

Simulation and Scientific Computing
Assignment 3

The Conjugate Gradient Method and MPI Parallelization

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Contents

1 Task 2a	2
2 Task 2b	3

1 Task 2a

Latency is α

No. of Elements is k

BW of the transfer is β

So the time required to transfer k elements $T_k = \frac{k}{\beta}$

So the total time required for communication adding the latency of transfer is,

$$T_t = \alpha + \frac{k}{\beta}$$

As k elements are transferred, total no. of k iterations are possible with one transfer.

And number of updates = $\sum_{i=1}^{k-1} i$ and X is the time required for each update.

So total no. of updates in k iteration = $X \cdot \sum_{i=1}^{k-1} i = X \cdot \frac{k(k-1)}{2}$

So total time for k iteration = $\alpha + \frac{k}{\beta} + X \cdot \frac{k(k-1)}{2}$

Hence parallel overhead/process/iteration = $\frac{1}{k} (\alpha + \frac{k}{\beta} + X \cdot \frac{k(k-1)}{2})$

So $T_{tot} = \frac{\alpha}{k} + \frac{X(k-1)}{2} + \frac{1}{\beta}$ (Answer.)

2 Task 2b

As from 2a we have,

$$T_{tot} = \frac{\alpha}{k} + \frac{X(k-1)}{2} + \frac{1}{\beta}$$

To get the best value of k we have to take the differentiation of above equation and equate to 0.

$$\frac{dT_{tot}}{dk} = -\frac{\alpha}{k^2} + \frac{X}{2} = 0$$

$$\text{As } k \geq 0, k = \sqrt{\frac{2\alpha}{X}}$$

So putting $\alpha = 2$ ms, $X = 0.2$ ms here, $k = \sqrt{\frac{4}{0.2}} = \sqrt{20} \approx 4.472$

$$\begin{aligned} \text{Let's take } k = 5, T_{tot} &= \frac{2}{5} + \frac{0.2 \times 4}{2} + \frac{1}{30} \\ &= 0.4 + 0.4 + .0333 \approx 0.833ms. \end{aligned}$$

So Answer is best value of $k = 5$, and $T_{tot} = 0.833ms$.