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Assignment - 1 - 12-11-2022

Q.1 Air Traffic Data

→ Let us consider a set observation recorded in a database

$$\therefore A = [\text{Day, season, Fog, Rain}]$$

with 20 tuples

$$\therefore C = [\text{On Time, Late, Very Late, Cancelled}]$$

To find most likely classification for any other unseen instance:

Week Day, Winter, High, None, ?

\therefore Conditional Probability: $\therefore P(Y/x_1, \dots, x_n)$

$$= P(x_1/y) \cdot P(x_2/y)$$

$$P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{P(B \cap A)}{P(B)} = \frac{P(x_1/y) \cdot P(x_2/y) \dots P(x_n/y)}{P(y)}$$

$$= P(B|A) \cdot P(A)$$

| | | Class | | | |
|-----------|----------|-------------|-----------|------------|-----------|
| Attribute | | On-Time | Late | Very Late | Cancelled |
| Day | Weekday | 9/14 = 0.64 | 1/2 = 0.5 | 3/3 = 1 | 0/1 = 0 |
| | Saturday | 2/14 = 0.14 | 1/2 = 0.5 | 0/3 = 0 | 1/1 = 1 |
| | Sunday | 1/14 = 0.07 | 0/2 = 0 | 0/3 = 0 | 0/1 = 0 |
| | Holiday | 2/14 = 0.14 | 0/2 = 0 | 0/3 = 0 | 0/1 = 0 |
| Season | Spring | 4/14 = 0.29 | 0/2 = 0 | 0/3 = 0 | 0/1 = 0 |
| | Summer | 6/14 = 0.43 | 0/2 = 0 | 0/3 = 0 | 0/1 = 0 |
| | Autumn | 2/14 = 0.14 | 0/2 = 0 | 0/3 = 0.33 | 0/1 = 0 |
| | Winter | 2/14 = 0.14 | 2/2 = 1 | 2/3 = 0.67 | 0/1 = 0 |

| | | | | | |
|-------------------|--------|----------------|---------------|---------------|---------------|
| Fog | None | $5/14 = 0.36$ | $0/2 = 0$ | $0/3 = 0$ | $0/1 = 0$ |
| | High | $4/14 = 0.29$ | $1/2 = 0.5$ | $1/3 = 0.33$ | $1/1 = 1$ |
| | Normal | $5/14 = 0.36$ | $1/2 = 0.5$ | $2/3 = 0.67$ | $0/1 = 0$ |
| Rain | None | $5/14 = 0.36$ | $1/2 = 0.5$ | $1/3 = 0.33$ | $0/1 = 0$ |
| | Slight | $8/14 = 0.57$ | $0/2 = 0$ | $0/3 = 0$ | $0/1 = 0$ |
| | Heavy | $1/14 = 0.07$ | $1/2 = 0.5$ | $2/3 = 0.67$ | $1/1 = 1$ |
| Prior Probability | | $14/20 = 0.70$ | $2/20 = 0.10$ | $3/20 = 0.15$ | $1/20 = 0.05$ |

Weekday - Winter - High - None - ???

Case 1: Class = On-Time : Prior Probability (On-time)
 \times Weekday (On-Time) - Day
 \times (Winter (On-Time) - season
 \times (Fog High (On-time) - Fog
 \times None (On-Time) - Rain

$$= 0.70 \times 0.64 \times 0.14 \times 0.29 \times 0.36$$

$$= \underline{0.0065}$$

Prior Probability (Late)

Case 2: Class = Late : $0.10 \times 0.5 \times 1 \times 0.5 \times 0.5$

$$= \underline{0.0125}$$

Prior Probability (Very Late)

Case 3: Class = Very Late : $0.15 \times 1 \times 0.67 \times 0.33 \times 0.36$

$$= \underline{0.0109}$$

prior probability (Cancelled)

Case 4: Class = Cancelled : $0.05 \times 0 \times 0 \times 1 \times 0$

$$= \underline{0.000}$$

Highest Probability Occurs for the case 2 (Late).

Therefore, Case 2 is the strongest;

Hence correct classification is Late.

So, When the day is Weekday, Season is Winter, Fog is High, Rain is None, Class mostly like to 'Late'

Q.2

1. Expected Frequencies

The expected e_{ij} frequency which can be computed as

$$e_{ij} = \frac{\text{count}(A=a_i) \times \text{count}(B=b_j)}{N}$$

where N = no. of data tuples.

$\text{count}(A=a_i)$ = no. of tuples having value a_i for A

$\text{count}(B=b_j)$ = no. of tuples having value b_j for B

Now,

$$e_{11} = [\text{count}(\text{male}) \times \text{count}(\text{fiction})] / N$$

$$\therefore e_{11} = [300 \times 450] / 1500 = \underline{\underline{90}}$$

$$\therefore e_{12} = [1200 \times 450] / 1500 = \underline{\underline{360}}$$

$$\therefore e_{13} = [300 \times 1050] / 1500 = \underline{\underline{210}}$$

$$\therefore e_{22} = [1200 \times 1050] / 1500 = \underline{\underline{840}}$$

$$\chi^2 = \sum_{i=1}^m \sum_{j=1}^n \frac{(O_{ij} - E_{ij})^2}{E_{ij}}$$

O_{ij} = Observed Frequency

E_{ij} = Expected frequency

m & n are no. of rows & no. of columns

| Gender preferred read | Male | Female | Total |
|--------------------------|----------|------------|-------|
| Fiction | 250 (90) | 200 (360) | 450 |
| Non-Fiction | 50 (210) | 1000 (840) | 1050 |
| Total | 300 | 1200 | 1500 |

H_0 : Preferred Reading & gender are independent of each other.

H_a : Preferred Reading & gender are not independent each other.

Noted that in any row, the sum of the expected frequencies must equal the total observed frequency for that row

$$\chi^2 = \sum \frac{(\text{Observed} - \text{Expected})^2}{\text{Expected}}$$

$$\begin{aligned} \therefore \chi^2 &= \frac{(250-90)^2}{90} + \frac{(50-210)^2}{210} + \frac{(200-360)^2}{360} \\ &\quad + \frac{(1000-840)^2}{840} \\ &= 284.44 + 121.90 + 71.11 + 30.48 \end{aligned}$$

$$\therefore \chi^2 = \underline{\underline{507.93}}$$

For this given table,

| | Male | Female | Sum (row) |
|-------------|----------|------------|-----------|
| Fiction | 250 (90) | 200 (360) | 450 |
| Non-fiction | 50 (210) | 1000 (840) | 1050 |
| sum (col.) | 300 | 1200 | 1500 |

the degree of freedom are $\frac{(m-1)(n-1)}{(2-1)(2-1)} = 1$,

For 1 degree of freedom,

Value χ^2 with degree of freedom 1 and 0.01 significance level from the standard statistical table is 6.635 or 10.828 (taken from the table of upper % points of χ^2)

Our receive value is above this value. Therefore we can reject the hypothesis that gender & preferred reading are independent and conclude that the two attributes are strongly correlated for given group of people.