

Homework 2

Please put your solutions in a .doc, .docx or .pdf to [CSNS](#) by **11:59pm, Monday 02/12**.

Total points: 5

1 (2pt) This problem provides a numerical example of encryption using a one-round version of DES. Suppose both the key and the output of the initial p-box are:

1010 1101 0101 0110 1100 1001 1101 1010 1001 0001 1011 1011 0001 1001 1011 1010

- Derive k_1 , the first round key
 - Derive L_0 , R_0
 - Expand R_0 to get $E[R_0]$ using the Expansion P-box
 - Calculate $A = E[R_0] \oplus K_1$
 - Group the 48-bit result of (d) into sets of 6 bits and get the corresponding S-box substitutions
 - Concatenate the results of (e) to get a 32-bit results, B
 - Apply the permutation to get $P(B)$
 - Calculate $R_1 = P(B) \oplus L_0$
 - Write down the output of the first round.
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2.(1pt) For the group $G = \langle \mathbb{Z}_{26}^*, x \rangle$

- Find the order of the group
 - Find the order of each element in the group
 - Is the group is a cyclic group? Prove your answer and find the generator(s) if the answer is yes.
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3(2pt) Using the irreducible polynomial $f(x) = x^5 + x^4 + x^3 + x^2 + 1$ to

- generate the elements of the field $GF(2^5)$
- based on the results of a)**, calculate the followings in $GF(2^5)$
 - $(x^4 - x + 1)^{-1}$
 - $(x^3 - x + 1) * (x^4 + x^2 - x + 1)$

b.3) $(x^4 - x^3 + 1) / (x^2 + x + 1)$

Note: You won't get credit if you don't use the results of a) to do b)
