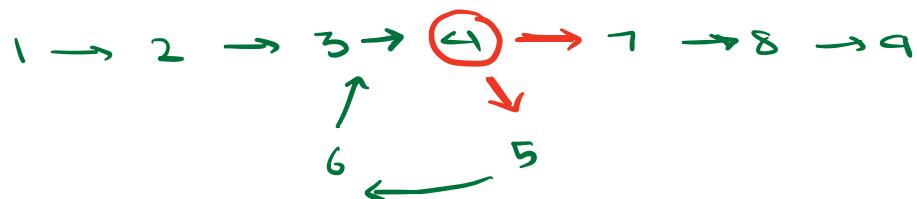
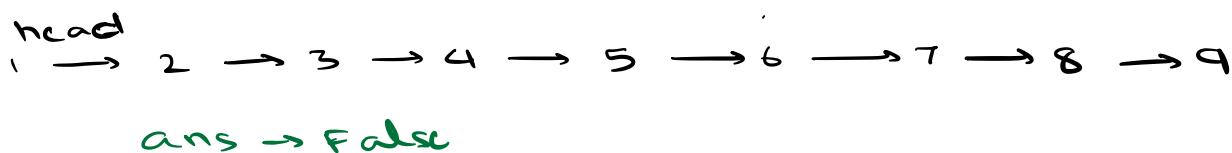
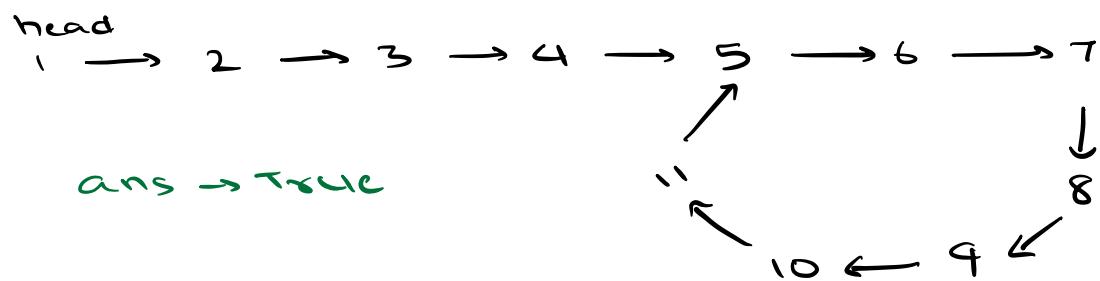


Agenda

1. Check for cycle in LL
2. Find starting point of loop
3. Introduction to Doubly LL
4. Insertion / Deletion in Doubly LL
5. LRU Cache

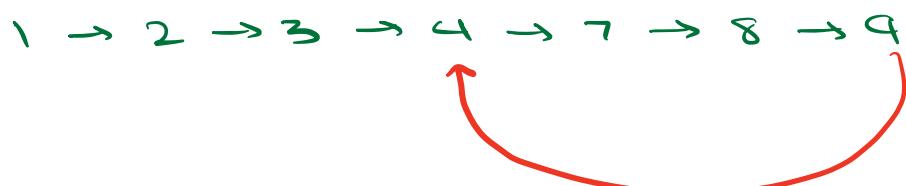
Done a LL → separate recording will
be added

Q1 Detect cycle in LL (nodes with duplicate data allowed)



NOTE: Loop cannot be in middle as one node will have 2 neighbours which is not possible

Conclusion : Loop (if present) at end of LL



Idea 1 : Start a **temp** at the head and **traverse LL** using **temp**

if **temp reaches null**

✓
No cycle
✗
cycle
(TLE)

Hashset < Node ?

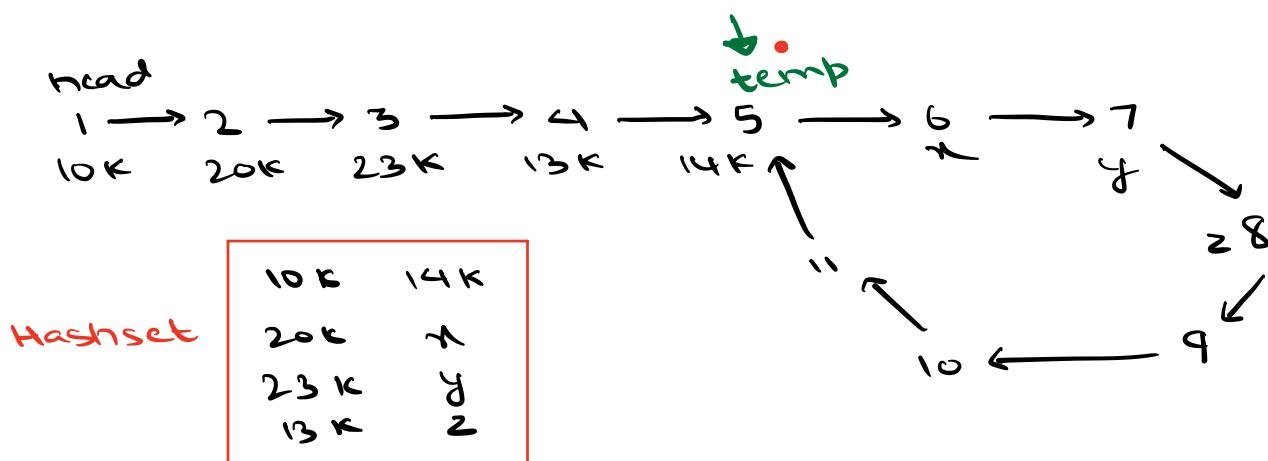
Idea 2 : Iterate LL, whatever node we visit \rightarrow put them in HS

TC : O(N)

SC : O(N)

If we find any node already in HS \rightarrow cycle in LL

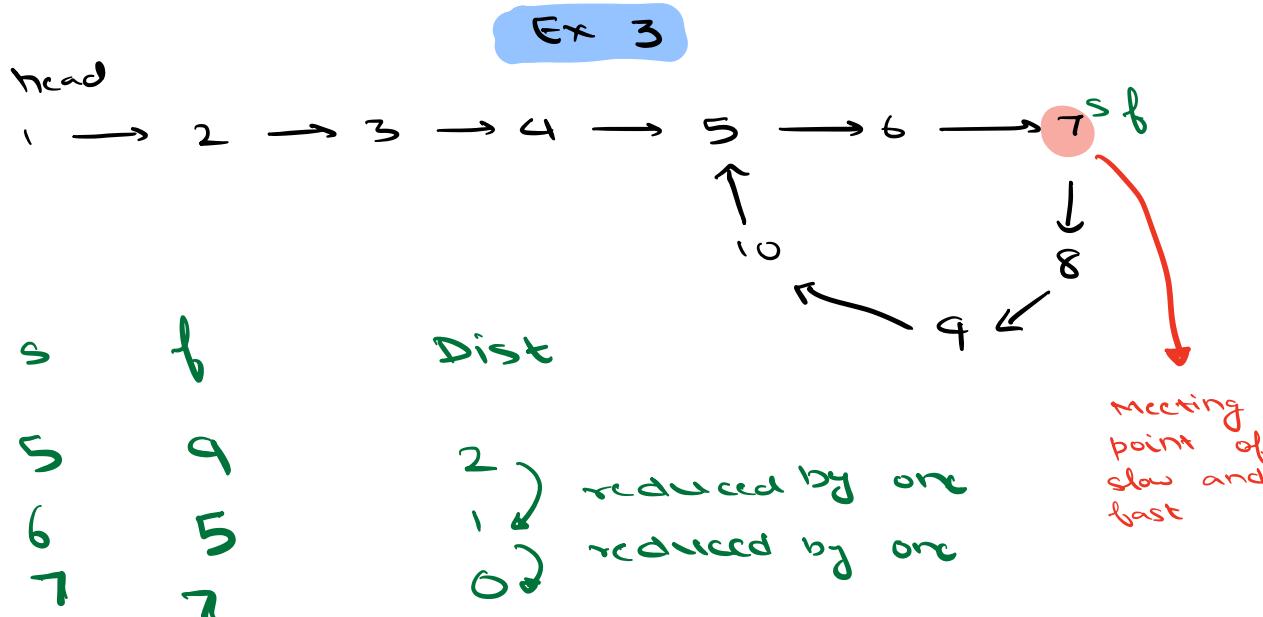
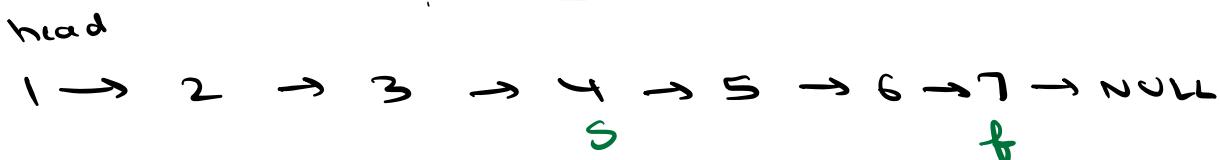
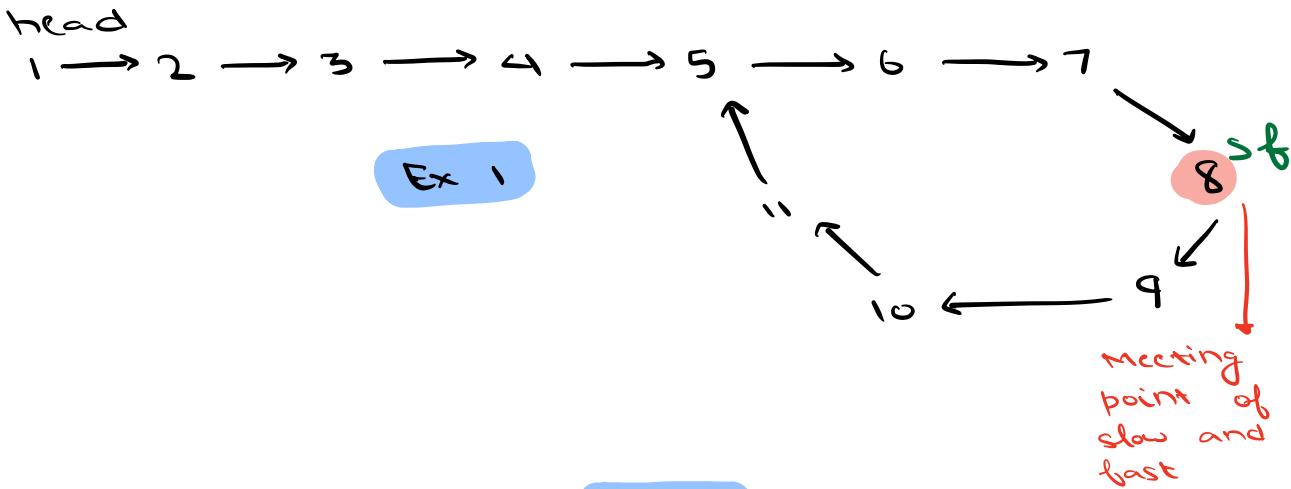
End of LL \rightarrow No cycle in LL



- When we reach node 5 the 2nd time, its address is already in HS ; suggesting a loop in LL.

Idea 3: Using slow and fast ref variable

Keep s and f at head. At a time move s by 1 step ($s=s.\text{next}$) and f by 2 steps ($f=f.\text{next}.\text{next}$). If they meet \rightarrow cycle

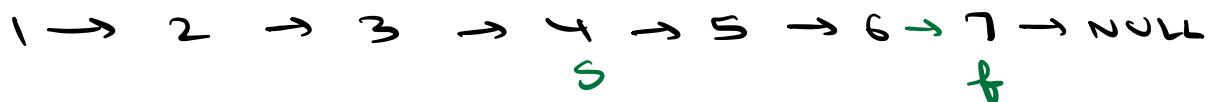


When slow ptr enters cycle, lets say
dist b/w them is x. Now we observe
that after every step, dist. reduces
by 1, hence dist. eventually becomes 0.

When to break the loop?

head

Ex 2



(a) In this case, when f reaches last node,
now it cannot move by 2 steps, so
stop traversal

head

Ex 4



(b) In this case, when f reaches NULL,
now it cannot move by 2 steps, so
stop traversal

while (f != NULL && f.next != NULL) {

 s = s.next

 f = f.next.next

 if (s == f) {

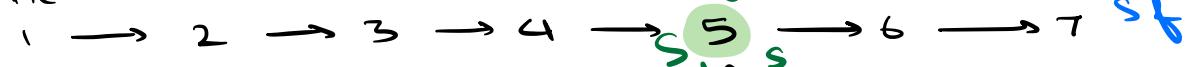
 return true

}

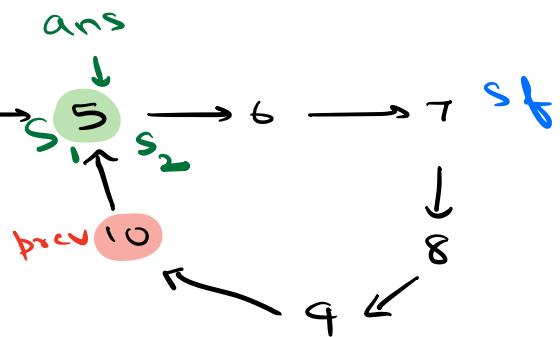
return false

-
2. If there is a loop in LL, find starting point of the loop.

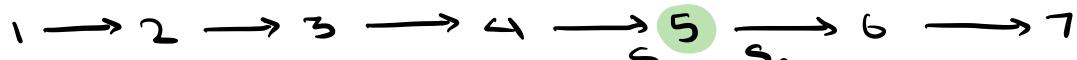
head



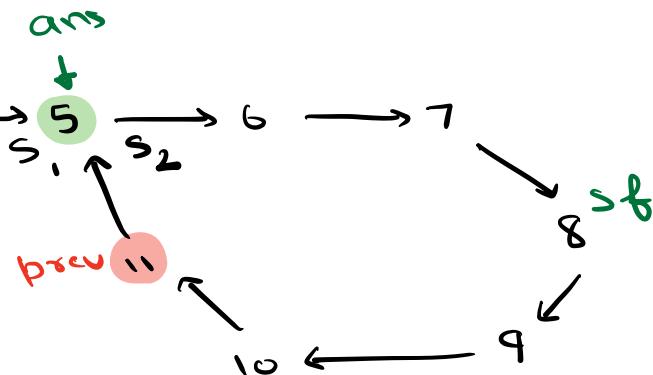
Making 10's next as
NULL breaks loop.



head



Making 11's next as
NULL breaks loop.



Take 2 ref variables s1 and s2

Node s1 = head

Node s2 = Intersection of s and f

Move both s1 and s2 1 step at a time.

Thus meeting point → start of loop

```
bool detectcycle (Node head) <
    Node s = h
    Node f = h
    bool iscycle = false
```

```
while (f != NULL && f.next != NULL) <
    s = s.next
    f = f.next.next
    if (s == f) <
        iscycle = true
        break
```

is (iscycle == false)
return false

Node s1 = head, s2 = s / f

Node prev = NULL → Maintain prev of

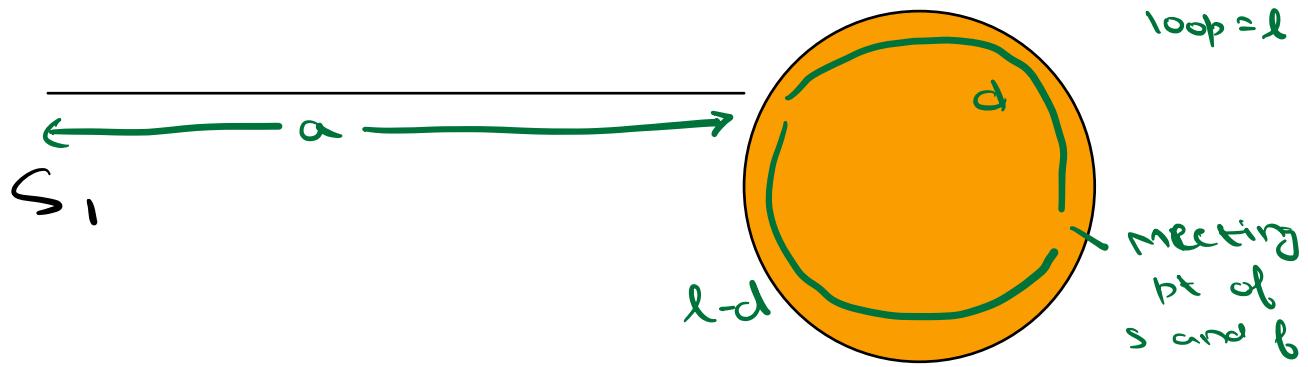
```
while (s1 != s2) <
```

```
    s1 = s1.next
    prev = s2
    s2 = s2.next
```

s2 as when
s2 reaches
starting pt
of loop,
prev node
in loop's
next → NULL

```
Node loopstart = s1
prev.next = NULL
```

↓
break
loop



$$d_s = a + d$$

$$d_f = a + c + l + d$$

$$d_f = 2 \times d_s$$

$$a + cl + d = 2a + 2d$$

$$cl = a + d$$

$$\begin{aligned} a &= cl - d \\ \Rightarrow a &= cl - d - \underline{l + d} \end{aligned}$$

$$a = cl - l + l - d$$

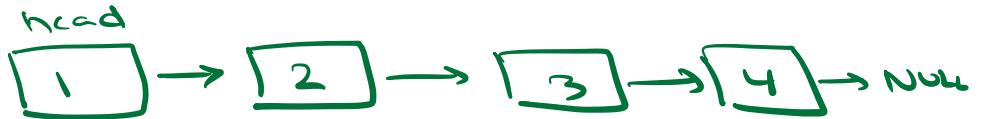
$$a = l(c-1) + l - d$$

$$a = \underline{l n} + l - d$$

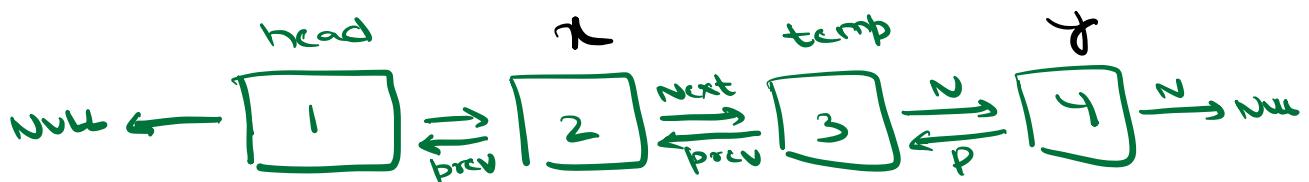
\downarrow Dist travelled by S_1 \downarrow Dist travelled by S_2

When S_1 covers ' a ' dist, it reaches loop start.
When S_2 covers the loop some no. of times, it reaches original pos. On covering ' $l-d$ ', it reaches loop start.

Singly LL



Doubly LL



class Node <

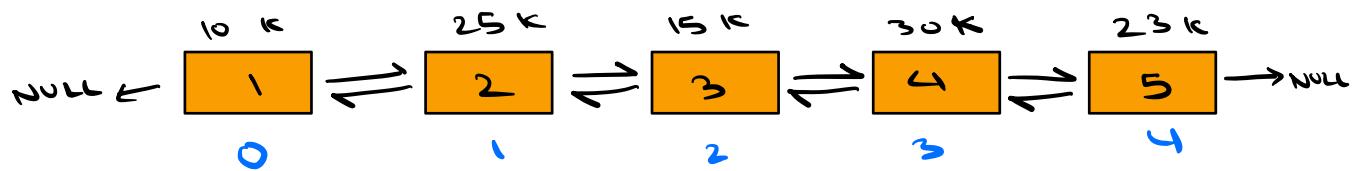
| int data
| Node next
| Node prev

→ right
→ left

Node x = temp.prev

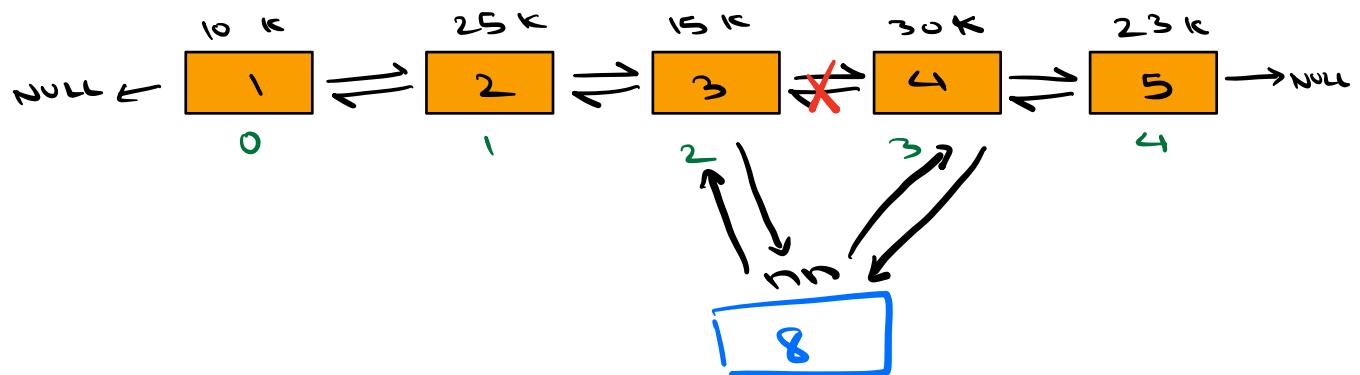
Node y = temp.next

3. A doubly linked list is given. A node is to be inserted with data x at position k . The range of k is between 0 and N where $N = \text{length of doubly LL}$.

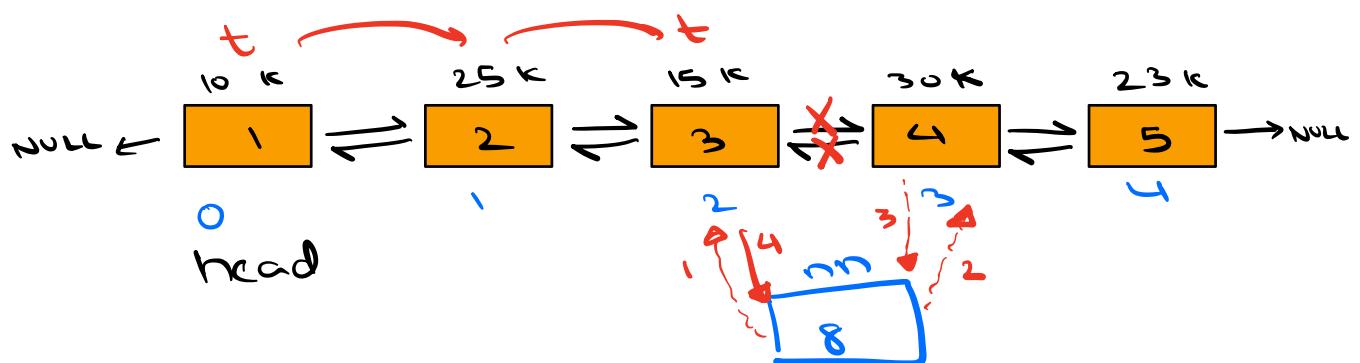


$k \rightarrow 0 \ 1 \ 2 \ 3 \ 4 \ 5$

$x = 8, k = 3$



Node $nn = \text{new Node}(x)$



$k = 3$

stop at $k-1$ i.e. 2



temp initially at head
jump 2 times

update

nn links

nn.prev = temp

①

nn.next = temp.next

②

temp.next.prev = nn

③

temp.next = nn

④

Node nn = new Node (n)

// Reach $k-1^{\text{th}}$ node

Node temp = head

for (i=0 ; i < k-1 ; i++) {

 temp = temp.next

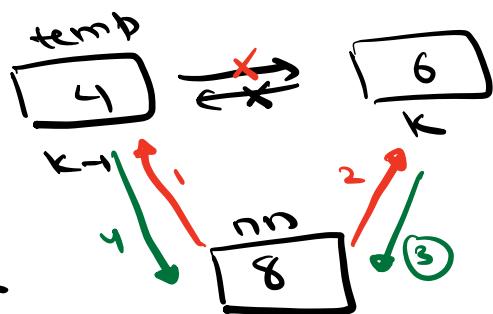
1 nn.prev = temp

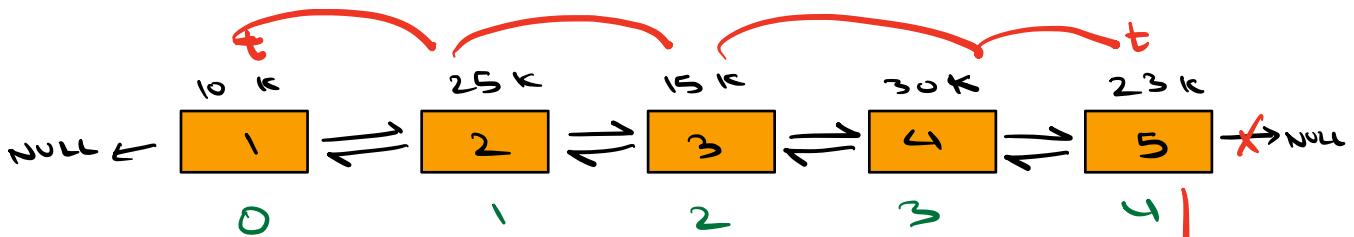
2 nn.next = temp.next

3 if (temp.next != NULL)

 temp.next.prev = nn ;

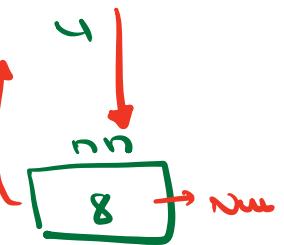
4 temp.next = nn





$x = 8, k = 5$

Inception at last
works fine



```

Node nn = new Node (n)
if (head == NULL)    return nn
if (k == 0) {
    nn.next = head
    head.prev = nn
    head = nn
    return head
}
// Reach k-1th node
Node temp = head
for (i=0 ; i< k-1 ; i++) {
    temp = temp.next
}

```

```

nn.prev = temp
nn.next = temp.next
if (temp.next != NULL)
    temp.next.prev = nn
temp.next = nn
return head

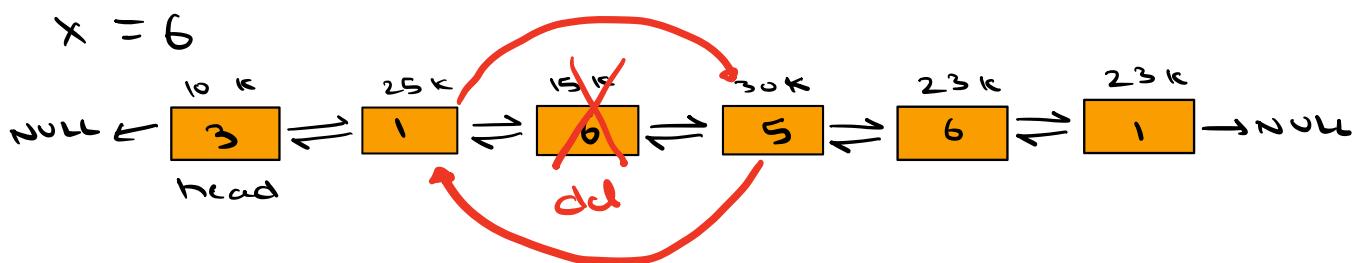
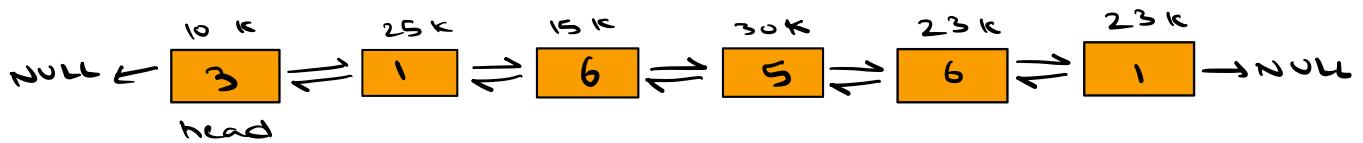
```

TC: O(N)
SC: O(1)

For insertion, edge cases :

- a) LL is empty \rightarrow head is NULL
- b) Insertion at head \rightarrow k=0

4. Given a doubly linked list of length N , we have to delete first occurrence of data x from given list. If x is absent, don't do anything.



Node temp = head

while (temp != NULL) <

{ if (temp. data == x) <
| break
|> temp = temp. next

if (temp == NULL)
return head

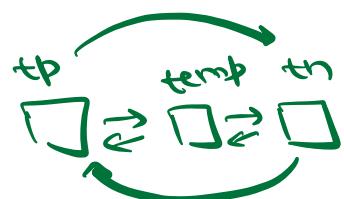
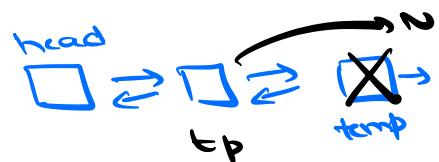
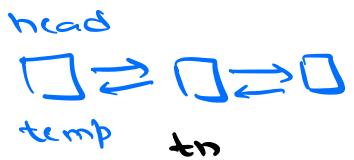
Find node to be deleted

//else delete

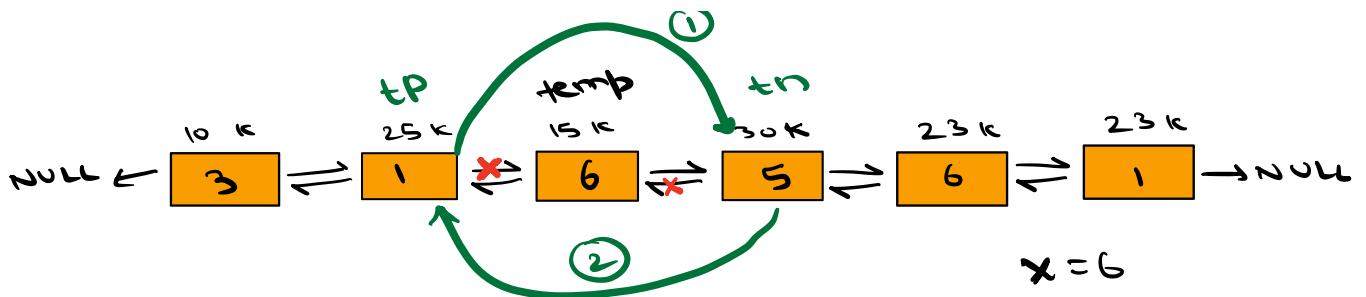
Reached end node but could not find x , hence no deletion

Node tp = temp.prev
Node tn = temp.next

- ① If LL has 1 node and that is deleted
if (tp == NULL && tn == NULL) <
|
| head = NULL
| return NULL
|
| C++
| +
| free(temp)
- ② Deleting head of LL
else if (tp == NULL) <
|
| tn.prev = NULL
| head = tn
| return head
|
|
- ③ Deleting last node of LL
else if (tn == NULL) <
|
| tp.next = NULL
| return head
|
|
- ④ Delete intermediate node
else <
|
| tp.next = tn
| tn.prev = tp
| free (temp)
| return head
|
|



TC : O(N)
SC : O(1)



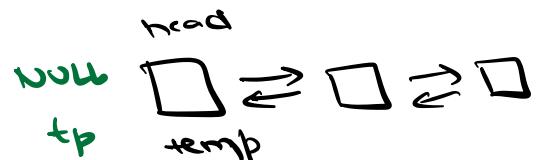
Node $tp = temp.\text{prev}$

Node $tn = temp.\text{next}$

$tp.\text{next} = tn$

$tn.\text{prev} = tp$

free (temp)



MOST RECENT INTEGER

LRU Cache \rightarrow temporary \rightarrow small storage

Delete Least Recently Used

7 3 9 2 6 10 14 2 10 15 8 14
 ↓ ↓



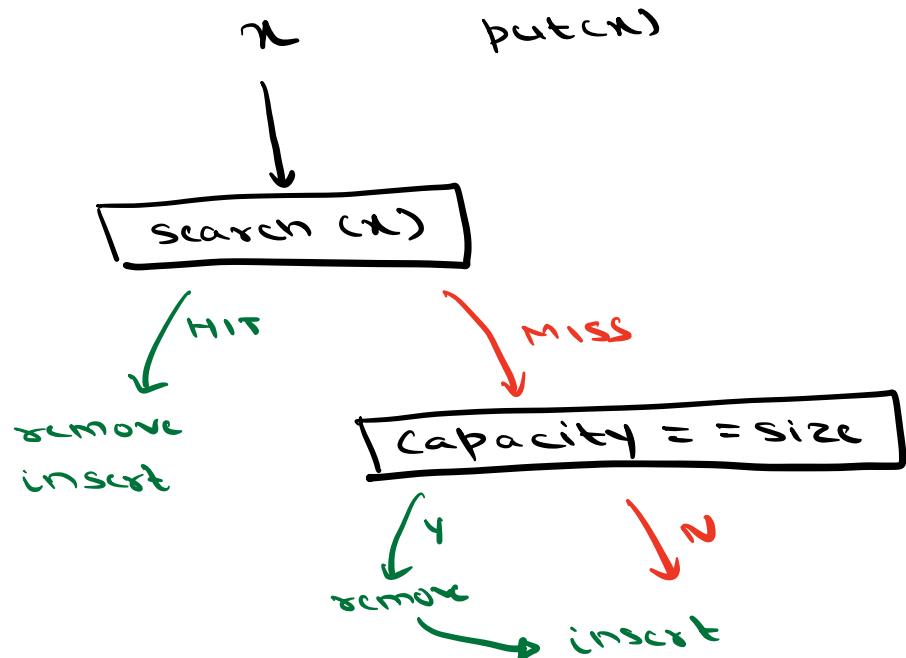
capacity = 5

size = $\emptyset \times 7 \neq 4 \times 5$

present not present
in cache cache

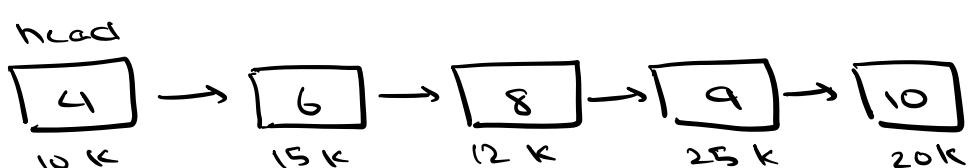
↓
hit / miss

Search
insert
delete



	array	LL	HM	LL+HM
search	$O(N)$	$O(N)$	$O(1)$	$O(1)$
insert	$O(1)$	$O(1)$	$O(1)$	$O(1)$
delete	$O(N)$	$O(1)$	order of insertion not maintained	$O(N)$

Del in LL $\rightarrow O(N)$



capacity = 5

Cache

4, 10 K
6, 15 K
8, 12 K
9, 25 K
10, 20 K

When data 8 comes \rightarrow HIT \rightarrow del 8 at 12 K
but 6.next has to be updated.

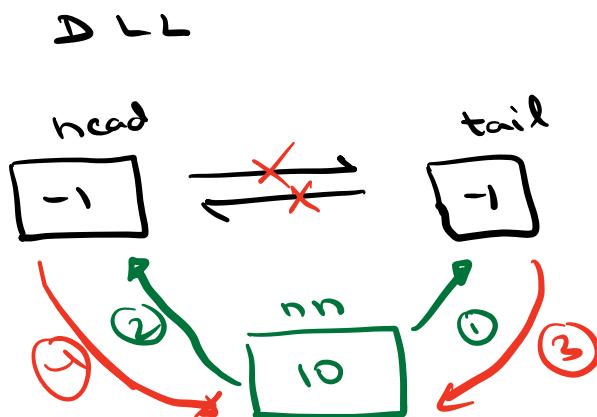
Iterating to reach prev of 8 takes $O(N)$
 Hence deletion in LL is $O(N)$.

Reaching prev from node 8 is $O(1)$ if we take DLL

	DLL + HM
search	$O(1)$
insert	$O(1)$
delete	$O(1)$

10 15 19 20 15 18 23 20 19 17 17

capacity = 5



HM
 $\langle \text{int, Node} \rangle$
 10, addr of 10

add To Tail (Node nn) <

$$nn.\text{next} = \text{tail} \quad (1)$$

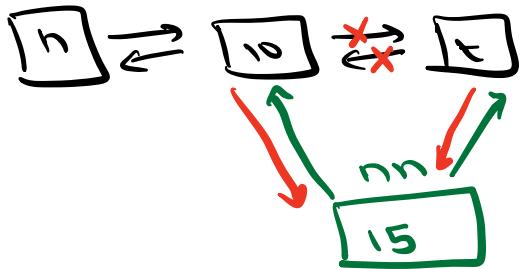
$$nn.\text{prev} = \text{tail}.\text{prev} \quad (2)$$

$$\text{tail}.\text{prev} = nn \quad (3)$$

$$nn.\text{prev}.\text{next} = nn \quad (4)$$

10 15 19 20 15 18 23 20 19

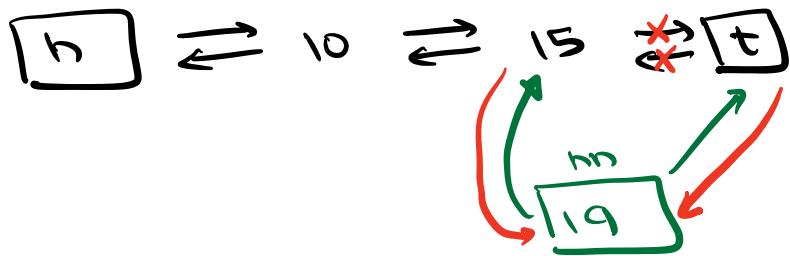
Add
15



Map

10, addr of 10
15, addr of 15

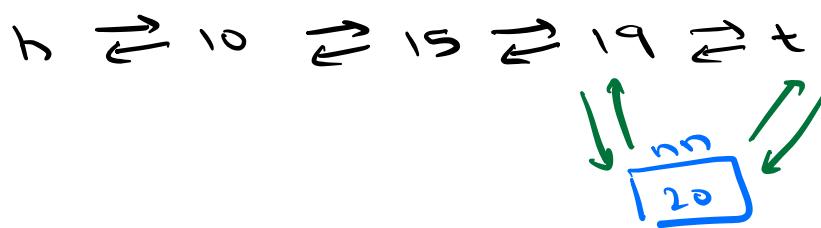
Add
19



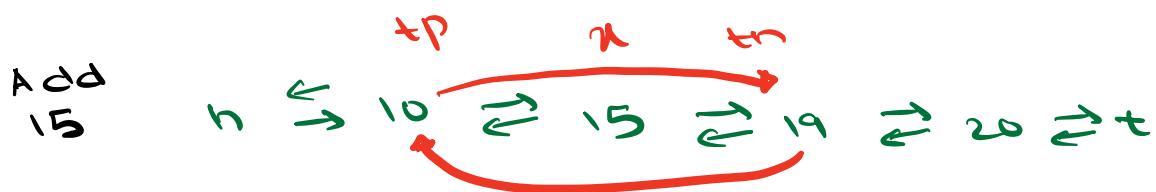
Map

10, addr
15, addr
19, addr

Add
20



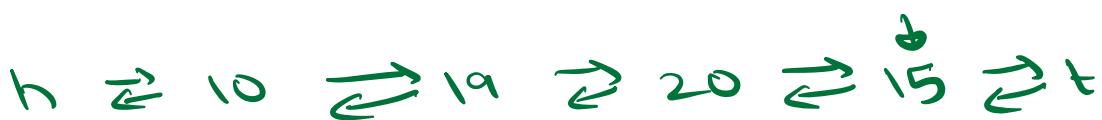
10, addr
15, addr
19, addr
20, addr



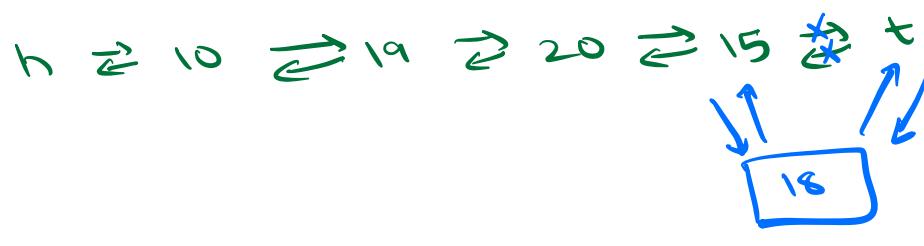
→ remove (Node x) <

$$\begin{aligned}
 \text{tp} &= x.\text{prev} \\
 \text{tn} &= x.\text{next} \\
 \text{tp}.\text{next} &= \text{tn} \\
 \text{tn}.\text{prev} &= \text{tp}
 \end{aligned}$$

→ add to Tail (x)



Add
18



HM

- 10, addr
- 15, addr
- 19, addr
- 20, addr
- 18, addr

Add
23



① remove (h.next)

// del 10 node

HM

~~10, addr~~

- ② hm.delete(10)
 ③ add to tail(23)

$\text{r} \rightarrow 19 \rightarrow 20 \rightarrow 15 \rightarrow 18 \rightarrow 23 \rightarrow \text{t}$

15, add
 19, add
 20, add
 18, add

Add
20

$\text{r} \rightarrow 19 \rightarrow \cancel{20} \rightarrow 15 \rightarrow 18 \rightarrow 23 \rightarrow \text{t}$

Node $\text{n} = \text{hm.get}(20)$

remove(n)

insert To tail(n)

HM	
15,	—
19,	—
20,	—
18,	—
23,	—

$\text{r} \rightarrow 19 \rightarrow 15 \rightarrow 18 \rightarrow 23 \rightarrow 20 \rightarrow \text{t}$

Add
19

$\text{r} \rightarrow \cancel{19} \rightarrow \cancel{20} \rightarrow 15 \rightarrow 18 \rightarrow 23 \rightarrow 20 \rightarrow 19 \rightarrow \text{t}$

HM	
15,	—
19,	—
20,	—
18,	—
23,	—

Node $\text{n} = \text{hm.get}(19)$

remove(n)

insert To tail(n)

put(x)

$\downarrow x$

search(x) in HM

$\downarrow h$

$\downarrow m$

- get ref from HM
Node xref
- remove (xref)
- insert at tail (xref)

capacity == size

$\downarrow y$

- remove (h.next)
- remove from HM

\downarrow

- create node
- insert in HM
 (x, mn)
- insert at tail (mn)

\nearrow

```
Node h = new Node (-1)
Node t = new Node (-1)
h.next = t
t.prev = h
```



```
HashMap<int, Node> hm
```

```
— LRU (int d, int cap) <
    if (hm.search(d)) <
        Node t = hm[d]
        remove(t)
        add to tail(t)
    else <
        if (hm.size() == cap) <
            Node del = h.next
            hm.delete(del.data)
            remove(del)
        Node nn = new Node (d)
        add to tail(nn)
        hm.insert (d, nn)
```

remove (Node n) <

 tp = n.prev
 tn = n.next
 tp.next = tn
 tn.prev = tp

add To Tail (Node nn) <

 nn.next = tail
 nn.prev = tail.prev
 tail.prev = nn
 nn.prev.next = nn

4