

# C++ Programming

## 1D Arrays Homework 2

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# Homework 9: Recamán's sequence

- Sequence is a series of numbers. The first terms are 0, 1, 3, 6, 2, **7**, ...
  - So last term **value** is 7 and its **index** is 5 (zero based)
  - The next value is either:
    - **Last value-last index-1** if 2 conditions satisfied
      - It is  $> 0$
      - It did not appear before
      - E.g.  $7 \text{ (last value)} - 5 \text{ (last index)} - 1 = 7 - 5 - 1 = 1$  ( $> 0$  but already exists)
    - Or last **value+last index+1** =  $7 + 5 + 1 = 13$
- Read integer index ([0, 200]) and print the value of this index
  - E.g.  $(6 \Rightarrow 13)$ ,  $(9 \Rightarrow 21)$ ,  $(17 \Rightarrow 25)$
- Don't use nested loops
- The series is: 0, 1, 3, 6, 2, 7, **13**, 20, 12, **21**, 11, 22, 10, 23, 9, 24, 8, **25**, 43

# Homework 10: Fixed sliding window

- Read Integers  $K$  and  $N$ , (where  $K \leq N$ ). then read  $N \leq 200$  integers. Then find a sub-array of  $K$  elements that has maximum sum.
- Input 3 7      1 0 3 -4 2 -6 9
  - Let's list all sub-arrays of length 3
  - 1 0 3       $\Rightarrow$  sum = 4
  - 0 3 -4       $\Rightarrow$  sum = -1
  - 3 -4 2       $\Rightarrow$  sum = 1
  - -4 2 -6       $\Rightarrow$  sum = -8
  - 2 -6 9       $\Rightarrow$  sum = 5
- Output: 4 6 5      (Sub-array from indices 4 to 6 has maximum sum of 5)
- Hard: Can you do without nested loops? There are 2 ways.

# Homework 11: Count increasing subarrays

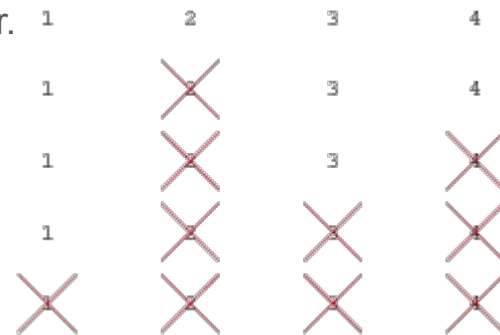
- Read an Integer N, then read  $N \leq 200$  integers. Count how many sub-arrays are increasing in the array. A sub-array is set of consecutive numbers in array
- E.g. If array is 1 2 3 4
  - We can find all sub-arrays of length 1  $\Rightarrow$  1 / 2 / 3 / 4
  - All sub-arrays of length 2  $\Rightarrow$  1, 2 / 2, 3 / 3, 4
  - All sub-arrays of length 3  $\Rightarrow$  1, 2, 3 / 2, 3, 4
  - All sub-arrays of length 4  $\Rightarrow$  1, 2, 3, 4
- Inputs  $\Rightarrow$  Outputs
  - 4 1 2 3 4  $\Rightarrow$  10 [10 sub-arrays from previous example, all are increasing]
  - 4 4 3 2 1  $\Rightarrow$  4 [only sub-arrays of length 1 can be considered]
  - 4 10 20 1 5  $\Rightarrow$  6
- Easy using 3 nested loops. Medium using 2 loops. Can you do it with 1 loop?

# Homework 12: Josephus problem

- Read integers  $N$  ( $\leq 200$ ) and  $K$  ( $\leq 1000000$ ). Find the game winner for following game:
- We have a group of  $N$  people in Circle. They are numbered 1, 2, ...,  $N$ 
  - Someone is the master of the game.
  - He starts from Person #1. Count  $K$ . Then remove this person from the circle.
  - He keeps doing so till only 1 person remains. This is the winner.

- Input 4 2

- Means we have people: 1, 2, 3, 4. Master starts at 1
- Count 2 persons (2 removed), start from 3
- Count 2 persons (4 removed), start from 1
- Count 2 persons (3 removed), 1 is winner



- Output

- People removed in order: 2 4 3 1 [same answer for 10 2 why?]

# Homework 13: longest subarray

- Read integers N ( $\leq 1000$ ) then N numbers each is either 0 or 1. Find longest **subarray** with number of zeros = numbers of ones
  - You can easily implement it using 3 loops
  - Or with little thinking using 2 loops (even with no extra arrays)
  - Hard: You can implement it without any nested loops
- Inputs  $\Rightarrow$  outputs
  - 7    1 0 0 0 1 1 1  $\Rightarrow$  6                      (e.g. 100011 or 000111)
  - 19   1 0 0 0 0 0 1 0 1 1 0 1 0 0 0 0 0 0 1  $\Rightarrow$  8                 (e.g. 00101101)
- Reduction
  - How may this problem be reduced to another problem: longest subarray of zero sum?

*“Acquire knowledge and impart it to the people.”*

*“Seek knowledge from the Cradle to the Grave.”*