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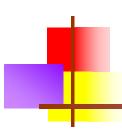


## Quicksort I

- To sort a[left...right]:
- 1. if left < right:

```
1.1. Partition a [left. right] such that:
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alta[left.h.pzdd4azezless_tban pt[p]]; and
all a[p+1...right] are >= a[p]
```

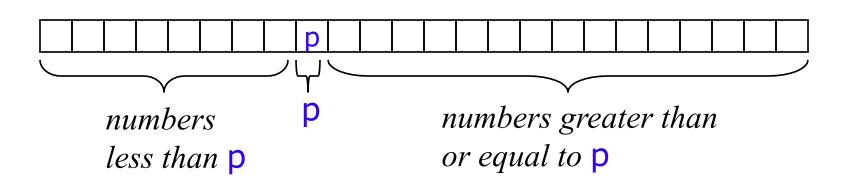
- 1.2. Quicksort a[left...p-1]
- 1.3. Quicksort a[p+1...right]
- 2. Terminate



### Partitioning (Quicksort II)

- A key step in the Quicksort algorithm is partitioning the array
  - We choose some (any) number p in the array to use as a pivot
  - We partition the array Into three parts:

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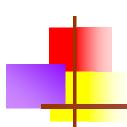


- Choose an array value (say, the first) to use as the pivot
- Starting from the left end, find the first element crethatis greater than or equal to the pixotland 2.0 23.1.
  - Searching backward from the right end, find the first element that is less than the pivot
  - Interchange (swap) these two elements
  - Repeat, searching from where we left off, until done

## **Partitioning**

- To partition a[left...right]:
- 1. Set pivot = a[left], l = left + 1, r = right;
- 2. while I < r, do
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  2.1. while I < right 25.04-2023 Aspose Pty Ltd.

  - 2.2. while r > left & a[r] >= pivot, set r = r 1
  - 2.3. if l < r, swap a[l] and a[r]
- 3. Set a[left] = a[r], a[r] = pivot
- 4. Terminate



### Example of partitioning

```
436924312189356
  choose pivot:
                  36924312189356
  search:
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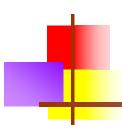
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  search: Copyright 2004920233 12018 8 Pt 6 L5 45
                433124312989656
  swap:
                433124312989656
  search:
                433122314989656
  swap:
                433122314989656 (left > right)
  search:
```

swap with pivot: 1 3 3 1 2 2 3 4 4 9 8 9 6 5 6



### The partition method (Java)

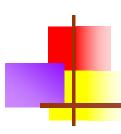
```
static int partition(int[] a, int left, int right) {
      int p = a[left], l = left + 1, r = right;
      while (l < r) {
         while (l < right that if op)/L++;
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         if Copyright 2004-2023 Aspose Pty Ltd.
            int temp = a[l]; a[l] = a[r]; a[r] = temp;
      a[left] = a[r];
      a[r] = p;
      return r;
```



### The quicksort method (in Java)

```
static void quicksort(int[] array, int left, int right) {
    if (left < right) {
        int p = partition(array, left, right);
        quicksort(array, left, right);
        quicksort(array, left, right).

Createquiditsort(prosy, slitles right);ET Standard 2.0 23.1.
        }
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}
```



#### Analysis of quicksort—best case

- Suppose each partition operation divides the array almost exactly in half
- Then the depth of the reconsiderin log<sub>2</sub>n
- Because that's now many times we can haive 2.0 23.1.

  However, there are many recursions!
  - - How can we figure this out?
    - We note that
      - Each partition is linear over its subarray
      - All the partitions at one level cover the array



### Partitioning at various levels



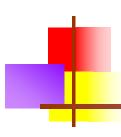
# Best case II

- We cut the array size in half each time
- So the depth of the recursion in log<sub>2</sub>n
- At each level of the recursion, all the partitions at that clevel do work that is sinear in ONET Standard 2.0 23.1.
- O(log<sub>2</sub>fi)Pyrig(th}<sup>0</sup><sup>4</sup> <del>O</del>(fi) fog<sub>2</sub>fi) Pty Ltd.
- Hence in the average case, quicksort has time complexity O(n log<sub>2</sub>n)
- What about the worst case?

# Worst case

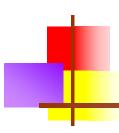
- In the worst case, partitioning always divides the size n array into these three parts:
  - A length one part, containing the pivot itself
  - A length zero part, and Created with Aspose Slides for .NET Standard 2.0 23.1.

    A length pyligart containing everything elsetd.
- We don't recur on the zero-length part
- Recurring on the length n-1 part requires (in the worst case) recurring to depth n-1



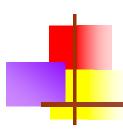
### Worst case partitioning





### Worst case for quicksort

- In the worst case, recursion may be n levels deep (for an array of size n)
- But the partitioning work done at each level is still n
- -Created with (As) pos Os Indes for .NET Standard 2.0 23.1.
- So worst case for Quicksort is Topia Pty Ltd.
- When does this happen?
  - There are many arrangements that *could* make this happen
  - Here are two common cases:
    - When the array is already sorted
    - When the array is *inversely* sorted (sorted in the opposite order)



### Typical case for quicksort

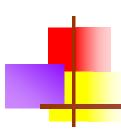
- If the array is sorted to begin with, Quicksort is terrible: O(n²)
- It is possible to construct other bad cases
- CreHewever, Quicksortisessically E (ataogan) 2.0 23.1.
  - The constants are so good that Quicksort is generally the fastest algorithm known
  - Most real-world sorting is done by Quicksort

## Tweaking Quicksort

- Almost anything you can try to "improve"
   Quicksort will actually slow it down
- One good tweak is to switch to a different Creating methods when the subarrays generall2.0 23.1.

(say, 19 oryright 2004-2023 Aspose Pty Ltd.

- Quicksort has too much overhead for small array sizes
- For large arrays, it *might* be a good idea to check beforehand if the array is already sorted
  - But there is a better tweak than this

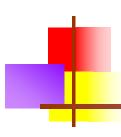


### Picking a better pivot

- Before, we picked the *first* element of the subarray to use as a pivot
  - If the array is already sorted, this results in  $O(n^2)$  behavior **Evaluation only.**

Creater's vio better if we pick the last element and 2.0 23.1.

- We could do an *optimal* quicksort (guaranteed O(n log n)) if we always picked a pivot value that exactly cuts the array in half
  - Such a value is called a median: half of the values in the array are larger, half are smaller
  - The easiest way to find the median is to *sort* the array and pick the value in the middle (!)



#### Median of three

- Obviously, it doesn't make sense to sort the array in order to find the median to use as a pivot
- Instead, compare just three elements of our (sub)array—the first, the last, and the middle Created with Associated Standard 2.0 23.1.

  Take the *median* (middle value) of these three as pivot

  - It's possible (but not easy) to construct cases which will make this technique  $O(n^2)$
  - Suppose we rearrange (sort) these three numbers so that the smallest is in the first position, the largest in the last position, and the other in the middle
    - This lets us simplify and speed up the partition loop



- Quicksort is the fastest known sorting algorithm
- For optimum efficiency, the pivot must be chosen carefully
- Evaluation only.

  -c"Medianief three" issugged technique for shoosing the pivot Copyright 2004-2023 Aspose Pty Ltd.
- However, no matter what you do, there will be some cases where Quicksort runs in  $O(n^2)$  time



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