## Linear regression

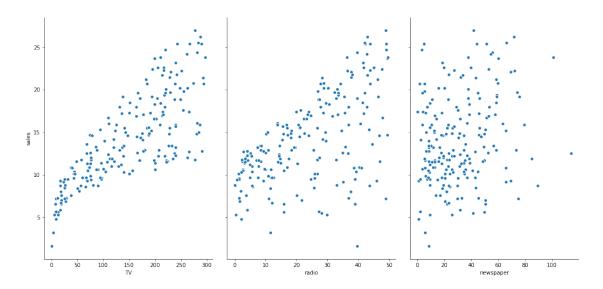
## May 1, 2018

```
In [1]: from sklearn import linear_model
In [2]: reg = linear_model.LinearRegression()
In [3]: reg.fit ([[0, 0], [1, 1], [2, 2]], [0, 1, 2])
Out[3]: LinearRegression(copy_X=True, fit_intercept=True, n_jobs=1, normalize=False)
In [4]: reg.coef_
Out[4]: array([ 0.5,  0.5])
In [5]: import pandas as pd
       import seaborn as sns
       import statsmodels.formula.api as smf
       from sklearn.linear_model import LinearRegression
       from sklearn import metrics
       from sklearn.cross_validation import train_test_split
        import numpy as np
        # allow plots to appear directly in the notebook
       %matplotlib inline
/usr/lib64/python2.7/site-packages/sklearn/cross_validation.py:41: DeprecationWarning: This modu
  "This module will be removed in 0.20.", DeprecationWarning)
In [6]: # read data into a DataFrame
       data = pd.read_csv('http://www-bcf.usc.edu/~gareth/ISL/Advertising.csv', index_col=0)
       data.head()
Out[6]:
             TV radio newspaper sales
       1 230.1
                  37.8
                             69.2
                                    22.1
       2 44.5
                  39.3
                             45.1 10.4
          17.2 45.9
                             69.3 9.3
       4 151.5 41.3
                             58.5 18.5
       5 180.8 10.8
                        58.4 12.9
In [7]: data.shape
```

Out[7]: (200, 4)

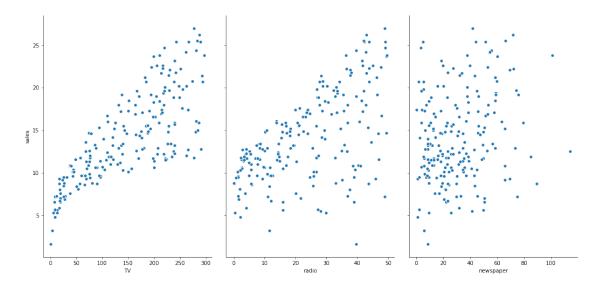
In [10]: # visualize the relationship between the features and the response using scatterplots sns.pairplot(data, x\_vars=['TV','radio','newspaper'], y\_vars='sales', size=7, aspect=0.

Out[10]: <seaborn.axisgrid.PairGrid at 0x6607550>

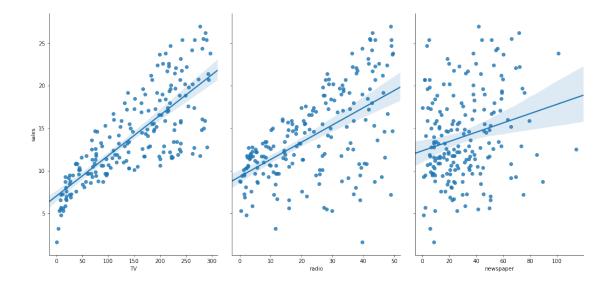


In [11]: # visualize the relationship between the features and the response using scatterplots sns.pairplot(data, x\_vars=['TV','radio','newspaper'], y\_vars='sales', size=7, aspect=0.

Out[11]: <seaborn.axisgrid.PairGrid at 0x6bbc090>



```
In [12]: lm1 = smf.ols(formula='sales ~ TV', data=data).fit()
In [13]: lm1.params
Out[13]: Intercept
                      7.032594
                      0.047537
         dtype: float64
In [14]: ### SCIKIT-LEARN ###
         # create X and y
         feature_cols = ['TV']
         X = data[feature_cols]
         y = data.sales
In [15]: # instantiate and fit
         lm2 = LinearRegression()
         lm2.fit(X, y)
Out[15]: LinearRegression(copy_X=True, fit_intercept=True, n_jobs=1, normalize=False)
In [16]: # print the coefficients
         print(lm2.intercept_)
         print(lm2.coef_)
7.03259354913
[ 0.04753664]
In [17]: ### STATSMODELS ###
         # you have to create a DataFrame since the Statsmodels formula interface expects it
         X_new = pd.DataFrame({'TV': [50]})
         # predict for a new observation
         lm1.predict(X_new)
Out[17]: 0
              9.409426
         dtype: float64
In [18]: lm2.predict(50)
Out[18]: array([ 9.40942557])
In [19]: sns.pairplot(data, x_vars=['TV', 'radio', 'newspaper'], y_vars='sales', size=7, aspect=0.
Out[19]: <seaborn.axisgrid.PairGrid at 0x79be750>
```



```
In [20]: lm1.conf_int()
Out[20]:
         Intercept 6.129719 7.935468
                    0.042231 0.052843
In [21]: lm1.pvalues
Out[21]: Intercept
                      1.406300e-35
                      1.467390e-42
         dtype: float64
In [22]: lm1.rsquared
Out[22]: 0.61187505085007099
In [23]: lm2.score(X, y)
Out [23]: 0.61187505085007099
In [24]: lm1.pvalues
Out[24]: Intercept
                      1.406300e-35
                      1.467390e-42
         dtype: float64
In [25]: ### STATSMODELS ###
         # create a fitted model with all three features
         lm1 = smf.ols(formula='sales ~ TV + radio + newspaper', data=data).fit()
         # print the coefficients
         lm1.params
```

```
Out[25]: Intercept
                    2.938889
        TV
                    0.045765
        radio
                    0.188530
                   -0.001037
        newspaper
        dtype: float64
In [26]: #Multiple Linear Regression
In [27]: #STATSMODEL
        lm1 = smf.ols(formula='sales ~ TV + radio + newspaper', data=data).fit()
        lm1.params
Out[27]: Intercept
                    2.938889
        TV
                    0.045765
        radio
                    0.188530
        newspaper -0.001037
        dtype: float64
In [28]: #scikit learn
        feature_cols = ['TV', 'radio', 'newspaper']
        X = data[feature_cols]
        Y = data.sales
        #instantaiate and fit
        lm2 = LinearRegression()
        lm2.fit(X, y)
        #print the coefficients
        print(lm2.intercept_)
        print(lm2.coef_)
2.93888936946
[ 0.04576465  0.18853002  -0.00103749]
In [29]: list(zip(feature_cols, lm2.coef_))
Out[29]: [('TV', 0.045764645455397601),
         ('radio', 0.18853001691820442),
         ('newspaper', -0.0010374930424763007)]
In [30]: lm1.summary()
Out[30]: <class 'statsmodels.iolib.summary.Summary'>
                                   OLS Regression Results
        ______
        Dep. Variable:
                                      sales
                                              R-squared:
                                                                             0.897
```

```
Method:
                        Least Squares F-statistic:
                                                             570.3
                                   Prob (F-statistic):
                                                          1.58e-96
      Date:
                     Tue, 01 May 2018
      Time:
                            18:12:24
                                   Log-Likelihood:
                                                           -386.18
      No. Observations:
                                200
                                    AIC:
                                                             780.4
      Df Residuals:
                                196
                                   BIC:
                                                             793.6
      Df Model:
                                 3
      Covariance Type: nonrobust
                  coef std err t P>|t| [0.025 0.975]
      ______
                2.9389
                          0.312 9.422 0.000
                                                   2.324
      Intercept
                                                             3.554
                         0.001 32.809 0.000
      TV
                                                   0.043
                0.0458
                                                             0.049
                 0.1885
                          0.009
                                 21.893
                                          0.000
                                                   0.172
      radio
                                                             0.206
                               -0.177 0.860
      newspaper -0.0010
                                                -0.013
                          0.006
      ______
      Omnibus:
                             60.414 Durbin-Watson:
                                                             2.084
      Prob(Omnibus):
                              0.000 Jarque-Bera (JB):
                                                           151.241
      Skew:
                             -1.327 Prob(JB):
                                                          1.44e-33
      Kurtosis:
                              6.332 Cond. No.
                                                              454.
      _____
      [1] Standard Errors assume that the covariance matrix of the errors is correctly specif
      11 11 11
In [31]: #Handling categorical feature with 2 categories
      np.random.seed(12345)
      nums = np.random.rand(len(data))
      mask_large = nums > 0.5
      data['Size'] = 'small'
      data.loc[mask_large, 'Size'] = 'large'
      data.head()
Out[31]:
           TV radio newspaper sales Size
      1 230.1 37.8
                      69.2 22.1 large
      2 44.5 39.3
                      45.1 10.4 small
      3 17.2 45.9
                      69.3 9.3 small
      4 151.5 41.3
5 180.8 10.8
                       58.5 18.5 small
                       58.4 12.9 large
In [32]: data['Size_large'] = data.Size.map({'small':0, 'large':1})
      data.head()
Out[32]:
           TV radio newspaper sales Size Size_large
      1 230.1 37.8
                       69.2 22.1 large
      2 44.5 39.3
                     45.1 10.4 small
```

OLS

Adj. R-squared:

0.896

Model:

3	17.2	45.9	69.3	9.3	small	0
4	151.5	41.3	58.5	18.5	small	0
5	180.8	10.8	58.4	12.9	large	1