Using the expression of e from Eq. (29.3), we have

$$R = 1 - \frac{\cot \alpha_1}{2(\cot \alpha_1 + \cot \beta_1)}$$
 (29.4)

The inlet blade angle  $\beta_1$  of a Francis runner varies  $_{45-120}^{o}$  and the guide vane angle angle  $\alpha_1$  from  $_{10-40}^{o}$ . The ratio of blade width to the diameter of runner B/D, at blade inlet, depends upon the required specific speed and varies from 1/20 to 2/3.

Expression for specific speed. The dimensional specific speed of a turbine, can be written as

$$N_{s_T} = \frac{NP^{1/2}}{H^{5/4}}$$

Power generated P for a turbine can be expressed in terms of available head H and hydraulic efficiency  $\eta_h$  as

$$P = \rho Q g H \eta_h$$

Hence, it becomes

$$N_{s_T} = N(\rho Q g \eta_h)^{1/2} H^{-3/4}$$
 (29.5)

Again,  $N = U_1 / \pi D_1$ ,

Substituting  $\,U_1\,$  from Eq. (29.2b)

$$N = \frac{V_{f_1} \left(\cot \alpha_1 + \cot \beta_1\right)}{\pi D_1}$$
 (29.6)

Available head H equals the head delivered by the turbine plus the head lost at the exit. Thus,

 $gH=e+(V_{f_2}^2 \ / \ 2)$  since  $V_{f_1}=V_{f_2}$   $gH=e+(V_{f_1}^2 \ / \ 2)$ 

with the help of Eq. (29.3), it becomes

$$gH = V_{f_1}^2 \cot \alpha_1 \left(\cot \alpha_1 + \cot \beta_1\right) + \frac{V_{f_1}^2}{2}$$
 or, 
$$H = \frac{V_{f_1}^2}{2g} [1 + 2 \cot \alpha_1 \left(\cot \alpha_1 + \cot \beta_1\right)] \tag{29.7}$$

Substituting the values of H and N from Eqs (29.7) and (29.6) respectively into the expression  $N_{\rm S}_T$  given by Eq. (29.5), we get,

$$N_{s_T} = 2^{3/4} g^{5/4} (\rho \eta_h Q)^{1/2} \frac{V_{f_1}^{-1/2}}{\pi D_1} (\cot \alpha_1 + \cot \beta_1) [1 + 2 \cot \alpha_1 (\cot \alpha_1 + \cot \beta_1)^{-3/4}]$$

Flow velocity at inlet  $V_{\hat{f_1}}$  can be substituted from the equation of continuity as

$$V_{f_1} = \frac{Q}{\pi D_1 B}$$

where B is the width of the runner at its inlet

Finally, the expression for  $N_{s_{\mathcal{T}}}$  becomes,

$$N_{sT} = 2^{3/4} g^{5/4} (\rho \eta_h)^{1/2} (\frac{B}{\pi D_l})^{1/2} (\cot \alpha_l + \cot \beta_l)$$

$$[1 + 2 \cot \alpha_l (\cot \alpha_l + \cot \beta_l))^{-3/4}$$
(29.8)

For a Francis turbine, the variations of geometrical parameters like  $\alpha_1,\beta_1$  B/D have been described earlier. These variations cover a range of specific speed between 50 and 400. Figure 29.2 shows an overview of a Francis Turbine. The figure is specifically shown in order to convey the size and relative dimensions of a

