

## Arrays

Leet-1 (2/12/2020)

- ① separate +ve and -ve numbers.
- ② separate 0, and 1.
- ③ 283 | Move zeroes.
- ④ Separate 0, 1, 2.
- ⑤ 75 | Separate colors.
- ⑥ 189 | Rotate array.
- ⑦ MAX sum of array and its index.

Leet-2 (6/12/2020)

- ① 3 | longest substring without repeating characters
- ② 76 | min window substring.

Leet-3 (8/12/2020)

- ① smallest window containing itself (777)
- ② 159 | find k distinct element in window?
- ③ 340 |
- ④ max vowel letter in any substring (1456)
- ⑤ count unique substring with non-repeating characters.
- ⑥ 239 | sliding window maximum.

Leet-4 (9/12/2020)

- ① longest subarray with equal no. of 0 and 1 ↗ same  
525
- ③ count subarray with equal no. of 0 & 1 ↗ ②
- ④ longest subarray with sum divisible by k ↗ ③
- ⑤ 974 subarray sum divisible by k ↗ ④
- ⑥ 781 rabbit in forest ↗ ⑤

## Lect-5 (11/12/2020) Notebook-3.

- ① 930 | count SubArray with sum equal to K
- ② 1248 | Count no. of nice subarray.
- ③ 1004 | Max consecutive one - III bitmasks
- ④ 904 | fruit into Basket || longest subarray with atmost K distinct character
- ⑤ 209 | min size subarray sum.

## Lect-6 (13/12/2020).

- ① Kadane algorithm.
- ② K-concatenation: maximum sum (10/1191)

## Lect-7 (14/12/2020). part 2

- ① 1077 | number of subarrays sum Target
- ② 363 | max sum of submatrix. Rest. sum not larger than k.
- ③ max product.

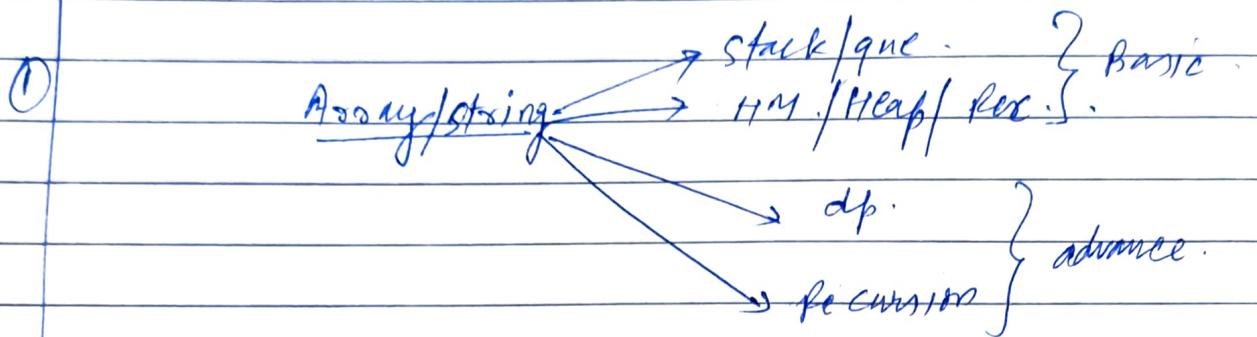
Assays | String      leet - 1

2/12/2020.

agenda-

- ① Separate +ve and negative numbers. ] 4(5) (same)
- ② Separate 0 and 1
- ③ Separate 0, 1, 2 ] same
- ④ 75 Sort colors. S: O(1), T: O(n).
- ⑤ 283. / Move zeroes.
- ⑥ 189 / Rotate Array.
- ⑦ Max sum of array and its index.

① Arrays:-



② Sorting

③ Binary Search.

④ Rotation.

Ques Separate +ve and negative numbers.

What? Given array with mixed +ve and negative separate them.

I/P = {12, 11, -13, -5, 6, -7, 5, -3, -6}

O/P = {-13, -5, -7, -3, -6, 12, 11, 6, 5}

Approach 1.

Keep left and right pointers and set your regions.  
 say left for →  $\ominus$  ve  
 right for →  $\oplus$  ve.

②

⊖

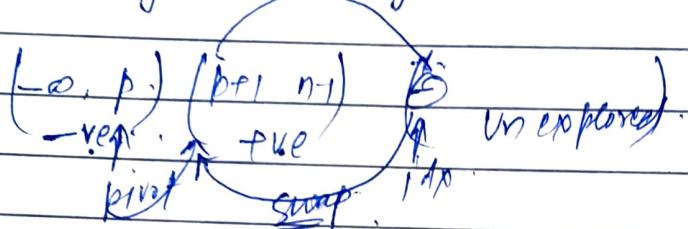
⊕

If get +ve on the left then left ++ when get -ve then  
 if +ve on right then right --  
 when ⊖ve then sink left

and swap (are cleff), are (right)).

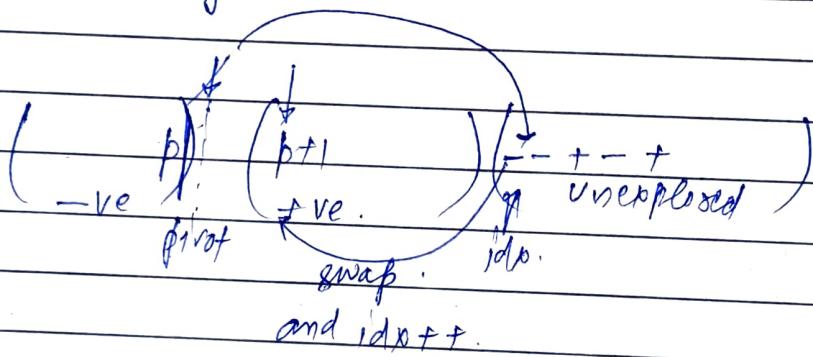
Approach 2:-

defined region and given them indexing.

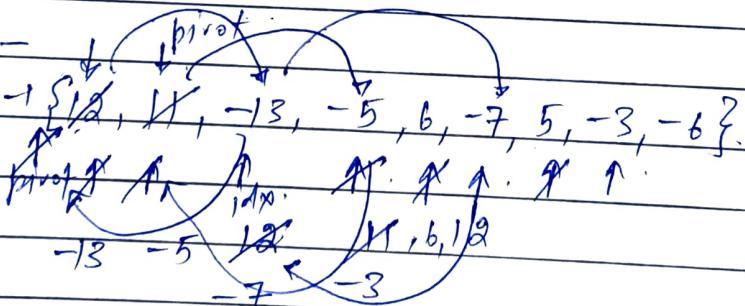


and -ve Region (Res).

- and +ve region get a guaranteed +ve so.
- $idx++$ .
- Unexplored region +ve.



dry Run:-



do this way.

Question 1, 2, 4 and 5 done using this Method

Code -

$\text{pivot} = -1, \text{id}x = 0.$

$\text{while } (\text{id}x < n) \{$

$\text{if } (\text{arr}[\text{id}x] == 0) \{$

$\text{swap}(\text{arr}, \text{tmp}[\text{id}x], \text{id}x);$

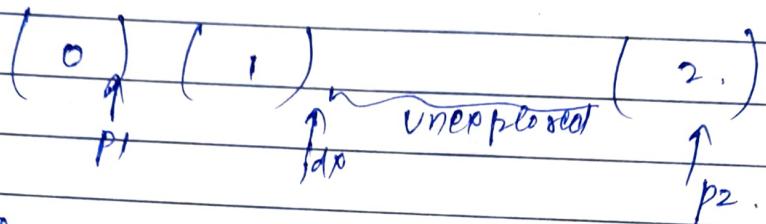
$\text{id}x++;$

$\}$ .

3. One separate 0, 1, 2 // [lc-75]

0	0	1	1	0	0	1	1	0	0	0
0	1	2	3	4	5	6	7	8	9	10.

define Region-



Algorithm.

- ① if arr(idx) = 0 swap with p1 and 1 idx because p1 is greater than arr[idx]
- ② if (arr(idx) = 2) swap with p2  
but don't ↑ idx because don't know about p arr(p2) element.
- ③ arr(idx) = 1 then idx++;

↓ p2,

day run:-

X	+ 0	2X	1	1	2	0	1	0	1	2	2	↓
0	0	X	1	1	X	2	0	1	0	1	2	
p1	p1	p2	2	3	4	5	6	7	8	9	10	
idx	↑	↑	↑	↑	↑	↑	↑	↑	↑	↑	↑	

we get

0	0	0	0	0	1	1	1	1	2	2	2	2
0	1	2	3	4	5	6	7	8	9	10	11	12

Code:

```
public void sortColors( int[] arr ) {  
    if ( arr.length == 0 ) {  
        return;  
    }  
    int p1 = -1, idx = 0, n = arr.length, p2 = n-1;  
    while ( idx <= p2 ) {  
        if ( arr[ idx ] == 0 ) {  
            swap( arr, idx, p1 );  
        } else if ( arr[ idx ] == 2 ) {  
            swap( arr, idx, p2 );  
            p2--;  
        } else {  
            idx++;  
        }  
    }  
}
```

Ques. 189 Rotate Array.

What :- Rotate Array to right by  $k$  ( $k > 0$ )

$$\text{I/P} = [1, 2, 3, 4, 5, 6, 7], \quad k=3$$

$$\text{O/P} = [5, 6, 7, 1, 2, 3, 4]$$

How :- We do this in two steps.

First reverse  $(0, k-1)$ . and reverse  $(k, n-1)$

Now reverse  $(p_1, p_2)'$

which will become nothing but.

$p_2-p_1$

$(0, k-1) \rightarrow (n-k, n-1)$ .

e.g.  $(4, 3, 2, 1, 7, 6, 5, 3)$ .

O/P: ~~4, 3, 2, 1, 7, 6, 5, 3~~  $(5, 6, 7, 1, 2, 3, 4)$ .

e.g. we have ab c de

-i	b	c	d	e	a	→ same as $k+l = -1+5$ = 4
0	a	b	c	d	e	
1	e	a	b	c	d	
2	d	e	a	b	c	
3	c	d	e	a	b	
4	e	d	c	b	a	
5	a	b	c	d	e	same
6	e	a	b	c	d	

different cases for k

① if  $k \geq a.l.$

$$k = k \% a.l.$$

② if  $k < 0$

( $a = \text{array size}$ )

$$k = (k + a.\text{length}) \% a.\text{length}.$$

Algorithm:

reverse ( $0, n-k-1$ ) and  $\text{reverse}(n-k, n-1)$ .

①  $P_1$  and  $P_2$

②  $P'_1$  and  $P'_2$  (reverse individual).

③  $P''_1$  and  $P''_2$

( $P_2$  and  $P_1$ ) will be our answer.

II code:-

① reverse : Public void reverse(int arr, int i, int j) {  
    while (i < j) {  
        swap(i++, j--);  
    }

}

?

Public void swap(int arr[], int i, int j) {  
    int temp = arr[i];  
    arr[i] = arr[j];  
    arr[j] = temp;

?

Public void rotate( int arr[], int k) {

if (arr.length == 0) return;

$k = (k \cdot n + n) \% n;$  // it handles all  $k$  (eve, -ve, all)  
[0, n]:

int n = arr.length;

reverse(arr, 0, n-1);

reverse(0, k-1);

reverse(k, n-1).

2.

3.

if we do first reversal of  $(0, n)$  then this algo work

if we do first part reversal then

①  $(0, n-k), ② (n-k, n-1)$ .

②  $(0, n-1)'$

Ques. Max sum of  $\sum_{i=0}^{n-1} a_i$  among all rotation of a given array (of  $n$ )

What :-

$$arr[] = \{8, 3, 1, 2\}$$

$$O/P = 29.$$

$$\textcircled{1} \quad \{8, 3, 1, 2\} = 8 \times 0 + 3 \times 1 + 1 \times 2 + 2 \times 3 = 11$$

$$\textcircled{2} \quad \{3, 1, 2, 8\} = 3 \times 0 + 1 \times 1 + 2 \times 2 + 3 \times 8 = 29.$$

$$\textcircled{3} \quad \{1, 2, 8, 3\} = 1 \times 0 + 2 \times 1 + 8 \times 2 + 3 \times 3 = 27$$

$$\textcircled{4} \quad \{2, 8, 3, 1\} = 2 \times 0 + 8 \times 1 + 3 \times 2 + 1 \times 3 = 17$$

$$\max(1, 2, 3, 4) = \underline{29}.$$

App:-  $T = O(n^2)$ .

① Rotate array for all value 0 to  $n$ .

② Calculate sum for each rotation.

③ check if max sum is greater than current sum  
then update.

App-2  $O(n)$

Given we have  $a, b, c, d \Rightarrow ax_0 + bx_1 + cx_2 + dx_3$ .

$$bx_0 + cx_1 + dx_2 + ax_3$$

$$\text{or } bx_{(1-1)} + cx_{(2-1)} + dx_{(3-1)} + ax_{(4-1+4)}$$

$$\text{or } (ax_0 + bx_1 + cx_2 + dx_3) - (a+b+c+d) + ax(i)n$$

eg.  $\left[ (a(0) + b(1) + c(2) + d(3)) - (a+b+c+d) + ax(i)n \right]$

Rotated sum       $\rightarrow$  Self sum

Algorithm :-

- ① calculate sum of all element
- ② calculate value  $\times$  index for element
- ③ for first rotation sum.

$$\text{rotated sum} = (\text{prev sum} - \text{sum} + nx \text{arr}(i))$$

II Code

```
public int maxSumInRotation(int arr[]) {
    int sum = 0, rotatedSum = 0, n = arr.length;
    for (int ele : arr) sum += ele;
    for (int i = 0; i < arr.length; i++) rotatedSum =
        int maxSum = rotatedSum;
    for (i = 0, i < n, i++) {
        rotatedSum = rotatedSum - sum + arr(i) * n;
        maxSum = max(rotatedSum, maxSum);
    }
}
```

return maxSum;

3.

Lecture-2 (Array)06/12/2020Agenda :-

- ① 3 // Longest substring without repeating characters
- ② 76 // Minimum window substring.

- ③ Ques :- 3 // Longest substring without Repeat character.

what :- find the length of longest substring without Repeating character.

s : a b c a b c b b.

$$O/P = 3.$$

a b c.

How :- These problems are like Sliding window and done using 2 step.

take si, ei two pointers.

- ① acquire till condition does not met (here count).
- ② settle till condition to make valid (here count).

- ③ release (P si)

and Count max lengtho bet si and ei.

dryRun: $\downarrow$   
 $s_i \uparrow$ 

abc ab c babb abcd e a

 $b_i \uparrow$ 

(to check repetition):

a -  $\neq 1$ 

b - 1

c - 1

 $\rightarrow \text{count} = \neq 3$ 

len =

si =

ei =

// code:

public int lengthOfLongestSubstring(String s){  
 if(s.length() <= 1) {

return s.length();

int n = s.length(), si = 0, ei = 0, count = 0, len = 0;

int maxSi = 0, MaxEi = 0;

int[] map = new int[128];

while(ei &lt; n) {

if(map[s.charAt(ei++)]++ &gt; 0) count++;

Note :-

Here all post ↑ run after token in next line of if.  
 and evaluation done from right  
 ↓.

means   ↑    count ++ ↑

then condition check

the first ↑

ei ++ ↑  
etc.

while ( count > 0 ) {

if ( map[ s.charAt( ei + i ) ] - - > 1 ) count--;

3.

if ( ei - si > len ) {

len = ei - si;

Maxei = ei;

Maxsi = si;

3.

return len;

3.

② Qn 76. Leetcode

## Ques 76 // Minimum Window Substring.

What :- Return min window in 'S' containing all character of 'T'

I/P = A D O B E C O D E B A N C      t = ABC.

O/P = B A N C.

How :- It is a kind of sliding window and work in 3 step.

- ① acquire , ② settle ③ Release.

### Algorithm:-

- ① Make 4 variables: si, ei, head, length and requirement.
- ② Make freq map of array to store freq of each character in string.
- ③ Now loop through the string.
  - ① if (Freq(s(ei)) > 0) requirement--;
  - ② while (requirement == 0) {
    - ① length cal and updation.
    - ② si ~~at~~ ~~at~~, ~~at~~ & check ~~at~~ ~~at~~ whether it is part of answer or not  
if not part the ↑ requirement.

dry Run:  $\downarrow$

$s = \text{ODDABE CODEBANC}$

$d: 1 2 3 4 5 6 7 8 9 10 11 12 13$

$\text{# AKAKAKA}$

$t = ABC$

A - X0.

head =

B - Y0.

$x_1 =$

C - Y0.

$e_1 =$

D -  $\emptyset$  fix (-2)

len = 7

E -  $\emptyset$  (-1)

requirement =  $\emptyset$  / X0

N -  $\emptyset$

O. -  $\emptyset$  (-1)

↑

is map

Note first acquired by  $e_i$  then done sufficient for  
min length.  
then released when condition violated ( $req > 0$ ).

Code Public string minWindow (String s, String t) {  
 int ns = s.length();  
 int nt = t.length();  
 int si = 0, ei = 0, len = ns + 1, head = 0;  
 int requirement = nt;  
 int[] freq = new int[128];  
 for (int i = 0; i < nt; i++) freq[t.charAt(i)]++;

while (ei < ns) {

if (freq[s.charAt(ei++)]-- > 0) requirement--;

while (requirement == 0) {

if (ei - si < len) len = ei - (head = si);

if (freq[s.charAt(si++)] == 0)  
 requirement++;

}.

return len == ns + 1 ? ":" : s.substring(head, head + len);

?.

;

:

:

Lect - 3 (Arrays)

8/12/2020

Agenda :-

- ① Smallest window containing itself (ggg). } 8' with k length.
- ② 159 // locked } same as 76.
- ③ 340 // locked }
- ④ Max vowel letter in any substring. 8' with k length. (1456)
- ⑤ Count unique substrings with non-repeating char (ggg).
- ⑥ 239 / sliding window Max.

Ques what Smallest window containing itself

I/P = a a b c b c d b c a .

O/P = d b c a .

Now :-

Same as previous but here we keep ff. of each element one not more/few because we want smallest window having all repetition characters & no repetition.

Output is same as 76 / prev.

dry run -

a -  $\text{X}^0$

b -  $\text{X}^0$

c -  $\text{X}^0$

d -  $\text{X}^0$

$\text{xy} = \text{A}^0 \text{Z}^0 \text{X}^0$

do same -

Code -

```
public int minWindow(String s) {
```

```
    int n = s.length();
```

```
    int[] freq = new int[128];
```

```
    for (int i = 0; i < n; i++) freq[s.charAt(i)] = 1;
```

int requirement = 0, si = 0, ei = 0, head = 0, len = (int) 1e8;

```
for (int ele : freq) requirement += ele;
```

```
while (ei < n) {
```

```
    if (freq[s.charAt(ei++)]-- > 0) requirement--;
```

```
    while (requirement == 0) {
```

```
        len = (ei - si) < len ? len : (head = si, len);
```

```
        if (freq[s.charAt(si++)]++ == 0) requirement++;
```

}

3.

return len;

7.

Ques. 159 | longest Substring with atmost two distinct character

What :- given a string 'S' find the length of the longest substring 'T' that contain atmost 2 distinct character.

I/P: echo.

O/P: 3 → ece.

How: Alg: make a distinct count variable.

① if (freq of any char encounter >= 3) then  
    ↑ distinct count.

② while (distinctCount > 2) {

    ① freq[char] --

    ② if freq(char) == 1). then ↓ distinct;

③ calculate length as well.

Code

Dayan.

String: C C a a b b b a a C C C d d c d c d .  
Index: 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17.

a - X X Z X

b - X Z Z

c - X Z X Ø 1

d -

distinct = X Z Z Ø 1.

similarly work goes on.

II code :-

Similarly for  $k$  distinct can can be done so do for  $k$ :

and check for  $k$  as well instead of '2'

$k=2$

Code :

```
int n = s.length();
int si=0, ei=0, head=0, len=0, discount=0;
vector<int> freq(128,0);
while(ei < n) {
    if(freq[s[si++]] == 0)
        discount++;
}
```

while (discount > k) {

```
if(freq[s[head++]] == 1)
    discount--;
```

$len = (ei - si > len) ? ei - (head = si) : len;$

}

return len;

}

Ques 1456 | Max vowel letters in Any substring is with K length.

What :- Max Vowel in window of K size.

$s = abciiiddef \quad K=3$   
 $\alpha/\rho = 3$

How :- do same as sliding window just make function to check vowel / not

① if vowel / then count++.

② during loop if  $i - si = k$  then  $\uparrow$  si and count max vowel.

$\uparrow$  si and if  $s(i)$  is vowel  
 then vowel count --

Algorithm.

K=3

$VC = 6 \times 2 \times 2^3$ .

$\uparrow \uparrow \uparrow$   
 $\downarrow \downarrow \downarrow$   
 $a b c i i i d e f$   
 $\uparrow \uparrow \uparrow \uparrow \uparrow \uparrow$   
 $1 2 3 4 5 6 7 8$

Ques:-

① bool isVowel (string s, int k) {

    return ch == 'a' || ch == 'e' || ch == 'i' || ch == 'o' || ch == 'u';

{.

int maxVowels (string s, int k) {

    int n = s.length();

    int si = 0, ei = 0, vc = 0, maxVC = 0;

    while (ei < n) {

        if (isVowel(s[ei]))

            vc++;

        if ((ei - si) == k)

            maxVowelsCount = max(maxVC, vc);

        if (!isVowel(s[si]))

            vc--;

}.

}.

    return maxVC;

{.

Ques. Count all unique substrings with non-repeating characters.

$$I/P = abba$$

$$O/P = 4$$

a, b, ab, ba

Gow 259. sliding window Maximum.

return max from 'K' size window.

name = [1, 3, -1, -3, 5, 3, 6, 7] .  $K = 3$  .

OP = [3, 3, 5, 5, 6, 7] .

How:

what Not do- Here I have thought range  $\Rightarrow$  19.  
of do not element ~~19~~ at ~~at~~

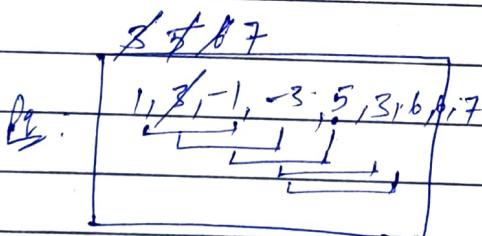
but it's wrong.

1, 3, -1  $\rightarrow$  Remove

but it will be part of next window.

Here popping done if (~~if~~ peek(index)  $\leq i-k$ ) .

dry Run:



$O(n \log n)$   
(for n element) to add

$t: O(n \log n)$

Code:

```
public int[] maxSlidingWindow(int[] nums, int k) {
    if (nums.length == 1 || k == 1) return nums;
```

Priority Queue < Integer > pq = new PriorityQueue<>((a, b) →

```
a -> nums[a], b -> nums[b]); // arr. element based
} ; // comparison (while index in pq).
```

int n = nums.length;

int[] ans = new int[n - k + 1];

int idx = 0;

for (int i = 0; i < n; i++) {

```
while (pq.size() != k || pq.peek() <= i - k) {
    pq.remove();
}
```

pq.add(i);

Time O(n) Space O(k)  
for initial if ( $i \geq k-1$ ) ans[idx] = nums[pq.peek()].  
into arr. }.

lecture-4 (9/12/2020)

## Agenda:

- ① Longest subArray with equal no. of 0 and 1 3 same ①
- ② Leet code 525
- ③ Count subArray with equal no. of 0 and 1 ②
- ④ Longest subArray with sum divisible by k. 3 same ③
- ⑤ 974. subArray sum divisible by k. a
- ⑥ 781 Rabbit in forest. ④

Ques:- Longest subArray with equal no. of 0 and 1.

Eg.

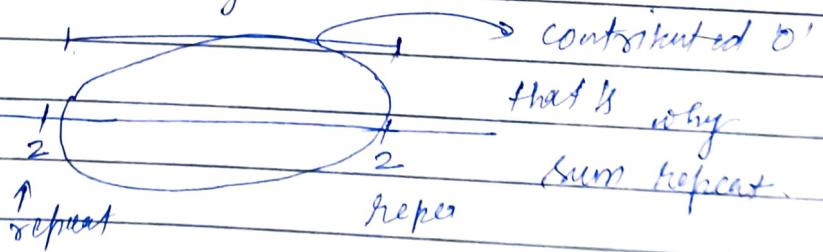
$$\text{arr} [ ] = \{ 1, 0, 1, 1, 1, 0, 0 \} .$$

$$\text{o/p} = \overset{1}{\cancel{1}}, \overset{2}{\cancel{2}}, \overset{3}{\cancel{3}}, \overset{4}{\cancel{4}}, \overset{5}{\cancel{5}}, \overset{6}{\cancel{6}}.$$

How:- Here we keep track of sum vs index.

if any sum get repeated that means.  
arr[1] arr[3] & arr[5] and  $\Rightarrow$  fill that element  
in contribution zero  $\Rightarrow$  0.

Eg.



eg.

1	-1	1	1	1	-1	-1	1	-1	1	-1	-1	1	1	1	-1	-1	1	1	1
1	0	1	2	3	2	1	2	1	2	1	0	-1	0	1	2	1	0	1	2
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19

Here we keep sum of zero as -1 initially.  
 so that we have easy to calculate  
 else have to manage count by adding(1).

eg for 0,1  $\Rightarrow 1-0 = 1$  (len) x.

$$\text{if } \underline{0} = -1 \quad 1 - (-1) = 2. \quad \checkmark$$

psum :      idx :

0                -1

1                0

2                3

3                4  
-1              12

len = 16 8 16 12 14 16  
- 18 20.

Code

```
int maxlen(int arr[], int N){
```

```
    if(N<1) return 0;
```

```
    HM<I,I> map = new HM<I>();
```

```
    map.put(0, -1); // for easy calculation.
```

```
    int sum = 0, len = 0;
```

```
    for(int i=0; i<N; i++){
```

```
        int val = arr[i];
```

```
        if(val == 0) val = -1;
```

```
        sum += val;
```

```
        if(map.containsKey(sum)) len = max(len, i - map.get(sum));
```

```
    } else map.put(sum, i);
```

```
    return len;
```

```
}
```

(3) ~~Ques~~ Count subarray with equal no. of 0 & 1

what :-

$$\text{array} = \{1, 0, 0, 1, 0, 1, 1\};$$

$$O/P = 8.$$

$$(0,1), (2,3), (0,3), (3,4), (4,5), (2,5), (0,5), (1,6).$$

How :- Here we will also do same as prev maintain sum Array.

→ make count of each sum. and take all combination of 2 eq  $n_2$ .

→ make default count of 0,  $n_1$  as it will help in calculation.

or initial 0 at count 1 & ~~sum 0~~.

dry run.

0	+1	+1	+1	-1	-1	-1	
+	+1	-1	+3	+2	+1	0.	
1	1	2	2	2	2	0.	

$$0 - X^2$$

$$1 - 2$$

$$2 - 2$$

$$3 - 0$$

$$\therefore \text{ans} = 2l_1 + 2c_2 + 2c_2 = 3.$$

\* code

```
int countless(int arr[], int N) {  
    if (N <= 1) return 0;
```

HM<int, int> map = new HM<int>;  
map.put(0, 1);

```
int sum = 0, count = 0;  
for (int i = 0; i < N; i++) {  
    int val = arr[i];  
    if (val == 0) val = -1;  
    sum += val;
```

```
count += map.getOrDefault(sum, 0);  
map.put(sum, map.getOrDefault(sum, 0) + 1);
```

}

```
/* for (Integer key : map.keySet()) {
```

Count += (map.get(key) \* (map.get(key - 1))) / 2;

\*/  
 }  
 return count;

(6)

781 // Rabbit in forest

What :- In a forest each rabbit has some color. Some subset of rabbit (possibly all of them) tell you how many other rabbit have the same colour as them. Those answer are placed in an array.

Return minimum number of rabbit that could be in the forest.

e.g. I/P : [1, 1, 2].

$$O/P = 5.$$

How :- Here if 1 → means there could be max 2 rabbit like or (itself) + 1 and popped from map.

if 1 occurs 3 times then, it will counted separate.

→ and remain till 2 in the map.

→ Note Any key remain in the map till its value  $\neq$  key + 1

if key + 1 = Remove it  
and insert again with 1 value.

$$\begin{array}{rcl} \times 1 - V_2 & \text{ans} = 2 + 3 \\ 2 - 1 & = 5 \end{array}$$

4	3	2	3	4	3	3	3	4	4	2	3	4
R	R	R	R	Brown								

 $4 \rightarrow 5$  $3 \rightarrow 4 (R)$  $2 \rightarrow 3$  $3 \rightarrow 4 (\text{Brown})$ 

## II code

```
public int numRabbits(int[] arr) {
    if (arr.length == 0) return 0;
    int n = arr.length;
    HM<I, I> map = new HM<I, I>();
}
```

```
int ans = 0;
```

```
for (int ele : arr) {
```

```
if (!map.containsKey(ele)) {
```

```
ans += ele + 1;
```

```
map.put(ele, 1);
```

```
}
```

```
map.put(ele, map.get(ele) + 1);
```

```
}
```

```
if (map.get(ele) == ele + 1) map.remove(ele);
```

```
return ans;
```

```
}
```

Ques. longest subarray with sum divisible by k. (2/9)

W.H.T.:- Find longest subarray with its sum divisible by k

$$\text{I/P} = \{2, 7, 6, 1, 4, 5\}$$

$$k = 3$$

$$\text{O/P} = 4 \text{ (size).}$$

$$\text{O/P} = \{7, 6, 1, 4\}$$

Approach - 1

① calculate the prefix sum.

$$\text{sum}(1, 4) = \text{psum}(4) - \text{psum}(0)$$

② calculate ps sum of all subarray and compare. it will give all subarray sum. largest will be answer (index diff).

$$t: O(n^2)$$

Dry Run:-

$$\{2, 7, 6, 1, 4, 5\}$$

0	2	9	15	16	20	25
1	2	3	4	5	6	

Here we have shifted index to avoid diff calculation error.

$$q. \text{ if not shifted } \text{psum}(2, 4) = \text{psum}(4) - \text{psum}(1).$$

$$\text{now } \text{psum}(2, 4) = \text{psum}(4) - \text{psum}(1).$$

$(e_i - s_i)$  directly.

```
for (int i = 0; i < n; i++) {
```

$$\text{psum}(i+1) = \text{psum}(i) + \text{arr}(i);$$

}

```
int len = 0;
```

```
for (int i = 0; i < n; i++) {
```

```
    for (int j = i; j < n; j++) {
```

$$\text{if } ((\text{psum}(j+1) - \text{psum}(i)) \% k == 0)$$

$$\text{len} = \max(\underbrace{j-i+1}, \text{len}).$$

}

$\rightarrow e_i - s_j$  directly

otherwise

$$\frac{(j-i+1)}{k}$$

normal  
case.

}

```
return len;
```

soln gives tle.

M-2

o(n) soln

map of sum vs index does not give us any thing but

to fig -

sum	index
2	
9	
15	
16	
20	
25	

no meaning.

But if we store remainder but index.

then it gives some valuable information.

eg:

<u>arr</u>	→	2	7	6	1	4	5
<u>sum</u> :		2	9	15	16	20	25
<u>Rem.</u> :		2	0	0	1	2	1

$0 \leftarrow 1$     no addition     $\rightarrow 5$

Repeating of rem. show. there is not any valuable addition in given range.

and state  $0 \rightarrow (-1) 8$

because we are assuming that our first 0 is at  $(-1)$  so that no need to add one and easy calculation

eg. if do not place  $(-1)$ .

$$\text{eg. } 0 \rightarrow 1 + 1 = 2$$

zero first occurs at index 1

but length is  $\neq 2$  so need to add 1.

$$\text{so. len} = 1$$

so need to add  $1^1$  (have to handle separately)

If place  $0 \rightarrow -1$  then just do simple calculation

$$0 \rightarrow -1$$

$$1 \rightarrow 3$$

$$2 \rightarrow 0$$

If remainder has already occurred then calculate len and compare from prev len).

Code :-

```
int longestSubArrayWithSumDivK(int arr[], int n, int k) {
    if (n == 0) return 0;
    int len = 0;
```

rem.

```
unordered_map<int, int> map; // sum, index
map[0] = -1;
```

```
int sum = 0;
for (int i=0; i<n; i++) {
    sum += arr[i];
    int sum = (sum + k) % k;
    if (map.find(sum) != map.end())
        len = max(len, i - map[sum]);
    else
        map[sum] = i;
}
```

5.

return len;

3.

Q

97# || LeetCode -

count all subarrays with sum divisible by |k|

$A = [4, 5, 0, -2, -3, 1]$   $k = 5$ .

O/P = 7

How :-

M-1 Here we are first counting then printing that remainder.  
Count

M-2 We can do here the nos for that particular sum.

arr	4	5	0	-2	-3	1	, k = 5 .
sum	4	9	9	7	4	5	
<u>Rem</u>	4	4	4	2	4	0	

$$0 \rightarrow +1+1 = 2 .$$

$$4c_2 = \frac{4 \times 3}{2} = \frac{12}{2} = 6 .$$

$$2c_2 = \frac{2 \times 1}{2} = 1 = 1$$

total = 7 | or Count at every level.

Code

```
public int subArraysDivByK( int[] arr, int k) {
    if( arr.length == 0 ) return 0;
    int[] map = new int[ k+1 ];
    map[0] = 1; // count // if len=map[0]=1
}
```

int sum = 0, int count = 0;

for( int i = 0; i < arr.length; i++ ) {

    sum += arr[i];

    int sum = ( ~~sum~~ sum / k + k ) / k;

    count += map[sum];

    map[sum]++;

}

return count;

}

lect - 5 (11/12/2020)

Agenda -

- ① 930 | Count Binary SubArray with sum equal to K
- ② 1248 | Count no. of nice subArray.
- ③ 1004 | Max consecutive one - III
- ④ 904 | fruit into basket
- ⑤ 209 | Min size subArray sum.

Ques. what?

An array of 0 and 1 how many non-empty subarray have sum s.

$$A = [1, 0, 1, 0, 1], s = 2$$

O/P →

$$\underline{[1, 0, 1]}, (1, 0, 1, 0), (0, 1, 01), (1, 01).$$

How:- → Here we just take the array and make map of sum vs freq count.

→ if a sum not present then put that and value 1 and increment it.

→ ~~if~~ <sup>to add</sup> check whether sum is present or not just ~~check~~.

(sum - k) of freq. into answers.

$$arr(ei) - arr(si) = k.$$

$$arr(ei) - k = arr(si).$$

↑  
perm (at ei index).                              ↑ starting index

Dry Run :-

$$\begin{matrix} 1, 0, 1, 0, 1 \\ \cancel{x} \cancel{x} \cancel{x} \uparrow \end{matrix} \quad k = 2$$

$k \neq 4$  dry

$$0 \rightarrow 1$$

$$\text{sum} = 1$$

$$1 - k \rightarrow \text{not contain}$$

$$2 - k \rightarrow \text{contain } f_1 = 1$$

$$3 - 1$$

$$3 - 2 \rightarrow 2$$

LL code

```
public int numSubarraysWithSum(int[] arr, int s),
```

```
int n = arr.length;
```

```
if (n == 0) return 0;
```

```
int ei = 0, count = 0, psum = 0;
```

```
// int freq = new int[3000 + 1];
```

```
// freq[0] = 1
```

```
HashMap<Integer, Integer> map = new HashMap<>();
```

```
map.put(0, 1);
```

```
while (ei < n) {
```

```
psum += arr[ei++];
```

```
// if (psum - s >= 0) count += freq[psum - s];
```

```
count += map.getOrDefault(psum - s, 0);
```

```
map.put(psum, map.getOrDefault(psum, 0) + 1);
```

```
// freq[psum]++;
```

```
}
```

```
return count;
```

```
}.
```

M-2. Here first calculate subarray with sum less than k/s  
 then take diff of  
all subArray of (s) - all subArray of (s-1). Ans.

II Code.

```
Public int numSubArrayWithAtmostSum[int[] arr, int s];
int si=0, ei=0, count=0, sum=0, n=arr.length;
```

```
while (ei < n) {
    sum += arr[ei++];
```

```
    while (sum > k) {
        sum -= arr[si];
    }
}
```

```
    count += ei - si;
}
```

```
Public int numSubArrayWithSum[int[] arr, int s];
int n = arr.length;
if (n == 0) return 0;
return numSubArray(arr, s) -
(s > 0 ? fn(arr, s-1) : 0);
```

Q. No. 1248. Count Number of Nice SubArrays

What

given array of integer numbers and integer  $k$ .

A subArray is called nice if there are ' $k$ ' odd numbers in it.

Find number of nice sub-arrays.

$$I/P = \{1, 1, 2, 1, 1\}, k = 3$$

$$O/P = 2$$

How :- do same as done in previous.

- ① Count all subArrays with atmost ' $k$ ' odd numbers.  
here len then ' $k$ ' are also included.
- ② Count all subArrays with ' $k-1$ ' odd.
- ③ Subtract ① - ②

dryRun:

$$(2, 2, 2, 1, 2, 2, 1, 2, 2, 2) \quad k=2$$

odd count = ~~2~~ 2

total subArray len than ( $k$ ).

$$res = 1 + 2 + 3 + 4 + 5 + 6 + 7 + 8$$

2

2, 22

2, 22, 222

1, 21, 221, 2221

22212, 2212, 2121, 12121, 2

222121, 22121, 2121, 12121, 1

now subtract ( $k-1$ )

all odd subArray

// Code -

Public int numberofSubArrayAtmost(int s, arr, int k);

int n = arr.length;

int si=0, ei=0, oddCount=0, yes=0;

while(ei < n) {

if(arr[ei+1] % 2 != 0) oddCount++;

while(oddCount > k) {

if(arr[ei+1] % 2 != 0) oddCount--;

}.

yes += ei - si;

}.

return yes;

}.

Public int numberofSubArrays( int s, arr, int k);

int n = arr.length;

if(n == 0) return 0;

return f(arr, k) - f(arr, k-1);

}.

S.Q. 1004 | max consecutive one - III

what? given Array of 0 and 1 we may change up to  
value from 0 and 1  
return length of longest subArray that contain  
only 1.

$$I/P = \{1, 1, 1, 0, 0, 0, 1, 1, 1, 1, 0\} \quad K = 2$$

- How:-
- ① make a zero count and sum loop from left make 2 pointer si and ei.
  - ② if zero count  $> K$  then  $si++$ .
  - ③ now calculate the len if max then update.

Dry Run:

1 1 0 1 0 1 0 1 1 0 0 0 1 0 1  
~~1 1 0 1 0 1 0 1 1 0 0 0 1 0 1~~  
 $K = 3 \cdot 0 \ 1 \ 2 \ 3$

$$\text{zeroCount} = \cancel{K} 3$$

$$\text{len} = \cancel{K} 3 \cancel{K} 5 \cancel{K} 8 \cancel{K} 9$$

Code -

Public int longestEneS (int r) arr, int k) {

int n = arr.length, ei=0, si=0, len=0, zCount=0;

while (ei < n) {

if (arr[ei] == 0) zCount++;

while (zCount > k) {

if (arr[si] == 0) zCount--;

}

len = Math.max(len, ei - si);

}

return len;

}

Ques. Min size subarray with sum greater equal to k.

$$\text{sum} \geq k/s$$

$$s = 7$$

$$\text{nums} = [2, 3, 1, 2, 4, 3].$$

$$o/p = 2 \rightarrow [1, 3]$$

Lecture-6 (13/12/2020)

## Agenda -

- ① kadane algorithm | for maximum subArray sum.
  - ② 1191 - k concatenation maximum sum.

Q1 Maximum SubArray sum. (Kadane algorithm).

$$2 \mid 3 \mid -4 \mid 1 \mid -7 \mid 4 \mid -1 \mid -2 \mid 1 \mid 5 \mid -3 \mid 6 \mid -19.$$

How -

- ① Maintain two variable gsum, gmaxSum, and running sum.
  - ② add element into running sum till  $\geq 0$ , once it is less than '0' set it to '0'
  - ③ Set gmaxSum, tmaxSum by a max of running sum and gmaxSum.

dry Run

$$\frac{9}{x}, \frac{3}{1}, -\frac{4}{1}, \frac{1}{1}, -\frac{7}{1}, \frac{4}{1}, -\frac{1}{1}, \frac{-2}{1}, \frac{1}{1}, \frac{5}{1}, -\frac{3}{1}, \frac{6}{1}, -\frac{10}{1}$$

$$g_{\text{LMM}} = f_{1,9}$$

$$x_m \text{ min} = 23.5 - 1.01x_1 - x_2 + 0.1x_3$$

- Here in this method if element is negative then set arr sum '0'
- but in generic method if -ve element occurs then set that to that value.

// code -

```
public static void KadaneAlgo(int[] arr){  
    int gmaxSum = -1000, runningSum=0;  
    for(int ele : arr){  
        runningSum += ele;  
        if(runningSum > gmaxSum)  
            gmaxSum = runningSum;  
        if(runningSum <= 0)  
            runningSum = 0;  
    }  
    return gMaxSum;  
}
```

Return the ~~g~~ max sum subarray.

- do that keep two extra variable  
gesi, gesi, (global starting index),  
xesi (running or starting index to keep update  
temporarily).  
and xesi is keep on going  
if gesi <= runningSum > gmaxSum then update  
gesi, gesi → xesi.  
→ xesi update them.

|| code -

```

public static void KadaneAlgoSubArray (int[] arr) {
    int gMaxSum = -(int) 1e8, xrunningSum = 0;
    int gesi = 0, gesi = 0, gesi = 0; // gesi = global si
    // running si = xesi.           // gesi = global ei;

    for (int xesi = 0; xesi < arr.length; xesi++) {
        xrunningSum += arr[xesi];
        if (xrunningSum > gMaxSum) {
            gMaxSum = xrunningSum;
            gesi = gesi;
            gesi = gesi;
        }
    }

    if (xrunningSum < 0) {
        xrunningSum = 0;
        gesi = gesi + 1;
    }

    return gMaxSum;
}

```

T-2 Kadane algo.

This algo set that -ve value as max. as sum.  
If all are negative element but not 0' at as prev.

Public static long KadaneAlgo generic (int[] arr) {

long gmaxSum = arr[0], runningSum = arr[0];

for (int i = 1; i < arr.length; i++) {

runningSum = max (arr[i], arr[i] + runningSum);

gmaxSum = max (runningSum, gmaxSum);

}

return gmaxSum;

}

Ques. 1191. K - Concatenation maximum sum.

What? given an integer arr and integer 'K' modify array by repeating it ' $K$ ' times.

Eg arr = [1, 2],  $K = 3$

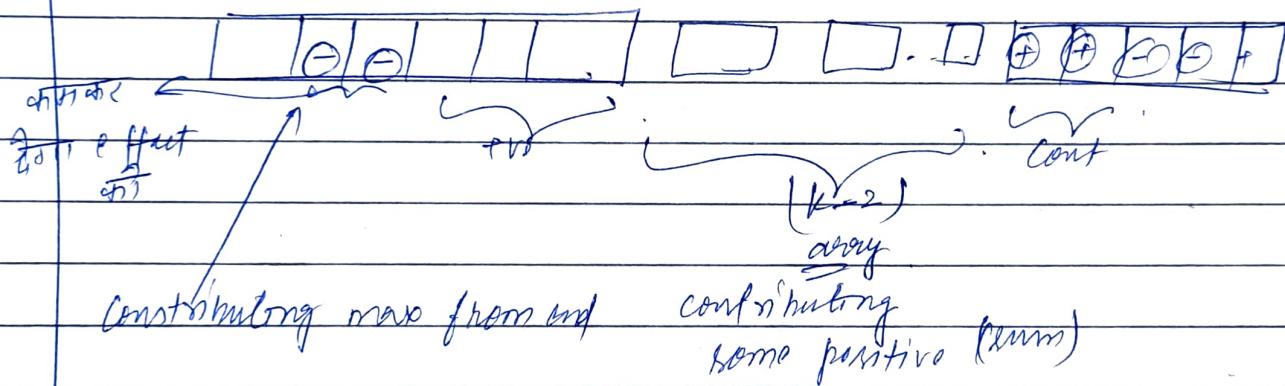
[1, 2, 1, 2, 1, 2]

max sub array sum = 9.

How:-

M-1. Here arises two situation if (arr sum > 0) and  $K-2 > 0$

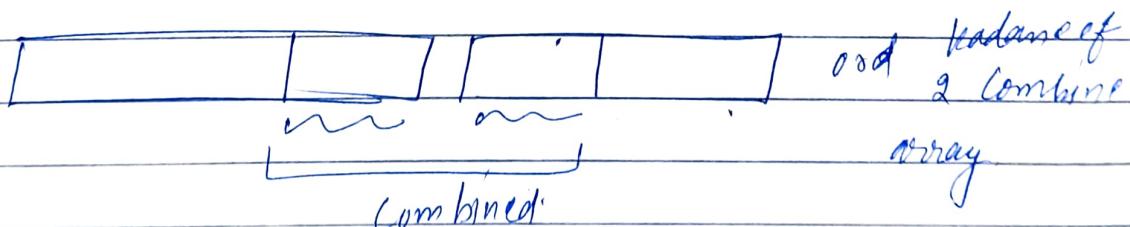
then situation will be like.



C-2 if arr sum < 0

then

answer will be



C=2

if  $\underline{k=1}$  ans will be kadane of  $\underline{arr}$ .

eg.

$$\boxed{8 \ 5 \ -8 \ 2 \ 3 \ -3} , k=4.$$

$$\underline{C=1} \quad \text{kadane sum} = 7.$$

$$\text{prefix sum} = 7.$$

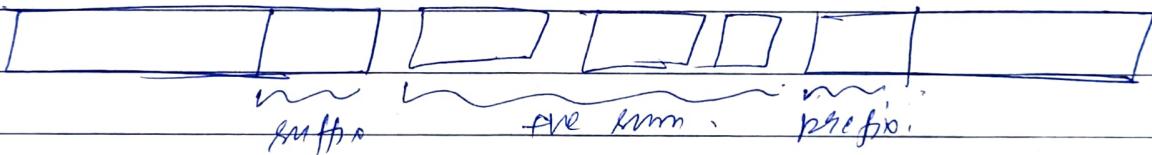
$$\text{suff sum} = 9$$

$$\text{arr sum} = 1$$

arr sum > 0

$$\begin{aligned} \text{ans} &= ps + ss + (k-2) \times 1 \\ &= 7 + 9 + (4-2) \times 1 \\ &= 8 + 2 = 10. \end{aligned}$$

situation is line-

C=2 if

$$\text{arr sum} < 0$$

$$\boxed{2 \ 5 \ -1 \ 2 \ 3 \ -3} , \underline{k=4}.$$

arr sum = -1

$$\text{kadane sum} = 7$$

$$\text{plum} = 7$$

$$\text{sum} = 9$$

$$\begin{aligned} \text{ans} &= \max (ps + sum, k) \\ &= (7, 9) \\ &= 9 \end{aligned}$$

Code M-1

① long int mod = (int) 1e9 + 7;

Kadane Algo. (int r) arr) {

int gmaxSum = 0, runningSum = 0;  
for (int ele : arr) {

runningSum += ele;

if (runningSum > gmaxSum) gmaxSum = runningSum;

if (runningSum > 0) runningSum = 0;

}

return gmaxSum;

}

② prefixSum

Public long prefixSum(int r) arr) {

long gSum = -(int) 1e9;

long cSum = 0;

for (int ele : arr) {

cSum = (cSum + ele) % mod;

gSum = max(cSum, gSum);

}

return gSum;

}

③ // Sum from last.

```
Public long suffSum(int[] arr){
```

```
long gsum = -(int)1e9;
```

```
long csum = 0;
```

```
for (int i = arr.length - 1; i >= 0; i--) {
```

```
csum = (csum + arr[i]) % mod;
```

```
gsum = max(gsum, csum);
```

};

```
return gsum % mod;
```

}.

④ Public int k concatenation MaxSum(int[] arr, int k){

```
long ksum = kadaneAlgo(arr) % mod;
```

```
if (k == 1) return (int) kadaneSum;
```

```
long sumofArray = 0;
```

```
for (int ele : arr) = sumofArray += ele;
```

```
long preFixSum = prefixSum(arr);
```

```
long suffixSum = suffSum(arr);
```

```
if (sumofArray > 0) {
```

```
long Apsum = ((k - 2) * sumofArray + p1 + n) % mod;
```

```
return (int) max(apsum, ksum);
```

};

```
return (int) max(psum + ssum, kadaneSum);
```

M-2

what we are doing is. doing sum + min. among one for loop till  $k=3$ . ( $k \geq 3$ ).

Here prevsum = suffixsum + prefixsum.

How:

→ if it is Kadane of two array and always become equal to individual sum.

eg  
C-1.

2	5	-8	2	3	-3
2	7.5	-8	2	3	-3

$$\text{KMM} = 7 - 9.$$

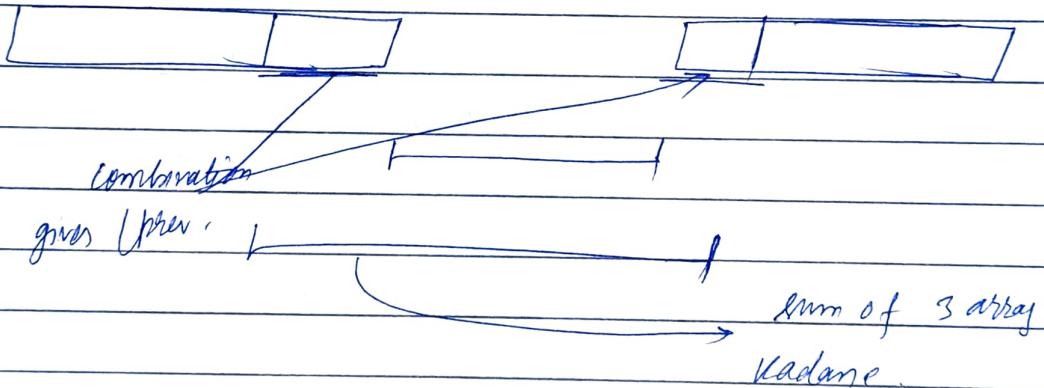
$$M = 2.$$

$$\text{KMM of two (prevsum)} = 9. \quad \left\{ \begin{array}{l} \text{equal.} \\ \text{eqn.} \end{array} \right.$$

C-2

and Kadane of 3 array - prev(M+bs) give sum of one array.

How:



$$\text{so one array} = \underline{\text{Kadane sum - prev}}$$

Lecture-714/12/2020Agenda-

- ① 1074 - Number of submatrix that sum to target
- ② 368 - max sum of rectangle sum no larger than k.
- ③ 152 - min product subarray

Ques 1074. Number of submatrices that sum to target

What? given a matrix and a target return number of non-empty submatrix that sum to target

eg.

0	0	1	0	0
1	1	1		
0	1	0		

target = 0.

$$O/P = 4.$$

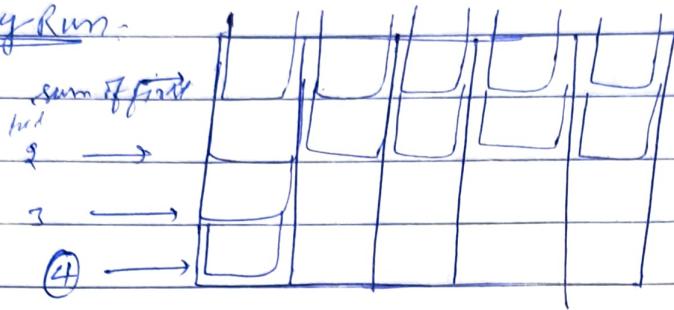
How: Algorithm.

- ① do column wise sum and store them at each cell from top to bottom.
- ② Run a nested loop on Row and column.
- ③ for each Row treat them as single row and count all sub-Array divisible by k.

Alternate :-

- ① we can do it as from bottom to top, left to right / right to left as well.
- ② do further steps accordingly.

dry run:



set a base at top and slide them by one after each iteration and if (base != 0) then subtract prev. cell pe value from current

eg.

	1	2	3	4	5
b →	6 $6-1=5$	7 $7-2=5$	8 $8-3=5$	9 $9-4=5$	10 $10-5=5$
	11 $11-1=10$	12 $12-2=10$	13 $13-3=10$	14 $14-4=10$	15 $15-5=10$

similarly do for other base when shift them.

II Code :-

```
target +  
Public int submatrixSumTarget (int r1[] matrix, int k) {  
    int n = matrix.length, m = matrix[0].length;  
  
    for (int row = 1; row < n; row++) {  
        for (int col = 0; col < m; col++) {  
            matrix[row][col] += matrix[row-1][col];  
        }  
    }  
}
```

int count = 0;

```
for (int base = 0; base < n; base++) {  
    for (int row = base; row < n; row++) {  
        HashMap<I, I> map = new HM<>();  
        map.put(0, 1);  
        int sum = 0;  
        for (int j = 0; j < m; j++) {  
            sum += matrix[row][j] - (base != 0 ?  
                matrix[base-1][j] : 0);  
            Count += map.getOrDefault(sum - k, 0);  
            map.put(sum, map.getOrDefault(sum, 0) + 1);  
        }  
    }  
}
```

return Count;

}

Ques. Max sum of Rectangle sum no larger than  $k$ .

what :-

given non-empty 2-d matrix. and integer ' $k$ ' find max. sum of Rectangle in  $\star$  matrix. sum not larger than  $k$ .

1	0	1	
0	-2	3	$k = 2$

$O/P = 2$

Rectangle means submatrix.

How :- Here do the same as previous qn.

same ?

- ① Calculate ans sum of each cell and put into cell.
- ② Make loop for base and run row no. of time ..

different ?

Here Have to calculate sum not greater than  $k$ .  
if ( $\text{sum} = k$ ) found then return.

otherwise ceil

$+ + + +$  ——————  
(sum -  $k$ )              sum

Floor  $\curvearrowleft$  val will be ceil

and  $\max \text{sum} = \max(\max \text{sum}, \text{sum} - \text{val})$

→ Here instead of HM, tree map used because it is capable to give ceil or floor if value not found in map.

2, 4, 8, 10, 15

note - A ceil of (16) will be null in ceiling function.

dry run -

1	2	2	1	4	2	1	3	5
---	---	---	---	---	---	---	---	---

0	1	3	5	6	10	12	13	16	21
X	X	X	X	X	T	T	T		

$K = 11$

$$\text{num} = 1$$

$$\text{val} = \emptyset \emptyset$$

$$\text{max} = X \not\exists \not\exists 10$$

$$(10, 11) \ni 11$$

II code.

```
public int maxSumSubmatrix(int[][] matrix, int k) {
    int n = matrix.length, m = matrix[0].length;
    for (int i=0; i < n; i++) {
        for (int j=0; j < m; j++) {
            matrix[i][j] += matrix[i-1][j];
        }
    }
}
```

```
int maxSum = - (int) 1e9;
for (int base = 0; base < n; base++) {
    for (int row = base; row < n; row++) {
        int gsum = - (int) 1e9, xsum = 0;
        for (int j = 0; j < m; j++) {
            int val = matrix[row][j] - (base != 0 ?
                matrix[base-1][j] : 0);
            xsum = max (val, xsum + val);
            gsum = max (gsum, xsum);
            if (gsum == k) return k;
        }
    }
}
```

part of  
hardone  
and make  
code faster

```
if (gsum < k)
    maxSum = max (maxSum, gsum);
continue;
```

}

TreeSet<Integer> map = new TreeSet<>();

int sum = 0;

map.add(0);

```
for (int j=0; j < m; j++) {
```

```
    sum += matrix[row][j] - (base[j] == matrix[base[j]] ?
```

```
    j : 0);
```

```
    if (map.contains(sum - k)) return k;
```

original  
code:

```
Integer val = map.ceiling(sum - k);
```

```
if (val != null) {
```

```
    maxSum = max(maxSum, sum - val);
```

```
}
```

```
    map.add(sum);
```

```
}
```