

Choose the correct answer in the Exercises 11 and 12.

11. If A, B are symmetric matrices of same order, then  $AB - BA$  is a

- (A) Skew symmetric matrix (B) Symmetric matrix  
(C) Zero matrix (D) Identity matrix

12. If  $A = \begin{bmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix}$ , then  $A + A' = I$ , if the value of  $\alpha$  is

- (A)  $\frac{\pi}{6}$  (B)  $\frac{\pi}{3}$   
(C)  $\pi$  (D)  $\frac{3\pi}{2}$

### 3.7 Elementary Operation (Transformation) of a Matrix

There are six operations (transformations) on a matrix, three of which are due to rows and three due to columns, which are known as *elementary operations* or *transformations*.

- (i) *The interchange of any two rows or two columns.* Symbolically the interchange of  $i^{\text{th}}$  and  $j^{\text{th}}$  rows is denoted by  $R_i \leftrightarrow R_j$  and interchange of  $i^{\text{th}}$  and  $j^{\text{th}}$  column is denoted by  $C_i \leftrightarrow C_j$ .

For example, applying  $R_1 \leftrightarrow R_2$  to  $A = \begin{bmatrix} 1 & 2 & 1 \\ -1 & \sqrt{3} & 1 \\ 5 & 6 & 7 \end{bmatrix}$ , we get  $\begin{bmatrix} -1 & \sqrt{3} & 1 \\ 1 & 2 & 1 \\ 5 & 6 & 7 \end{bmatrix}$ .

- (ii) *The multiplication of the elements of any row or column by a non zero number.* Symbolically, the multiplication of each element of the  $i^{\text{th}}$  row by  $k$ , where  $k \neq 0$  is denoted by  $R_i \rightarrow kR_i$ .

The corresponding column operation is denoted by  $C_i \rightarrow kC_i$

For example, applying  $C_3 \rightarrow \frac{1}{7}C_3$ , to  $B = \begin{bmatrix} 1 & 2 & 1 \\ -1 & \sqrt{3} & 1 \end{bmatrix}$ , we get  $\begin{bmatrix} 1 & 2 & \frac{1}{7} \\ -1 & \sqrt{3} & \frac{1}{7} \end{bmatrix}$

- (iii) *The addition to the elements of any row or column, the corresponding elements of any other row or column multiplied by any non zero number.*

Symbolically, the addition to the elements of  $i^{\text{th}}$  row, the corresponding elements of  $j^{\text{th}}$  row multiplied by  $k$  is denoted by  $R_i \rightarrow R_i + kR_j$ .