

-6.063e-17 s^3 + 0.09261 s^2 + 0.2321 s + 0.04396
-----
s^4 - 1.479 s^3 + 1.46 s^2 - 0.8131 s + 0.2221

Continuous-time transfer function.

poles(3)

z5 =

1.0e+15 *

1.5274
-0.0000
-0.0000

p5 =

0.2323 + 0.7679i
0.2323 - 0.7679i
0.5071 + 0.2965i
0.5071 - 0.2965i
```

The Magnitude of the poles found from the console window:

the magnitude of each pole

```
p3_1 =  
0.8022
```

```
p3_2 =  
0.8022
```

```
p3_3 =  
0.5874
```

```
p3_4 =  
0.5874
```

The Angle of the poles found from the console window:

the angle of each pole

```
A3_1 =  
73.1702
```

```
A3_2 =  
-73.1702
```

```
A3_3 =  
30.3081
```

```
A3_4 =  
-30.3081
```

$|Z_p|$ max valus from the console window:

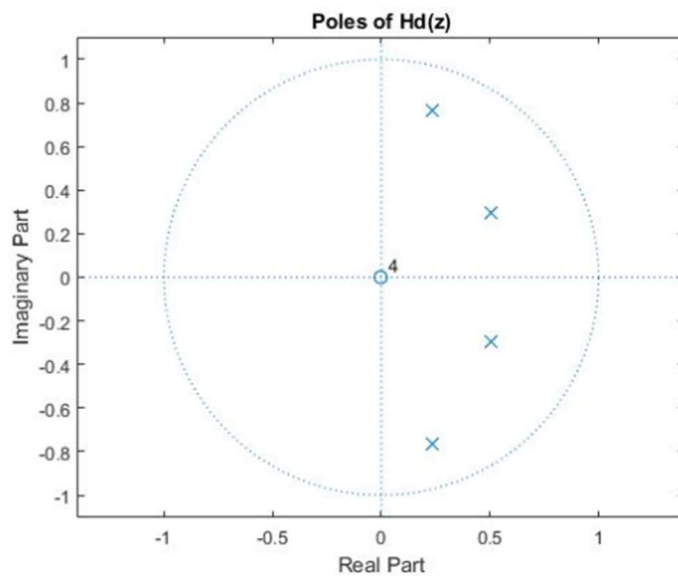
```

Zp1max =
    0.8022

Zp3max =
    0.8022

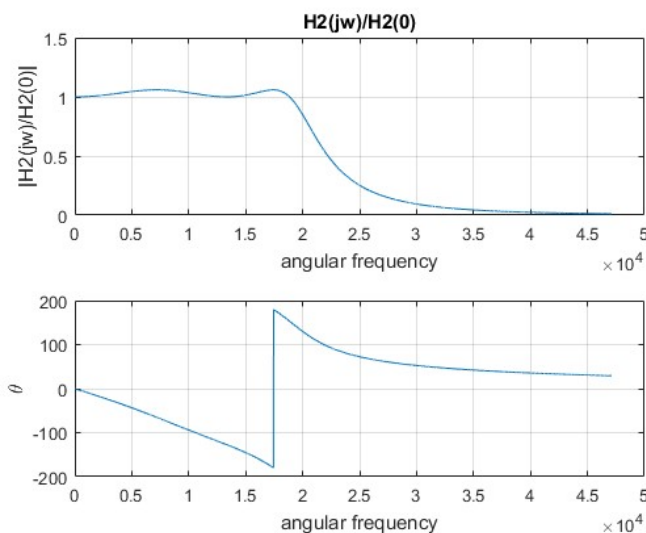
```

Comparing problem 1.b and this one, we get $|Z_p|_{\max}$ for 1.b = $|Z_p|_{\max}$ for 3. Because that the ratio of the passband frequency is equal to that of the sampling frequency, pole locations in question 1 and question 3 are same.

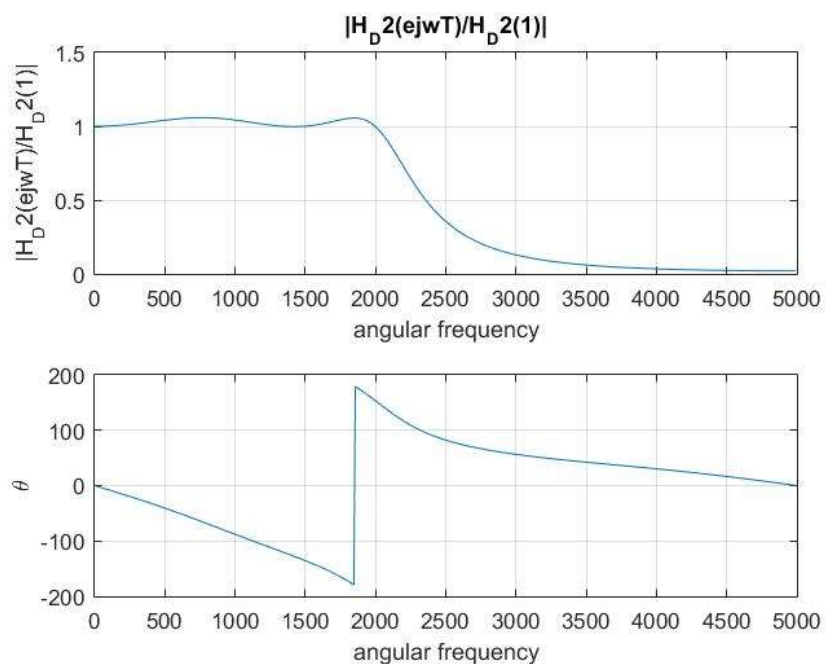


Since all the poles are inside the unit circle, the system is stable.

The Analog filter response is as follows:

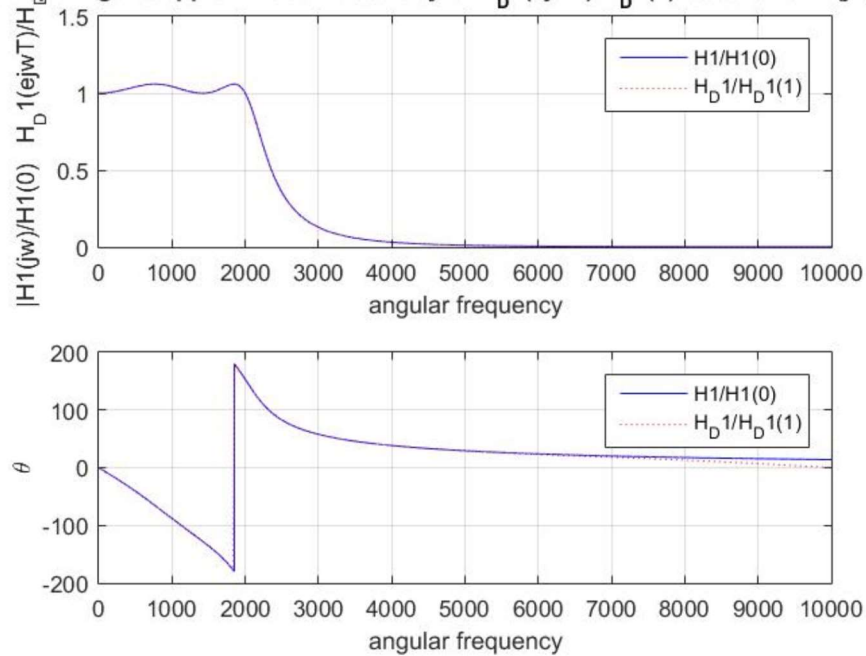


The Digital filter response is as follows:



Comparing the approximation accuracy

Comparing the approximation accuracy of $H_D 1(e^{j\omega T})/H_D 1(1)$ relative to $H_1(j\omega)/H_1(0)$



Question 4:

Here, we repeat question 2 with $f_1=4\text{KHz}$ and $f_s=40\text{KHz}$.

The console output is as follows:

```
-----Answer to question 4-----
4a Hd(z) for f1=4KHz fs=40KHz

ans =

2.274e-17 s^3 + 0.007521 s^2 + 0.02436 s + 0.005167
-----
s^4 - 2.918 s^3 + 3.518 s^2 - 2.032 s + 0.4713

Continuous-time transfer function.

poles(4)

z7 =

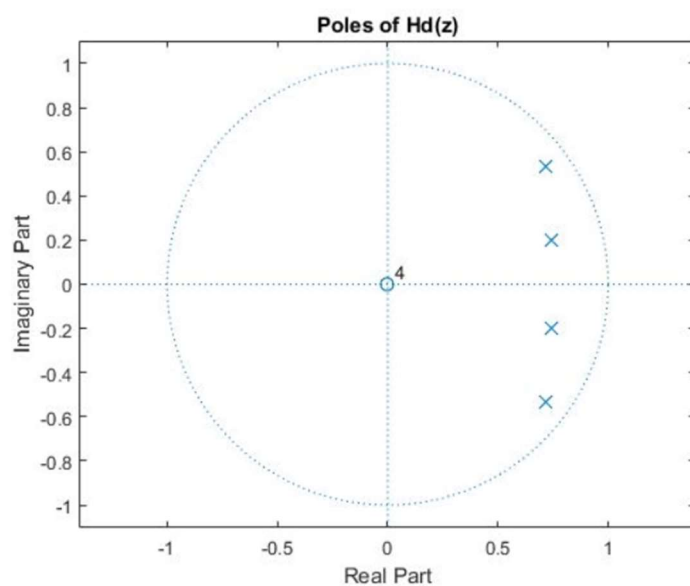
1.0e+14 *

-3.3076
-0.0000
-0.0000

p7 =

0.7192 + 0.5338i
0.7192 - 0.5338i
0.7398 + 0.2004i
0.7398 - 0.2004i
```

The pole locations are following:



Since all the poles are inside the unit circle, the system is stable.

The Magnitude of the poles found from the console window:

```
the magnitude of each pole
```

```
p4_1 =
```

```
0.8957
```

```
p4_2 =
```

```
0.8957
```

```
p4_3 =
```

```
0.7664
```

```
p4_4 =
```

```
0.7664
```

The Angle of the poles found from the console window:

```
the angle of each pole
```

```
A4_1 =
```

```
36.5851
```

```
A4_2 =
```

```
-36.5851
```

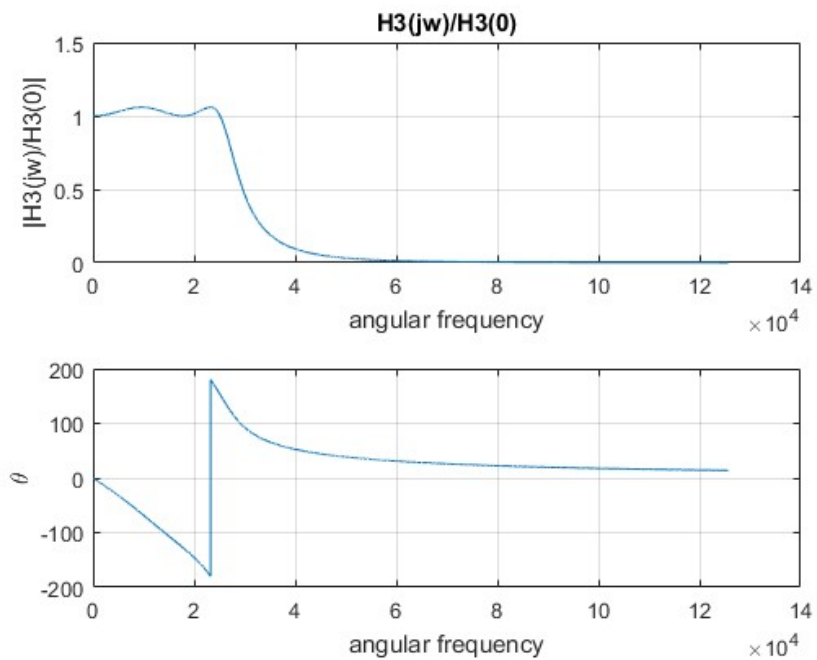
```
A4_3 =
```

```
15.1541
```

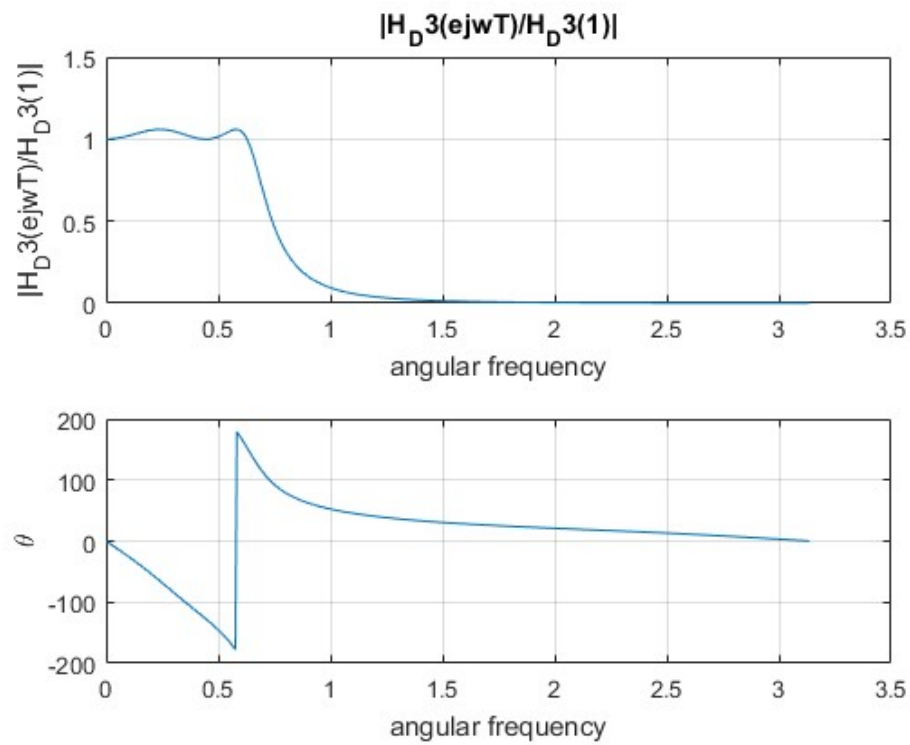
```
A4_4 =
```

```
-15.1541
```

The Analog filter response is as follows:

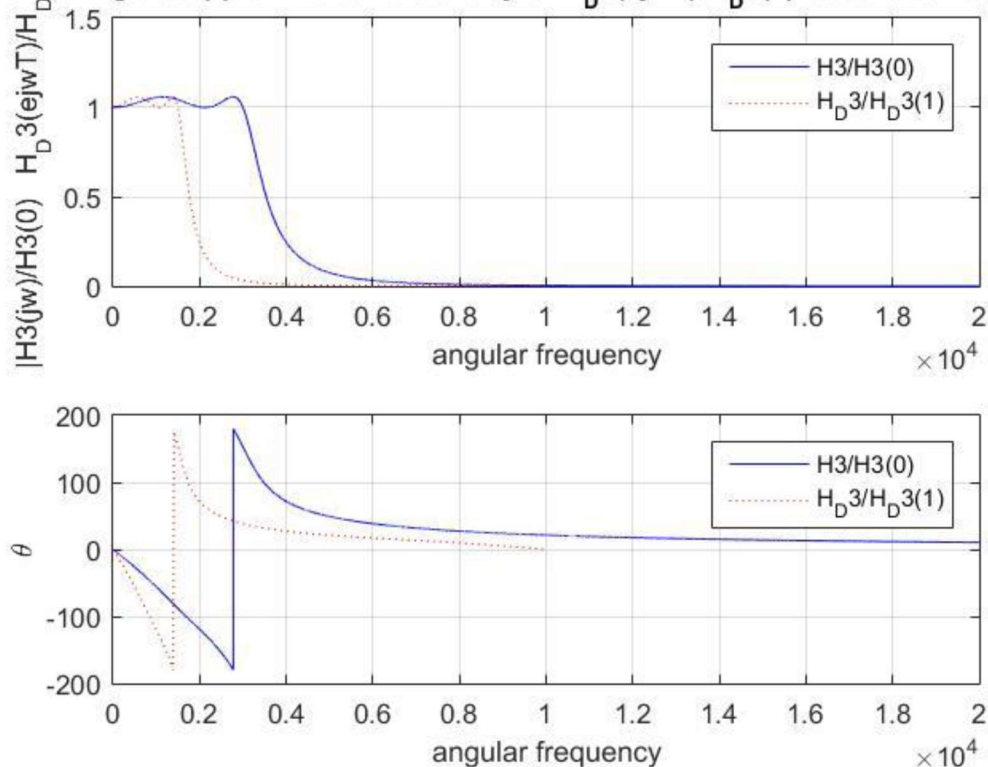


The Digital filter response is as follows:



Comparing the approximation accuracy of $HDe^{j\omega T}/H_D(1)$ relative to $H(j\omega)/H(0)$:

Comparing the approximation accuracy of $H_D^3(e^{j\omega T})/H_D^3(1)$ relative to $H_3(j\omega)/H_3(0)$



Question 5:

Here, we repeat question 1 using bilinear transformation method. We compute the new value of f_1 of $H_D(z)$ analytically.

Bilinear Transformation is used to map a transfer function from the analog to the digital domain. This maps from s-plane to z-plane by using the following transformation of s.

$$s = \frac{2(z-1)}{T(z+1)}$$

$$\omega_c = 2\pi f_s = 1.4 \times 10^4 \text{ rad/sec}$$

$$\begin{aligned} \Omega_c &= \frac{2}{T} \tan^{-1} \left(\frac{\omega_c T}{2} \right) \\ &= 1.2 \times 10^4 \text{ rad/sec} \end{aligned}$$

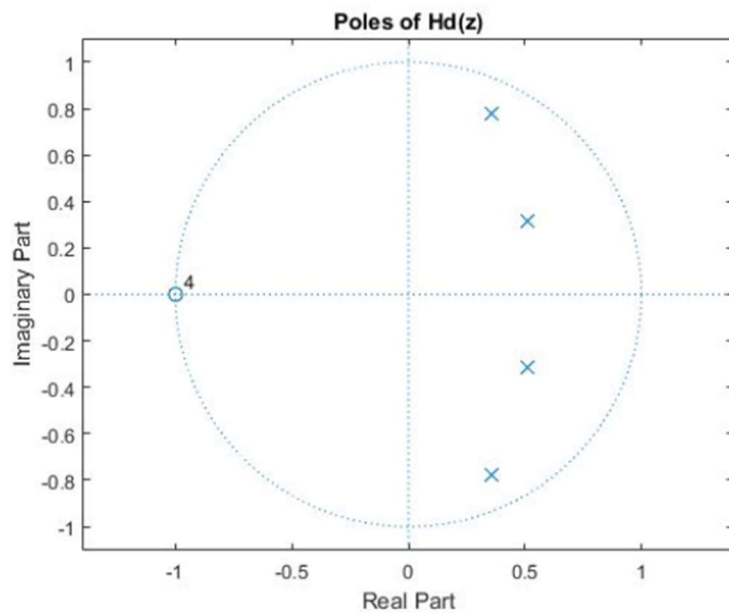
$$\text{So } f_1 = 1.9 \text{ kHz}$$

From MATLAB Console:

```
-----Answer to question 5-----  
_____ Hd(z) when fs=40KHz _____  
  
ans =  
  
0.02033 s^4 + 0.08131 s^3 + 0.122 s^2 + 0.08131 s + 0.02033  
-----  
s^4 - 1.735 s^3 + 1.822 s^2 - 1.009 s + 0.2661
```

Continuous-time transfer function.

The pole locations are following:



The Magnitude of the poles found from the console window:

the magnitude of each pole

```
p5_1 =  
0.8552
```

```
p5_2 =  
0.8552
```

```
p5_3 =  
0.6033
```

```
p5_4 =  
0.6033
```

The Angle of the poles found from the console window:

the angle of each pole

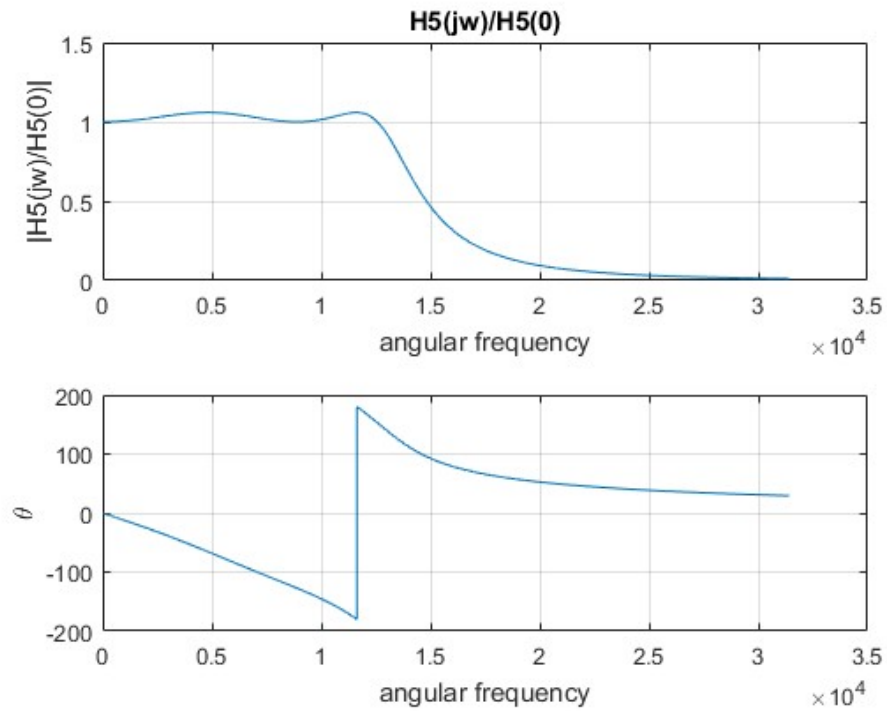
```
A5_1 =  
65.5688
```

```
A5_2 =  
-65.5688
```

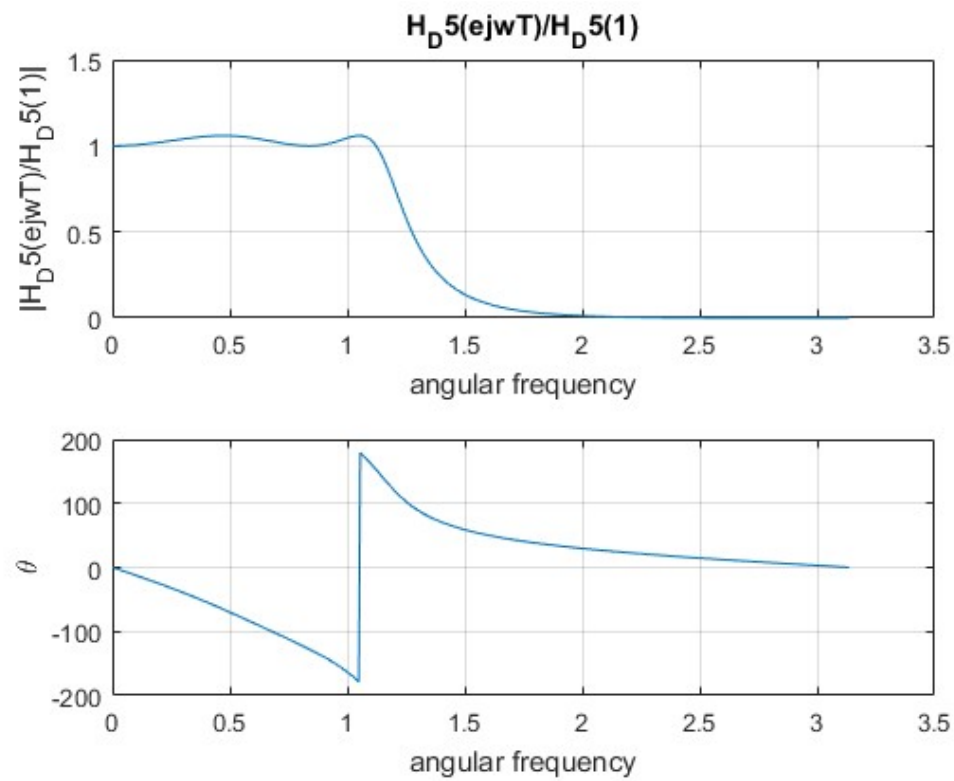
```
A5_3 =  
31.6162
```

```
A5_4 =  
-31.6162
```

The Analog filter response is as follows:



The Digital filter response is as follows:



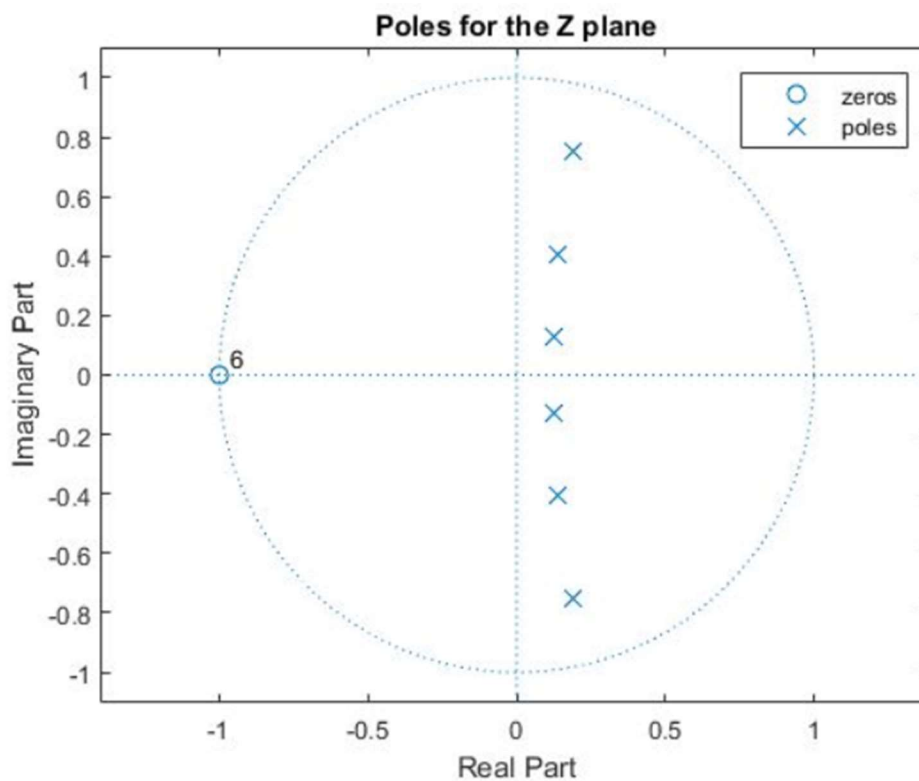
Question 6:

Here, We repeat question 1 for a 6th order HP Butterworth filter $H(j\omega)$ where $\omega_s = 4\omega_{3dB}$. We compute 3dB frequency for digital filter and compare with graph.

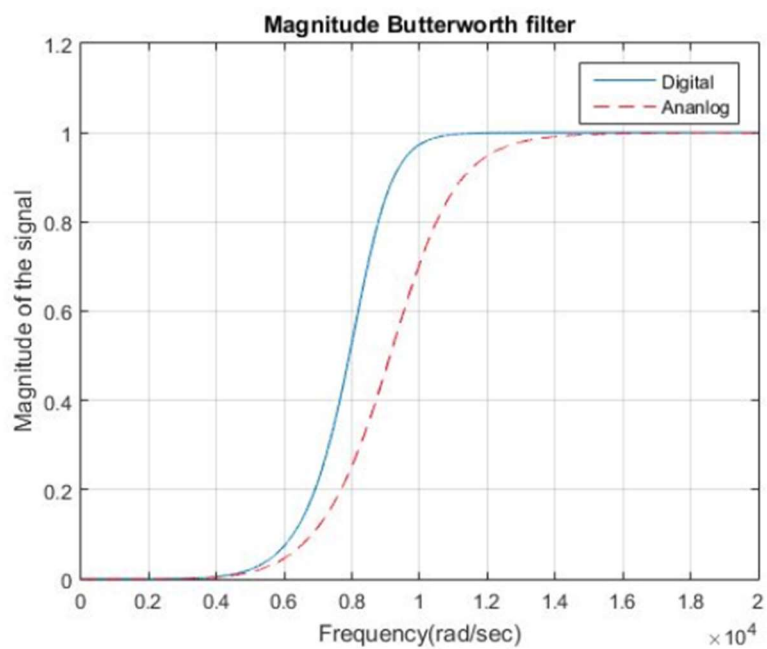
The console output is as follows:

```
H_bilinear =  
  
(- 4.524e-7 + 1.524i)/((6366.0*(2.0*z - 2.0))/(z + 1.0) + (7071.0 + 7071.0i)) +  
(- 2.285 - 1.319i)/((6366.0*(2.0*z - 2.0))/(z + 1.0) + (9659.0 - 2588.0i)) +  
(- 4.524e-7 - 1.524i)/((6366.0*(2.0*z - 2.0))/(z + 1.0) + (7071.0 - 7071.0i)) +  
(0.3536 - 0.2041i)/((6366.0*(2.0*z - 2.0))/(z + 1.0) + (2588.0 - 9659.0i)) +  
(- 2.285 + 1.319i)/((6366.0*(2.0*z - 2.0))/(z + 1.0) + (9659.0 + 2588.0i)) +  
(0.3536 + 0.2041i)/((6366.0*(2.0*z - 2.0))/(z + 1.0) + (2588.0 + 9659.0i))  
  
cutoff frequency: 8477.00 rad/seconds  
analytical cutoff frequency : 8476.89 rad/seconds
```

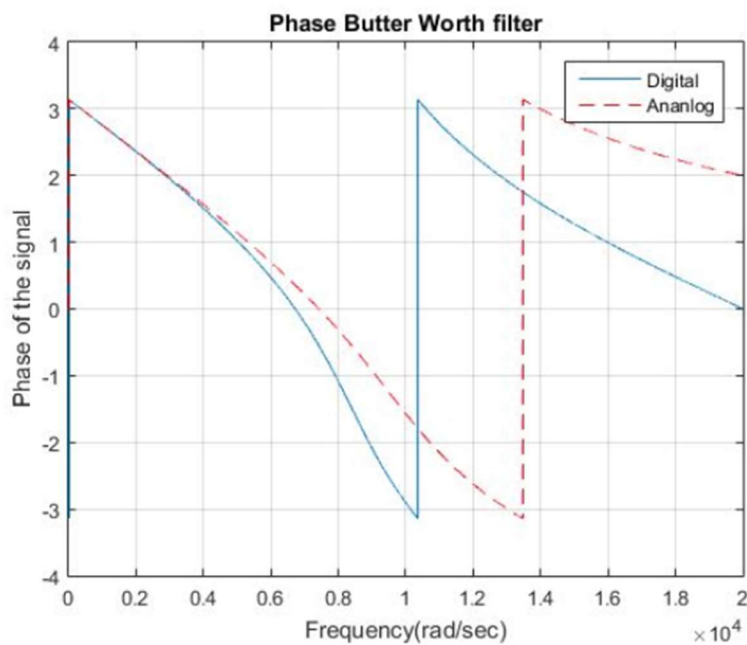
The pole zero plot is like the following:



Plot of the magnitude of the Butterworth filter:



Plot of the phase of the Butterworth filter:

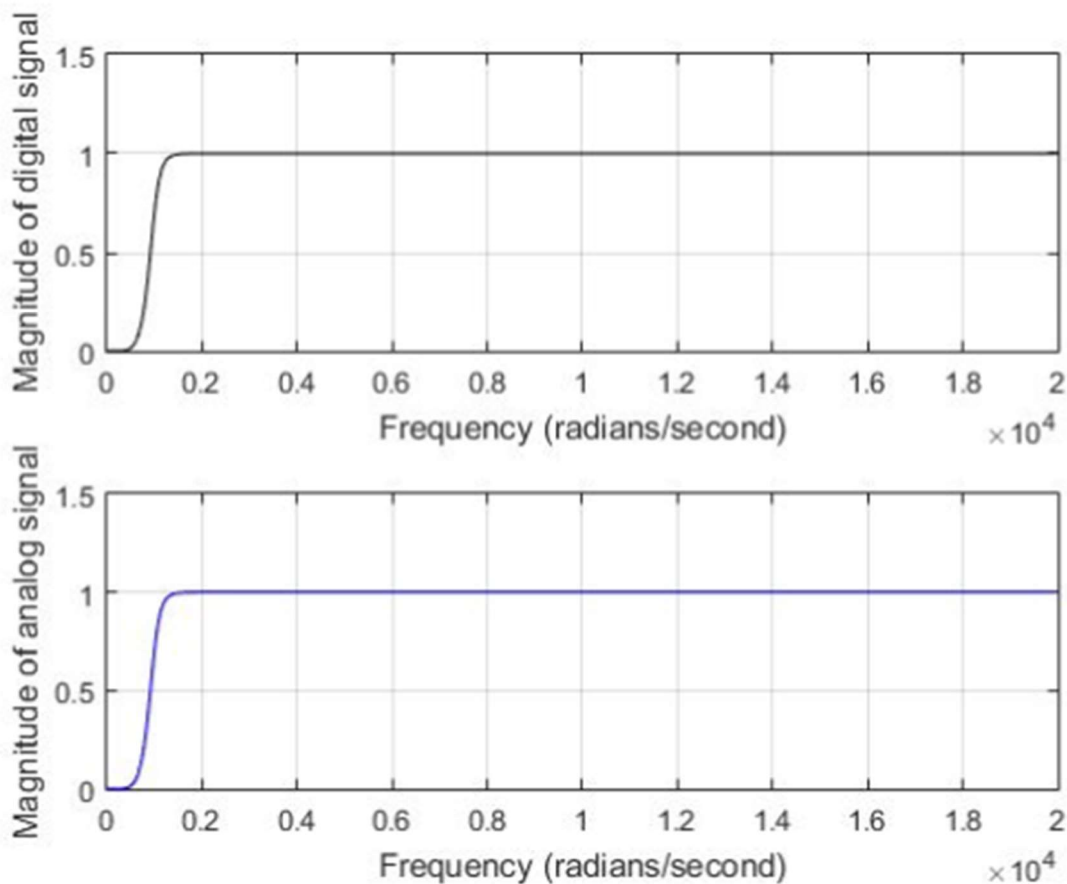


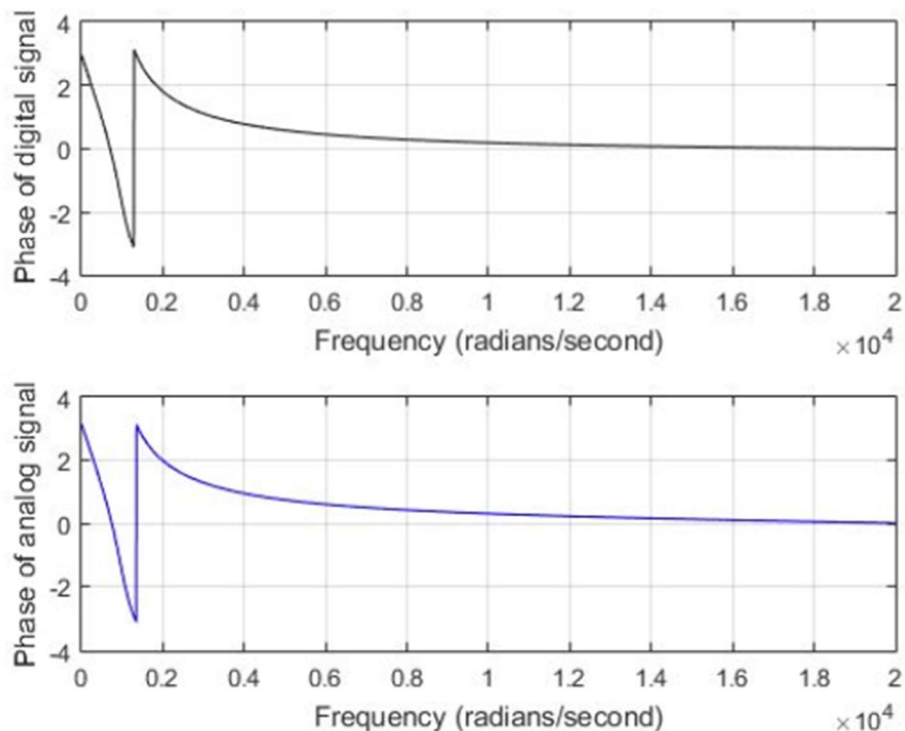
Question 7:

Here, we repeat 6 by prewarping the prototype to get the exact 3-dB frequency of the digital filter.

The continuous time filter frequency $\omega_a=0$ corresponds to the discrete time filter frequency $\omega_d=0$. The continuous time filter frequency $\omega_a=\pm\infty$ corresponds to the discrete time frequency $\omega_d=\pm(\pi T)$. This is called *frequency warping*. The continuous-time filter can be designed to compensate for this frequency warping by setting $\omega_a=2T \tan \omega_d T/2$ for every frequency specification that the designer has control over (such as corner frequency or center frequency). This is called *pre-warping* the filter design.

The MATLAB output is as follows:





Conclusion:

In this project we have worked on Chebyshev and Butterworth filters using MATLAB. Using Bilinear transformation method, we calculated the new value of f_1 . Then we warped to get the 3-db frequency of the digital filter.

Reference:

1. https://en.wikipedia.org/wiki/Butterworth_filter
2. <https://www.mathworks.com/>
3. https://en.wikipedia.org/wiki/Chebyshev_filter
4. https://en.wikipedia.org/wiki/Bilinear_transform
5. John G. Proakis, Dimitri K. Manolakis, Digital Signal Processing, Pearson, 4th edition

The following is the codes and plots of the entire project in MATLAB.

MATLAB Code

```
% ----- Applications of DSP -----
% -----Project 2 -----
%-----Submitted by-----
%-----Rajib Dey -----

clc
close all
clear all

f1=2000;
fs=10000;
fsp=0:0.1:fs/2;
w=2*pi*fsp;

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% 1(a)
[z,p,k]=cheblap(4,0.5);% low pass filter prototype
[b,a] = zp2tf(z,p,k); % % Convert to transfer function form
[b,a] = lp2lp(b,a,2*pi*f1);% analog low pass filter to low pass filter of
specified frequency
[bz,az]=impinvar(b,a,fs);% using impulse invariant method
disp('-----Answer to question 1-----')
disp ('1a) _____ Hd(z)when f1=2KHz fs=10KHz _____')
tf(bz,az)

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%1(b) poles of Hd(z)
disp ('poles(1)')
[z1,p1,k1] = tf2zp(bz,az)
disp ('_____1b_____')
disp ('the magnitude of each pole')
p1_1 = abs(p1(1))
p1_2 = abs(p1(2))
p1_3 = abs(p1(3))
p1_4 = abs(p1(4))
zplane(z,p)
disp ('the angle of each pole')
A1_1= angle(p1(1))*57.2958
A1_2=angle(p1(2))*57.2958
A1_3=angle(p1(3))*57.2958
A1_4=angle(p1(4))*57.2958

%1(c) magnitude and phase plot for |H(jw)/H(0)|

H = freqs(b,a,w);

figure(11);
subplot(2,1,1);
plot(w, abs(H/H(1)));
grid on;
xlabel('angular frequency')
ylabel('|H(jw)/H(0)|')
title('H(jw)/H(0)')
```

```

subplot(2,1,2);
plot(w,angle(H/H(1))*180/pi);
xlabel('angular frequency')
ylabel('\theta')
grid on;

% magnitude and phase plot for |(H_D)/(H_D(1))|

[H_D,w1] = freqz(bz,az);

figure(12);
subplot(2,1,1);
plot(w1,abs((H_D)/(H_D(1))));
xlabel('frequency, [Hz]')
ylabel('|H_D(ejwT)/H(1)|')
title('|H_D(ejwT)/H(1)|')
grid on;
subplot(2,1,2);
plot(w1,angle((H_D)/(H_D(1)))*180/pi);
xlabel('frequency, [Hz]')
ylabel('\theta')
grid on;
%comparing the approximation accuracy of H_D(ejwT)/H(0) and H(jw)/H(0)
figure(100);
subplot(2,1,1);
plot(w,abs(H/H(1)),'b-');
ylabel('|H(jw)/H(0) H_D(ejwT)/H_D(1)|')
xlabel('angular frequency')
title('Comparing the approximation accuracy of H_D(ejwT)/H_D(1) relative to H(jw)/H(0)')
hold on;
plot(w1,abs(H_D/H_D(1)),'r:');
legend('H/H(0)', 'H_D/H_D(1)')
grid on;

subplot(2,1,2);
plot(w,angle(H/H(1))*180/pi,'b-');
hold on;
plot(w1,angle(H_D/H_D(1))*180/pi,'r:');
ylabel('\theta')
xlabel('angular frequency')
legend('H/H(0)', 'H_D/H_D(1)')
grid on;
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% (2)for f1= 2000 fs1=20000

fs1=20000;
fsp1=0:1:fs1/2;
w1=2*pi*fsp1;

[z2,p2,k2]=cheblap(4,0.5);% low pass filter prototype
[b1,a1] = zp2tf(z2,p2,k2); % % Convert to transfer function form
[b1,a1] = lp2lp(b1,a1,2*pi*f1);% analog low pass filter to low pass filter of
specified frequency
[bz1,az1]=impinvar(b1,a1,fs1);% using impulse invariant method

```

```

disp('-----Answer to question 2-----')
disp('2a _____ Hd(z) when f1=2KHz fs=20KHz _____')
tf(bz1,az1)
disp('poles(2)')
[z3,p3,k3] = tf2zp(bz1,az1)
disp('_____2b_____')
disp('the magnitude of each pole')
p2_1 = abs(p3(1))
p2_2 = abs(p3(2))
p2_3 = abs(p3(3))
p2_4 = abs(p3(4))
zplane(z,p)
disp('the angle of each pole')
A2_1= angle(p3(1))*57.2958
A2_2=angle(p3(2))*57.2958
A2_3=angle(p3(3))*57.2958
A2_4=angle(p3(4))*57.2958

%%comparing the Zpmax at (1) and (2)
Zp1max = max(abs(p1))
Zp2max = max(abs(p3))

%%comparing the approximation accuracy of  $H_D(e^{j\omega T})/H(0)$  and  $H(j\omega)/H(0)$ 

H1 = freqs(b1,a1,w1);
figure(21);
subplot(2,1,1);
plot(w1, abs(H1/H1(1)));
grid on;
xlabel('angular frequency')
ylabel('|H1(jw)/H1(0)|')
title('H1(jw)/H1(0)')
subplot(2,1,2);
plot(w1,angle(H1/H1(1))*180/pi);
xlabel('angular frequency')
ylabel('\theta')
grid on;
[H_D1,w2] = freqz(bz1,az1);
figure(22);
subplot(2,1,1);
plot(w2, abs((H_D1)/(H_D1(1))));
xlabel('frequency, [Hz]')
ylabel('|H_D1(ejwT)/H_D1(1)|')
title('|H_D1(ejwT)/H_D1(1)|')
grid on;
subplot(2,1,2);
plot(w2,angle((H_D1)/(H_D1(1)))*180/pi);
xlabel('frequency, [Hz]')
ylabel('\theta')
grid on;

figure(3);
subplot(2,1,1);
plot(w1, abs(H1/H1(1)), 'b-');

```

```

ylabel('|H1(jw)/H1(0)    H_D1(ejwT)/H_D(1)|')
xlabel('angular frequency')
title('Comparing the approximation accuracy of H_D1(ejwT)/H_D(1) relative to
H1(jw)/H1(0)')
hold on;
plot(w2, abs(H_D1/H_D(1)), 'r:');
legend('H1/H1(0) ', 'H_D1/H_D(1) ')
grid on;

subplot(2,1,2);
plot(w1, angle(H1/H1(1))*180/pi, 'b-');
hold on;
plot(w2, angle(H_D1/H_D(1))*180/pi, 'r:');
ylabel('\theta')
xlabel('angular frequency')
legend('H1/H1(0) ', 'H_D1/H_D(1) ')
grid on;

%%%%%%%%%%%%%(3) for f2=3khz and fs2=15khz

f2=3000;
W2=2*pi*f2;
fs2=15000;

fsp2=0:1:fs2/2;
w3=2*pi*fsp2;

[z4,p4,k4]=cheblap(4,0.5);% low pass filter prototype
[b2,a2] = zp2tf(z4,p4,k4); % % Convert to transfer function form
[b2,a2] = lp2lp(b2,a2,2*pi*f2);% analog low pass filter to low pass filter of
specified frequency
[bz2,az2]=impinvar(b2,a2,fs2);% using impulse invariant method

%%%%%%%%%%%%poles of Hd3(z)
disp('-----Answer to question 3-----')
disp('3a_____ Hd(z)when f1=3KHz fs=15KHz _____')
tf(bz2,az2)
disp('poles(3)')
[z5,p5,k5] = tf2zp(bz2,az2)
disp('the magnitude of each pole')
p3_1 = abs(p5(1))
p3_2 = abs(p5(2))
p3_3 = abs(p5(3))
p3_4 = abs(p5(4))
zplane(z,p)
disp('the angle of each pole')
A3_1= angle(p5(1))*57.2958
A3_2=angle(p5(2))*57.2958
A3_3=angle(p5(3))*57.2958
A3_4=angle(p5(4))*57.2958
%%%%%%%%%%%%comparing the Zpmax at (1) and (3)
Zp1max = max(abs(p1))
Zp3max = max(abs(p5))

H2 = freqs(b2,a2,w3);

```

```

figure(31);
subplot(2,1,1);
plot(w3, abs(H2/H2(1)));
grid on;
xlabel('angular frequency')
ylabel('|H2(jw)/H2(0)|')
title('H2(jw)/H2(0)')
subplot(2,1,2);
plot(w3,angle(H2/H2(1))*180/pi);
xlabel('angular frequency')
ylabel('\theta')
grid on;

```

```
[H_D2,w4] = freqz(bz2,az2);
```

```

figure(32);
subplot(2,1,1);
plot(w4, abs((H_D2)/(H_D2(1))));
xlabel('angular frequency')
ylabel('|H_D2(ejwT)/H_D2(1)|')
title('|H_D2(ejwT)/H_D2(1)|')
grid on;
subplot(2,1,2);
plot(w4,angle((H_D2)/(H_D2(1)))*180/pi);
xlabel('angular frequency')
ylabel('\theta')
grid on;

```

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Code for 4
```

```

f3=4000;
W3=2*pi*f3;
fs3=40000;
df=1;
fsp3=0:df:fs3/2;
w4=2*pi*fsp3;

```

```

[z6,p6,k6]=cheblap(4,0.5);% low pass filter prototype
[b3,a3] = zp2tf(z6,p6,k6); % % Convert to transfer function form
[b3,a3] = lp2lp(b3,a3,2*pi*f3);% analog low pass filter to low pass filter of
specified frequency
[bz3,az3]=impinvar(b3,a3,fs3);% using impulse invariant method

```

```

% poles of Hd4(z)
disp('-----Answer to question 4-----')
disp('4a_____ Hd(z)for f1=4KHz fs=40KHz_____')
tf(bz3,az3)

```

```

disp('poles(4)')
[z7,p7,k7] = tf2zp(bz3,az3)
disp('the magnitude of each pole')
p4_1 = abs(p7(1))

```

```

p4_2 = abs(p7(2))
p4_3 = abs(p7(3))
p4_4 = abs(p7(4))
zplane(z,p)
disp ('the angle of each pole')
A4_1= angle(p7(1))*57.2958
A4_2=angle(p7(2))*57.2958
A4_3=angle(p7(3))*57.2958
A4_4=angle(p7(4))*57.2958
%%%comparing the Zpmax at (2) and (4)
Zp2max = max(abs(p3))
Zp4max = max(abs(p7))

H3 = freqs(b3,a3,w4);

figure(41);
subplot(2,1,1);
plot(w4, abs(H3/H3(1)));
grid on;
xlabel('angular frequency')
ylabel('|H3(jw)/H3(0)|')
title('H3(jw)/H3(0)')
subplot(2,1,2);
plot(w4,angle(H3/H3(1))*180/pi);
xlabel('angular frequency')
ylabel('\theta')
grid on;
[H_D3,w5] = freqz(bz3,az3);
figure(42);
subplot(2,1,1);
plot(w5, abs((H_D3)/(H_D3(1))));
xlabel('angular frequency')
ylabel('|H_D3(ejwT)/H_D3(1)|')
title('|H_D3(ejwT)/H_D3(1)|')
grid on;
subplot(2,1,2);
plot(w5,angle((H_D3)/(H_D3(1)))*180/pi);
xlabel('angular frequency')
ylabel('\theta')
grid on;
figure(43)
subplot(2,1,1);
plot(w4/2/pi, abs(H3/H3(1)), 'b-');
ylabel('|H3(jw)/H3(0) H_D3(ejwT)/H_D3(1)|')
xlabel('frequency, [Hz]')
title('Comparing the approximation accuracy of H_D3(ejwT)/H_D3(1) relative to
H3(jw)/H3(0)')
hold on;
plot(w5/2/pi*fs1, abs(H_D3/H_D3(1)), 'r:');
legend('H3/H3(0)', 'H_D3/H_D3(1)')
grid on;

subplot(2,1,2);
plot(w4/pi/2,angle(H3/H3(1))*180/pi, 'b-');
hold on;
plot(w5/pi*fs1/2,angle(H_D3/H_D3(1))*180/pi, 'r:');

```

```

ylabel('\theta')
xlabel('frequency, [Hz]')
legend('H3/H3(0)', 'H_D3/H_D3(1)')
grid on;

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%(5) using bilinear transformation

%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%% (a)
[z,p,k] = cheblap(4,0.5) ;
[A,B,C,D] = zp2ss(z,p,k);
[A1,B1,C1,D1] = lp2lp(A,B,C,D,2*pi*f1);
[b4,a4] = ss2tf(A1,B1,C1,D1);
[bz4,az4] = bilinear(b,a,fs);

%(b)
disp('-----Answer to question 5-----')
disp('_____ Hd(z) when fs=40KHz _____')
tf(bz4,az4)
disp('poles(5)')
[z8,p8,k8] = tf2zp(bz4,az4);
disp('the magnitude of each pole')
p5_1 = abs(p8(1))
p5_2 = abs(p8(2))
p5_3 = abs(p8(3))
p5_4 = abs(p8(4))
zplane(z,p)
disp('the angle of each pole')
A5_1= angle(p8(1))*57.2958
A5_2=angle(p8(2))*57.2958
A5_3=angle(p8(3))*57.2958
A5_4=angle(p8(4))*57.2958
%(c)

H4 = freqs(b,a,w);

figure(51);
subplot(2,1,1);
plot(w, abs(H4/H4(1)));
grid on;
xlabel('angular frequency')
ylabel('|H5(jw)/H5(0)|')
title('H5(jw)/H5(0)')
subplot(2,1,2);
plot(w,angle(H4/H4(1))*180/pi);
xlabel('angular frequency')
ylabel('\theta')
grid on;

[H_D4,w6] = freqz(bz4,az4);

figure(52);
subplot(2,1,1);
plot(w6, abs(H_D4/H_D4(1)));
xlabel('angular frequency')
ylabel('|H_D5(ejwT)/H_D5(1)|')

```

```

title('H_D5(ejwT)/H_D5(1)')
grid on;
subplot(2,1,2);
plot(w6,angle(H_D4/H_D4(1))*180/pi);
xlabel('angular frequency')
ylabel('\theta')
grid on;
f1_5 = atan(f1*2*pi/fs/2)*2*fs/2/pi % new value of cutoff frequency
%% Code for (6)

W3db=10e4;
ws=4*W3db;
fs4=(ws/2/pi);
df=1;
fsp4=0:df:fs4/2;
w4=2*pi*fsp4;

num=[0 0 0 0 0 0 1];
den=[1 3.8637033 7.4641016 9.1416202 7.4641016 3.8637033 1];
[b5,a5] = lp2hp(num,den,W3db);
[bz5,az5]=bilinear(b5,a5,fs4);

H5 = freqs(b5,a5,w4);

figure(61);
subplot(2,1,1);
plot(w4/2/pi, abs(H5));
xlabel('frequency, [Hz]')
ylabel('|H5(jw)|')
title('normalized |H5(jw)/H5(3184)|')
grid on;
subplot(2,1,2);
plot(w4/2/pi,angle((H5)*180/pi));
xlabel('frequency, [Hz]')
ylabel('\theta')
grid on;

[H_D5,w7] = freqz(bz5,az5);

figure(62);
subplot(2,1,1);
plot(w7/pi/2*fs4, abs(H_D5/H_D5(512)));
xlabel('frequency, [Hz]')
ylabel('|H_D5(ejwT)|')
title('|H_D5(ejwT)/H_D5(512)|')
grid on;
subplot(2,1,2);
plot(w7/pi/2*fs4,angle((H_D5/H_D5(512))*180/pi));
xlabel('frequency, [Hz]')
ylabel('\theta')
grid on;

disp('poles(6)')
[z9,p9,k9] = tf2zp(bz5,az5);
disp('the magnitude of each pole')

```



```

p6_1 = abs(p9(1))
p6_2 = abs(p9(2))
p6_3 = abs(p9(3))
p6_4 = abs(p9(4))
zplane(z,p)
% new value of cutoff for digital filter calculated analytically
w3db=atan(W3db/fs4/2)*2*fs4

%(7) Prewarping
T=1;
ws=4*10e4;
Ts=1/fs4;

num=[0 0 0 0 0 0 1];
den=[1 3.8637033 7.4641016 9.1416202 7.4641016 3.8637033 1];
[b5,a5] = lp2hp(num,den,W3db);

w8=2*fs4*tan(W3db/2/fs4);
fp=(w8/2/pi);

[bz6,az6]=bilinear(b5,a5,fs4,fp);

H5 = freqs(b5,a5,w4);

figure(71);
subplot(2,1,1);
plot(w4/2/pi, abs(H5));
xlabel('frequency, [Hz]')
ylabel('|H6(jw)|')
title('|H6(jw)/H6(3184)|')
grid on;
subplot(2,1,2);
plot(w4/2/pi,angle((H5)*180/pi));
xlabel('frequency, [Hz]')
ylabel('\theta')
grid on;

[H_D6,w8] = freqz(bz6,az6);

figure(72);
subplot(2,1,1);
plot(w8/pi*fs4/2, abs(H_D6/H_D6(512)));
xlabel('frequency, [Hz]')
ylabel('|H_D6(ejwT)|')
title('|H_D6(ejwT)/H_D6(512)|')
grid on;
subplot(2,1,2);
plot(w8/pi*fs4/2,angle((H_D6/H_D6(512))*180/pi));
xlabel('frequency, [Hz]')
ylabel('\theta')
grid on;

```