Data Structure arrdy Algorithm Created with Aspose Slides for NET Standard 2.0 23.1. Copyright 2004-2023 Aspose Pty Ltd.

Heap

Heap

- A heap is a complete binary tree except the bottom level adjusted to the left.
- The value of each node is greater than that of its two children. (Max Heap)
- The value of each node is less than that of its two children. (Min Heap)
- Height of the heap is $\log_2 n$.

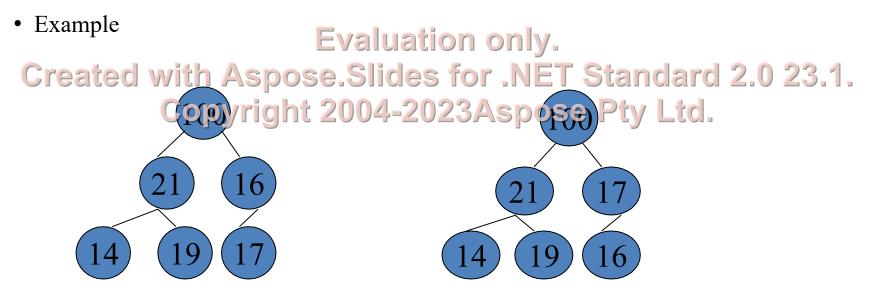


Figure: Not a

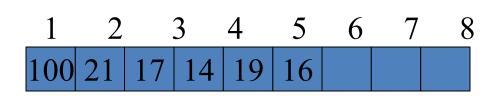
Heap

Figure: A Heap

Heap Implementation

- We can use an array (due to the regular structure or completeness of binary tree).
- For a node N with location i, the following factors can be calculated.
 - 1. Left child of N is in location (2 * i).
 - 2. Right child of N is in location (2 * i + 1).
 - Evaluation only.

 3 Parent of N is in location [i/2]. Slides for .NET Standard 2.0 23.1.
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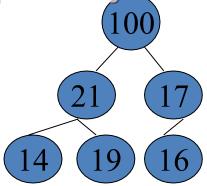


Figure: Heap and Its Array Representation

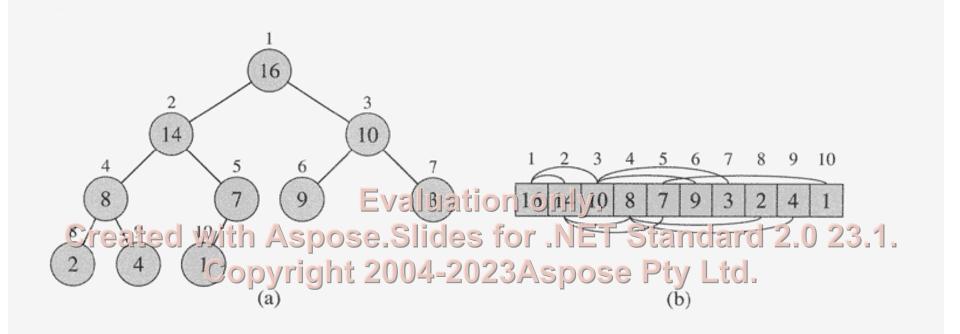
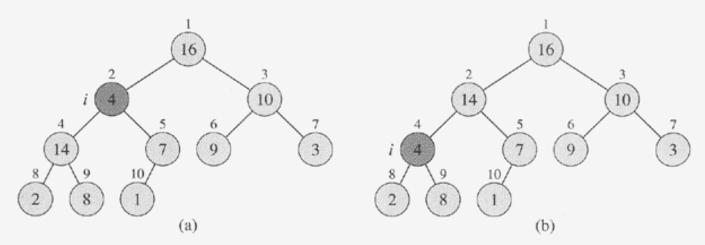


Figure 6.1 A max-heap viewed as (a) a binary tree and (b) an array. The number within the circle at each node in the tree is the value stored at that node. The number above a node is the corresponding index in the array. Above and below the array are lines showing parent-child relationships; parents are always to the left of their children. The tree has height three; the node at index 4 (with value 8) has height one.

```
MAX-HEAPIFY (A, i)
    l \leftarrow \text{LEFT}(i)
 2 r \leftarrow RIGHT(i)
 3 if l \leq heap\text{-}size[A] and A[l] > A[i]
4 then largest Created with Aspose Slides for NET Standard 2.0 23.1.
         dspyrighten04-2023Aspose Pty Ltd.
     if r \leq heap\text{-size}[A] and A[r] > A[largest]
         then largest \leftarrow r
     if largest \neq i
         then exchange A[i] \leftrightarrow A[largest]
               MAX-HEAPIFY(A, largest)
```



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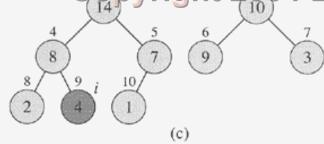


Figure 6.2 The action of MAX-HEAPIFY(A, 2), where heap-size[A] = 10. (a) The initial configuration, with A[2] at node i = 2 violating the max-heap property since it is not larger than both children. The max-heap property is restored for node 2 in (b) by exchanging A[2] with A[4], which destroys the max-heap property for node 4. The recursive call MAX-HEAPIFY(A, A) now has A[4] with A[6], as shown in (c), node 4 is fixed up, and the recursive call A[6] MAX-HEAPIFY(A, A[6] yields no further structure and A[6] are dataserithme.

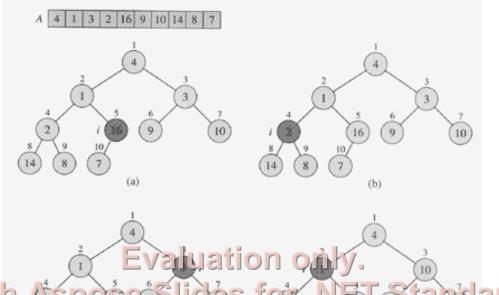
```
BUILD-MAX-HEAP(A)

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2 for i \leftarrow [length[A]/2] downto 1

3 do MAX-HEAPIFY (A, i)
```



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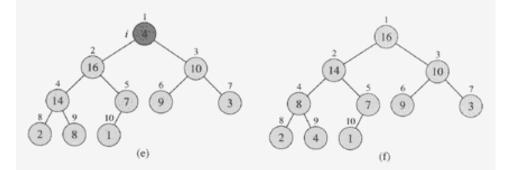


Figure 6.3 The operation of BUILD-MAX-HEAP, showing the data structure before the call to MAX-HEAPIFY in line 3 of BUILD-MAX-HEAP. (a) A 10-element input array A and the binary tree it represents. The figure shows that the loop index i refers to node 5 before the call MAX-HEAPIFY(A, i). (b) The data structure that results. The loop index i for the next iteration refers to node 4. (c)-(e) Subsequent iterations of the for loop in BUILD-MAX-HEAP. Observe that whenever MAX-HEAPIFYD attac Structure and Augorithm ode are both max-heaps. (f) The max-heap after BUILD-MAX-HEAP finishes.

```
HEAPSORT (A)

1 BUILD-MAX-HIMAP (A).

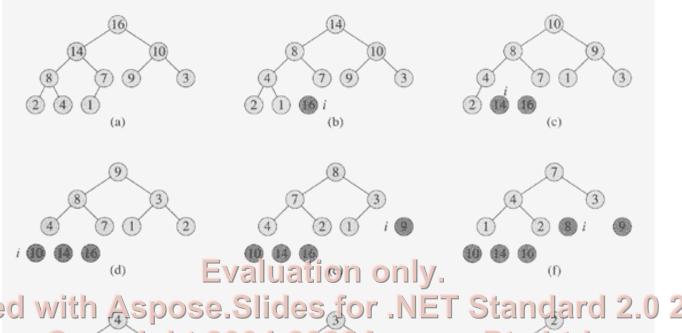
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3 do exchange A[1] \leftrightarrow A[i]

4 heap-size [A] \leftarrow heap-size [A] - 1

5 MAX-HEAPIFY (A, 1)
```



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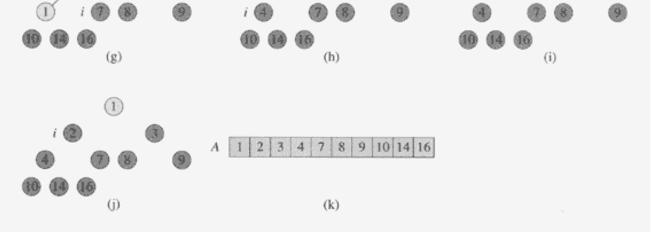


Figure 6.4 The operation of HEAPSORT. (a) The max-heap data structure just after it has been built by BUILD-MAX-HEAP. (b)—(j) The max-heap just after each call of MAX-HEAPIFY in line 5. The value of i at that tile at as Structure igner Algorithm remain in the heap. (k) The resulting sorted array A.

HEAP-Multi MonMUM (A) Created with Aspose Slides for .NET Standard 2.0 23.1. Copyright 2004-2023 Aspose Pty Ltd. $1 \quad \text{return } A[1]$

HEAP-EXTRACT-MAX(A)

- 1 if heap-size[A] < 1
- then error "heap underflow"
- Greated Math Aspose Slides for .NET Standard 2.0 23.1.
- 4 $A[I] \leftarrow A[heap-size[A]]$
- 5 heap- $size[A] \leftarrow heap$ -size[A] 1
- 6 MAX-HEAPIFY (A, 1)
- 7 return max

```
HEAP-INCREASE-KEY (A, i, key)

1 if key < A[i]

2 then error resides yes smaller than current key"

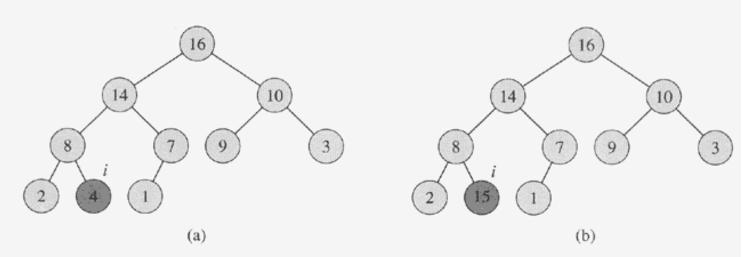
3 A[i]

4 while i > 1 and A[PARENT(i)] < A[i]

5 do exchange A[i] \leftrightarrow A[PARENT(i)]

6 i \leftarrow PARENT(i)
```

```
MAX-HEAP-INSERT (A, key) (A, key)
```



Evaluation only.

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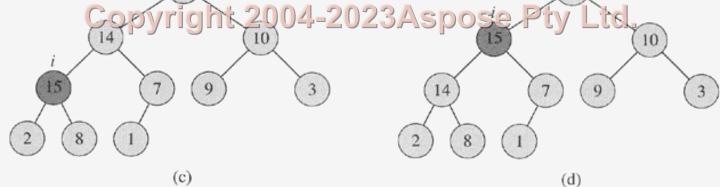


Figure 6.5 The operation of HEAP-INCREASE-KEY. (a) The max-heap of Figure 6.4(a) with a node whose index is i heavily shaded. (b) This node has its key increased to 15. (c) After one iteration of the while loop of lines 4–6, the node and its parent have exchanged keys, and the index i moves up to the parent. (d) The max-heap after one more iteration of the while loop. At this point, 11/05/08 A[PARENT(i)] ≥ A[i]. The max Datap Structure and Algorithm he procedure terminates.

```
BUILD-MAX-HEAP(A)

Evaluation only.

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2 for i \leftarrow \lfloor length[A]/2 \rfloor downto 1

3 do MAX-HEAPIFY(A, i)
```