# ST625 Chapter 3 Example using R

## Ryan

September 7, 2015

## 3.9 A complete example

Step1. Model is  $y = \beta_0 + \beta_1 x + \epsilon$ 

```
formula = formula('damageY~distanceX')
```

#### Step2. get the data

fire damage data

## Step3 fit the model using the data

model fitting using lm

```
fireModel <- lm(formula, data = fire)
fireModel$coefficients</pre>
```

```
## (Intercept) distanceX
## 10.277929 4.919331
```

model fitting using formula

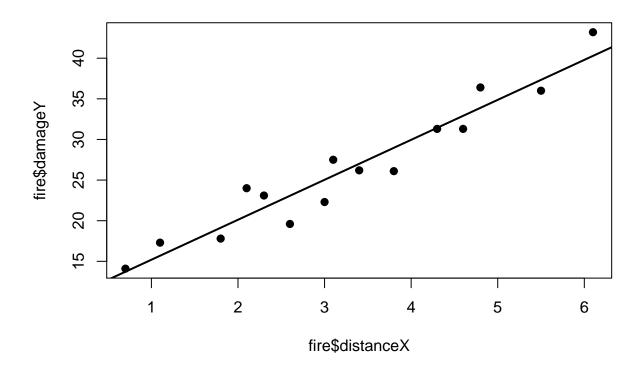
```
SSxx = sum((fire$distanceX-mean(fire$distanceX))^2)
SSxy = sum((fire$distanceX-mean(fire$distanceX))*(fire$damageY-mean(fire$damageY)))
b1 = SSxy/SSxx
b0 = mean(fire$damageY) - b1 * mean(fire$distanceX)
b0;b1
```

```
## [1] 10.27793
```

## [1] 4.919331

scatter plot with the regression line

plot(x = fire\$distanceX, y = fire\$damageY, pch = 19)
abline(fireModel, lwd = 2)



Step4. Check assumptions on random error

$$\mathbf{1} \ \mathbb{E}(\epsilon) = 0$$

## mean(fireModel\$residuals)

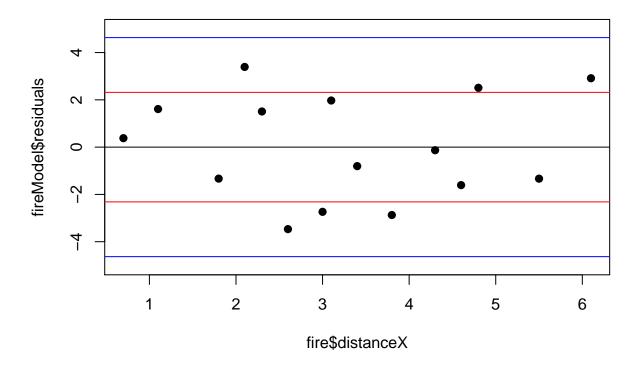
## [1] 4.070818e-17

2  $Var(\epsilon)$  is constant

MSE = sum(fireModel\$residuals^2)/fireModel\$df.residual
MSE

## [1] 5.36546

```
RMSE = sqrt(MSE)
plot(fire$distanceX, fireModel$residuals, pch = 19, ylim = c(-5,5))
abline(0,0)
abline(2.316,0, col = 'red')
abline(-2.316,0, col = 'red')
abline(2 * 2.316,0, col = 'blue')
abline(2 * -2.316,0, col = 'blue')
```

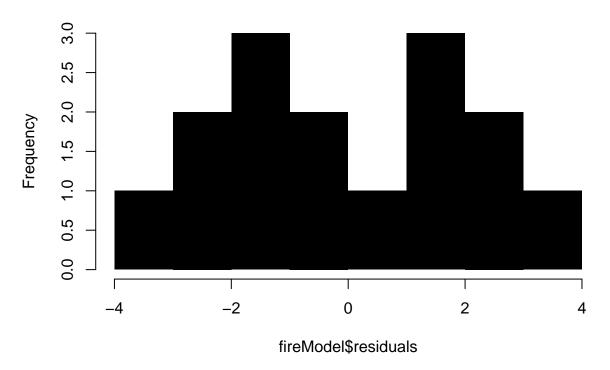


## 3 $\epsilon$ normally distributed

 $using\ histogram$ 

```
hist(fireModel$residuals, border = F, col = 'black')
```

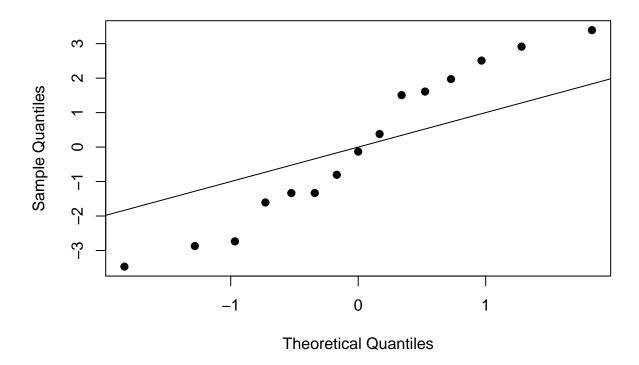
## Histogram of fireModel\$residuals



using qq plot

```
qqnorm(fireModel$residuals, pch = 19)
abline(0,1)
```

## Normal Q-Q Plot



coefficient of variation

## 100\*RMSE/mean(fire\$damageY)

## [1] 8.769609

Summary information

## summary(fireModel)

```
##
## Call:
## lm(formula = formula, data = fire)
##
## Residuals:
##
               1Q Median
                                      Max
  -3.4682 -1.4705 -0.1311 1.7915 3.3915
##
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 10.2779
                           1.4203
                                   7.237 6.59e-06 ***
## distanceX
                4.9193
                           0.3927 12.525 1.25e-08 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 2.316 on 13 degrees of freedom
## Multiple R-squared: 0.9235, Adjusted R-squared: 0.9176
## F-statistic: 156.9 on 1 and 13 DF, p-value: 1.248e-08
```

## Step5. Assess model adequacy

a Test of model utility

```
SE = RMSE/sqrt(SSxx)
t = b1/SE
2*pt(-1*abs(t), df = fireModel$df.residual)
```

```
## [1] 1.2478e-08
```

#### b Confidence interval for slope

using the R function

#### confint(fireModel)

```
## 2.5 % 97.5 %
## (Intercept) 7.209605 13.346252
## distanceX 4.070851 5.767811
```

hand calculation

```
b1 + qt(0.025, df = fireModel$df.residual) * SE * <math>c(1,-1)
```

```
## [1] 4.070851 5.767811
```

c Numerical descriptive measures of model adequacy

R Squared calculated by hand

```
SSE = sum(fireModel$residuals^2)
SSyy = sum((fire$damageY-mean(fire$damageY))^2)
RSquare = 1- SSE/SSyy
RSquare
```

## [1] 0.9234782

## summary(fireModel)

```
##
## Call:
## lm(formula = formula, data = fire)
##
```

```
## Residuals:
##
      Min
               1Q Median
                              30
                                     Max
## -3.4682 -1.4705 -0.1311 1.7915 3.3915
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 10.2779 1.4203 7.237 6.59e-06 ***
                           0.3927 12.525 1.25e-08 ***
## distanceX
               4.9193
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.316 on 13 degrees of freedom
## Multiple R-squared: 0.9235, Adjusted R-squared: 0.9176
## F-statistic: 156.9 on 1 and 13 DF, p-value: 1.248e-08
```

Coefficient of correlation by hand and using function

```
cor(fire$damageY, fire$distanceX)
```

## [1] 0.9609777

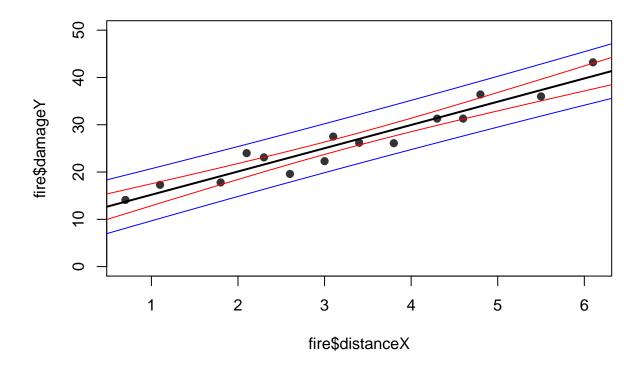
```
SSxy/sqrt(SSxx*SSyy)
```

## [1] 0.9609777

#### Step6. Prediction

ignore the tideous calculation

```
linspace = seq(0,7,0.01)
confInterval <- predict(fireModel,</pre>
                          newdata = data.frame(distanceX = linspace),
                           interval = "confidence")
predInterval <- predict(fireModel,</pre>
                          newdata = data.frame(distanceX = linspace),
                          interval = "prediction")
plot(x = fire$distanceX,
     y = fire$damageY,
     pch = 19,
     ylim=c(0,50),
      col = adjustcolor('black', alpha.f = 0.8))
abline(fireModel, lwd = 2)
points(x= linspace, y = confInterval[,2], type = 'l', col = 'red')
points(\underline{x}= linspace, \overline{y} = confInterval[,3], \overline{type} = '1', \underline{col} = 'red')
points(x= linspace, y = predInterval[,2], type = '1', col = 'blue')
points(x= linspace, y = predInterval[,3], type = '1', col = 'blue')
```



Make perdiction on perticular value

## fit lwr upr ## 1 27.49559 22.32394 32.66723