Part 2: Unsupervised Learning (K-means)

Due April 19, 2020 by 11:59pm AZ time.

Project Overview:

In this part, you are required to implement the k-means algorithm and apply your implementation on the given dataset, which contains a set of 2-D points. You are required to implement two different strategies for choosing the initial cluster centers.

**A data file for you to download:**

[AllSamples.mat](https://d3c33hcgiwev3.cloudfront.net/dcG9m8gvEemRPArJHNevzg_b3ba7dd655bd4dafb06a913ff8515732_AllSamples.mat?Expires=1587081600&Signature=G8QDyPXdEepjtLuyILVZ2fapH3japylolp8iuZ~kH1IvCBTcmRgTqxkinaT~x6b18Fp1i43J6XFhr1vOWxBnaSvQ32aEwfC9bjTb3TqRB5SjDjcE3MpAW739S8vYIWi-5mOZuytbN~j9X0I14oSv8Dh1uP~8XrLq8B7MAjafJiI_&Key-Pair-Id=APKAJLTNE6QMUY6HBC5A)

Strategy 1: randomly pick the initial centers from the given samples.

Strategy 2: pick the first center randomly; for the i-th center (i>1), choose a sample (among all possible samples) such that the average distance of this chosen one to all previous (i-1) centers is maximal.

You need to test your implementation on the given data, with the number k of clusters ranging from 2-10. Plot the objective function value vs. the number of clusters k. Under each strategy, plot the objective function twice, each start from a different initialization.

(Referring to the course notes:  When clustering the samples into k clusters/sets Di, with respective center/mean vectors 𝜇1, 𝜇2, … 𝜇k,  the objective function is defined as ∑*ki*=1∑*x*∈*Di*||*x*−*μi*||2 )

Algorithms:

k-Means Clustering

Resources:

A 2-D dataset to be provided.

Workspace:

Any Python programming environment.

Software:

Python environment.

Language(s):

Python.

Required Tasks:

1. Write code to implement the k-means algorithm with Strategy 1.

2. Use your code to do clustering on the given data; compute the objective function as a function of k (k = 2, 3, …, 10).

3. Repeat the above step with another initialization.

4. Write code to implement the k-means algorithm with Strategy 2.

5. Use your code to do clustering on the given data; compute the objective function as a function of k (k = 2, 3, …, 10).

6. Repeat the above step with another initialization.

7. Submit a short report summarizing the results, including the plots for the objective function values under different settings described above.

What to Submit and Due Dates

1. Code file with comments explaining what you do for each part as directed

2. A report that summarizes the results and includes the plots for each of the objective function values.

The code and reports are due at the end of Week 5.

Evaluation criteria:

Working code and correct final results:

Code:

* 4 points - Correctly implements the k-Means algorithm with Strategy 1
* 1 point - Code is used to correctly do clustering on the given data; computes the objective function as a function of k (k - 2, 3, …, 10).
* 4 points - Correctly implements the k-Means algorithm with Strategy 2
* 1 point - Code is used to correctly do clustering on the given data; computes the objective function as a function of k (k - 2, 3, …, 10).
* 4 points - Each of these code parts is correctly documented in comments

Report:

* 2 points - Report summarizes results
* 4 points - The plots for the objective function values under each of the settings described in the code criteria