

Table S1: Seesaw domain level sequences. Here and elsewhere all sequences start from the 5' end.

c	= CA	t	= TCT		
c*	= TG	t*	= AGA		
S1	= CATCCATTCCACTCA	S2	= CAAAACAAAACCTCA	S3	= CACCCTAAAAATCTCA
S1*	= TGAGTGGAATGGATG	S2*	= TGAGGTTTTGTTTTG	S3*	= TGAGATTTTAGGGTG
S4	= CACATAACAACCACA	S5	= CACCACCAAACCTCA	S6	= CATAACACAATCACA
S4*	= TGTGGTTGTTATGTG	S5*	= TGAAGTTTGGTGGTG	S6*	= TGTGATTGTGTTATG
S7	= CAACATATCAATTCA	S8	= CACTAACATACAACA	S9	= CACCATCAAATAACA
S7*	= TGAATTGATATGTTG	S8*	= TGTGTATGTATTAGTG	S9*	= TGTTATTTGATGGTG
S10	= CATAACAATCTACA	S11	= CAATATCCATAACCA	S12	= CATCAATCAACACCA
S10*	= TGTAGATGTTGTATG	S11*	= TGGTTATGGATATTG	S12*	= TGGTGTGATTGATG
S13	= CACAACCTATTACCA	S14	= CATTATTCAAACCCA	S15	= CACACTATAATTCCA
S13*	= TGGTAATGAGTTGTG	S14*	= TGGGTTTGAATAATG	S15*	= TGGAATTATAGTGTG
S16	= CACTTCATAAATCCA	S17	= CAACTCCTAATATCA	S18	= CATCTTCTAACATCA
S16*	= TGGATTATGAAGTG	S17*	= TGATATTAGGAGTTG	S18*	= TGATGTTAGAAGATG
S19	= CACCTCTTAAACACA	S20	= CAATCTAACACTCCA	S21	= CAACCATACTAAACA
S19*	= TGTGTTTAAGAGGTG	S20*	= TGGAGTGTTAGATTG	S21*	= TGTTTAGTATGGTTG
S22	= CATTCTACATTTCA	S23	= CAAATCTTCATCCCA	S24	= CACTCATCCTTTACA
S22*	= TGAAATGTAGGAATG	S23*	= TGGGATGAAGATTTG	S24*	= TGTAAGGATGAGTG
S25	= CAATCACTCAATCA	S26	= CATTCAATACCTCCA	S27	= CAAACACTCTATTCA
S25*	= TGATTGAGTGAATTG	S26*	= TGGAGGTAATGAATG	S27*	= TGAATAGAGTGTGTTG
S28	= CATCTACAATTCACA	S29	= CACCAATACTCCTCA	S30	= CACCATTACAATCCA
S28*	= TGTGAATTGTAGATG	S29*	= TGAGGAGTATTGGTG	S30*	= TGGATTGTAATGGTG
S31	= CAATCCACACTTCCA	S32	= CACACTTCAAACCTCA	S33	= CAACTCAAACATACA
S31*	= TGGAAGTGTTGATTG	S32*	= TGAGTTTGAAGTGTG	S33*	= TGTATGTTTGAGTTG
S34	= CACATAACAAAACCA	S35	= CACTCTCCATCACCA	S36	= CAAACTAAACAACCA
S34*	= TGGTTTTGTTATGTG	S35*	= TGGTGATGGAGAGTG	S36*	= TGGTTGTTTAGTTTG
S37	= CACCTCTTCCCTTCA	S38	= CATACCTTTTCTCA	S39	= CACTATACACACCCA
S37*	= TGAAGGGAAGAGGTG	S38*	= TGAGAAAAGGGTATG	S39*	= TGGGTGTGTATAGTG
S40	= CAATACAAATCCACA	S41	= CAACAAACCATTACA	S42	= CACTTTTCACTATCA
S40*	= TGTGGATTGTATTG	S41*	= TGTAATGGTTTGTTG	S42*	= TGATAGTGAAAAGTG
S43	= CATCATACCTACTCA	S44	= CAAACTCTCTCTCA	S45	= CACCCAAAACCCACA
S43*	= TGAGTAGGTATGATG	S44*	= TGAGAGAGAGTTTTG	S45*	= TGTGGGTTTTGGGTG
S46	= CAAACCCAACTCACA	S47	= CATTCTCCACCTCA	S48	= CATCACCCTATACA
S46*	= TGTGAGTTGGGTTTG	S47*	= TGAGGTGGGAGAATG	S48*	= TGTATAGTGGTGATG
S49	= CATCCTTAACTCCCA	S50	= CATTACCAACCACCA	S51	= CACAACTACATCCA
S49*	= TGGGAGTTAAGGATG	S50*	= TGGTGGTTGGTAATG	S51*	= TGGATGTAGTTTGTG
S52	= CACTTCACAACTACA	S53	= CATATCTAATCTCCA	Sf	= CATTTTTTTTTTTCA
S52*	= TGTAGTTGTGAAGTG	S53*	= TGGAGATTAGATATG		

Table S2: Seesaw small circuit sequences (part one). Shading indicates which strands were used in which circuits. P indicates PAGE purification by IDT, used only for input strands. H indicates HPLC purification by IDT, used only for reporter strand with fluorophores or quenchers. All other strands were ordered without any purification. See Fig. S16 for details of the clamp design that modifies the toehold T implementation.

Circuit number			1	2	3	4	5	6	7	8	9
$w_{5,6}$	= S6 T S5	= CATAACACAATCACA TCT CACCACCAAACCTCA									
G_{5-b}	= $T^* S5^* T^*$	= TG AGA TGAAGTTTGGTGGTG AGA TG									
$w_{5,7}$	= S7 T S5	= CAACATATCAATTCA TCT CACCACCAAACCTCA									
$Th_{2,5,5-t}$	= S5	= CACCACCAAACCTCA									
$Th_{2,5,5-b}$	= $s2^* T^* S5^*$	= TGTTTTG AGA TGAAGTTTGGTGGTG									
$w_{2,5}$	= S5 T S2	= CACCACCAAACCTCA TCT CAAAACAAAACCTCA	P	P							
G_{2-b}	= $T^* S2^* T^*$	= TG AGA TGAGGTTTTGTTTGTG AGA TG									
$w_{1,2}$	= S2 T S1	= CAAAACAAAACCTCA TCT CATCCATTCCACTCA			P						
G_{1-b}	= $T^* S1^* T^*$	= TG AGA TGAGTGAATGGATG AGA TG									
$w_{1,10}$	= S10 T S1	= CATAACAACATCTACA TCT CATCCATTCCACTCA									
$Th_{4,1,1-t}$	= S1	= CATCCATTCCACTCA									
$Th_{4,1,1-b}$	= $s4^* T^* S1^*$	= TTATGTG AGA TGAGTGAATGGATG									
$w_{4,1}$	= S1 T S4	= CATCCATTCCACTCA TCT CACATAACAACCACA									
G_{4-b}	= $T^* S4^* T^*$	= TG AGA TGTGTTTGTATGTG AGA TG									
$w_{3,2}$	= S2 T S3	= CAAAACAAAACCTCA TCT CACCCTAAAATCTCA			P	P	P	P			
G_{3-b}	= $T^* S3^* T^*$	= TG AGA TGAGATTTTAGGGTG AGA TG									
$w_{3,11}$	= S11 T S3	= CAATATCCATAACCA TCT CACCCTAAAATCTCA									
$Th_{12,3,3-t}$	= S3	= CACCCTAAAATCTCA									
$Th_{12,3,3-b}$	= $s12^* T^* S3^*$	= ATTGATG AGA TGAGATTTTAGGGTG									
$w_{12,3}$	= S3 T S12	= CACCCTAAAATCTCA TCT CATCAATCAACACCA									
G_{12-b}	= $T^* S12^* T^*$	= TG AGA TGGTGTGATTGATG AGA TG									
$w_{8,4}$	= S4 T S8	= CACATAACAACCACA TCT CACTAACATACAACA				P					
G_{8-b}	= $T^* S8^* T^*$	= TG AGA TGTTGTATGTTAGTG AGA TG									
$w_{8,15}$	= S15 T S8	= CACACTATAATTCCA TCT CACTAACATACAACA									
$Th_{16,8,8-t}$	= S8	= CACTAACATACAACA									
$Th_{16,8,8-b}$	= $s16^* T^* S8^*$	= TGAAGTG AGA TGTTGTATGTTAGTG									
$w_{16,8}$	= S8 T S16	= CACTAACATACAACA TCT CACTTCATAAATCCA									
G_{16-b}	= $T^* S16^* T^*$	= TG AGA TGGATTTATGAAGTG AGA TG									
$w_{17,16}$	= S16 T S17	= CACTTCATAAATCCA TCT CAACTCCTAATATCA					P				
G_{17-b}	= $T^* S17^* T^*$	= TG AGA TGATATTAGGAGTTG AGA TG									
$w_{17,19}$	= S19 T S17	= CACCTCTTAAACACA TCT CAACTCCTAATATCA									
$Th_{20,17,17-t}$	= S17	= CAACTCCTAATATCA									
$Th_{20,17,17-b}$	= $s20^* T^* S17^*$	= TAGATTG AGA TGATATTAGGAGTTG									
$w_{20,17}$	= S17 T S20	= CAACTCCTAATATCA TCT CAATCTAACACTCCA									
G_{20-b}	= $T^* S20^* T^*$	= TG AGA TGGAGTGTTAGATTG AGA TG									

Table S3: Seesaw small circuit sequences (part two). Shading indicates which strands were used in which circuits. P indicates PAGE purification by IDT, used only for input strands. H indicates HPLC purification by IDT, used only for reporter strand with fluorophores or quenchers. All other strands were ordered without any purification. See Fig. S16 for details of the clamp design that modifies the toehold *T* implementation.

Circuit number			1	2	3	4	5	6	7	8	9
$w_{21,20}$	= S20 T S21	= CAATCTAACACTCCA TCT CAACCATACTAAACA							P	P	P
$w_{22,20}$	= S20 T S22	= CAATCTAACACTCCA TCT CATTCCTACATTTC							P	P	P
$w_{18,16}$	= S16 T S18	= CACTTCATAAATCCA TCT CATCTTCTAACATCA						P	P	P	P
$w_{9,4}$	= S4 T S9	= CACATAACAACCACA TCT CACCATCAAATAACA			P	P	P	P	P	P	P
$w_{13,12}$	= S12 T S13	= CATCAATCAACACCA TCT CACAACCTCATTACCA							P	P	P
$w_{14,12}$	= S12 T S14	= CATCAATCAACACCA TCT CATTATTCAAACCCA							P	P	P
$w_{8,2}$	= S2 T S8	= CAAAACAAAACCTCA TCT CACTAACATAACAACA									
$w_{17,2}$	= S2 T S17	= CAAAACAAAACCTCA TCT CAACTCCTAATATCA									
$w_{23,4}$	= S4 T S23	= CACATAACAACCACA TCT CAAATCTTCATCCCA								P	
$w_{24,16}$	= S16 T S24	= CACTTCATAAATCCA TCT CACTCATCCTTTACA								P	
$w_{3,4}$	= S4 T S3	= CACATAACAACCACA TCT CACCCTAAAATCTCA									
$w_{3,16}$	= S16 T S3	= CACTTCATAAATCCA TCT CACCCTAAAATCTCA									
$w_{3,20}$	= S20 T S3	= CAATCTAACACTCCA TCT CACCCTAAAATCTCA									
$w_{1,23}$	= S23 T S1	= CAAATCTTCATCCCA TCT CATCCATTCCACTCA									
$w_{8,24}$	= S24 T S8	= CACTCATCCTTTACA TCT CACTAACATAACAACA									
$w_{17,25}$	= S25 T S17	= CAATTCACTCAATCA TCT CAACTCCTAATATCA									
$w_{22,2}$	= S2 T S22	= CAAAACAAAACCTCA TCT CATTCCTACATTTC									P
Rep ₆ -t	= RQ S6	= /5IAbRQ/ CATAACACAATCACA	H	H	H	H	H	H	H	H	H
Rep ₆ -b	= T* S6* ROX	= TG AGA TGTGATTGTGTTATG /3ROXN/	H	H	H	H	H	H	H	H	H
Rep ₂₃ -t	= FQ S23	= /5IAbFQ/ CAAATCTTCATCCCA									H
Rep ₂₃ -b	= T* S23* FAM	= TG AGA TGGGATGAAGATTTG /36-FAM/									H
Rep ₂₄ -t	= RQ S24	= /5IAbRQ/ CACTCATCCTTTACA									H
Rep ₂₄ -b	= T* S24* TYE563	= TG AGA TGTAAGGATGAGTG /3TYE563/									H
Rep ₂₅ -t	= RQ S25	= /5IAbRQ/ CAATTCACTCAATCA									H
Rep ₂₅ -b	= T* S25* TYE665	= TG AGA TGATTGAGTGAATTG /3TYE665/									H

Table S4: Seesaw square root circuit sequences (part one).

Gate strands (IDT unpurified)		
$w_{1,23}$	= S23 T S1	= CAAATCTTCATCCCA TCT CATCCATTCCACTCA
$w_{1,f}$	= Sf T S1	= CATTTTTTTTTTTTCA TCT CATCCATTCCACTCA
G_1-b	= $T^* S1^* T^*$	= TG AGA TGAGTGAATGGATG AGA TG
$Th_{10,1:1-t}$	= S1	= CATCCATTCCACTCA
$Th_{10,1:1-b}$	= $s10^* T^* S1^*$	= TTGTATG AGA TGAGTGAATGGATG
$w_{10,1}$	= S1 T S10	= CATCCATTCCACTCA TCT CATAACAACATCTACA
G_{10-b}	= $T^* S10^* T^*$	= TG AGA TGATAGTGTGTATG AGA TG
$w_{5,6}$	= S6 T S5	= CATAACACAATCACA TCT CACCACCAAACCTCA
$w_{5,f}$	= Sf T S5	= CATTTTTTTTTTTTCA TCT CACCACCAAACCTCA
G_5-b	= $T^* S5^* T^*$	= TG AGA TGAAGTTTGGTGGTG AGA TG
$Th_{53,5:5-t}$	= S5	= CACCACCAAACCTCA
$Th_{53,5:5-b}$	= $s53^* T^* S5^*$	= AGATATG AGA TGAAGTTTGGTGGTG
$w_{53,5}$	= S5 T S53	= CACCACCAAACCTCA TCT CATATCTAATCTCCA
G_{53-b}	= $T^* S53^* T^*$	= TG AGA TGGAGATTAGATATG AGA TG
$w_{8,25}$	= S25 T S8	= CAATTCACCTCAATCA TCT CACTAACATACAACA
$w_{8,f}$	= Sf T S8	= CATTTTTTTTTTTTCA TCT CACTAACATACAACA
G_8-b	= $T^* S8^* T^*$	= TG AGA TGTGTATGTTAGTG AGA TG
$Th_{20,8:8-t}$	= S8	= CACTAACATACAACA
$Th_{20,8:8-b}$	= $s20^* T^* S8^*$	= TAGATTG AGA TGTTGTATGTTAGTG
$w_{20,8}$	= S8 T S20	= CACTAACATACAACA TCT CAATCTAACACTCCA
G_{20-b}	= $T^* S20^* T^*$	= TG AGA TGGAGTGTTAGATTG AGA TG
$w_{13,24}$	= S24 T S13	= CACTCATCCTTTACA TCT CACAACCTCATTACCA
$w_{13,f}$	= Sf T S13	= CATTTTTTTTTTTTCA TCT CACAACCTCATTACCA
G_{13-b}	= $T^* S13^* T^*$	= TG AGA TGTAATGAGTTGTG AGA TG
$Th_{26,13:13-t}$	= S13	= CACAACCTCATTACCA
$Th_{26,13:13-b}$	= $s26^* T^* S13^*$	= ATGAATG AGA TGGTAATGAGTTGTG
$w_{26,13}$	= S13 T S26	= CACAACCTCATTACCA TCT CATTCTTACCTCCA
G_{26-b}	= $T^* S26^* T^*$	= TG AGA TGGAGGTAATGAATG AGA TG
$w_{18,53}$	= S53 T S18	= CATATCTAATCTCCA TCT CATCTTCTAACATCA
$w_{18,f}$	= Sf T S18	= CATTTTTTTTTTTTCA TCT CATCTTCTAACATCA
G_{18-b}	= $T^* S18^* T^*$	= TG AGA TGATGTTAGAAGATG AGA TG
$Th_{34,18:18-t}$	= S18	= CATCTTCTAACATCA
$Th_{34,18:18-b}$	= $s34^* T^* S18^*$	= TTATGTG AGA TGATGTTAGAAGATG
$w_{34,18}$	= S18 T S34	= CATCTTCTAACATCA TCT CACATAACAAAACCA
G_{34-b}	= $T^* S34^* T^*$	= TG AGA TGGTTTTGTTATGTG AGA TG

Table S5: Seesaw square root circuit sequences (part two).

$w_{21,10}$	= S10 T S21	= CATACAACATCTACA TCT CAACCATACTAAACA
$w_{21,f}$	= Sf T S21	= CATTTTTTTTTTTTCA TCT CAACCATACTAAACA
G_{21-b}	= $T^* S_{21}^* T^*$	= TG AGA TGTTTAGTATGGTTG AGA TG
$Th_{36,21:21-t}$	= S21	= CAACCATACTAAACA
$Th_{36,21:21-b}$	= $s_{36}^* T^* S_{21}^*$	= TAGTTTG AGA TGTTTAGTATGGTTG
$w_{36,21}$	= S21 T S36	= CAACCATACTAAACA TCT CAACTAAACAACCA
G_{36-b}	= $T^* S_{36}^* T^*$	= TG AGA TGGTTGTTTAGTTTG AGA TG
$w_{22,53}$	= S53 T S22	= CATATCTAATCTCCA TCT CATTCTACATTTCA
$w_{22,f}$	= Sf T S22	= CATTTTTTTTTTTTCA TCT CATTCTACATTTCA
G_{22-b}	= $T^* S_{22}^* T^*$	= TG AGA TGAAATGTAGGAATG AGA TG
$Th_{39,22:22-t}$	= S22	= CATTCTACATTTCA
$Th_{39,22:22-b}$	= $s_{39}^* T^* S_{22}^*$	= TATAGTG AGA TGAAATGTAGGAATG
$w_{39,22}$	= S22 T S39	= CATTCTACATTTCA TCT CACTATACACACCCA
G_{39-b}	= $T^* S_{39}^* T^*$	= TG AGA TGGGTGTGTATAGTG AGA TG
$w_{27,10}$	= S10 T S27	= CATACAACATCTACA TCT CAAACACTCTATTCA
$w_{27,f}$	= Sf T S27	= CATTTTTTTTTTTTCA TCT CAAACACTCTATTCA
G_{27-b}	= $T^* S_{27}^* T^*$	= TG AGA TGAATAGAGTGTTTG AGA TG
$Th_{40,27:27-t}$	= S27	= CAAACACTCTATTCA
$Th_{40,27:27-b}$	= $s_{40}^* T^* S_{27}^*$	= TGTATTG AGA TGAATAGAGTGTTTG
$w_{40,27}$	= S27 T S40	= CAAACACTCTATTCA TCT CAATACAAATCCACA
G_{40-b}	= $T^* S_{40}^* T^*$	= TG AGA TGTGGATTTGTATTG AGA TG
$w_{28,34}$	= S34 T S28	= CACATAACAAAACCA TCT CATCTACAATTCACA
$w_{28,40}$	= S40 T S28	= CAATACAAATCCACA TCT CATCTACAATTCACA
$w_{28,f}$	= Sf T S28	= CATTTTTTTTTTTTCA TCT CATCTACAATTCACA
G_{28-b}	= $T^* S_{28}^* T^*$	= TG AGA TGTGAATTGTAGATG AGA TG
$Th_{41,28:28-t}$	= S28	= CATCTACAATTCACA
$Th_{41,28:28-b}$	= $s_{41}^* T^* S_{28}^*$	= TTTGTTG AGA TGTGAATTGTAGATG
$w_{41,28}$	= S28 T S41	= CATCTACAATTCACA TCT CAACAAACCATTACA
G_{41-b}	= $T^* S_{41}^* T^*$	= TG AGA TGTAATGGTTTGTTG AGA TG
$w_{29,36}$	= S36 T S29	= CAACTAAACAACCA TCT CACCAATACTCCTCA
$w_{29,39}$	= S39 T S29	= CACTATACACACCCA TCT CACCAATACTCCTCA
$w_{29,f}$	= Sf T S29	= CATTTTTTTTTTTTCA TCT CACCAATACTCCTCA
G_{29-b}	= $T^* S_{29}^* T^*$	= TG AGA TGAGGAGTATTGGTG AGA TG
$Th_{42,29:29-t}$	= S29	= CACCAATACTCCTCA
$Th_{42,29:29-b}$	= $s_{42}^* T^* S_{29}^*$	= AAAAGTG AGA TGAGGAGTATTGGTG
$w_{42,29}$	= S29 T S42	= CACCAATACTCCTCA TCT CACTTTTCACTATCA
G_{42-b}	= $T^* S_{42}^* T^*$	= TG AGA TGATAGTGAAAAGTG AGA TG

Table S6: Seesaw square root circuit sequences (part three).

$w_{30,40}$	= S40 T S30	= CAATACAAATCCACA TCT CACCATTACAATCCA
$w_{30,f}$	= Sf T S30	= CATT TTT TTT TTT TTT TCA TCT CACCATTACAATCCA
G_{30-b}	= $T^* S30^* T^*$	= TG AGA TGGATTGTAATGGTG AGA TG
$Th_{43,30:30-t}$	= S30	= CACCATTACAATCCA
$Th_{43,30:30-b}$	= $s43^* T^* S30^*$	= TATGATG AGA TGGATTGTAATGGTG
$w_{43,30}$	= S30 T S43	= CACCATTACAATCCA TCT CATCATACCTACTCA
G_{43-b}	= $T^* S43^* T^*$	= TG AGA TGAGTAGGTATGATG AGA TG
$w_{31,39}$	= S39 T S31	= CACTATACACACCCA TCT CAATCCACACTTCCA
$w_{31,f}$	= Sf T S31	= CATT TTT TTT TTT TTT TCA TCT CAATCCACACTTCCA
G_{31-b}	= $T^* S31^* T^*$	= TG AGA TGAAGTGTGGATTG AGA TG
$Th_{44,31:31-t}$	= S31	= CAATCCACACTTCCA
$Th_{44,31:31-b}$	= $s44^* T^* S31^*$	= AGTTT TG AGA TGAAGTGTGGATTG
$w_{44,31}$	= S31 T S44	= CAATCCACACTTCCA TCT CAAAAC TCTCTCTCA
G_{44-b}	= $T^* S44^* T^*$	= TG AGA TGAGAGAGAGTTTTG AGA TG
$w_{33,34}$	= S34 T S33	= CACATAACAAAACCA TCT CAACTCAAACATACA
$w_{33,43}$	= S43 T S33	= CATCATACCTACTCA TCT CAACTCAAACATACA
$w_{33,26}$	= S26 T S33	= CATT CATTACCTCCA TCT CAACTCAAACATACA
$w_{33,f}$	= Sf T S33	= CATT TTT TTT TTT TTT TCA TCT CAACTCAAACATACA
G_{33-b}	= $T^* S33^* T^*$	= TG AGA TGTATGTTTGAGTTG AGA TG
$Th_{49,33:33-t}$	= S33	= CAACTCAAACATACA
$Th_{49,33:33-b}$	= $s49^* T^* S33^*$	= AAGGATG AGA TGTATGTTTGAGTTG
$w_{35,36}$	= S36 T S35	= CAAACTAAACAACCA TCT CACTCTCCATCACCA
$w_{35,44}$	= S44 T S35	= CAAACTCTCTCTCA TCT CACTCTCCATCACCA
$w_{35,20}$	= S20 T S35	= CAATCTAACACTCCA TCT CACTCTCCATCACCA
$w_{35,f}$	= Sf T S35	= CATT TTT TTT TTT TTT TCA TCT CACTCTCCATCACCA
G_{35-b}	= $T^* S35^* T^*$	= TG AGA TGGTGATGGAGAGTG AGA TG
$Th_{50,35:35-t}$	= S35	= CACTCTCCATCACCA
$Th_{50,35:35-b}$	= $s50^* T^* S35^*$	= GGTAATG AGA TGGTGATGGAGAGTG
$w_{37,34}$	= S34 T S37	= CACATAACAAAACCA TCT CACCTCTTCCCTTCA
$w_{37,44}$	= S44 T S37	= CAAACTCTCTCTCA TCT CACCTCTTCCCTTCA
$w_{37,26}$	= S26 T S37	= CATT CATTACCTCCA TCT CACCTCTTCCCTTCA
$w_{37,f}$	= Sf T S37	= CATT TTT TTT TTT TTT TCA TCT CACCTCTTCCCTTCA
G_{37-b}	= $T^* S37^* T^*$	= TG AGA TGAAGGGAAGAGGTG AGA TG
$Th_{51,37:37-t}$	= S37	= CACCTCTTCCCTTCA
$Th_{51,37:37-b}$	= $s51^* T^* S37^*$	= GTTTGTG AGA TGAAGGGAAGAGGTG

Table S7: Seesaw square root circuit sequences (part four).

$w_{38,36}$	= S36 T S38	= CAAACTAAACAACCA TCT CATACCCTTTTCTCA
$w_{38,43}$	= S43 T S38	= CATCATACCTACTCA TCT CATACCCTTTTCTCA
$w_{38,20}$	= S20 T S38	= CAATCTAACACTCCA TCT CATACCCTTTTCTCA
$w_{38,f}$	= Sf T S38	= CATTTTTTTTTTTTCA TCT CATACCCTTTTCTCA
G_{38-b}	= T* S38* T*	= TG AGA TGAGAAAAGGGTATG AGA TG
$Th_{52,38:38-t}$	= S38	= CATACCCTTTTCTCA
$Th_{52,38:38-b}$	= s52* T* S38*	= TGAAGTG AGA TGAGAAAAGGGTATG
Reporter strands (IDT HPLC purified)		
Rep_6-t	= RQ S6	= /5IAbRQ/ CATAACACAATCACA
Rep_6-b	= T* S6* ROX	= TG AGA TGTGATTGTGTTATG /3ROXN/
Rep_{23-t}	= FQ S23	= /5IAbFQ/ CAAATCTTCATCCCA
Rep_{23-b}	= T* S23* FAM	= TG AGA TGGGATGAAGATTG /36-FAM/
Rep_{24-t}	= RQ S24	= /5IAbRQ/ CACTCATCCTTTTACA
Rep_{24-b}	= T* S24* TYE563	= TG AGA TGTAAGGATGAGTG /3TYE563/
Rep_{25-t}	= RQ S25	= /5IAbRQ/ CAATTCACCTCAATCA
Rep_{25-b}	= T* S25* TYE665	= TG AGA TGATTGAGTGAATTG /3TYE665/
Input strands (IDT PAGE purified)		
$x_1^0 : w_{45,42}$	= S42 T S45	= CACTTTTCACTATCA TCT CACCCAAAACCCACA
$x_1^1 : w_{46,41}$	= S41 T S46	= CAACAAACCATTACA TCT CAAACCCAACTCACA
$x_2^0 : w_{47,42}$	= S42 T S47	= CACTTTTCACTATCA TCT CATTCTCCACCTCA
$x_2^1 : w_{48,41}$	= S41 T S48	= CAACAAACCATTACA TCT CATCACCACCTATACA
$x_3^0 : w_{49,33}$	= S33 T S49	= CAACTCAAACATACA TCT CATCCTTAACTCCCA
$x_3^1 : w_{50,35}$	= S35 T S50	= CACTCTCCATCACCA TCT CATTACCAACCACCA
$x_4^0 : w_{51,37}$	= S37 T S51	= CACCTCTTCCCTTCA TCT CACAACTACATCCA
$x_4^1 : w_{52,38}$	= S38 T S52	= CATACCCTTTTCTCA TCT CACTTCACAACCTACA
Internal fan-out strands for readout (IDT unpurified)		
$w_{21,32}$	= S32 T S21	= CACACTTCAAACCTCA TCT CAACCATACTAAACA
$w_{28,32}$	= S32 T S28	= CACACTTCAAACCTCA TCT CATCTACAATTCACA
$w_{31,32}$	= S32 T S32	= CACACTTCAAACCTCA TCT CAATCCACACTTCCA
Internal readout reporter strands (IDT HPLC purified)		
Rep_{32-t}	= RQ S32	= /5IAbRQ/ CACACTTCAAACCTCA
Rep_{32-b}	= T* S32* Cy5.5	= TG AGA TGAGTTTGAAGTGTG /3Cy55Sp/

Table S8: Seesaw sequences without clamps.

Domain level sequences			
T	= CTCT	T*	= AGAG
S1	= CATCCATTCCACTAT	S2	= CCAAACAAAACCTAT
S1*	= ATAGTGAATGGATG	S2*	= ATAGGTTTTGTTTGG
S4	= AACAAAACAACCACT	S5	= AACCACCAAACCTTAT
S4*	= AGTGGTTGTTTTGTT	S5*	= ATAAGTTTGGTGGTT
S7	= CCACAAAACAAAACCT	S8	= CCCAAATAAACAACT
S10	= TCAAAACCAACTACT	S9	= CACCATCAAATAACT
Gate strands (IDT unpurified)			
w _{5,6}	= S6 T S5	= CCTAACACAATCACT CTCT AACCACCAAACCTTAT	
G _{5-b}	= T* S5* T*	= AGAG ATAAGTTTGGTGGTT AGAG	
w _{5,7}	= S7 T S5	= CCACAAAACAAAACCT CTCT AACCACCAAACCTTAT	
Th _{2,5:5-t}	= S5	= AACCACCAAACCTTAT	
Th _{2,5:5-b}	= s2* T* S5*	= TTTGG AGAG ATAAGTTTGGTGGTT	
w _{2,5}	= S5 T S2	= AACCACCAAACCTTAT CTCT CCAAACAAAACCTAT	
G _{2-b}	= T* S2* T*	= AGAG ATAGGTTTTGTTTGG AGAG	
w _{1,2}	= S2 T S1	= CCAAACAAAACCTAT CTCT CATCCATTCCACTAT	
G _{1-b}	= T* S1* T*	= AGAG ATAGTGAATGGATG AGAG	
w _{1,10}	= S10 T S1	= TCAAAACCAACTACT CTCT CATCCATTCCACTAT	
Th _{4,1:1-t}	= S1	= CATCCATTCCACTAT	
Th _{4,1:1-b}	= s4* T* S1*	= TTGTT AGAG ATAGTGAATGGATG	
w _{4,1}	= S1 T S4	= CATCCATTCCACTAT CTCT AACAAAACAACCACT	
G _{4-b}	= T* S4* T*	= AGAG AGTGGTTGTTTTGTT AGAG	
Reporter strands (IDT HPLC purified)			
Rep _{5,6-t}	= RQ S6 T	= /5IAbRQ/ CCTAACACAATCACT CTCT	
Rep _{5,6-b}	= s5* T* S6* ROX	= TGGTT AGAG AGTGATTGTGTTAGG/3ROXN/	
Input strands (IDT PAGE purified)			
w _{3,2}	= S2 T S3	= CCAAACAAAACCTAT CTCT CACCCTAAAATCTAT	
w _{8,4}	= S4 T S8	= AACAAAACAACCACT CTCT CCCAAATAAACAACT	
w _{9,4}	= S4 T S9	= AACAAAACAACCACT CTCT CACCATCAAATAACT	

Table S9: Seesaw hairpin sequences.

Domain level sequences			
T	= TGAGG	T*	= CCTCA
S1	= TAGTTGGAAGAGGGC	S3	= GATGTAAGTATTTGC
S1*	= GCCCTCTTCCAACATA	S3*	= GCAAATACTTACATC
S2	= GGATTAGGGGGTAGC	S4	= AGTATGTAGTGTGGC
		S4*	= GCCACACTACATACT
Excised hairpin sequences with restriction enzyme recognition sites			
EH-Hgal	= NNNNNNNNNNGCGTCNTTTTNGACGCNNNNN		
EH-MlyI	= NNNNNGACTCNTTTTNGAGTCNNNNN		
Gate strands (IDT unpurified)			
G _{3:3,1} -h	= S1 T S3 EH-Hgal T* S3* T*	= TAGTTGGAAGAGGGC TGAGG GATGTAAGTATTTGC TGAGGCGCTGGCGTCGTTTTCGACGCCAGCG CCTCA GCAAATACTTACATC CCTCA	
w _{3,2}	= S2 T S3	= GGATTAGGGGGTAGC TGAGG GATGTAAGTATTTGC	
Th _{4,3:3} -h	= s4* T* S3* EH-MlyI S3	= ACT CCTCA GCAAATACTTACATC AACCAGACTCGTTTTTCGAGTCTGGTT GATGTAAGTATTTGC	
Reporter strands (IDT HPLC purified)			
Rep ₁ -t	= TET S1	= /5TET/ TAGTTGGAAGAGGGC	
Rep ₁ -b	= T* S1* BHQ	= CCTCA GCCCTCTTCCAACATA /3BHQ_1/	
Input strands (IDT unpurified)			
w _{4,3}	= S3 T S4	= GATGTAAGTATTTGC TGAGG AGTATGTAGTGTGGC	