

Number of subsequences of the form $a^i b^j c^k$

Given a string, count number of subsequences of the form $a^i b^j c^k$, i.e., it consists of i 'a' characters, followed by j 'b' characters, followed by k 'c' characters where $i \geq 1, j \geq 1$ and $k \geq 1$.

Note: Two subsequences are considered different if the set of array indexes picked for the 2 subsequences are different.

Expected Time Complexity : $O(n)$

String = (a b c a b c a b c a a b b) (C)

(suppose if answer
agya hai)

""
empty
String.

aⁱ
a
a
a
a
a

aCount

> isme bs aⁱ
form ke string
hai.

> every 'a'
charcater
aCount mai sirf
'a' pe khatam
hone wale
subsequence
store krega.

aⁱb^j
aⁱb
aⁱb
aⁱb
aⁱb

bCount

> isme bs
aⁱb^j form ke
string hai.

> every 'b'
charcater
bCount mai sirf
'b' pe khatam
hone wale
subsequence
store krega.

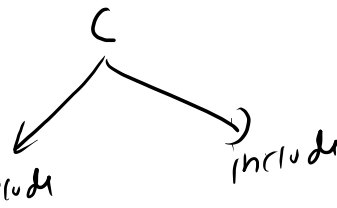
aⁱb^jc^k
aⁱb^jc
aⁱb^jc
aⁱb^jc
aⁱb^jc

cCount

> isme bs
aⁱb^jc^k form
ke string hai.

> every 'c'
charcater
cCount mai sirf
'c' pe khatam
hone wale
subsequence
store krega.

option 1.



agar 'c' nahi ana
chhata hai to vo ese
answer store krwayega
jisme pattern
aⁱb^jc^k pe khatam
ho. jo 'c' pe khatam ho.

agar c aana chhata
hai to bhi vo
aⁱb^jc^k wale
pattern ka count
store krwayega. jo 'c'
pe khatam ho

(ccount) + (ccount + bcount)
aⁱb^jc^k + (aⁱb^jc^{k+1} + aⁱb^jc^k)

abhi tak ka
aⁱb^jc^k
ese hi
ajyega.

abhi tak ke
(aⁱb^jc^k) ke
peeche ek 'c' or
add hoga and ye
pattern bnjyega
aⁱb^jc^{k+1}

abhi tak ke aⁱb^j
ke sath 'c' laag ke
ek aⁱb^jc¹ wale
pattern generate
krega.

same for b -> aⁱb^j ye pattern chahiye. (bcount + (bcount + acount)) - (exclude + include)
same for a -> aⁱ ye pattern chahiye. (acount + (account + emptyString)) - (exclude + include)