

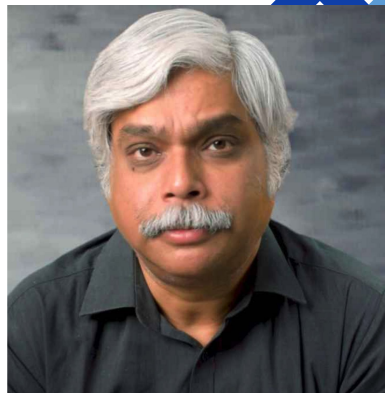
# Linear Regression

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# Meet Your Speaker



## **Dr. Abhinanda Sarkar**

### **Academic Director at Great Learning**

- Alumnus - Indian Statistical Institute, Stanford University
- Faculty - MIT, Indian Institute of Management, Indian Institute of Science
- Experienced in applying probabilistic models, statistical analysis and machine learning to diverse areas
- Certified Master Black Belt in Lean Six Sigma and Design for Six Sigma in GE

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# Learning Objectives

By the end of this session, you should be able to:

- Relate correlation and simple linear regression in the context of understanding linear relationships.
- Explore simple linear regression models to capture the linear relationship between a pair of attributes.
- Build multiple linear regression to model relationships between two or more input attributes and the output, to predict business outcomes.
- Evaluate linear regression models and identify the levers to improve their performance.
- Discover the applications of linear regression to solve a variety of business problems.

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# Agenda

In this session, we'll discuss:

- Business Problem and Solution Space
- Correlation and Linear Relationships
- Simple Linear Regression
- Multiple Linear Regression
- Categorical Variables in Regression
- Evaluation Metrics for Regression

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# Common Business Questions

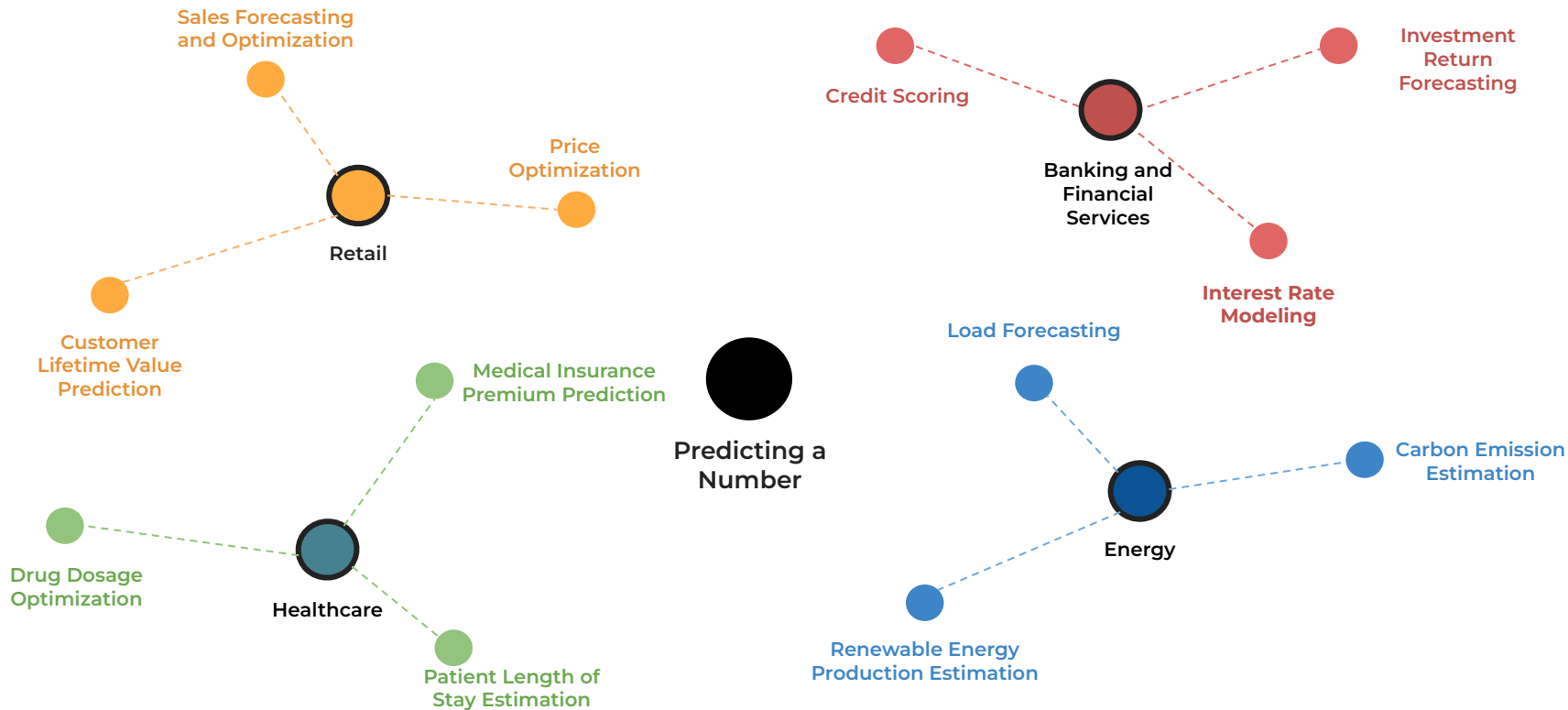
- How can we forecast sales based on historical sales data and marketing expenditure?
- How do we determine medical insurance premiums for customers based on attributes like blood pressure, blood sugar level, and smoking habits?
- How do we determine the credit card limit to be assigned to customers based on their past spending behavior, demographic information, etc?
- How can we predict future power load requirements to ensure reliable grid operation and prevent outages?

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# Problem Space

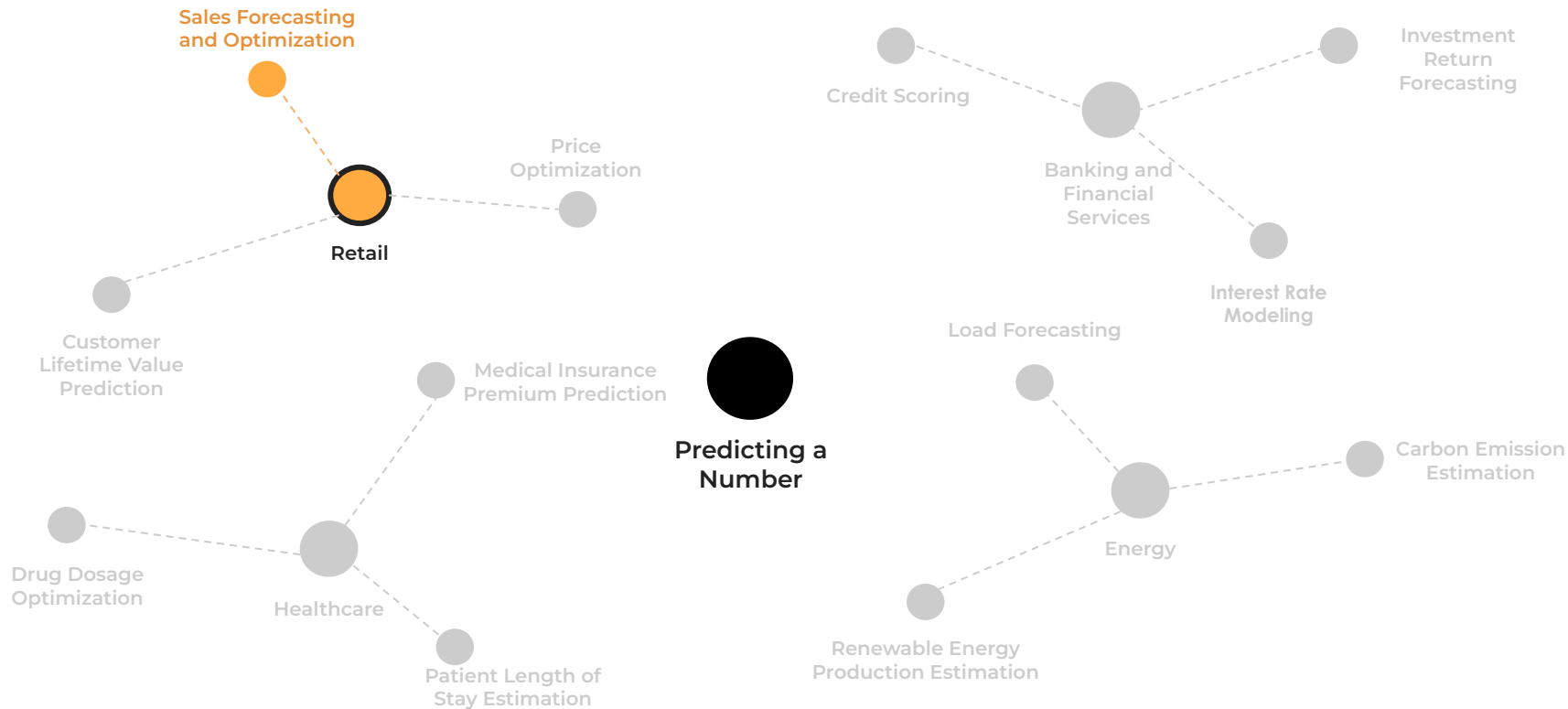


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# Problem Space



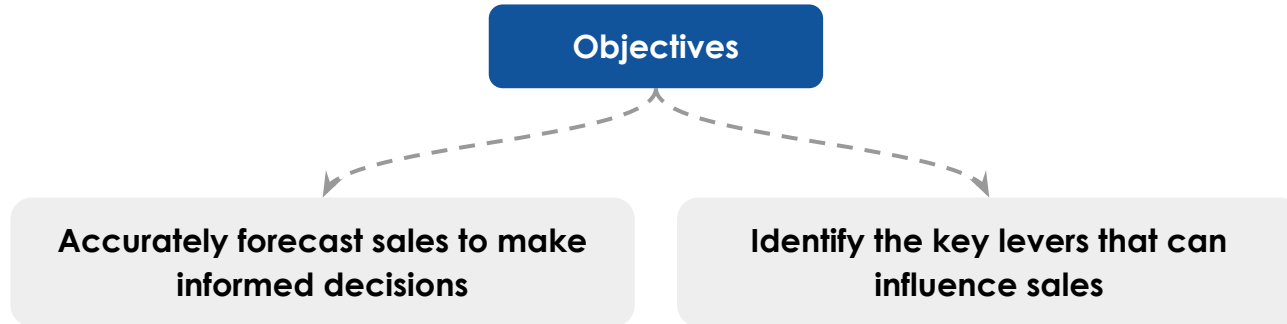
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# Problem Statement

- Consider an online retailer of mobiles and tablets
- Crucial to stay ahead of market trends and consumer preferences to maximize sales
- Need to effectively manage inventory and marketing efforts to attract and retain customers



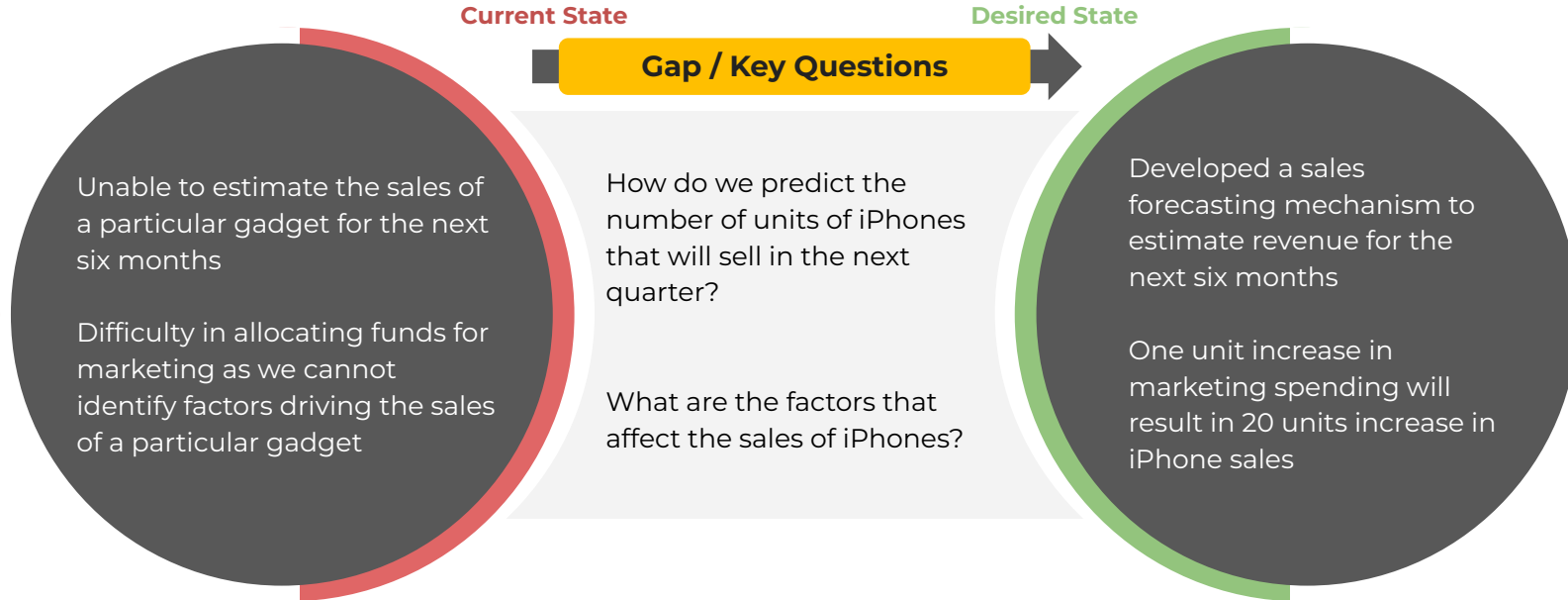
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# Sales Forecasting and Optimization

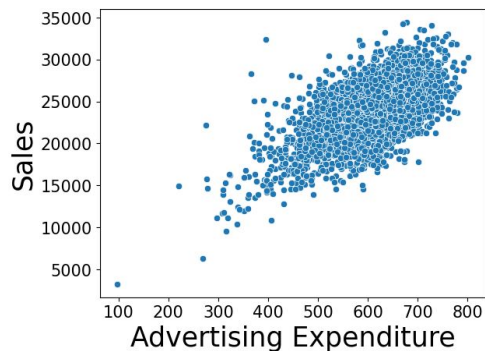


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# Visualizing Relationships



What happens to Sales as Advertising Expenditure increases?

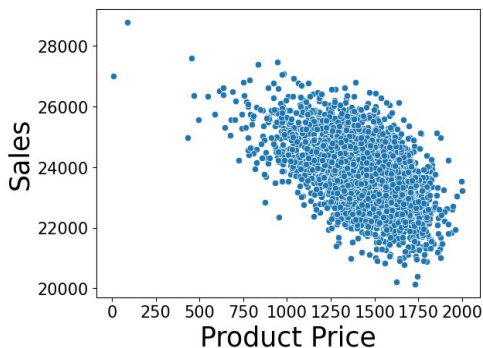
Advertising Expenditure



Sales



**Positive relationship**



What happens to Sales as Product Price increases?

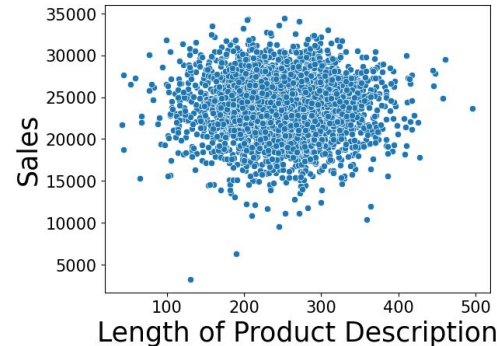
Product Price



Sales



**Negative relationship**



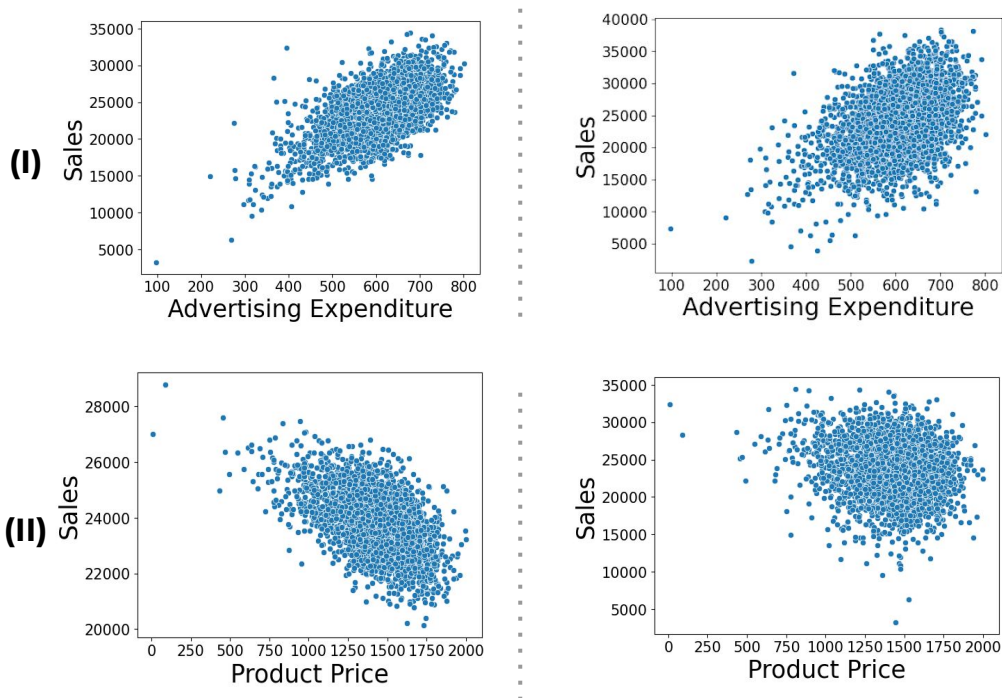
**No relationship**

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# Visualizing Relationships



(I) In both the cases, we observe a **positive relationship** between sales and advertising expenditure

What is the **difference**?

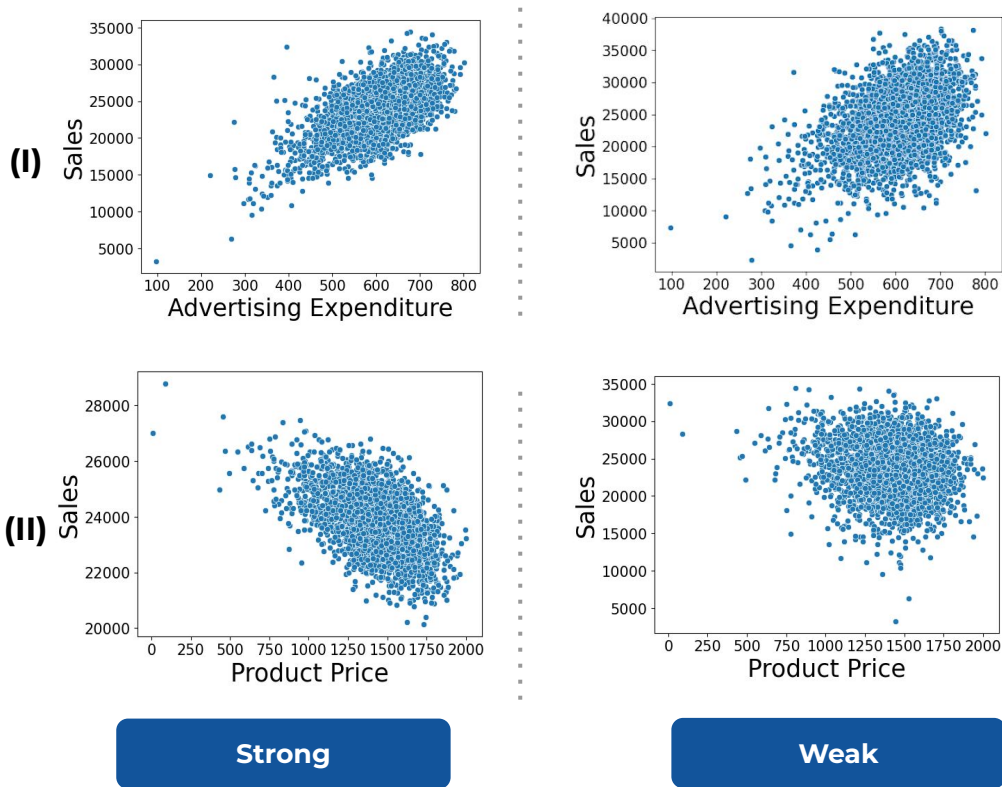
(II) In both the cases, we observe a **negative relationship** between the sales and product price

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# Visualizing Relationships



The cases on the left - in both (I) and (II) - exhibit a **stronger relationship (positive or negative)** than the ones on the right

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# Correlation

- We have seen how to **visually identify relationships** between a pair of variables from two aspects - **direction** and **strength**
- But we need a **quantitative measure** of the relationship

**Correlation** is a **statistical measure** that describes the **strength and direction** of a **relationship** between two variables.

- Indicates the **degree** to which two variables tend to **change together**
- Quantifies both the **direction** and **strength** of the relationship

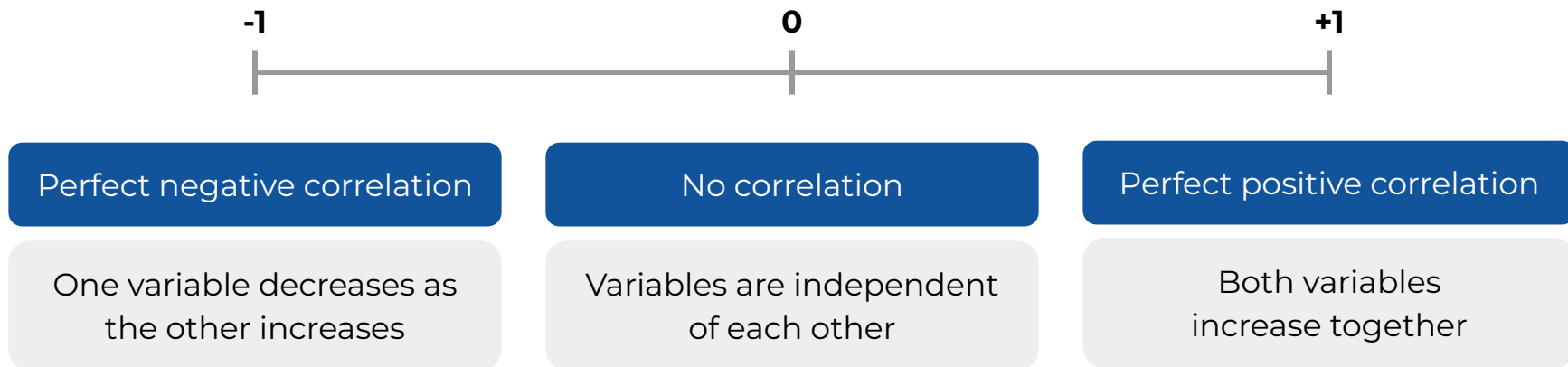
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# Correlation

Correlation typically **ranges between -1 and 1**.



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# Pearson's Correlation Coefficient

- One of the most commonly used measures of correlation.

A statistical measure that quantifies the **strength** and **direction** of the **linear relationship** between **two continuous variables**.

$$r = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2 \sum_{i=1}^n (y_i - \bar{y})^2}}$$

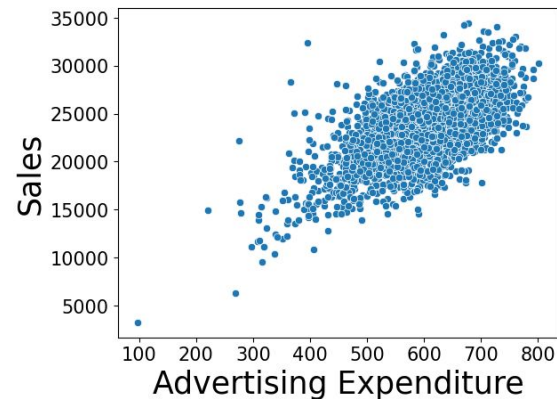
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# Correlation vs. Causation

- We observed advertising expenditure exhibits a strong positive correlation with sales.
- As advertising expenditure increased, sales increased.
- Does it mean advertising expenditure **causes** an increase in sales?
- **Not necessarily true!**
- There might be **other factors** at play.



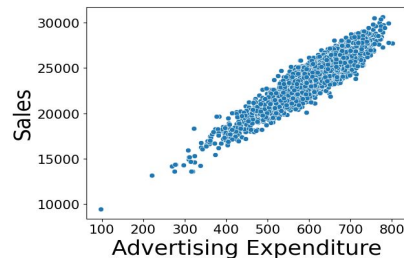
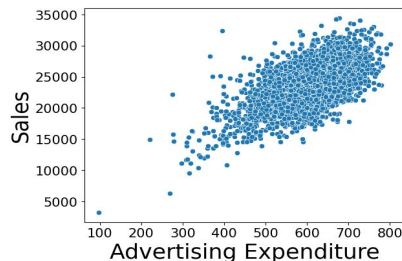
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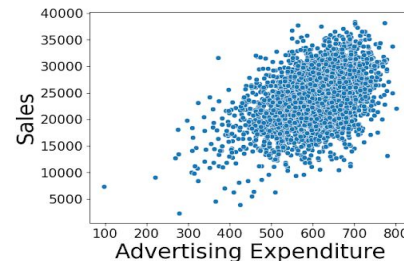
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# Correlation vs. Causation



Economic Zone 1



Economic Zone 2

- Let's split the data with respect to **another factor - economic zone**.
- Economic Zone 1 has a **booming economy** - sales will be higher here even if we don't spend as much on marketing.
- Economic Zone 2 has a **stagnant economy** - sales might have been higher due to data collected in a festive season.

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# Correlation vs. Causation

**Correlation  $\neq$  Causation**



**Variable 1 and Variable 2**  
are **highly correlated**

**$\neq$**

**Variable 1 causes** a change  
in **Variable 2**

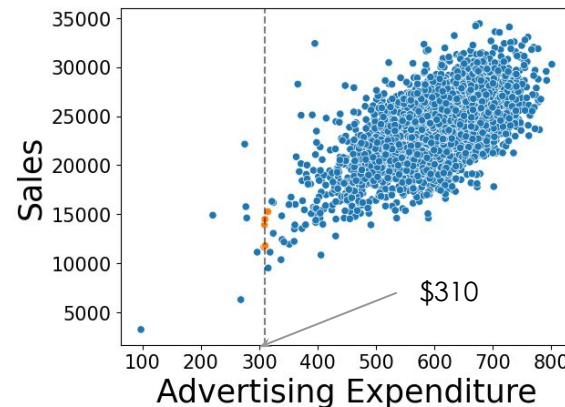
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# The Need for Regression

- We observed advertising expenditure exhibits a strong positive correlation with sales.
- Let's say we now decide to spend \$310 for the marketing campaign of the latest iPhone.
- **How much sales should we expect?**
- **We don't know!**
- **Historically**, we've had **different sales** for **similar marketing spending**.



**Correlation measures** the strength and direction of the **relationship**, but **doesn't** provide a way to **predict** the output given an input.

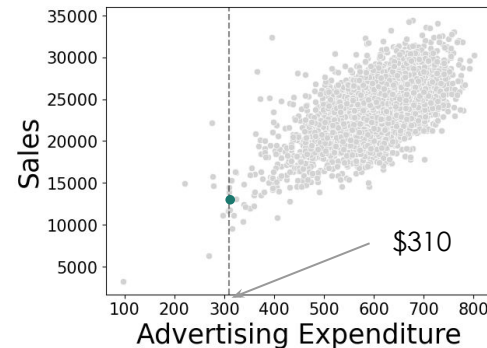
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# The Need for Regression

- It is important for us to be able to determine the output (sales).
- It is also important to identify the lever(s) that drive the output (sales).
- Hence, the need for a mathematical model.



Input value  
(\$310 marketing spend)



Mathematical  
model



Output value  
(\$13040.50 sales)

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# Simple Linear Regression

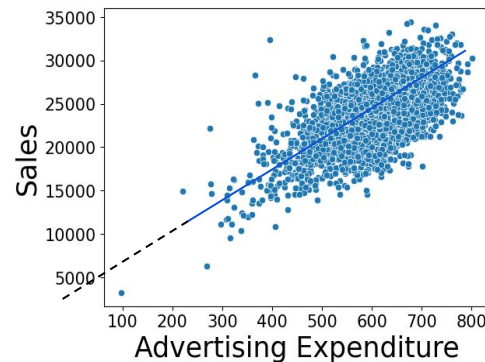
- The **simplest** mathematical model is **linear** - a **straight line**.

**Linear Regression** is a **statistical model** which **estimates** the **linear relationship** between a **response** and one or more **explanatory variables**.

- Simple Linear Regression - **one explanatory** and **one response variable**.
- Assumes that there is a linear relationship between the explanatory (independent) variable and the response (dependent) variable.

advertising expenditure

sales



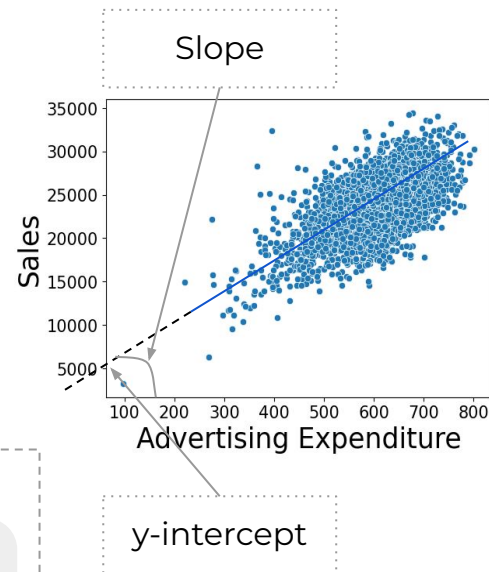
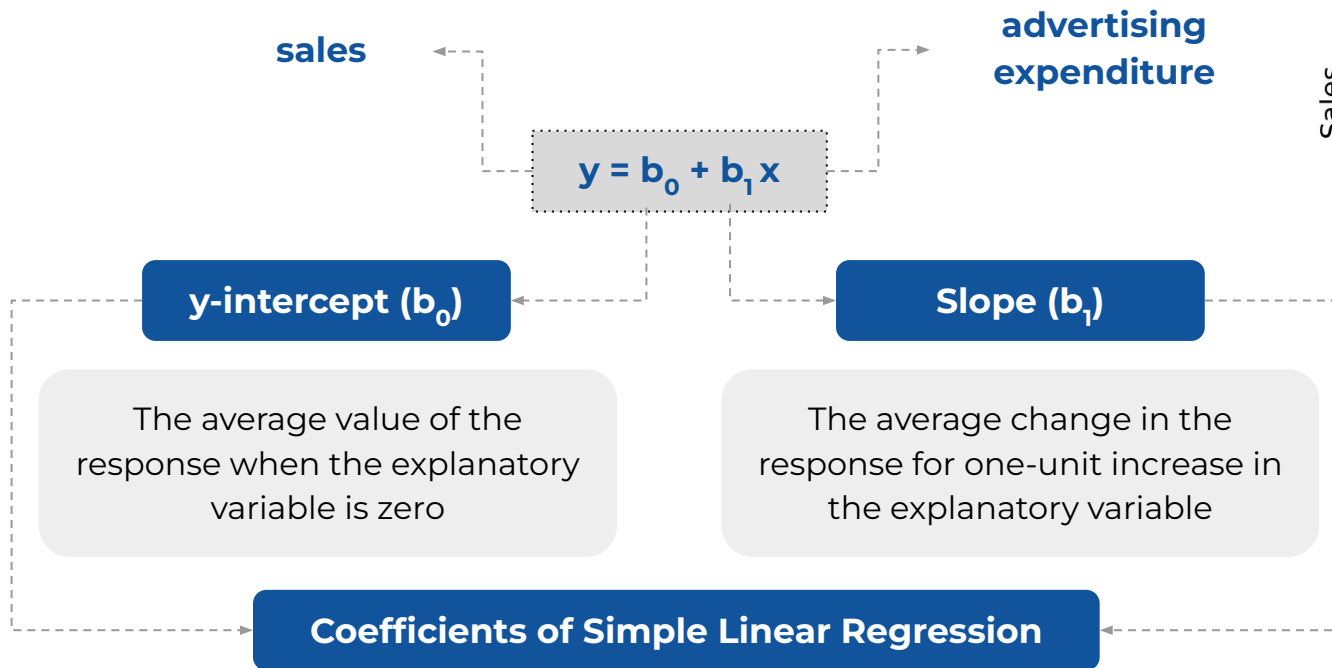
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# Simple Linear Regression

- The equation of line is represented by:



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# Coefficient Interpretation

- Consider the following model for our context:

$$\text{sales} = 1.01 + 2.45 * \text{advertising expenditure}$$

- For a **unit increase** in advertising expenditure, the sales will increase by **2.45 units**.

This **interpretation** is **valid ONLY IF** the **assumptions** of linear regression hold **true**.

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# Coefficient Interpretation

- Consider the following model for our context:

$$\text{sales} = 1.01 + 2.45 * \text{advertising expenditure}$$

- If we have zero marketing expenditure:

$$\text{sales} = 1.01 + 2.45 * 0 = 1.01$$

- Makes **business sense** — we can have **organic sales**.

What if the business context changes?

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# Coefficient Interpretation

- Consider the case of predicting the price of a house using the following model:

$$\text{house price} = 291.07 + 105.45 * \text{square footage}$$

- For a **unit increase** in square footage, the price of the house increases by **105.45 units**.

This **interpretation** is **valid ONLY IF** the **assumptions** of linear regression hold **true**.

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# Coefficient Interpretation

- Consider the case of predicting the price of a house using the following model:

$$\text{house price} = 291.07 + 105.45 * \text{square footage}$$

- In the case of zero square footage:

$$\text{house price} = 291.07 + 105.45 * 0 = 291.07$$

- **Doesn't make business sense!**

y-intercept doesn't always make business sense.

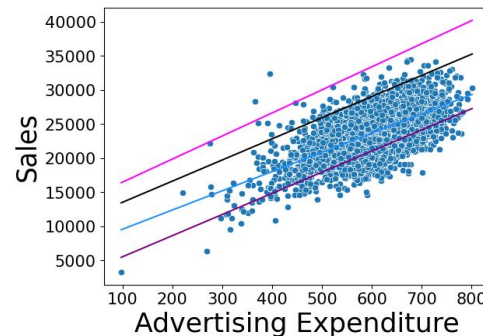
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# Best-Fit Line

- We observed one line that described the relationship between sales and advertising expenditure.
- But we can draw multiple lines!



Which line do we choose?

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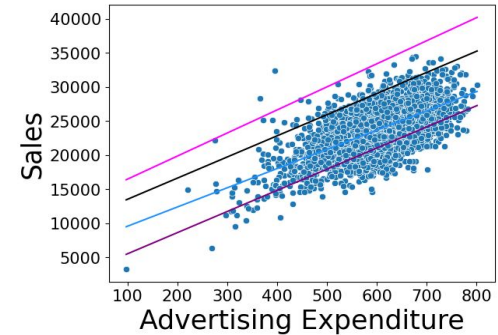
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# Best-Fit Line

- We first need to understand the **difference** between these **lines**.
- We have actual data points (actual sales) and predicted data points (model's predicted sales).

$$\text{Prediction Error} = \text{Actual Value} - \text{Predicted Value}$$

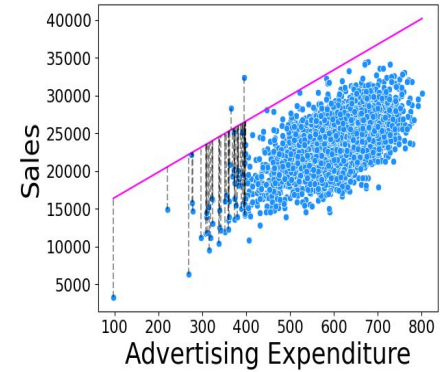
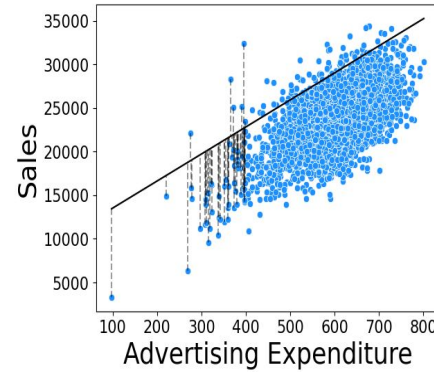
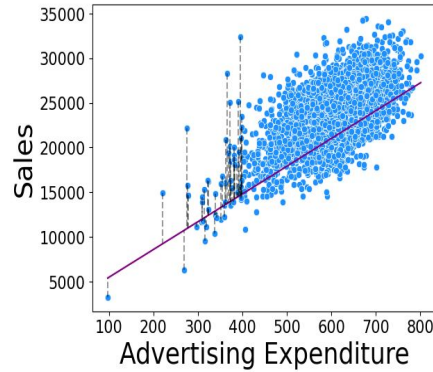
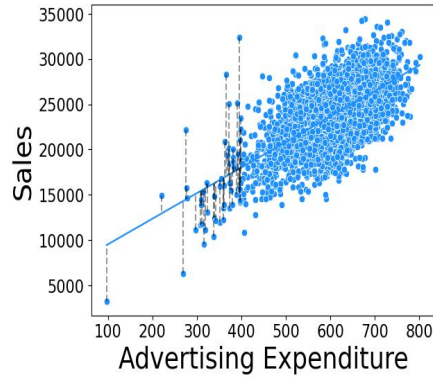


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# Best-Fit Line



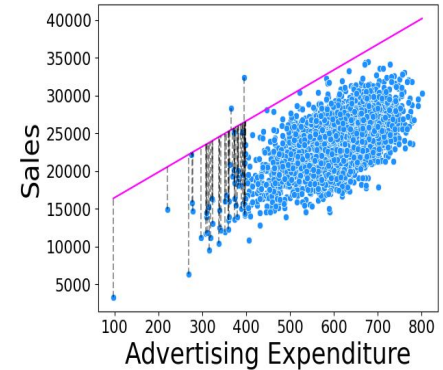
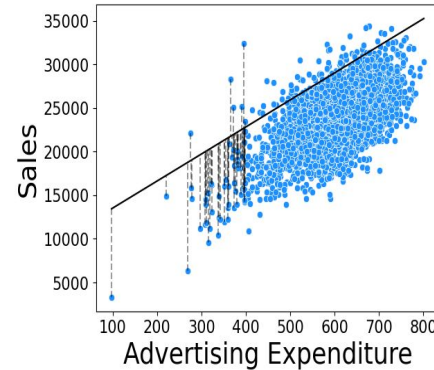
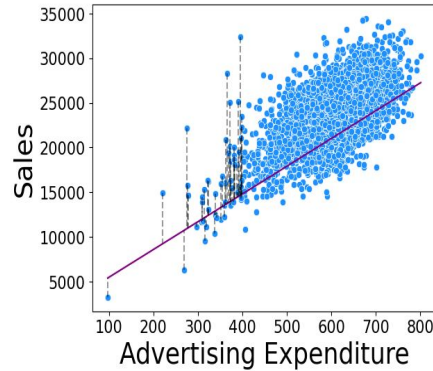
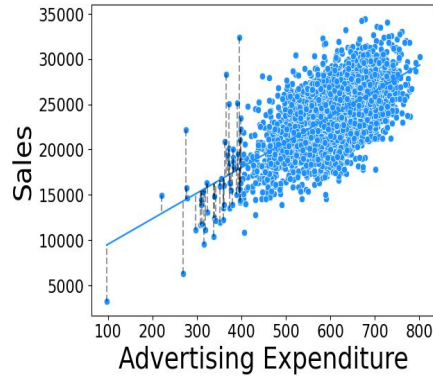
- There are multiple data points to consider.
- Take the aggregate of the errors across the data points.

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# Best-Fit Line



- The **line** with the **least aggregate error** across all data points is the one **we want**.

This is called the **best-fit line**.

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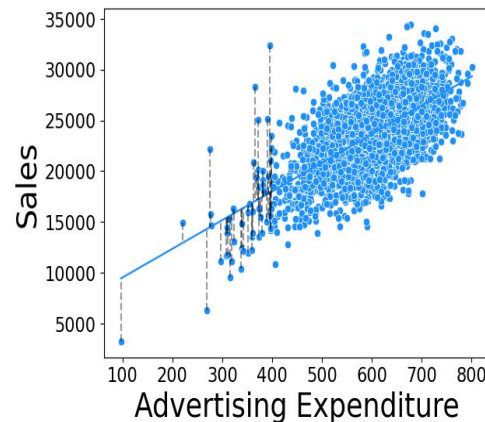
# Best-Fit Line Computation

- How to find the error?

$$Error = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)$$

Actual  
Value

Predicted  
Value



- Difference** between actual and predicted values can be **positive** or **negative**
- Direct addition will give a false picture of low overall error

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# Best-Fit Line Computation

- Take **absolute values**

$$Error = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i|$$



$$Error = \frac{1}{n} \sum_{i=1}^n |y_i - (b_0 + b_1 x_i)|$$

How to minimize the error?

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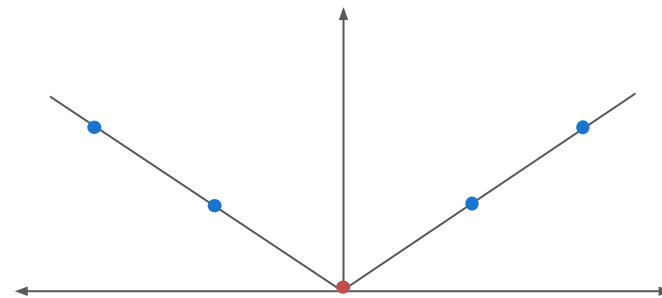


# Best-Fit Line Computation

- Need to find the **values** of the **coefficients** ( $b_0$  and  $b_1$ ) that yield the **minimum error**
- Use **differentiation**

**Differentiate** the **error** with respect to the **coefficients** ( $b_0$  and  $b_1$ )

- Differentiating absolute values is **mathematically inconvenient**



- **Differentiable**
- **Not differentiable**

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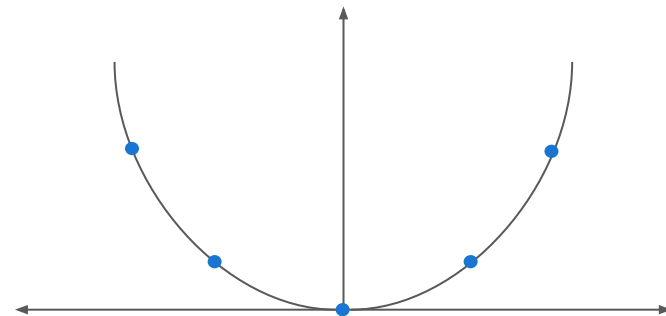
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# Best-Fit Line Computation

- Use **squared values** instead

$$Error = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

- **Accommodates** both **positive** and **negative** errors
- **Mathematically convenient** - differentiable



● **Differentiable**

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# Best-Fit Line Computation

- Use **squared values** instead

$$Error = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$



$$Error = \frac{1}{n} \sum_{i=1}^n (y_i - (b_0 + b_1 x_i))^2$$

This is known as the **Method of Least Squares**

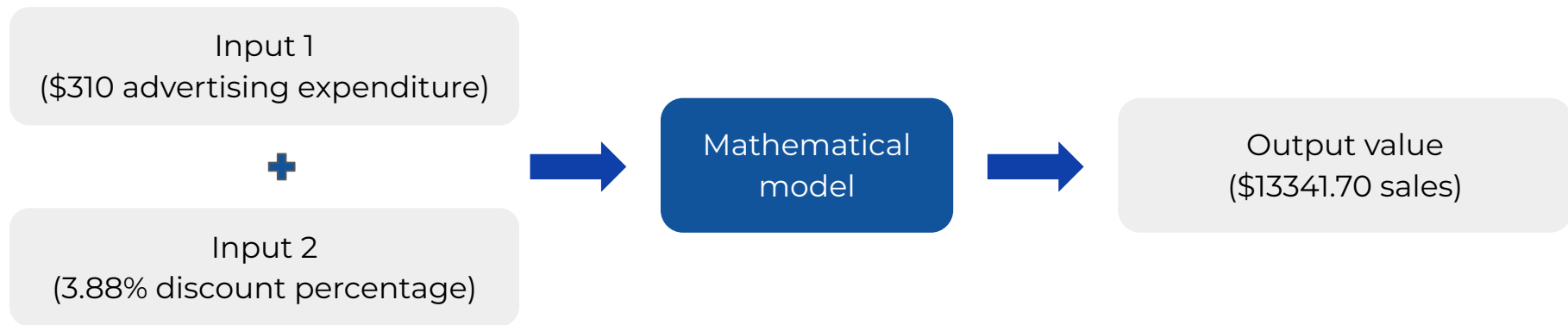
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# Multiple Linear Regression

- We have checked the relationship between sales and advertising expenditure
- What if there is another variable which can be used to predict the sales?



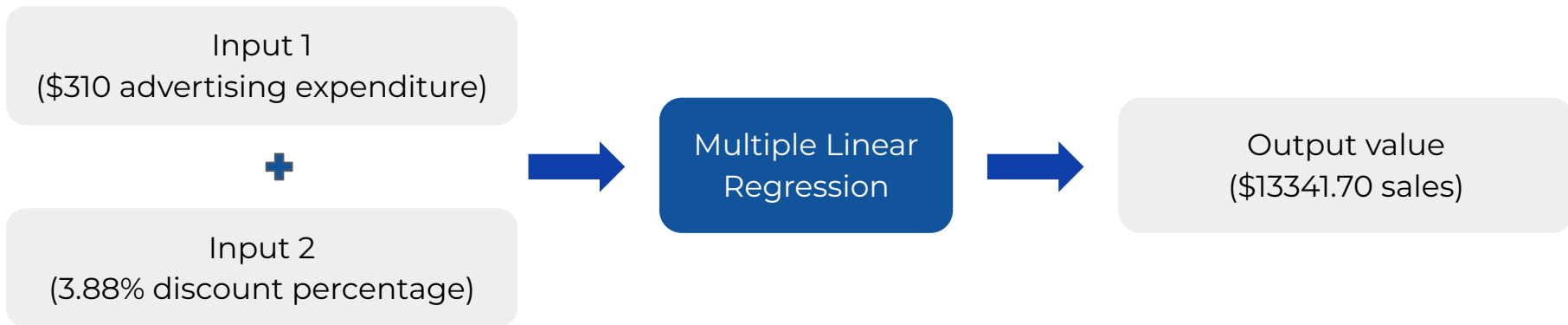
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# Multiple Linear Regression

- Multiple Linear Regression - **two or more explanatory** and **one response variable**
- Extension of Simple Linear Regression



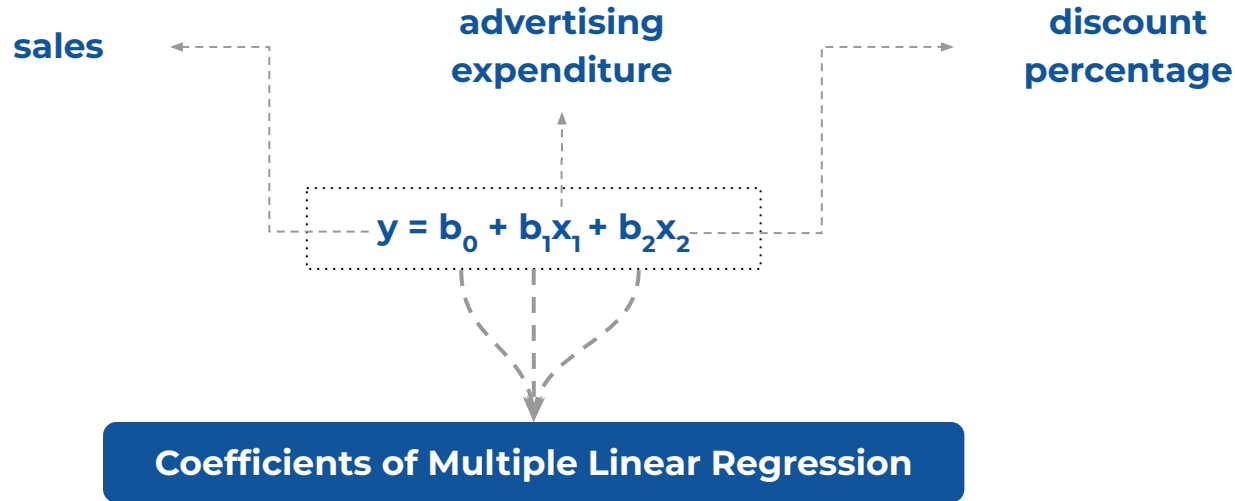
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# Multiple Linear Regression

- Multiple Linear Regression equation - two explanatory variables

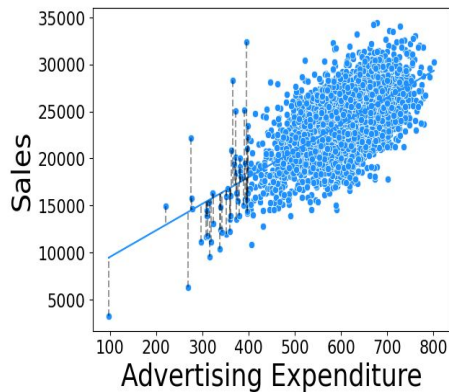


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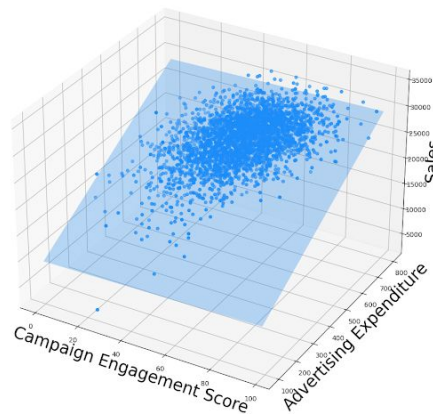
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# Multiple Linear Regression



$$y = b_0 + b_1x_1$$



$$y = b_0 + b_1x_1 + b_2x_2$$

- For **one explanatory variable**, the **equation** was that of a **line**
- For **two explanatory variables**, the **equation** will be that of a **plane**

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# Coefficient Interpretation

- Consider the following model for our context

$$\text{sales} = 1.01 + 2.45 * \text{advertising expenditure} + 7.88 * \text{discount percentage}$$

- For a **unit increase** in advertising expenditure, the sales will increase by **2.45 units**, provided all other variables are held constant
- For a **unit increase** in discount percentage, the sales will increase by **7.88 units**, provided all other variables are held constant

These **interpretations** are **valid ONLY IF** the **assumptions** of linear regression hold **true**

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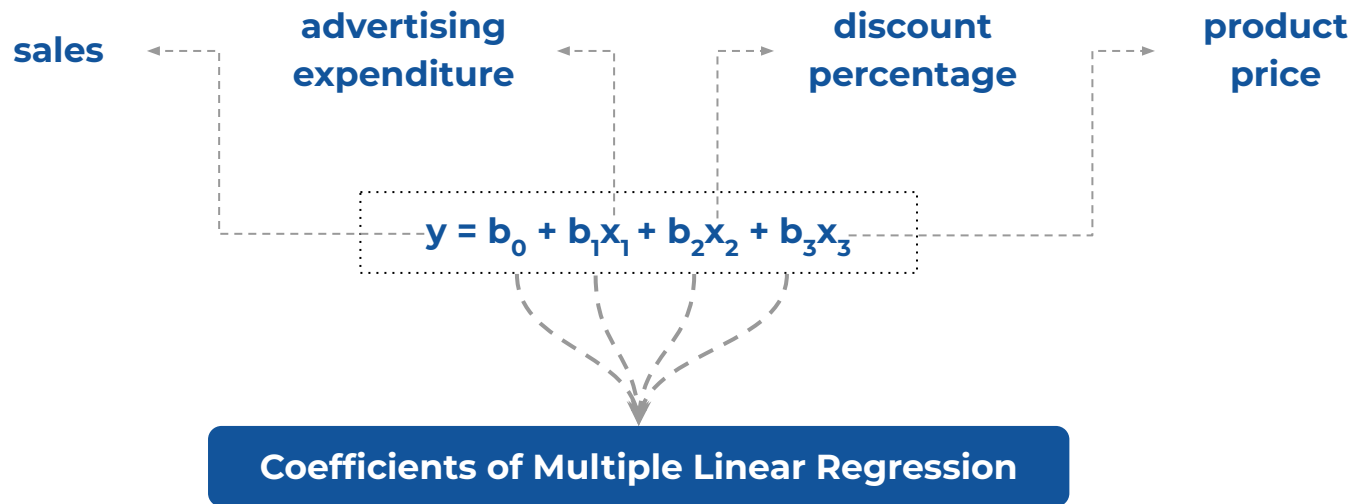
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# Multiple Linear Regression

- Multiple Linear Regression equation - more than two explanatory variables



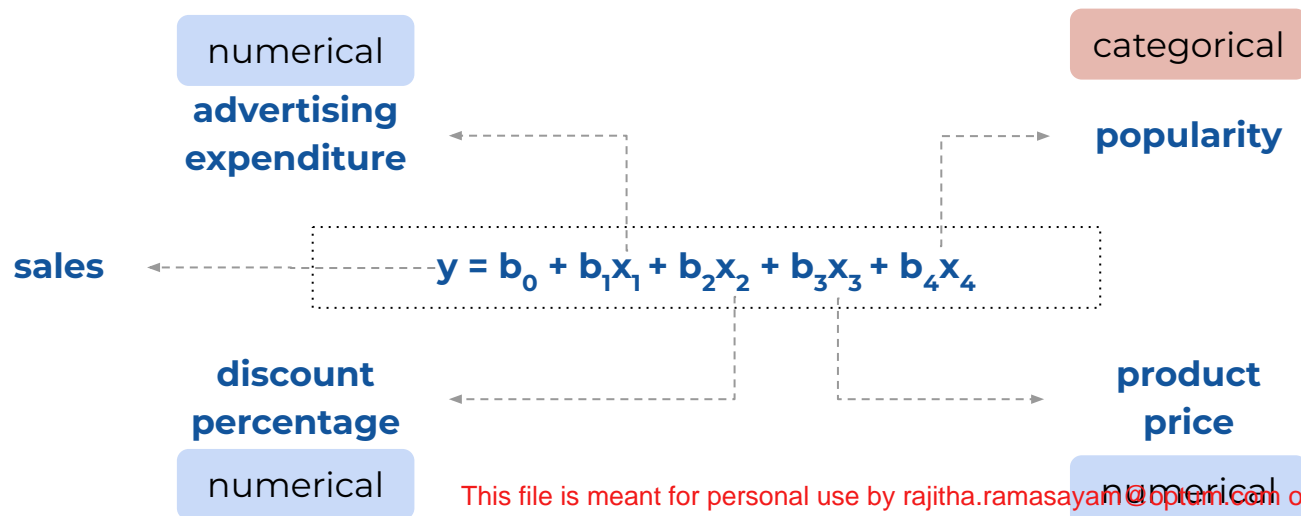
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# Categorical Variables in Regression

- So far we've worked with **numerical variables**
- But real-world data often contains **categorical variables**
- Consider the following case



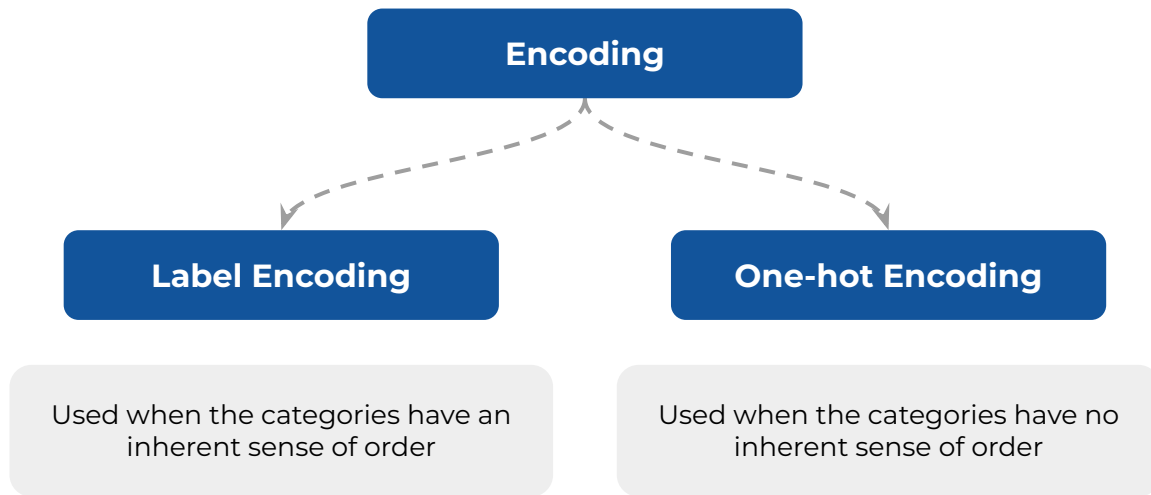
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# Categorical Variables in Regression

- Categorical variables are not numbers - even if they might be represented by numbers
- Can't be utilized directly in a linear regression model
- Need to be converted into a numerical format



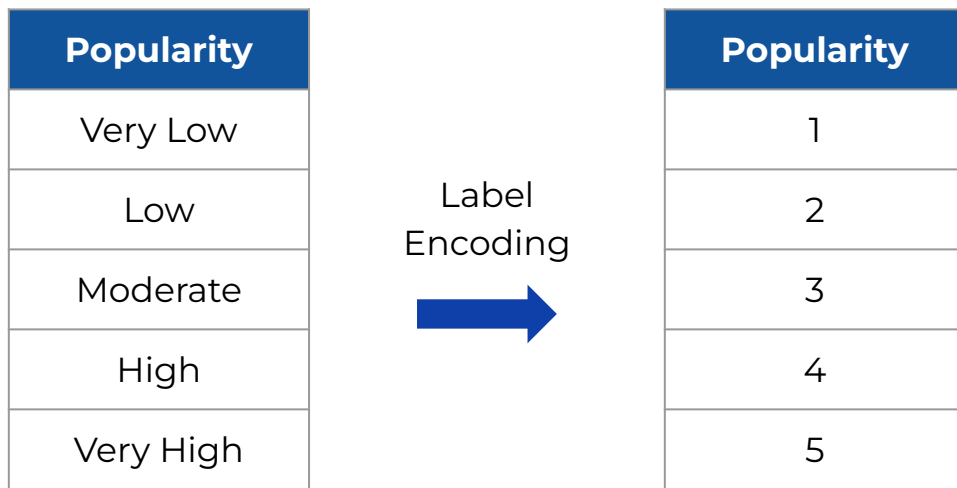
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# Label Encoding

- Assigns a unique integer to each category
- Order of the integers represents the order of the categories



# One-hot Encoding

- A new column is created for each category
- If the data point contains the category, corresponding column has value 1
- If the data point doesn't contain the category, corresponding column has value 0

Region	Region _North	Region _East	Region _West	Region _South
East	0	1	0	0
South	0	0	0	1
West	0	0	1	0
East	0	1	0	0
North	1	0	0	0

One-hot  
Encoding



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# Evaluation Metrics

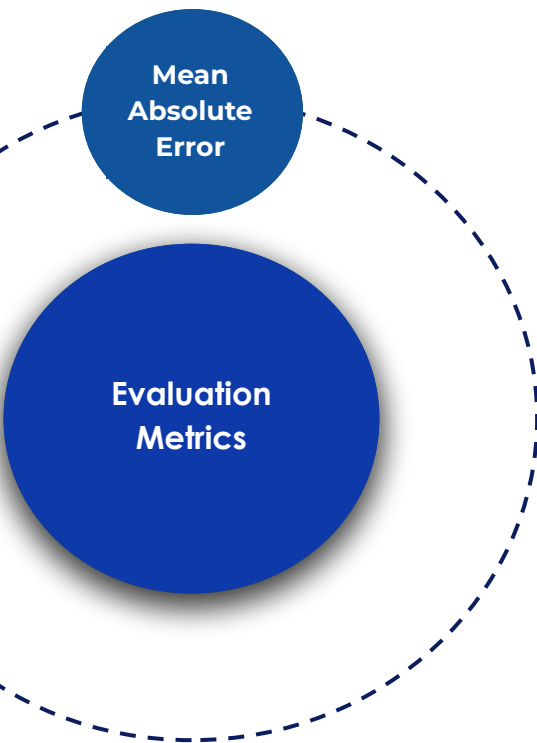
- We have seen multiple models so far
- We don't know **'how well'** these models are **performing**
- Need to **evaluate** the models to gauge if they're performing 'well'
- **Model performance** is measured using **metrics**
- **Quantify** how well the model predictions align with the actual values

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# Evaluation Metrics



- An intuitive metric

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i|$$

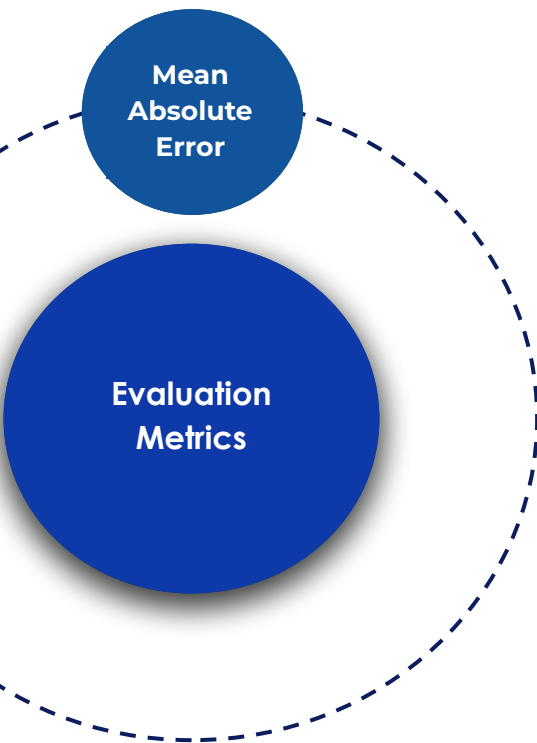
- Gives an idea of how much the model predictions deviate from the actual observations
- Relative to the range of the response

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# Evaluation Metrics



- Problem with considering the absolute value of errors is it doesn't penalize larger errors
- Needed to ensure that the model learns to do better when encountering edge cases

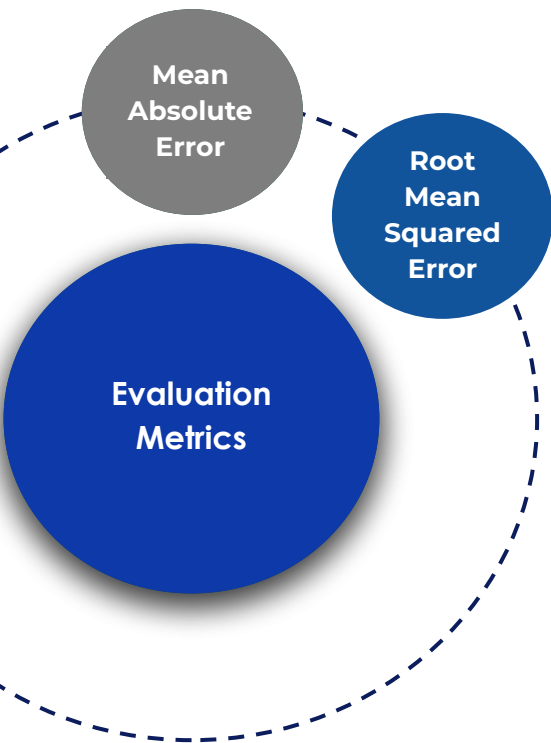
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# Evaluation Metrics



- Problem with considering the absolute value of errors is it doesn't penalize larger errors
- Needed to ensure that the model learns to do better when encountering edge cases

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2}$$

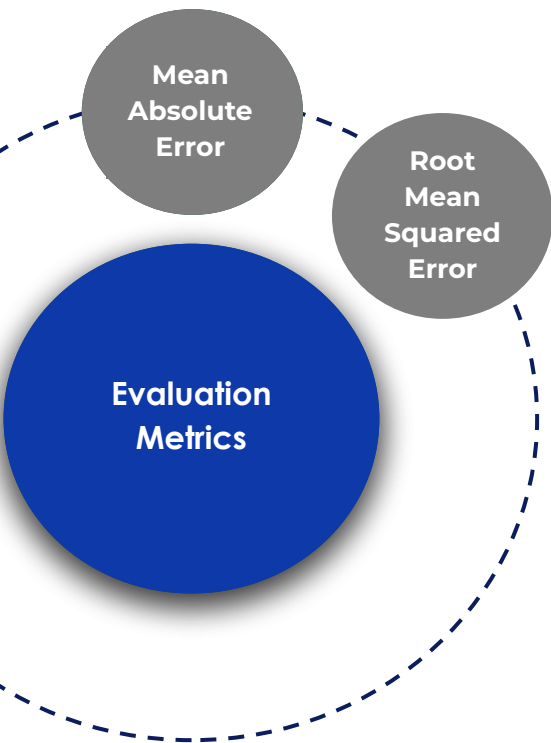
- Relative to the range of the response

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# Evaluation Metrics



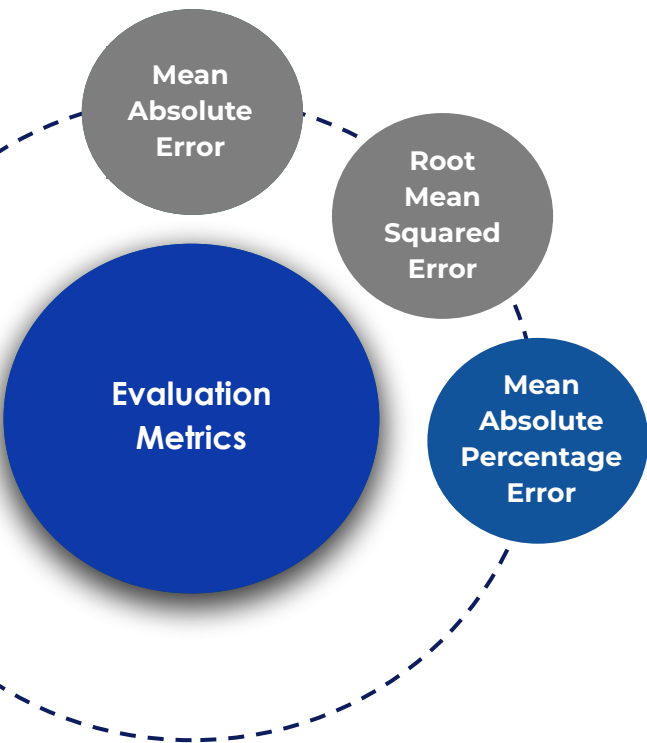
- MAE and RMSE are relative to the scale of the response
- Cannot compare models across different data and scale of response value

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# Evaluation Metrics



- MAE and RMSE are relative to the scale of the response
- Cannot compare models across different data and scale of response value

$$MAPE = \frac{1}{n} \sum_{i=1}^n \left| \frac{y_i - \hat{y}_i}{y_i} \right| * 100$$

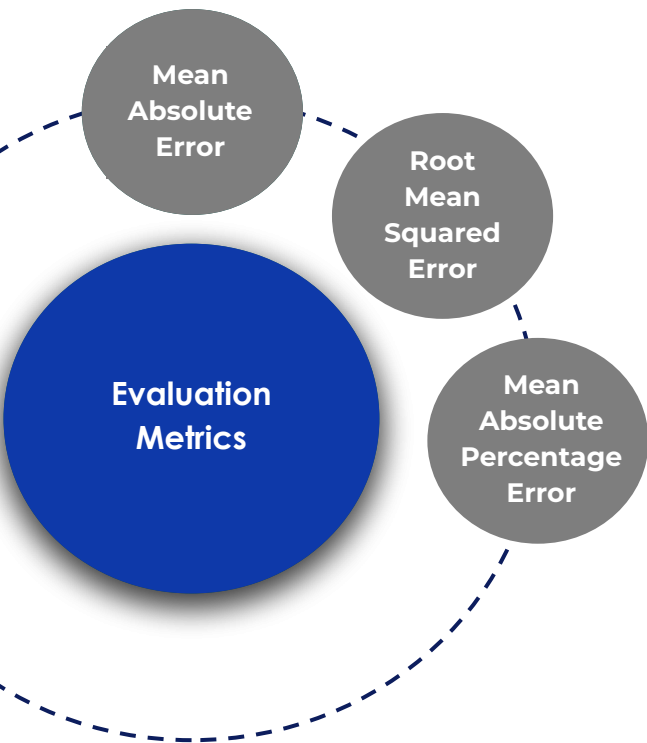
- Indifferent of the range of the response
- Needs to be adjusted when the actual value of the response is zero

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# Evaluation Metrics



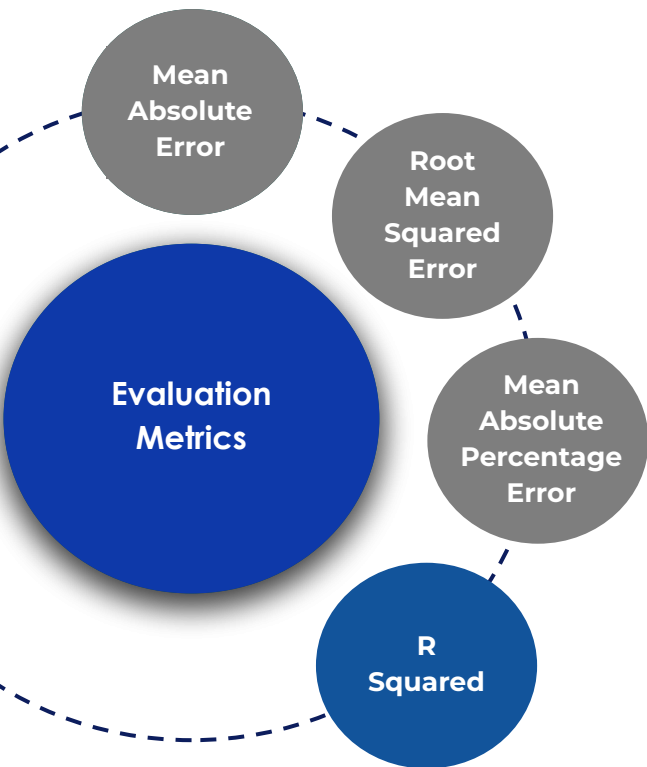
- Previous metrics do not clearly quantify how well the model explains the variability in the data

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# Evaluation Metrics



- Previous metrics do not clearly quantify how well the model explains the variability in the data

$$R^2 = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2}$$

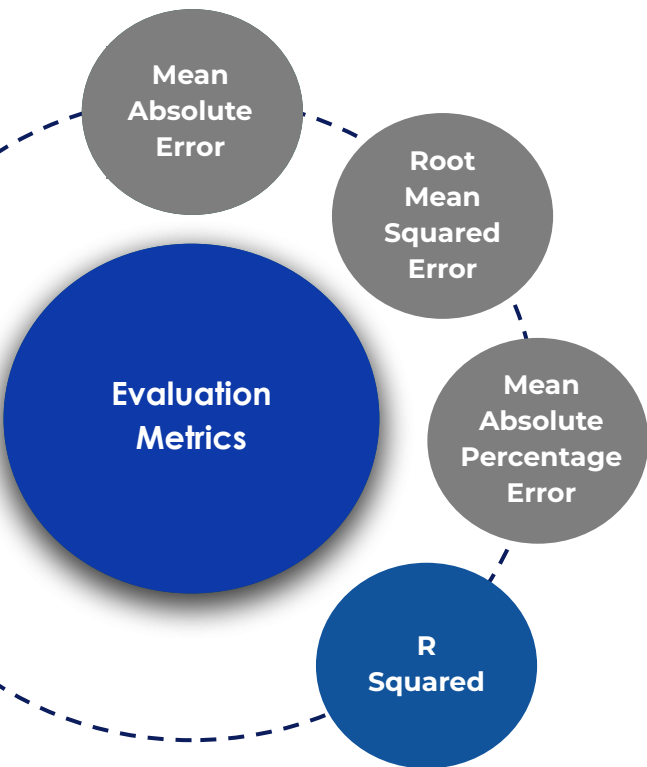
- Generally ranges between 0 and 1

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# Evaluation Metrics



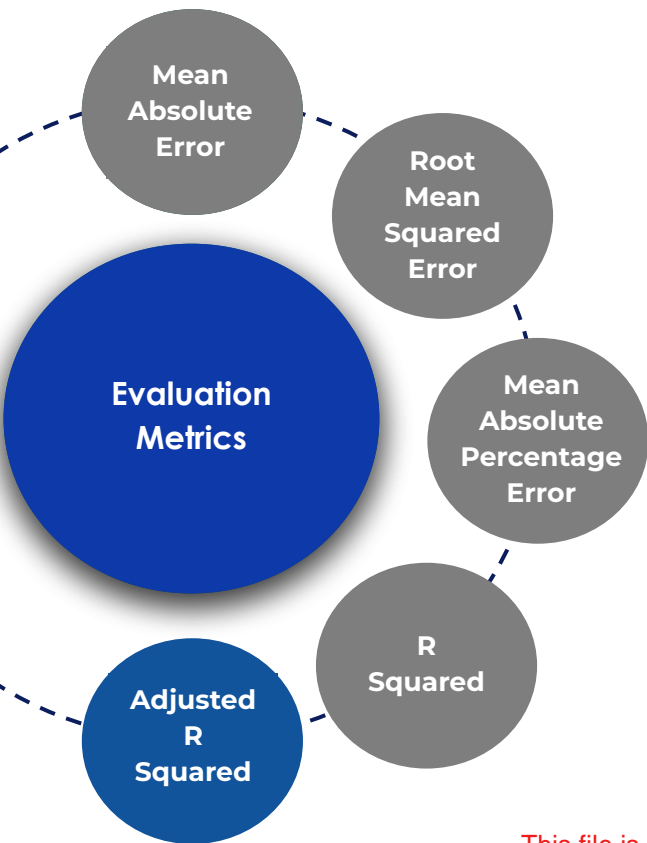
- Tends to increase when adding more explanatory variables
- Does not account for the value addition from the added explanatory variables

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# Evaluation Metrics



- Tends to increase when adding more explanatory variables
- Does not account for the value addition from the added explanatory variables

$$Adjusted R^2 = 1 - \frac{(1 - R^2) * (n - 1)}{n - k - 1}$$

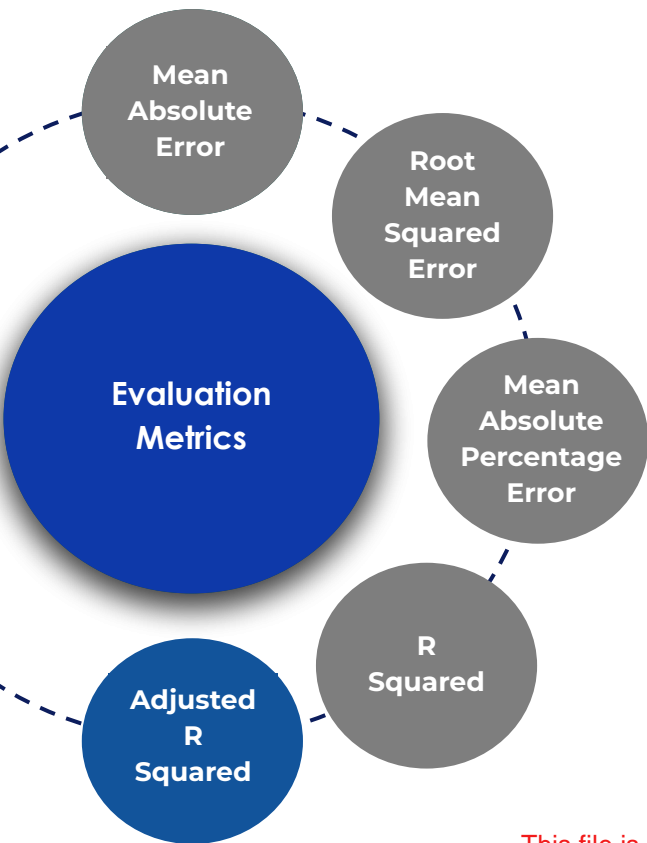
- Accounts for the number of explanatory variables in the model

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# Evaluation Metrics



- Gives a sense of which variables actually help in prediction and which ones do not
- Provides a balance between model fit and complexity (number of explanatory variables)

$$Adjusted R^2 = 1 - \frac{(1 - R^2) * (n - 1)}{n - k - 1}$$

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# Summary

Here's a quick recap of what we've learned:

- **Business Problem and Solution Space:** Identifies the specific problem that linear regression aims to solve and defines the scope of its application in business contexts.
- **Correlation and Linear Relationships:** Explores how correlation measures the strength and direction of linear relationships between variables, laying the foundation for understanding linear regression.
- **Simple Linear Regression:** Introduces the basic concept of simple linear regression, which models the relationship between a dependent variable and one independent variable using a straight line.

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# Summary

- **Multiple Linear Regression:** Expands on the concept of simple linear regression by incorporating multiple independent variables to predict a dependent variable, accommodating more complex relationships.
- **Categorical Variables in Regression:** Discusses strategies for encoding categorical variables in regression models to include qualitative data effectively in predictive analysis.
- **Evaluation Metrics for Regression:** Covers key metrics such as Mean Squared Error (MSE), R-squared, and others used to assess the accuracy and performance of regression models in predicting outcomes.

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# Learning Outcomes

You should now be able to:

- Explain how correlation measures the strength and direction of linear relationships, and apply this understanding to build simple linear regression models effectively.
- Gain proficiency in constructing and interpreting simple linear regression models to analyze and predict relationships between two variables.
- Develop multiple linear regression models to enable the prediction of business outcomes using multiple input variables.

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# Learning Outcomes

- Evaluate linear regression models using key metrics and implement strategies to enhance model performance and accuracy.
- Identify and apply linear regression techniques to solve various real-world business problems, leveraging its predictive capabilities across different domains.

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