

4. Consider S and T as variables and the following relation representing the relationships:

- (i) a:  $\neg(S \vee T)$
- (ii) b:  $(S \wedge T)$
- (iii) c:  $T \vee \neg T$
- (iv) d:  $\neg(S \rightarrow S)$
- (v) e:  $\neg S \wedge \neg T$

Analyze the following for PL-TT entailment and show whether

- (i). 'a' entails 'b',
- (ii). 'a' entails 'c',
- (iii). 'a' entails 'd' and
- (iv). 'a' entails 'e'

Program:

→ when s=True, t=True

```
s=True
t=True
a = not (s or t)
print(a)
b = s and t
print(b)
c = t or (not t)
print(c)
d = not ((not s or s) and (not s or s))
print(d)
e = not(not s) and (not t)
print(e)

if a==b:
    print("a entails b")
if a==c:
    print("a entails c")
if a==d:
    print("a entails d")
if a==e:
    print("a entails e")
else:
    print("no entailment")
```

Output:

```
False
True
True
False
False
a entails d
a entails e
>>>
```

→ when s=True, t=False:

```
s=True
t=False
a = not(s or t)
print(a)
b = s and t
print(b)
c = t or(not t)
print(c)
d = not((not s or s) and (not s or s))
print(d)
e = not(not s) and (not t)
print(e)

if a==b:
    print("a entails b")
if a==c:
    print("a entails c")
if a==d:
    print("a entails d")
if a==e:
    print("a entails e")
else:
    print("no entailment")
```

### Output:

```
False
False
True
False
True
a entails b
a entails d
no entailment
```

→ when s=False, t=True

```
s=False
t=True
a = not(s or t)
print(a)
b = s and t
print(b)
c = t or(not t)
print(c)
d = not((not s or s) and (not s or s))
print(d)
e = not(not s) and (not t)
print(e)

if a==b:
    print("a entails b")
if a==c:
    print("a entails c")
if a==d:
    print("a entails d")
if a==e:
    print("a entails e")
else:
    print("no entailment")
```

**Output:**

```
False
False
True
False
False
a entails b
a entails d
a entails e
```

→ when s=False, t=False

```
s=False
t=False
a = not(s or t)
print(a)
b = s and t
print(b)
c = t or(not t)
print(c)
d = not((not s or s) and (not s or s))
print(d)
e = not(not s) and (not t)
print(e)

if a==b:
    print("a entails b")
if a==c:
    print("a entails c")
if a==d:
    print("a entails d")
if a==e:
    print("a entails e")
else:
    print("no entailment")
```

### Output:

```
True
False
True
False
False
a entails c
no entailment
```