Arithmetic Expression Conversion Using stack

Conversion of Infix Expression into Postfix Expression

Algorithm: Infix-to-Postfix (Q, P)

Here Q is an arithmetic expression in infix notation and this algorithm generates the postfix expression P using stack.

1. Scan the infix expression Q from left to right.

2. Initialize an empty stack.

3. Repeat step 4 to 5 until all characters in Q are scanned.

4. If the scanned character is an operand, add it to P.

5. If the scanned character is an operator Φ, then

   (a) If stack is empty, push Φ to the stack.

   (b) Otherwise repeatedly pop from stack and add to P each operator which has the same or higher precedence than Φ.

   (c) Push Φ to the stack.

6. If scanned character is a left parenthesis "(", then push it to stack.

7. If scanned character is a right parenthesis ")", then

    (a) Repeatedly pop from stack and add to P each operator until "(" is encountered.

    (b) Remove "(" from stack.

8. If all the characters are scanned and stack is not empty, then

    (a) Repeatedly pop the stack and add to P each operator until the stack is empty.

9. Exit.

Example: Q: 5 * (6 + 2) - 12 / 4   and P: ?

Infix Expression Q	Stack	Postfix Expression P
5		5
*	*	5
(	* (	5
6	* (	5, 6
+	* (+	5, 6
2	* (+	5, 6, 2
)	*	5, 6, 2, +
-	-	5, 6, 2, +, *
12	-	5, 6, 2, +, *, 12
/	- /	5, 6, 2, +, *, 12
4	- /	5, 6, 2, +, *, 12, 4
	-	5, 6, 2, +, *, 12, 4, /
		5, 6, 2, +, *, 12, 4, /, -

Postfix Expression P : 5,   6,   2,   +,   *,   12, 4,   /,   -

Example: Q: A * ((B + C) - D) / E   and   P: ?

Infix Expression Q	Stack	Postfix Expression P
A		A
*	*	A
(	* (	A
(	* ((	A
B	* ((	A B
+	* ((+	A B
C	* ((+	A B C
)	* (	A B C +
-	* (-	A B C +
D	* (-	A B C + D
)	*	A B C + D -
/	/	A B C + D - *
E	/	A B C + D - * E
		A B C + D - * E /

Postfix Expression P :   A   B   C   +   D   -   *   E   /

Postfix Expression Evaluation

Algorithm: Postfix-Evaluation (P, Value)

Here P is an arithmetic expression in postfix notation and this algorithm finds

the value of this expression using stack.

1. Scan the postfix expression P from left to right.

2. Initialize an empty stack.

3. Repeat step 4 to 5 until all characters in P are scanned.

4. If the scanned character is an operand, push it to the satck.

5. If the scanned character is an operator Φ, then

   (a) Remove two top elements of stack where A is the top element and B is

   the next-to-top element.

   (b) Evaluate T = B Φ A and push T to the stack.

6. Pop the stack and assign the top element of the stack to Value.

7. Exit

Example: P :   5, 6, 2, +, *, 12, 4, /, -   and   Value: ?

Postfix Expression Q	Stack
5	5
6	5, 6
2	5, 6, 2
+	5, 8
*	40
12	40, 12
4	40, 12, 4
/	40, 3
-	37

Value: 37

END!!!!

Data Structure and Algorithm