

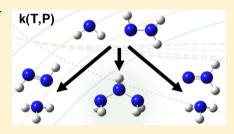
Large Intermediates in Hydrazine Decomposition: A Theoretical Study of the N₃H₅ and N₄H₆ Potential Energy Surfaces

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Supporting Information

ABSTRACT: Large complex formation involved in the thermal decomposition of hydrazine (N_2H_4) is studied using transition state theory-based theoretical kinetics. A comprehensive analysis of the N₃H₅ and N₄H₆ potential energy surfaces was performed at the CCSD(T)-F12a/aug-cc-pVTZ//ωB97x-D3/6-311++G(3df,3pd) level of theory, and pressure-dependent rate coefficients were determined. There are no low-barrier unimolecular decomposition pathways for triazane (n-N₃H₅), and its formation becomes more significant as the pressure increases; it is the primary product of N₂H₃ + NH₂ below 550, 800, 1150, and 1600 K at 0.1, 1, 10, and 100 bar, respectively. The N₄H₆ surface has two important entry channels,



 $N_2H_4 + H_2NN$ and $N_2H_3 + N_3H_3$, each with different primary products. Interestingly, $N_2H_4 + H_2NN$ primarily forms $N_3H_3 + H_3NN$ N_2H_3 , while disproportionation of $N_2H_3 + N_2H_3$ predominantly leads to the other N_2H_2 isomer, HNNH. Stabilized tetrazane $(n-N_4H_6)$ formation from $N_2H_3 + N_2H_3$ becomes significant only at relatively high pressures and low temperatures because of fall-off back into $N_2H_3 + N_2H_3$. Pressure-dependent rate coefficients for all considered reactions as well as thermodynamic properties of triazane and tetrazane, which should be considered for kinetic modeling of chemical processes involving nitrogenand hydrogen-containing species, are reported.

1. INTRODUCTION

Hydrazine (N₂H₄), the main component of diamine-based rocket fuels, is an excellent propellant: using oxygen as the oxidizer, it is only second to hydrogen in terms of the specific impulse (thrust developed per fuel mass per unit time) it generates. Its decomposition could lead to autoignition and detonation,²⁻⁴ and it is sometimes used as a monopropellant, usually by decomposing over a catalyst. Hydrazine and hydrazine-based fuels such as monomethyl hydrazine are more commonly used as bipropellants with N2O5 as the oxidizer. Hydrazine is used in thruster engines for attitude and in-orbit control of satellites and spacecraft, where it is being stored and utilized at a maximal pressure of about 25 bar.⁵

No detailed kinetic models for hydrazine-based fuel combustion in N₂O₅ exist in the current literature; a step toward this goal is understanding hydrazine decomposition better. Detailed kinetic models for hydrazine decomposition were previously suggested by Halat-Augier et al.8 as well as by Konnov and De Ruyck. More recently, however, computations of the N_2H_2 , N_2H_3 , N_2H_3 , and N_2H_4 potential energy surfaces (PESs) determined updated kinetics. Interestingly, none of the previous works on hydrazine decomposition has considered species containing more than two nitrogen atoms. In the absence of an oxidizer, a monopropellant's decomposition could be thought of as an extreme case of fuelrich combustion, a chemistry region in which fuel-radical recombination reactions often play a significant role. At low pressures, chemically activated isomerization and decompositions are often important. As the working pressure increases, radical recombination reactions, leading to the formation of relatively large complexes, become more significant because of collisional stabilization.

Unlike carbon, nitrogen does not normally form the major elemental backbone of large molecules. For example, an experimental study of tetrazene (linear unsaturated N₄H₄) determined that its thermolysis in the solid phase begins at room temperature, whereas in the gas phase it is metastable.¹³ Moreover, cyclic nitrogenous rings, and specifically tetrazetidine (cyclic N_4H_4), were determined to have relatively high ring strain energies. ^{14–16} However, a theoretical study of triazane (N₃H₅) concluded that it is kinetically stable.¹⁷ Tetrazane (saturated N_4H_6) was also studied theoretically, and its most stable stereoisomer was determined, 18 yet its overall kinetic stability was not assessed. A subatmospheric roomtemperature experimental observation of N₂H₃ self-reaction concluded that the disproportionation reaction yielding N₂H₄ + N₂H₂ is approximately four times faster than a recombination reaction yielding tetrazane, unlike the tendency of the analogous hydrocarbon radical, C₂H₅. Yet, the behavior of the N₂H₃ + N₂H₃ system at high temperatures and different pressures, and specifically the importance of well-skipping chemically activated reactions, has not been reported in the literature.

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In the present contribution, we examine the hypothesis that abundant radicals in decomposing hydrazine might form relatively large complexes such as triazane and tetrazane, becoming more significant as the pressure increases. We therefore explore the NH $_2$ + N $_2$ H $_3$ and N $_2$ H $_3$ + N $_2$ H $_3$ reactions which lead to pressure-dependent kinetic networks on the N $_3$ H $_5$ and N $_4$ H $_6$ PESs, respectively. Specifically, collisional-stabilized formation of the complexes along with well-skipping reactions is considered, and pressure-dependent rate coefficients are determined.

2. THEORETICAL METHODS

2.1. Characterization of the PES. Geometric structures and vibrational frequencies for all wells and saddle points considered here were obtained using density functional theory employing the ω B97x-D3 functional²⁰ and the 6-311++G-(3df,3pd) basis set.²¹ Frequencies were scaled by a recommended factor of 0.97027²⁷ to account for their average overestimation, due in part to anharmonicity. The growing string method (GSM)²² was used to provide initial guesses for some of the transition state geometries. Intrinsic reaction coordinate (IRC) calculations²³ were used to verify all transition state configurations by tracking the minimum energy paths, leading to adjacent local minima.

Higher level single-point energies were obtained by employing the explicitly correlated coupled-cluster CCSD-(T)-F12a method 24,25 and using an augmented Dunning's correlation consistent, polarized valence triple-ζ (aug-ccpVTZ) basis set.²⁶ Zero-point energy (ZPE) corrections were incorporated into the final energies reported here. Previously, Hwang and Mebel¹⁰ showed that CCSD(T)/6-311G(d,p) level energies are reliable (do not deviate by more than 2 kcal mol⁻¹ from respective multireference CASSCF calculations using the full valence active space) for similar N/H systems on the N_2H_4 potential. The comparison included the iminoammonium (NH3NH) species, a zwitterionic compound similar in structure to other zwitterions discussed in the present work. A high value of the T_1 diagnostic parameter²⁸ implies that additional dynamic electron correlation retrieved by a multireference method could be significant. At the CCSD(T)-F12a/aug-cc-pVTZ level, the T_1 value for NH₃NH is 0.0112, similar to the T_1 range of the various stable species reported in the present work (0.0090-0.0151). However, radicals such as N₂H₃ and N₃H₄ have higher T₁ values in the range of 0.0211-0.0247, indicating a larger uncertainty in their energies.

Starting from the optimized geometries, separate relaxed potential energy scans were performed as a function of the dihedral angle around each single bond for all stationary points on the PES. All scans had a 10° increment resolution, unless otherwise noted. These hindered rotor (HR) scans were performed using density functional theory employing the Becke-3-Lee-Yang-Parr (B3LYP) functional²⁹ and the 6-311++G(3df,3pd) basis set.²¹ The potential energies were fitted to truncated Fourier series and used as an input to Arkane, an open-source master equation (ME) and transition state theory (TST) solver included within the Reaction Mechanism Generator (RMG) suite, 30,31 to compute the partition functions. The potential scans are given in the Supporting Information (Figures S1-S10). The optimized geometry was verified to have the lowest energy on these potential scans.

Q-Chem 4.4.0³² was used for geometry optimizations and frequency calculations. Molpro 2015.1^{33,34} was used for coupled-cluster electronic energy calculations. Gaussian³⁵ was used for all dihedral angle rotor scans, IRC, and GSM calculations. Radical species were computed using unrestricted methods. IQmol³⁶ was used to plot molecular orbitals generated using the NBO 6.0 population analysis software.³⁷

2.2. Calculation of Thermodynamic Parameters. Energies at zero K (E_0) of n-N₃H₅, n-N₃H₄, i-N₃H₄, and n-N₄H₆ were computed at the CCSD(T)-F12/cc-pVTZ-F12 level of theory using geometries optimized at the ω B97x-D3/6-311++D(3df,3pd) level of theory. Frequencies were calculated at the same level as the geometries, and scaled using a recommended factor of 0.984. ^{38,39} 1D HR scans were done at the B3LYP/6-311++G(3df,3pd) level of theory. Finally, bond additivity corrections (BACs) were implemented using Arkane.

2.3. Calculation of Kinetic Parameters. Both highpressure (P) limit and P-dependent thermal rate coefficients, k(T) and k(T,P), were calculated at CCSD(T)-F12a/aug-ccpVTZ//ωB97x-D3/6-311++G(3df,3pd) using Arkane. Values of k(T) for every elementary chemical reaction which has an energy barrier were calculated by a TST analysis 40 using the rigid-rotor harmonic oscillator (RRHO) approximation with low-energy (<40 kJ mol⁻¹ barrier) internal rotations modeled as 1D HRs. The effect of internal rotation(s) on the harmonic frequencies was eliminated by projection. 41 One-dimensional asymmetric tunneling through tight transition states was incorporated by assuming that the reaction path can be described by an Eckart function. 42 Phenomenological k(T,P)'s were computed by applying the microcanonical RRKM (Rice-Ramsperger-Kassel-Marcus) theory to solve the ME⁴³ under the modified strong collision (MSC) approximation (RRHO and 1D HR approximations were also used in calculating the densities of states). 44 Calculations were performed at a mesh of (T_i, P_i) points, and the $k(T_i, P_i)$ was fitted to a Chebyshev polynomial suitable for use in Cantera⁴⁵ or the commercial version of CHEMKIN.⁴⁶ The reported rate coefficients incorporate appropriate degeneracy factors. For barrierless pathways, high-P(T)'s estimates (either using literature data or estimated by the respective RMG template) were input into Arkane and converted into k(E)'s for solution of the ME using an inverse Laplace transform. 44 As is usually done when constructing the ME, the input channel was treated as pseudofirst-order and dissociations into bimolecular products in Pdependent networks were treated as irreversible. The rate coefficients of collisional energy transfer for deactivating collisions were modeled using the "single exponential down" expression

$$P(E \leftarrow E') \propto \exp\left(-\frac{E' - E}{\langle \Delta E_{\rm d} \rangle}\right), \qquad E' > E$$

where $\langle \Delta E_{\rm d} \rangle$ is a measure of the collision efficiency. We computed $\langle \Delta E_{\rm d} \rangle$ for N₃H₅ + N₂ and N₄H₆ + N₂ at several temperatures using classical trajectory approaches^{47–49} and PES construction strategies⁵⁰ described in detail elsewhere. The trajectory-based results are well-represented (to better than 10%) by the expressions $\langle \Delta E_{\rm d} \rangle = 175 (T/298~{\rm K})^{0.52}~{\rm cm}^{-1}$ and $\langle \Delta E_{\rm d} \rangle = 250 (T/298~{\rm K})^{0.30}~{\rm cm}^{-1}$ from T=300 to 3000 K for N₃H₅ + N₂ and N₄H₆ + N₂, respectively. The calculated values of $\langle \Delta E_{\rm d} \rangle$ for the two systems are similar at high T, while $\langle \Delta E_{\rm d} \rangle$ is larger for N₄H₆ than for N₃H₅ at low T. These trends are consistent with those reported previously for hydrocarbons

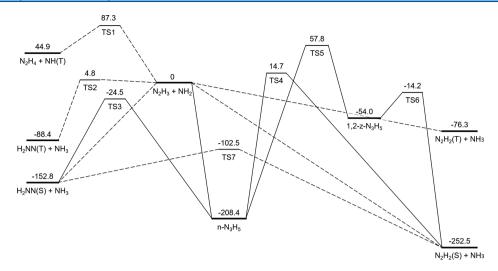


Figure 1. Reaction path diagram for the N_3H_5 PES. Dashed lines represent nonpressure-dependent pathways. (S) and (T) represent singlet or triplet multiplicities, respectively. Energies are in kJ mol⁻¹ and scaled relative to the $N_2H_3 + NH_2$ entry channel, which was set at zero.

and several bath gases, 51 where we also showed that trajectory-based values of $\langle \Delta E_{\rm d} \rangle$ often have a weaker temperature dependence than the $T^{0.85}$ appearing in the empirical standard expression. 52 In addition to uncertainties arising from the value of $\langle \Delta E_{\rm d} \rangle$, errors in the present collision model may be attributed to simplifications in the expression for $P(E \leftarrow E')$ given above and to the neglect of rovibrational anharmonicity when evaluating the density of states near threshold. Hopewhen, we often find empirically (e.g., for methane, and 2-methyl-allyl radical that the use of the single exponential down model along with trajectory-based values of $\langle \Delta E_{\rm d} \rangle$ predicts k_0 with errors of a factor of two or less, thanks in part to a cancellation of errors when rovibrational anharmonicity is neglected.

Transport parameters (Lennard-Jones parameters, dipole moment, and polarizability) were calculated using the OneDMin code, 56 Molpro, and Gaussian. These Lennard-Jones parameters (well depth and collision diameter) are also necessary for pressure-dependent rate coefficient calculations, specifically for the collision frequency calculation. Lennard-Jones parameters were calculated using a DF-MP2/aug-ccpVDZ PES with N₂ as the collider. Similar calculations (MP2/ aug-cc-pVDZ) were previously shown to be within 10% of the more accurate MP2/CBS and QCISD(T)/CBS computations; 56 similar errors were found in tests of this approach against experimental and higher-level theoretical diffusion coefficients.⁵⁷ The dipole moment and polarizability parameters were computed at the B2PLYPD3/cc-pVTZ level. All transport parameters are given in the Supporting Information (Table S1).

Network sensitivity analysis was conducted using Arkane by perturbing each of the relevant wells and transition states in the PES and determining the effect on the calculated pressuredependent rate coefficients.

3. RESULTS AND DISCUSSION

3.1. N_3H_5 **System.** An N_3 isomer with the empirical chemical formula N_3H_5 could be generated in systems with relatively high concentrations of N_2H_3 and NH_2 radicals. This N_3H_5 potential energy diagram describes several ammoniaforming pathways (Figure 1). It consists of a pressure-dependent network on the singlet surface (Figure 1) with

two isomers, $n-N_3H_5$ (triazane, NH_2NHNH_2) and 1,2-z- N_3H_5 (NH_2NH_2NH) (Figure 2), as well as bimolecular pathways on

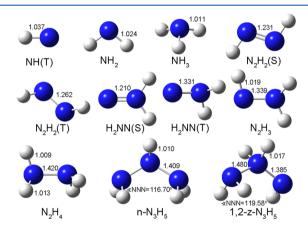


Figure 2. Geometric representation of species on the N_3H_5 PES optimized at the ω B97x-D3/6-311++G(3df,3pd) level of theory. Bond orders shown for illustration purpose only. Bond lengths are in angstroms and angles in degrees. Quantitative geometric data were added where it benefits the discussion; geometric coordinates for all species are available in the Supporting Information.

both the singlet and triplet surfaces. The "n" and "z" in the species names above stand for normal and zwitterion, respectively. Geometric representations of relevant species and saddle points are given in Figures 2 and 3, respectively. Table 1 lists point groups, rotational constants, and unscaled harmonic frequencies for all relevant species and transition states.

The entry channel of the pressure-dependent network, $N_2H_3 + NH_2$, leads via the $n-N_3H_5$ intermediate to two lower-energy bimolecular exit channels, each consisting of an N_2H_2 isomer and ammonia. The barrierless high-pressure limit rate coefficient for the complex formation reaction, $N_2H_3 + NH_2 \leftrightarrow n-N_3H_5$ (reaction B1, Table 2), was assumed to equal the rate coefficient of a similar reaction, $CH_3NH + NH_2 \leftrightarrow CH_3NHNH_2$, calculated at the CASPT2/aug-cc-pVDZ level. For simplicity, highly energetic wells were excluded from the PES. For example, $N_2H_2(S) + NH(S)$ formed barrierlessly

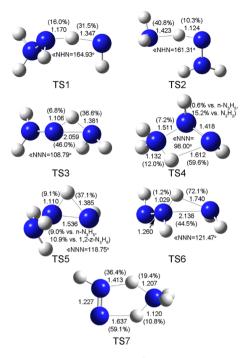


Figure 3. Geometric representation of transition states on the N_3H_5 PES optimized at the ω B97x-D3/6-311++G(3df,3pd) level of theory. Bond lengths are in angstroms and angles in degrees. Numbers in parentheses indicate the bond stretch fraction relative to the respective stable species. Quantitative geometric data were added where it benefits the discussion; geometric coordinates for all transition states are available in the Supporting Information.

Table 2. High-Pressure-Limit Rate Coefficients of Elementary Reactions on the N₃H₅ PES^a

				E_{2}	
no.b	reaction	A^c	n	$(kJ \text{ mol}^{-1})$	source ^d
R1	$\begin{array}{c} N_2H_4 + NH(T) \leftrightarrow \\ N_2H_3 + NH_2 \end{array}$	6.09×10^{1}	3.61	24.3	pw
R2	$N_2H_3 + NH_2 \leftrightarrow H_2NN(T) + NH_3$	3.10×10^{0}	3.43	-8.2	pw
R3	$\begin{array}{c} \text{n-N}_3 \text{H}_5 \leftrightarrow \\ \text{H}_2 \text{NN}(\text{S}) + \text{NH}_3 \end{array}$	1.04×10^{10}	1.14	177.1	pw
R4	$\begin{array}{c} \text{n-N}_3 \text{H}_5 \leftrightarrow \\ \text{N}_2 \text{H}_2 (\text{S}) + \text{NH}_3 \end{array}$	1.40×10^9	0.92	213.3	pw
R5	$\begin{array}{c} \text{n-N}_3\text{H}_5 \leftrightarrow \text{1,2-z-} \\ \text{N}_3\text{H}_5 \end{array}$	7.94×10^9	0.85	103.9	pw
R6	$ \begin{array}{c} 1,2-z-N_3H_5 \leftrightarrow \\ N_2H_2(S) + NH_3 \end{array} $	6.57×10^{11}	0.57	41.2	pw
R7	$\begin{array}{l} H_2NN(S) + NH_3 \\ \leftrightarrow N_2H_2(S) + \\ NH_3 \end{array}$	2.07×10^{-1}	3.64	31.1	pw
B1	$\begin{array}{c} N_2H_3 + NH_2 \leftrightarrow n - \\ N_3H_5 \end{array}$	5.02×10^{14}	-0.43	0.2	ref 58
B2	$\begin{array}{c} N_2H_3 + NH_2 \leftrightarrow \\ H_2NN(S) + NH_3 \end{array}$	3.00×10^{10}	0.50	0	est., pw
В3	$\begin{array}{c} N_2H_3 + NH_2 \leftrightarrow \\ N_2H_2(S) + NH_3 \end{array}$	9.20×10^{5}	1.94	4.8	ref 62

^aParameters are for the modified Arrhenius expression, $k = AT^n \exp(-E_a/[RT])$, in the 500–3000 K temperature range; the rate coefficient of reaction B1 is valid in the 200–2500 K temperature range. ^bThe R notations refer to reactions as discussed in the text; numbers match the transition states in Figure 3. The B notations refer to barrierless reactions. ^cUnits are s⁻¹ or cm³ mol⁻¹ s⁻¹ for first- or second-order reactions in the forward direction, respectively. ^dpw—calculated in the present work (see text); est.—estimated (see text).

Table 1. Point Groups, Rotational Constants, and Unscaled Vibrational Frequencies Calculated at the ω B97x-D3/6-311++G(3df,3pd) Level of Theory for Stationary Points on the N₃H₅ PES

stationary point	point group	rotational constants (cm ⁻¹)	harmonic frequencies (cm ⁻¹)
NH(T)	$C_{\infty \nu}$	16.66	3326.8
NH_2	$C_{2\nu}$	23.77, 12.93, 8.37	1519.9, 3418.0, 3510.4
NH_3	$C_{3\nu}$	10.02, 10.02, 6.31	1030.0, 1664.9, 1677.8, 3518.4, 3644.2, 3644.2
$H_2NN(S)$	$C_{2\nu}$	11.18, 1.34, 1.18	1016.2, 1342.2, 1642.3, 1735.5, 3154.9, 3165.2
$H_2NN(T)$	C_s	10.02, 1.13, 1.05	727.2, 1102.3, 1265.6, 1587.7, 3448.1, 3555.2
$N_2H_2(S)$	C_{2h}	10.25, 1.34, 1.18	1351.8, 1355.3, 1601.8, 1701.2, 3309.3, 3335.2
$N_2H_2(T)$	C_2	11.72, 1.17, 1.16	783.5, 1079.8, 1088.7, 1509.7, 3363.1, 3384.5
N_2H_3	C_1	6.91, 1.04, 0.91	519.0, 710.8, 1154.5, 1293.8, 1496.0, 1668.8, 3485.1, 3549.2, 3687.8
N_2H_4	C_2	4.89, 0.82, 0.82	444.4, 829.7, 973.6, 1154.1, 1311.8, 1342.6, 1681.1, 1693.0, 3515.3, 3524.0, 3619.1, 3623.6
$n-N_3H_5$	C_1	1.37, 0.34, 0.30	334.5, 449.9, 493.8, 824.4, 850.8, 962.2, 1160.4, 1183.5, 1253.9, 1361.3, 1532.8, 1669.9, 1697.6, 3447.3, 3462.0, 3584.0, 3599.0, 3610.7
$1,2-z-N_3H_5$	C_1	1.35, 0.33, 0.30	241.6, 452.6, 482.2, 820.8, 936.0, 982.5, 1169.0, 1203.3, 1403.5, 1457.6, 1504.8, 1645.9, 1671.8, 3357.0, 3466.1, 3482.1, 3520.1, 3559.7
TS1	C_1	1.09, 0.19, 0.17	1900.0i, 25.3, 163.7, 244.1, 463.5, 660.1, 748.7, 844.3, 1163.5, 1175.4, 1363.4, 1443.2, 1557.7, 1667.4, 3380.8, 3520.4, 3561.1, 3661.9
TS2	C_1	1.11, 0.21, 0.18	1229.9i, 164.8, 191.2, 379.7, 542.4, 608.6, 673.5, 878.7, 1079.1, 1262.4, 1297.9, 1498.5, 1553.4, 1632.0, 3444.4, 3499.3, 3535.9, 3655.8
TS3	C_1	1.33, 0.25, 0.22	1409.4i, 232.8, 293.8, 415.5, 557.1, 644.0, 767.8, 812.5, 1221.3, 1346.0, 1515.4, 1569.9, 1690.0, 2568.3, 3503.0, 3522.2, 3619.1, 3627.1
TS4	C_1	1.19, 0.37, 0.31	1194.1i, 286.9, 543.7, 656.7, 847.9, 977.5, 985.2, 1127.7, 1196.8, 1418.5, 1483.3, 1547.7, 1607.4, 2262.6, 3432.7, 3469.5, 3490.7, 3574.8
TS5	C_1	1.37, 0.32, 0.28	1603.4i, 317.7, 362.8, 429.3, 811.7, 914.5, 976.4, 1136.5, 1243.4, 1392.0, 1472.9, 1533.3, 1680.1, 2751.3, 3439.8, 3452.8, 3594.0, 3622.4
TS6	C_1	1.48, 0.22, 0.20	870.5i, 184.6, 284.0, 478.1, 546.1, 632.8, 712.6, 987.4, 1178.4, 1459.8, 1540.9, 1545.8, 1705.5, 3325.9, 3469.7, 3476.7, 3566.4, 3624.4
TS7	C_1	1.18, 0.25, 0.21	1358.0i, 393.8, 453.4, 476.6, 722.7, 752.5, 769.0, 1178.8, 1460.0, 1557.1, 1559.4, 1642.2, 1657.3, 1749.3, 2375.8, 3156.2, 3610.3, 3706.0

from 1,2-z- N_3H_5 is 192.0 kJ mol^{-1} above the N_2H_3 + NH_2 entry channel.

The $N_2H_2(S) + NH_3$ product well is the most stable product channel in Figure 1, yet the pathway forming the $H_2NN(S) + NH_3$ product well has a lower barrier (Figure 1). Nevertheless, all barriers surrounding $n-N_3H_5$ are relatively high; consequently, even moderate pressures would be enough for the excited complex to be stabilized as $n-N_3H_5$.

Iminoammonium (NH₃NH) and H₂NNHN were previously shown to be important intermediates in hydrazine decomposition 10,12 and triazene (N₃H₃) rearrangements, 59 respectively. Three similar nitrenes on the N₃H₅ surface could potentially exist, namely, NH₂NH₂NH, NH₃NNH₂, and NH₃NHNH, resulting from all possible intrahydrogen transfers in the system. Nevertheless, only NH₂NH₂NH (referred to herein as 1,2-z-N₃H₅, Figure 2) is unimolecularly connected to the entry channel, whereas rearrangements of n-N₃H₅ into NH₃NNH₂ and NH₃NHNH immediately lead to bimolecular products (i.e., via TS3 and TS4 in 1,2- and 1,3-NH₃ elimination reactions, respectively).

In addition to recombining to form n-N₃H₅, N₂H₃ + NH₂ can also react to directly form bimolecular products without going through the n-N₃H₅ well (see dashed lines in Figure 1). On the singlet surface, disproportionation reactions proceed barrierlessly, forming either $N_2H_2(S) + NH_3$ or $H_2NN(S) +$ NH₃. The triplet surface accommodates two hydrogen abstraction reactions via TS1 and TS2, forming N₂H₄ + NH(T) and $H_2NN(T) + NH_3$, respectively, as well as a barrierless reaction forming $N_2H_2(T) + NH_3$. The rate coefficient of the barrierless disproportionation reaction $N_2H_3 + NH_2 \leftrightarrow H_2NN(S) + NH_3$ (reaction B2 in Table 2) was estimated by ascribing an activation energy of zero to the rate coefficient of the respective nonbarrierless triplet reaction; in this estimation, the rate coefficient of the latter was refitted, constraining its temperature exponent to be 0.5 to obey the collision theory. The rate coefficient of $N_2H_3 + NH_2 \leftrightarrow$ N₂H₂(S) + NH₃ was adopted from Dean and Bozzelli⁶⁰ (reaction B3 in Table 2). No rate coefficient was assigned for the $N_2H_3 + NH_2 \leftrightarrow N_2H_2(T) + NH_3$ reaction, which leads to the least stable product channel in the system.

We note that optimization efforts of $N_3H_5(T)$ at the ω B97x-D3/6-311++G(3df,3pd) level of theory resulted in conformers that could be further stabilized by rotating one of the dihedral angles in the molecule. However, all such rotations (of the two identical rotors) resulted in β -scission of the central hydrogen atom, yielding i-N₃H₄ + H. Because N₃H₅(T) rapidly dissociates, intersystem crossing (ISC) behavior in the N₃H₅ PES is expected to be negligible. Additional ISC effects might play a role in the exit channels of this PES and were not determined within the present framework.

Reactions R1 and R2 (Table 2) describe hydrogen abstractions between N_2H_3 and NH_2 , where the abstracting radical is different in each reaction. Both transition states, TS1 and TS2 (Figure 3), have similar angles between the atoms participating in the reaction, $\angle NHN$, of about $160-165^{\circ}$. The reactions are synchronous and the transition states resemble the reactant geometry in the exothermic direction: TS1 has a 16.0% N-H bond stretch fraction relative to N_2H_4 and a 31.5% stretch relative to NH_2 , whereas TS2 has 10.3 and 40.8% stretches relative to N_2H_3 and NH_3 , respectively. Bond stretch fractions throughout the discussion are defined as $(r_{TS} - r_{\text{stable}})/r_{\text{stable}}$, where r_{stable} and r_{TS} are the relevant bond lengths in the stable species (either reactant or product, where

this bond exists) and the TS, respectively. In the exothermic direction, reaction R2 has an exceptionally low energy barrier of just 4.8 kJ mol^{-1} (Figure 1). It could be explained by the hydrogen bond formed between the nitrogen atom in the abstracting NH₂ group and one of the hydrogen atoms in N₂H₃, stabilizing this saddle point (Figure 4).

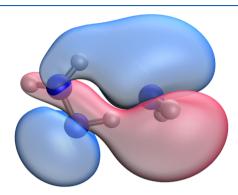


Figure 4. Highest *α*-electron occupied molecular orbital (MO 12) in the triplet saddle point TS2, computed at the ωB97x-D3/6-311++G(3df,3pd) level of theory.

The transition state of reaction R3, leading to $H_2NN(S)$ + NH₃ from the n-N₃H₅ isomer via a 1,2-NH₃ elimination route, is asynchronous, characterized by relatively large stretches in both N-N (46.0%) and terminal N-H (36.6%) bonds. These relatively large stretches explain the high E_0 of TS3, 128.3 and 183.9 kJ mol⁻¹ above the $H_2NN(S) + NH_3$ and $n-N_3H_5$ wells, respectively. The N-H bond stretch fraction in the intermediate nitrogen site, however, is significantly lower (6.8%). The ∠NNN backbone angle is smaller than in the n-N₃H₅ isomer (108.79° vs 116.70°). Indeed, a Mulliken electronic population analysis⁶¹ showed that the reacting NH₂ group (which leaves as NH₃) and the nonreacting NH₂ group have net formal charges of -0.33 and +0.24, respectively, while each of these groups has a net formal charge of -0.03 in the n-N₃H₅ isomer. The resulting electrostatic attraction forces cause the backbone angle to be smaller than in the isomer.

TS4 is the saddle point of a 1,3-NH₃ elimination reaction of n-N₃H₅. While the cyclic group in TS3 (describing a 1,2-NH₃ elimination reaction) is -N-H-N-, the geometry of TS4 involves a very strained four-membered ring group, -N-H-N-N-, distorting the molecule backbone. The formed ∠NNN angle in TS4 is significantly smaller than in n-N₃H₅, only 98.00° versus 116.70°. The N-N bond not directly participating in the reaction (with a bond length of 1.418 Å, Figure 3) is stretched relative to both reactant and product, in accordance with the high strain induced by the cyclic transition: slightly versus $n\text{-}N_3H_5$ (0.6%) and more significantly versus N₂H₂(S) (15.2%). As expected from the energetics of the reaction, the length of this bond is more similar to the respective value in n-N₃H₅. This transition is asynchronous because the hydrogen transfer has significantly progressed (having a 12.0% stretch relative to ammonia and a 59.6% stretch relative to n-N₃H₅), while the N-N scission has only started (7.2% stretch relative to n-N₃H₅).

The isomerization pathway via TS5 involves an internal hydrogen transfer between two adjacent nitrogen atoms in $n-N_3H_5$; yet unlike TS3, here the intermediate nitrogen atom is a hydrogen acceptor instead of a donor, resulting in a saddle

point raised 82.3 kJ mol⁻¹ above TS3. In contrast to TS3, the N-N bond is stretched significantly less (9.0% vs n-N₃H₅ and 10.9% vs 1,2-z-N₃H₅ compared to 46.0% in TS3) and does not result in scission. The ∠NNN backbone angle is also intermediate relative to the reacting isomers and slightly closer to the angle in the higher energy nitrene isomer. The distances of the migrating hydrogen with respect to both nitrogen atoms are markedly uneven (9.1% vs 1,2-z-N₃H₅ and 37.1% vs n-N₃H₅); this criterion too suggests a greater resemblance of the saddle point geometry to the nitrene isomer, in accordance with the reaction energetics.

An additional 1,2-NH3 elimination reaction in this system passes through TS6. Similar to TS3 which belongs to the same reaction family, TS6 is also asynchronous with significant bond stretch fractions with regard to $1,2-z-N_3H_5$ (44.5% N-N stretch) as well as NH₃ (a 72.1% N-H stretch). The large N-H bond stretch fraction is particularly peculiar when compared to the minor N-H bond stretch fraction of the intermediate nitrogen site (only 1.2%), as well as to the respective stretch in TS3 (only 36.6%). Moreover, the N-N bond not directly participating in the reaction is closer in length to the $N_2H_2(S)$ product (1.260 Å in TS6 vs 1.231 Å in $N_2H_2(S)$ and 1.385 Å in 1,2-z-N₃H₅). Finally, the formed \angle NNN backbone angle is slightly larger than in the reacting isomer $(121.47^{\circ} \text{ vs } 119.58^{\circ})$, unlike the TS3 case. A Mulliken electronic population analysis of TS6 shows that the reacting NH2 group and the nonreacting NH group have net formal charges of -0.45 and -0.19, respectively. The resulting electrostatic repulsion forces cause the backbone angle to be wider than in the isomer. It is noted that these groups have net formal charges of +0.12 and -0.43, respectively, in 1,2-z-N₃H₅. Calculated high-pressure-limit rate coefficients for the above reactions R1-R6 as well as estimated rate coefficients for barrierless reactions on the N₃H₅ diagram are given in Table 2.

Reaction R7 catalyzes the $H_2NN(S)$ to $N_2H_2(S)$ transformation using ammonia via a five-membered ring TS. This simultaneous hydrogen transfer TS is asynchronous. The bond lengths of the reacting hydrogens and their neighboring nitrogen atoms suggests an early TS, resembling H₂NN(S) + NH₃. Nevertheless, the N–N bond length (1.227 Å) is closer to the respective bond in $N_2H_3(S)$ (1.231 Å) rather than to the bond in $H_2NN(S)$ (1.210 Å).

It is noted that the N₂H₃ radical has strong coupling between large amplitude fluxional inversion of the amine group and a HR mode (Figure S3). This behavior, characterized by discontinuities in the relaxed potential scan curve due to an abrupt geometry change in the nitrogen backbone, is known to occur in similar systems. ¹⁶ A local maximum of ~80 kJ mol⁻¹, reached before the inversion point, and a global maximum of \sim 100 kJ mol⁻¹ suggest that this mode is significantly hindered. It was therefore not considered as a rotor in any of the calculations in the present work. Although thermodynamic properties of N₂H₃ are known, ^{63,64} the authors are not aware of a literature discussion of its 1D HR.

The rate coefficient of reaction R1 (Table 2) was previously estimated by Konnov and De Ruyck9 based on experimental and theoretical values for other $NH(T) + RH \leftrightarrow NH_2 + R$ hydrogen abstraction reactions, implementing an activation energy correction based on the Evans-Polanyi correlation. The present calculation and the previous estimation were found to be similar at ∼1250 K, yet the Konnov and De Ruyck rate coefficient has a slightly lower temperature dependence despite efforts to adjust its activation energy in that study

(Figure 5). Overall, the disagreement between these rate coefficients is acceptable, considering that one of the rate coefficients is an estimate.

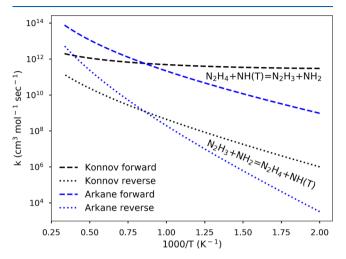


Figure 5. Rate coefficient comparisons of reaction R1 (forward) and R-1 (reverse) between the present work calculation using Arkane and the rate coefficient estimated and reported by Konnov and De Ruyck. Thermodynamic data from Curran et al. 4 were used to compute reverse rate coefficients.

As mentioned above, while $N_2H_2(S) + NH_3$ is more stable, the formation route of $H_2NN(S) + NH_3$ has a lower barrier (TS3, Figure 1). Indeed, the rate coefficient of the wellskipping reaction $N_2H_3 + NH_2 \leftrightarrow H_2NN(S) + NH_3$ is orders of magnitude faster than the respective rate coefficient of the competing reaction forming $N_2H_2(S)$ throughout the entire temperature and pressure ranges considered here (Figure 6a,b). The RRK (Rice-Ramsperger-Kassel) estimation by Dean and Bozzelli⁶⁰ for $N_2H_3 + NH_2 \leftrightarrow H_2NN(S) + NH_3$ by a well-skipping reaction via n-N₃H₅ is shown here to overestimate the respective calculated rate coefficients by about 2 orders of magnitude (Figure 6a) because Dean and Bozzelli assumed that TS3 had a lower barrier. Because of higher collisional stabilization of n-N₃H₅, the $k(T_1P)$ for N₂H₃ + NH₂ \leftrightarrow H₂NN(S) + NH₃ decreases at high pressures. Interestingly, this rate coefficient is not monotonic with temperature at low pressures (Figure 6a) because this reaction over TS3 is competing with dissociation back to the reactants.

Each of the product channels on this PES could also be formed via bimolecular nonpressure-dependent routes from $N_2H_3 + NH_2$. While the direct route forming $N_2H_2(S)$ is faster than the respective well-skipping reaction, the major formation route of H₂NN(S) is the well-skipping reaction at low pressures and temperatures and it is not negligible at the other studied conditions (Figure 6a,b). Accounting for both unimolecular and bimolecular pathways, H2NN(S) formation is favorable over H₂N₂(S) in this PES, contrary to a past kinetic stability estimation. 17 Because rate coefficients for both direct routes were estimated (in the present work and by Dean and Bozzelli), further work to determine these values with lower uncertainties is desired.

While 1,2-z-N₃H₅ formation in this network is negligible (rate coefficients not shown), n-N₃H₅ formation is significant because of the relatively high barriers surrounding this isomer (Figure 1). As expected, n-N₃H₅ formation becomes more significant at high pressures because of collisional stabilization

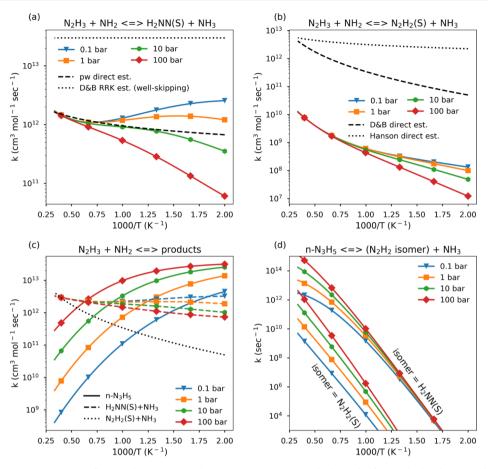


Figure 6. Rate coefficient comparisons of selected reactions on the N_3H_5 PES. "D&B" in the legend refers to the book chapter by Dean and Bozzelli from 2000, 60 and "Hanson" refers to a N/H/O rate coefficient review by Hanson and Salimian from 1984. 65 The present work is denoted as "pw". In (c), line types refer to the product/s, while the color refers to the pressure; the pressure dependence of the $N_2H_2(S) + NH_3$ formation rate is negligible, while formation rates of $H_2NN(S) + NH_3$ include both pressure-dependent and direct routes; the updated Dean and Bozzelli rate coefficient for $N_2H_2(S) + NH_3$ is shown.

(Figure 6c). It is also the major product in the network below a pressure-dependent temperature threshold: at 0.1, 1, 10, 25, and 100 bar, this threshold is about 550, 800, 1150, 1250, and 1600 K, respectively. The n-N₃H₅ isomer decomposes either while still excited at relatively low pressures if the temperature is high enough, forming preferably H₂NN(S) and NH₃ (Figure 6d), or after stabilization via hydrogen abstraction reactions mediated by the radical pool (mostly H, NH₂, and N₂H₃ in hydrazine decomposition systems). All relevant pressure-dependent rate coefficients for this PES are available in the Supporting Information.

A sensitivity analysis of pressure-dependent rate coefficients on the N_3H_5 PES was conducted, implementing the chemically significant eigenstate approach. This approach is more accurate than the MSC approximation, yet less robust, that is, often fails to converge for relatively large systems. Therefore, only the $N_2H_3 + NH_2$, $n-N_3H_5$, and $H_2NN(S) + NH_3$ wells on the N_3H_5 PES were considered for the sensitivity analysis. Results for three selected pressure-dependent reactions, describing $H_2NN(S) + NH_3$ formation either via formation of the $n-N_3H_5$ intermediate or skipping the isomer well, are shown (Figure 7).

The sensitivity coefficients for the $N_2H_3 + NH_2 \leftrightarrow n-N_3H_5$ reaction (Figure 7a) suggest that this reaction is in the pressure-dependent "fall-off" region at 1 bar and 1500 K. Increasing E_0 of either the $N_2H_3 + NH_2$ or the $n-N_3H_5$ wells

changes the density of states around the entry well, increasing or decreasing the rate, respectively. The sensitivity coefficients for $n-N_3H_5$ are lower at the higher pressure because at higher pressures the excited complex lifetime is much shorter, leading to less significant competition from the route via TS3. The $N_2H_3 + NH_2$ well has a higher sensitivity coefficient at the higher pressure because the leak rate through the submerged barrier TS3 forming $H_2NN(S) + NH_3$ is much lower at this condition, and a change in the entrance well E_0 has a larger relative impact.

The $n-N_3H_5 \leftrightarrow H_2NN(S) + NH_3$ reaction rate has a complex dependency on E_0 of the adduct, the $N_2H_3 + NH_2$ asymptote, and TS3 (Figure 7b). Perturbing the $n-N_3H_5$ well or the TS3 saddle point results in the expected behavior of the system: increasing E_0 of $n-N_3H_5$ or TS3 increases or decreases the rate, respectively. The system is slightly more sensitive to these parameters at the higher pressure (unlike the previous case) because this is a thermally activated reaction. Increasing E_0 of the $N_2H_3 + NH_2$ channel results in a slower reverse rate $(n-N_3H_5 \leftrightarrow N_2H_3 + NH_2)$, changing the branching ratio more in favor of the $H_2NN(S) + NH_3$ products. As the pressure increases, the reverse reaction becomes even less favorable, as reflected in the respective sensitivity coefficients at the different pressures.

The rate coefficient of the well-skipping reaction N_2H_3 + $NH_2 \leftrightarrow H_2NN(S)$ + NH_3 (Figure 7c) is sensitive to the

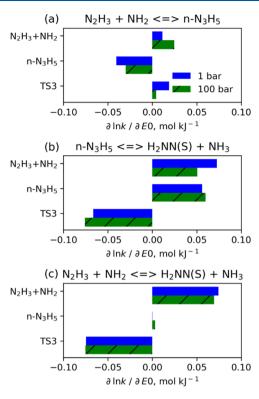


Figure 7. Normalized sensitivity coefficients to ZPE-corrected energies of $N_2H_3 + NH_2$, n- N_3H_5 , and TS3 for selected pressure-dependent rate coefficients on the N_3H_5 potential at 1 and 100 bar and at 1500 K.

energies of the entry channel and transition state, as expected. Increasing E_0 of the entry channel broadens the energy gap between this well and TS3, resulting in a higher rate, while increasing E_0 of TS3 has the opposite effect. This rate coefficient is relatively insensitive to the energy of n-N₃H₅.

The pressure-dependent rate sensitivity analysis allows one to assess the effects of uncertainties in this system. All sensitivity coefficients had values below 0.1 mol kJ^{-1} . The sensitivity coefficients of the important $N_2H_3 + NH_2 \leftrightarrow n-N_3H_5$ reaction, which has a significant flux in this system (Figure 6c), were below 0.05 mol kJ^{-1} . Therefore, if we can

determine the E_0 's to within about 10 kJ mol⁻¹, the rate coefficient uncertainty due to uncertainties in energies will be less than a factor of 2.

To assess the uncertainties due to estimations of barrierless reaction rate coefficients, we conducted a sensitivity analysis for the pressure-dependent rate coefficient of $N_2H_3 + NH_2 \leftrightarrow H_2NN(S) + NH_3$ by perturbing the PES entry channel, $N_2H_3 + NH_2 \leftrightarrow n-N_3H_5$. At 1, 15, and 80 bar, these normalized (dimensionless) sensitivity coefficients were 0.06, 0.10, and 0.14, respectively. At 15 bar, for example, perturbing the rate coefficient of the barrierless entry channel by factors of 1.05 and 1.50 resulted in 0.5% or 3.4% change, respectively, in the $k(T_2P)$ of $N_2H_3 + NH_2 \leftrightarrow H_2NN(S) + NH_3$.

We note that at high temperatures well merging could add additional uncertainties to the calculated rate coefficients. For example, at high enough temperatures, the 1,2-z-N₃H₅ isomer could merge with the N₂H₂(S) + NH₃ product well. Calculating the pressure-dependent rate coefficient of the well-skipping reaction N₂H₂ + NH₂ \leftrightarrow N₂H₂(S) + NH₃ after forcing the above wells to merge has no significant effect at 1000 K yet reduces the rate by a factor of 1.25 at 3000 K.

3.2. N_4H_6 **System.** High N_2H_3 concentration may lead to high fluxes on the N_4H_6 potential. The N_3H_5 and N_4H_6 systems are related because $H_2NN(S)$, a major product of the N_3H_5 PES, could react with hydrazine which has a high concentration at early times in the system. The N_2H_4 + $H_2NN(S)$ well, in turn, is one of the entry channels on the potential. Nevertheless, it is noted that $H_2NN(S)$ may have more important formation routes such as N_2H_3 disproportionation reactions. An additional entry channel on this potential is N_2H_3 + N_2H_3 . These two channels are interconvertible bimolecularly (Figure 8).

Various non-*P*-dependent dissociation products could be formed from the two reacting N_2H_3 radicals on both the singlet and triplet surfaces, of which the $N_2H_4 + N_2H_2(S)$ well is particularly stable. For simplicity, the highly energetic wells $NH_3NH + H_2NN(S)$, $NH_3NH + H_2NN(T)$, and $NH_3NH + N_2H_2(T)$ with energies (on the scale selected for Figure 8) of 183.1, 247.5, and 259.6 kJ mol⁻¹, respectively, are not shown. Two additional highly energetic product wells of the barrierless reactions 1,2-z- $N_4H_6 \leftrightarrow NHNH_2NH + NH_2$ and 2,3-z- $N_4H_6 \leftrightarrow NH_2NH_2N + NH_2$ with energies of 682.7 and 706.4 kJ

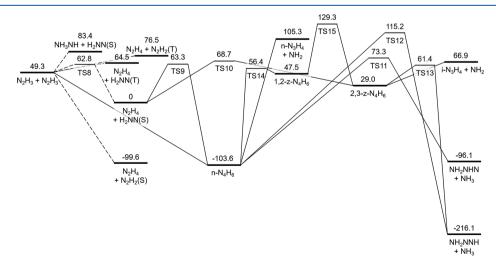


Figure 8. Reaction path diagram for the N_4H_6 potential. Dashed lines represent nonpressure-dependent pathways. (S) and (T) represent singlet or triplet multiplicities, respectively. Energies are in kJ mol⁻¹ and scaled relative to the $N_2H_4 + H_2NN(S)$ entry channel, which was set at zero.

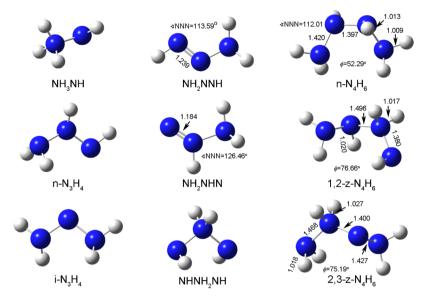


Figure 9. Geometric representation of species on the N_4H_6 PES optimized at the ω B97x-D3/6-311++G(3df,3pd) level of theory. Species already given in Figure 2 were not reproduced here. Bond orders shown for illustration purpose only. Bond lengths are in angstroms and angles in degrees. ϕ is the dihedral angle between the four nitrogen backbone atoms. Quantitative geometric data were added where it benefits the discussion; geometric coordinates for all species are available in the Supporting Information.

mol⁻¹, respectively, were excluded. Geometric representations of relevant species and saddle points are given in Figures 9 and 10, respectively. Table S2 lists point groups, rotational constants, and unscaled vibrational frequencies for all relevant species and transition states.

The high-pressure-limit rate coefficient for the entry channel $N_2H_3 + N_2H_3 \leftrightarrow n-N_4H_6$ (reaction B4, Table 3) was estimated using RMG³⁰ based on its radical recombination reaction family ("R_Recombination"). This rate coefficient was estimated to be slower by a factor of 2 with respect to the estimate of Zhang et al. for the similar recombination reaction B1 (Table 2).⁵⁸ The high-pressure-limit rate coefficients for the exit channels $n-N_4H_6 \leftrightarrow n-N_3H_4 + NH_2$, $1,2-z-N_4H_6 \leftrightarrow NHNH_2NH + NH_2$, and $2,3-z-N_4H_6 \leftrightarrow iN_3H_4 + NH_2$ (reactions B5–B7) were estimated similarly using the radical recombination family in RMG. All high-pressure-limit rate coefficients are given in Table 3. The respective microcanonical rate coefficients were calculated by Arkane using an inverse Laplace transform.

The pressure-dependent network on the singlet surface potential has three stable isomers, $n-N_4H_6$ (tetrazane), $1,2-z-N_4H_6$, and $2,3-z-N_4H_6$ (Figures 8 and 9). Similar to the N_3H_5 case, additional zwitterionic isomers could theoretically be thought of, yet only the two isomers listed above and illustrated in Figure 9 were found to be connected to the network by isomerizations. Most of the saddle points on the N_4H_6 potential are located within a relatively narrow energy range of 56.4-73.3 kJ mol⁻¹ above $N_2H_4+H_2NN(S)$ (Figure 8), making the various transitions quite competitive. The two exceptions are TS12 and TS15 with relatively high energies, which are expected to significantly inhibit the flux through the respective channels.

Consequently, an interesting phenomenon emerges where a different entry channel would favor a different final product. A chemically activated complex formed by a $N_2H_4 + H_2NN(S)$ collision could form $n-N_4H_6$ via TS9 or 2,3-z- N_4H_6 via TS10. The energized $n-N_4H_6$ is likely to either be collisionally stabilized or rapidly dissociate to form two N_2H_3 radicals,

depending on the pressure and temperature. If 2,3-z- N_4H_6 is formed via TS10, it will rapidly dissociate to form either i- $N_3H_4 + NH_2$ or $NH_2NNH + NH_3$.

On the other hand, an excited complex formed by a $N_2H_3 + N_2H_3$ collision will most likely be collisionally stabilized, forming $n\text{-}N_4H_6$, or dissociate back to $N_2H_3 + N_2H_3$. The alternative pathways for continued reaction via TS9 or TS11 or the barrierless dissociation to $n\text{-}N_3H_4 + NH_2$ are all significantly uphill compared to the $N_2H_3 + N_2H_3$ entry channel. Note that the $N_2H_3 + N_2H_3$ and $N_2H_4 + H_2NN(S)$ entry channels are interconvertible bimolecularly via a relatively low energy saddle point, TS8, but $N_2H_3 + N_2H_3$ is more likely to undergo barrierless disproportionation to $N_2H_3 + N_2H_2(S)$.

TS8 is the saddle point of the $N_2H_3 + N_2H_3$ disproportionation reaction forming $N_2H_4 + H_2NN(S)$. It is an early and synchronous transition state, as expected from the reactant and product energetics. It is noted that this reaction was found to be intrinsically different from a similar reaction on the N_3H_5 potential, $N_2H_3 + NH_2 \leftrightarrow H_2NN(S) + NH_3$ (reaction B2, Table 2), where the latter was determined to be barrierless.

TS9, a saddle point of a nitrene insertion into an N–N bond, is asynchronous. Most interestingly, the N–N bond length in the substructure originated from N_2H_4 is shorter than the respective bond lengths in both the reactant N_2H_4 and the product n-N₄H₆ (1.379 vs 1.420 and 1.397 Å, respectively). TS8 and TS9 are geometrically and energetically similar (Figures 8 and 10). The major difference between these geometries is the orientation of the terminal hydrogens not directly participating in the reaction, which causes the complex to either recombine or fall apart because of electrostatic forces.

The addition reaction $N_2H_4 + H_2NN(S) \leftrightarrow 2,3$ -z- N_4H_6 passes through TS10. This TS has a similar geometry to the product except the central N–N bond which has stretched significantly. It is an asynchronous transition in which the N–N bond length of the $H_2NN(S)$ reactant stretches considerably (81.6% stretch fraction) before reaching the saddle point, while the N–N bond length of the N_2H_4 reactant hardly stretches

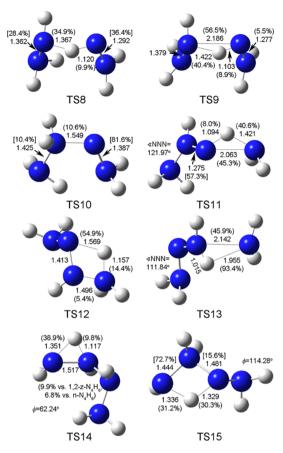


Figure 10. Geometric representation of transition states on the N_4H_6 PES optimized at the ω B97x-D3/6-311++G(3df,3pd) level of theory. Bond lengths are in angstroms and angles in degrees. Numbers in parentheses indicate the bond stretch fraction relative to the respective stable species. Numbers in brackets indicate the relative bond stretch fraction out of the total change between the respective reactant and product in the direction specified in Table 3. ϕ is the dihedral angle between the four nitrogen backbone atoms. Quantitative geometric data were added where it benefits the discussion; geometric coordinates for all transition states are available in the Supporting Information.

(10.4% stretch fraction). Relative bond stretch fractions throughout the discussion are defined as $(r_{\rm TS}-r_{\rm reactant})/(r_{\rm product}-r_{\rm reactant})$, where $r_{\rm reactant}$, $r_{\rm product}$ and $r_{\rm TS}$ are the relevant bond lengths in the reactant, product, and the TS, respectively.

Two reactions of the 1,2-NH $_3$ elimination family on this potential pass through transition states TS11 and TS13. In both cases, the \angle NNN backbone angles of the forming products in the TS are close to the values of the stable NH $_2$ NHN and NH $_2$ NNH products, respectively. Both are asynchronous, primarily characterized by a highly stretched N-N bond of the leaving NH $_2$ group (45.3 and 93.4%, respectively) and a low stretch of the N-H bond to be ruptured. In fact, the respective N-H bond in TS13 is shorter than in the reactant, and overall the geometry and energies indicate that NH $_2$ was nearly dissociated but grabbed an H atom as it departed. Methods developed for roaming reactions 68 may be helpful for better evaluating this rate coefficient.

A 1,3-NH₃ elimination reaction on this surface, $n-N_4H_6 \leftrightarrow NH_2NNH + NH_3$, has a strained four-membered ring transition geometry, TS12. This transition state is also

Table 3. High-Pressure-Limit Rate Coefficients of Elementary Reactions on the N₄H₆ PES^a

no.b	reaction	A^c	n	$(kJ \text{ mol}^{-1})$	source ^d
R8	$N_2H_3 + N_2H_3 \leftrightarrow N_2H_4 + H_2NN(S)$	1.11×10^{-1}	3.21	-1.5	pw
R9	$N_2H_4 + H_2NN(S) \leftrightarrow n-N_4H_6$	4.73×10^{-1}	3.55	50.6	pw
R10	$N_2H_4 + H_2NN(S) \leftrightarrow 2,3-z-N_4H_6$	2.29×10^{0}	2.96	55.4	pw
R11	$\begin{array}{l} \text{n-N}_4\text{H}_6 \leftrightarrow \text{NH}_2\text{NHN} \\ + \text{NH}_3 \end{array}$	3.00×10^{12}	0.83	178.7	pw
R12	$ \begin{array}{c} \text{n-N}_4\text{H}_6 \leftrightarrow \text{NH}_2\text{NNH} \\ + \text{NH}_3 \end{array} $	7.70×10^{10}	0.84	214.1	pw
R13	$2,3-z-N_4H_6 \leftrightarrow NH_2NNH + NH_3$	4.03×10^{13}	0.26	38.7	pw
R14	$\begin{array}{c} \text{n-N}_4\text{H}_6 \leftrightarrow 1,2\text{-z-} \\ \text{N}_4\text{H}_6 \end{array}$	7.90×10^{11}	0.59	158.6	pw
R15	$\begin{array}{c} \text{1,2-z-N}_4\text{H}_6 \leftrightarrow \text{2,3-z-} \\ \text{N}_4\text{H}_6 \end{array}$	1.74×10^{10}	0.91	74.4	pw
B4	$N_2H_3 + N_2H_3 \leftrightarrow n-N_4H_6$	2.51×10^{14}	-0.43	0.2	est., pw
B5	$n-N_3H_4 + NH_2 \leftrightarrow n-N_4H_6$	5.02×10^{14}	-0.43	0.2	est., pw
В6	$ \begin{array}{l} NHNH_2NH + NH_2 \\ \leftrightarrow 1,2-z-N_4H_6 \end{array} $	5.02×10^{14}	-0.43	0.2	est., pw
B7	$i-N_3H_4 + NH_2 \leftrightarrow 2,3-$ $z-N_4H_6$	1.17×10^{16}	-1.26	2.8	est., pw
В8	$N_2H_3 + N_2H_3 \leftrightarrow N_2H_4 + N_2H_2(S)$	1.20×10^{13}	0	0	ref 9

"Parameters are for the modified Arrhenius expression, $k = AT^n \exp(-E_a/[RT])$, in the 500–3000 K temperature range. ^bThe R notations refer to reactions as discussed in the text; numbers match the transition states in Figure 10. The B notations refer to barrierless reactions. ^cUnits are s⁻¹ or cm³ mol⁻¹ s⁻¹ for first- or second-order reactions in the forward direction, respectively. ^dpw—calculated in the present work (see text); est.—estimated (see text).

asynchronous with the central N−N bond stretched relative to both reactants and products and a small ∠NNN ring angle of 98.78°, all of which are similar characteristics to TS4 (Figure 3).

TS14 and TS15 are saddle points of isomerization reactions on this surface: n-N₄H₆ \leftrightarrow 1,2-z-N₄H₆ and 1,2-z-N₄H₆ \leftrightarrow 2,3z-N₄H₆. Note that no direct reaction was identified between n-N₄H₆ and 2,3-z-N₄H₆. Exhaustive searches for such saddle point always lead to dissociation of the complex into N₂H₄ and H₂NN(S), as this pathway resembles the geometry of TS9 (Figure 10). The transition geometry of TS14 is synchronous and late as expected from the reaction energetics. Facilitating the internal hydrogen transfer in this reaction causes the N-N bond over which this transfer occurs to stretch relative to both relevant isomers. The geometry of TS15, on the other hand, is asynchronous; although the hydrogen stretches nearly evenly on both sides (30.3 and 31.2%), the outer N-N bond stretches considerably (72.7% relative bond stretch fraction), whereas the internal N-N bond stretches slightly (15.6% relative bond stretch fraction).

The $n\text{-}N_4H_6$ formation rate is higher when entering from the $N_2H_3+N_2H_3$ channel, compared to $N_2H_4+H_2NN(S)$ (Figure 11), because of the relatively high energy barrier in the later (Figure 8). As expected, more $n\text{-}N_4H_6$ is formed with respect to both entry channels as the pressure increases. The rate coefficient of the estimated reaction B4 (Table 3) is within a factor of 2 from the rate coefficient of the calculated and comparable reaction B1 (Table 2) forming $n\text{-}N_3H_5$ for all studied conditions (Figures 6c and 11).

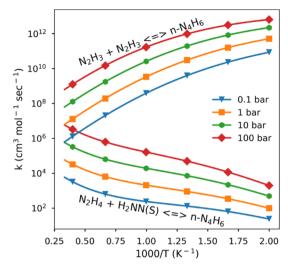


Figure 11. Rate coefficient comparison of n-N₄H₆ formation from each of the entry channels as a function of temperature and pressure.

Rate coefficient comparison starting from each of the entry channels on the N₄H₆ potential suggests a single dominant product channel, $N_2H_4 + N_2H_2(S)$, though at high pressures n- N_4H_6 formation is comparable; $N_2H_4 + H_2NN(S)$ would preferably form $N_2H_3 + N_2H_3$ (Figure 12a), which in turn mostly yield $N_2H_4 + N_2H_2(S)$ (Figure 12b). The tendency of N₂H₃ radicals to react via a disproportionation route rather than recombine to form n-N₄H₆ was previously observed experimentally at 298 K and low pressure, and a branching ratio of four was determined. 19 Our calculated rate coefficient for the recombination reaction R9 at these conditions (3.0 \times $10^{12}\ \mbox{cm}^{3}\ \mbox{mol}^{-1}\ \mbox{s}^{-1})$ is a factor of 3.3 lower than the disproportionation rate coefficient (reaction R8) estimated by Konnov and De Ruyck, in accordance with the experimental observation. Consequently, the experimental observation along with the present calculations suggests that the rate coefficient of reaction B8 could not be much lower than the value suggested by Konnov and De Ruyck⁹ at these conditions. The gap between the rates of the two routes is shown here to increase with temperature and decrease with pressure. At relatively high pressures and low temperatures, n-N₄H₆

formation becomes significant, yet at the conditions relevant to hydrazine decomposition (1500 K and 25 bar), the formation rate of tetrazane from N_2H_3 recombination is 2 orders of magnitude lower than the formation rate of the disproportionation products, $N_2H_4 + N_2H_2(S)$. Also of importance are reactions yielding $n\text{-}N_3H_4 + NH_2$ and $NH_2NHN + NH_3$, while formation rates of $NH_2NNH + NH_3$ and $i\text{-}N_3H_4 + NH_2$ from the $N_2H_3 + N_2H_3$ entry channel are negligible (Figure S11), in accordance with the above discussion.

3.3. Thermodynamic Properties. The present work emphasizes the importance of accounting for triazane (n-N₃H₅) when kinetically studying hydrazine decomposition systems (Figure 6c). Tetrazane (n-N₄H₆) formation in this system only becomes important at high pressures and relatively low temperatures (Figure 12) because of fall-off into N_2H_3 + N₂H₃. The main decomposition pathways of triazane are formation of $H_2NN(S) + NH_3$ at high temperatures (Figure 6d), as well as hydrogen abstraction reactions because of interactions with the radical pool (mainly H, NH₂, and N₂H₃). The latter results in the formation of primary or secondary radicals, n-N₃H₄ or i-N₃H₄, respectively (Figure 9). Preliminary RMG predictions suggest that the n-N₃H₄ radical primarily decomposes into NH₂ + N₂H₂(S) via a β -scission reaction, whereas the i-N₃H₄ radical primarily abstracts a hydrogen atom from N₂H₂(S), forming n-N₃H₅ + NNH. Consequently, n-N₃H₅, n-N₃H₄, and i-N₃H₄ should all be considered in future kinetic models of similar systems.

Thermodynamic properties were computed using Arkane at the CCSD(T)-F12a/cc-pVTZ-F12// ω B97x-D3/6-311+G-(3df,3pd) level of theory (Table 4). The T₁ diagnostic parameters²⁸ calculated at the CCSD(T)-F12a/cc-pVTZ-F12 level of theory for n-N₃H₅, n-N₃H₄, i-N₃H₄, and n-N₄H₆ are 0.0102, 0.0232, 0.0209, and 0.0107, respectively. The n-N₃H₄ and i-N₃H₄ radicals have strong coupling between large amplitude fluxional inversion and HR modes (Figures S6 and S7), which makes it challenging to compute their heat capacities. Therefore, only RRHO enthalpies and entropies at 298 K are reported for these radicals.

The calculated standard heat of formation and entropy of formation of n-N $_3$ H $_5$ (Table 4) are comparable with respective past values calculated using the G2 method, ⁶⁹ 198.7 kJ mol⁻¹

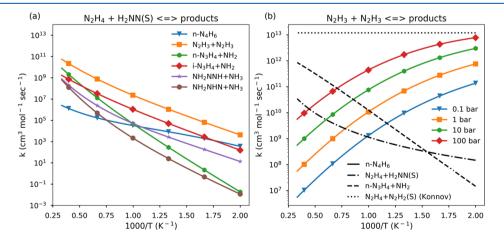


Figure 12. Rate oefficient comparisons of $N_2H_4 + H_2NN(S)$ and $N_2H_3 + N_2H_3$ reactions. Rates in (a) are given at a representative pressure of 10 bar. In (b), line types refer to the product/s, while the color refers to the pressure; the pressure-dependent rate for $n-N_3H_4 + NH_2$ formation via a well-skipping reaction is negligible; the rate for $N_2H_4 + H_2NN(S)$ formation includes both the direct route (via TS8) and the well-skipping route; the dotted line is an estimated rate by Konnov and De Ruyck.

Table 4. Thermodynamic Properties of n-N₃H₅, n-N₃H₄, i-N₃H₄, and n-N₄H₆ at the CCSD(T)-F12a/cc-pVTZ-F12/ ω B97x-D3/6-311++G(3df,3pd) Level of Theory^a

			$C_p(T)^b$								
species	$\Delta H_{ m f}^{ m o}$	$\Delta S_{ m f}^{ m o}$	300 K	400 K	500 K	600 K	800 K	1000 K	1500 K	2000 K	2400 K
$n-N_3H_5$	203.3	276.9	75.1	86.3	95.5	103.7	117.3	128.0	145.7	155.9	161.3
$n-N_3H_4$	322.5	274.1									
$i-N_3H_4$	289.6	262.7									
$n-N_4H_6$	299.7	289.8	80.6	99.4	115.2	128.6	150.4	166.6	191.5	205.4	213.3

[&]quot;Enthalpies are given in kJ mol⁻¹; entropies and constant pressure heat capacities are given in J mol⁻¹ K⁻¹. b No C_{p} values are reported for the N₃H₄ radicals, see text.

and 261.5 J mol⁻¹ K⁻¹, respectively. ¹⁷ The NASA polynomials for the thermodynamic properties of triazane and tetrazane are given in the Supporting Information.

4. CONCLUSIONS

A detailed kinetic analysis of the N_3H_5 and N_4H_6 potentials was presented. On the N_4H_6 potential, the $N_2H_4+H_2NN(S)$ entry channel mostly yields $N_2H_3+N_2H_3$, while the $N_2H_3+N_2H_3$ channel, in turn, would primarily result in the formation of $N_2H_4+N_2H_2(S)$ by direct disproportionation. Overall, hydrazine on this surface mainly catalyzes isomer transformation from $H_2NN(S)$ to $N_2H_2(S)$. At high pressures and low temperatures, tetrazane $\left(n\text{-}N_4H_6\right)$ formation becomes significant.

Starting from the $N_2H_3 + NH_2$ entry channel, all bimolecular product wells on the N_3H_5 potential can be reached directly via a bimolecular reaction. In fact, the rate contribution of the well-skipping pathway forming $N_2H_2(S) + NH_3$ to the overall rate is negligible, while the well-skipping route forming $H_2NN(S) + NH_3$ has a significant contribution and dominates in the low-pressure and low-temperature regime. Starting from $N_2H_3 + NH_2$, $H_2NN(S)$ formation is kinetically more favorable than $N_2H_2(S)$ under 2500 K. Triazane $(n-N_3H_5)$ becomes the dominant product of $N_2H_3 + NH_2$ reaction below 550, 800, 1150, 1250, and 1600 K at 0.1, 1, 10, 25, and 100 bar, respectively. Triazane is predicted to form either $H_2NN(S) + NH_3$ or primary/secondary N_3H_4 radicals, all of which should be taken into consideration in kinetic models of hydrazine.

Theoretical predictions of reaction rate coefficients have been derived from ab initio TST coupled with ME simulations as necessary. The determined pressure-dependent rates should be of considerable utility to future efforts of kinetic modeling of hydrazine decomposition and related systems.

ASSOCIATED CONTENT

S Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jpca.9b02217.

Transport properties, stationary point properties, relaxed rotor scans, branching ratios of $N_2H_3 + N_2H_3$, NASA polynomials for $n-N_3H_5$ and $n-N_4H_6$, geometric coordinates, and pressure-dependent rates (PDF)

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Notes

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