COMP 6721 Applied Artificial Intelligence (Winter 2021)

Worksheet #10: NLP: Applications, Vector Space Models

Information Extraction. The detection of *Named Entities* (NEs) is a standard NLP application, called *Information Extraction* (IE). A popular Python library for developing NLP applications is spaCy, which has an online IE demo at https://explosion.ai/demos/displacy-ent. Try it out on an example text (e.g., a Concordia News article).

Vector dot product. Given the following encoding for $sent_0 =$ "the big dog", $sent_1 =$ "the big cat" and $sent_2 =$ "the big cat and dog", compute their similarity as the dot product $(\vec{m} \cdot \vec{n} = \sum_i m_i \cdot n_i)$ of their vector representations:

	and	big	cat	dog	the	, →. →.
sent0	0	1	0	1	1	1. $sent_0 \cdot sent_1 =$
sent1	0	1	1	0	1	2 agent agent -
sent2	1	1	1	1	1	2. $sent_0 \cdot sent_2 =$

Term Frequency. Fill in the term frequency for the two documents (d_1, d_2) :

 $d_1 =$ "The big dog barks."

 $d_2 =$ "The big dog and the big cat."

Note: ignore words not in the table (we removed so-called *stopwords*).

				d_1			d_2	
token	df	idf	tf	tf.idf	p_i	tf	tf.idf	q_i
dog	50,000							
barks	10,000							
big	100,000							
cat	10,000							

Inverse Document Frequency. Now compute the *inverse document frequency*, $idf = log_{10} \frac{N}{df}$ and add it to the table. Assume N = 10,000,000 (number of documents).

tf-idf Weights. You can now compute the tf-idf weights:

$$w_{t,d} = \begin{cases} (1 + \log t f_{t,d}) \cdot i d f_t, & \text{if } t f_{t,d} > 0 \\ 0, & \text{otherwise} \end{cases}$$

(note that we already did the log-scaling for idf above). You now have each document represented as a vector $\vec{d_i} \in \mathbb{R}^{|V|}$ (here |V| = 4, the size of our vocabulary).

Cosine Similarity. We can now compute the similarity between the two documents. First, compute the length-normalized vectors \vec{p}, \vec{q} for the two documents and add them to the table above. To normalize a vector, you have to (1) compute its length $|\vec{q}| = \sqrt{x_1^2 + \ldots + x_n^2}$, then (2) divide each element by the length: $\frac{x_i}{||\vec{v}||}$. Now you can compute the cosine similarity using the dot product of the normalized vectors, $\sin(d_1, d_2) = \cos(\vec{p}, \vec{q}) = \vec{p} \cdot \vec{q} = \sum_i p_i \cdot q_i$:

$\bullet \cos(\vec{p}, \vec{q}) =$	
$-\cos(p,q)$	

¹https://explosion.ai/software#spacy