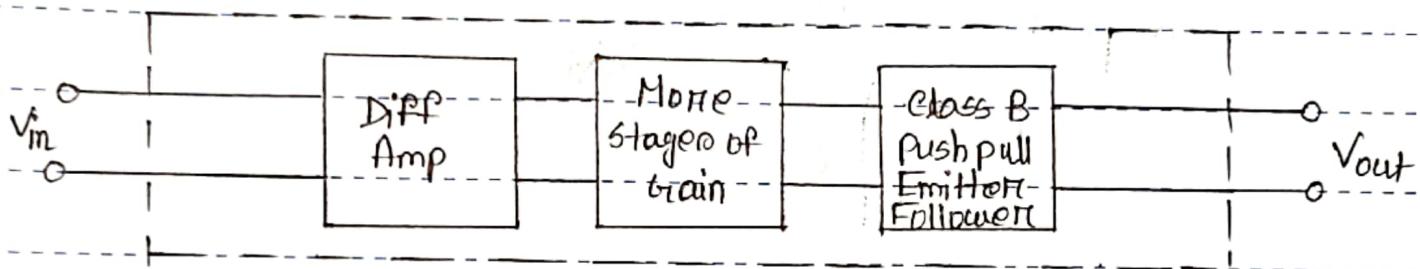


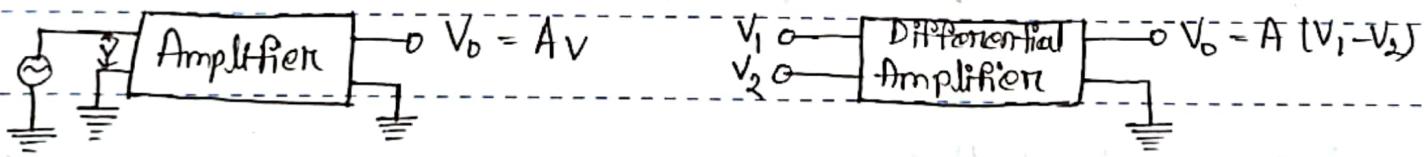
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Operational amplifier: An operational amplifier is a circuit that can perform such mathematical operations as addition, subtraction, integration and differentiation.

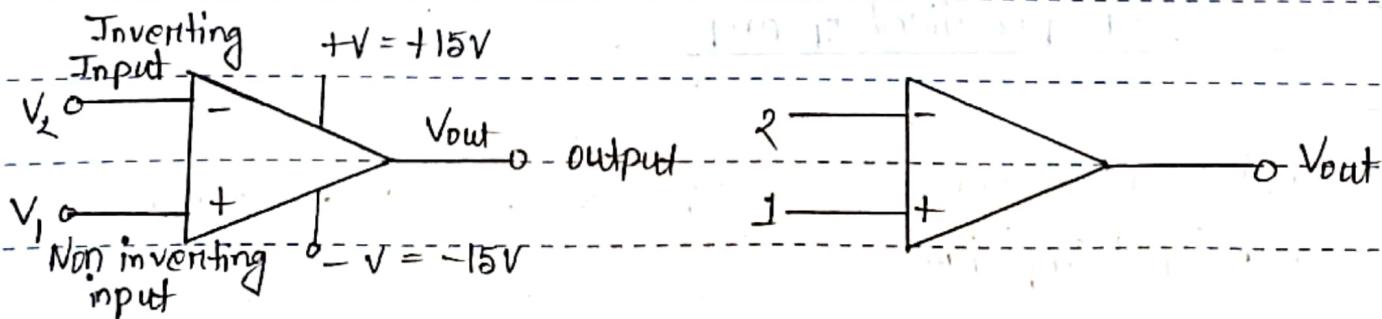


Block diagram of op-amp

Differential amplifier: A differential amplifier is a circuit that can input accept two input signals and amplify the difference between these two input signals.

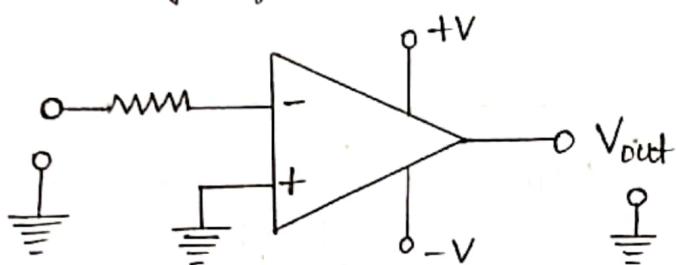


Schematic symbol of operational Amplifier:

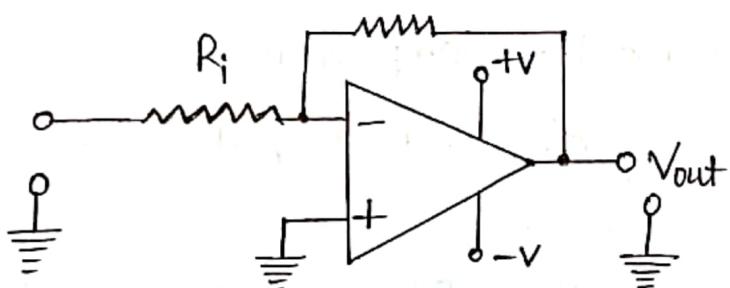


Voltage gain of op-amp: The maximum possible voltage gain from a given op-amp is called open-loop voltage gain and denoted by the symbol A_{OL} .

open-loop voltage gain:



Closed loop voltage gain:

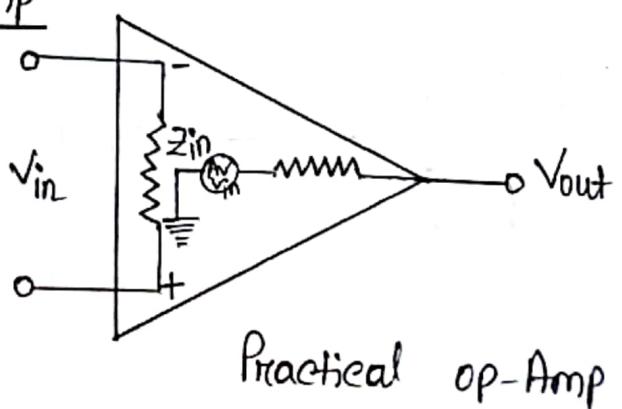


A.C analysis of op-Amp:

Equivalent circuit of practical op-Amp:

Characteristics of practical op-amp are:

- (i) Very high voltage gain
- (ii) Very high input impedance
- (iii) Very low output impedance



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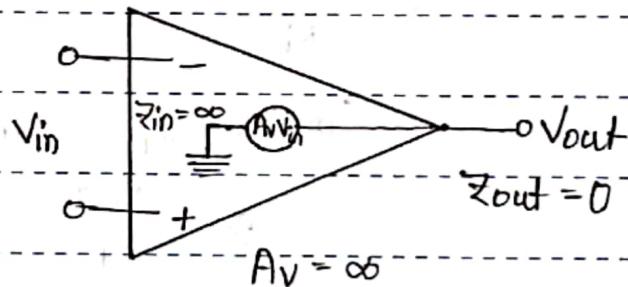
Properties of practical op-amp are -

- (a) Since the voltage gain (A_v) of a practical op-amp is very high, an extremely small input voltage (V_{in}) will produce a large output voltage (V_{out}).
- (b) Since the input impedance (Z_{in}) is very high, a practical op-amp has very small input current.
- (c) Since the output impedance (Z_{out}) of a practical op-amp is very low, it means the output voltage is practically independent of the value of load connected to op-amp.

Equivalent circuit of Ideal op-Amp:

The characteristics of an ideal op-amp are -

- (i) Infinite Voltage gain
- (ii) Infinite Input Impedance
- (iii) Zero output impedance

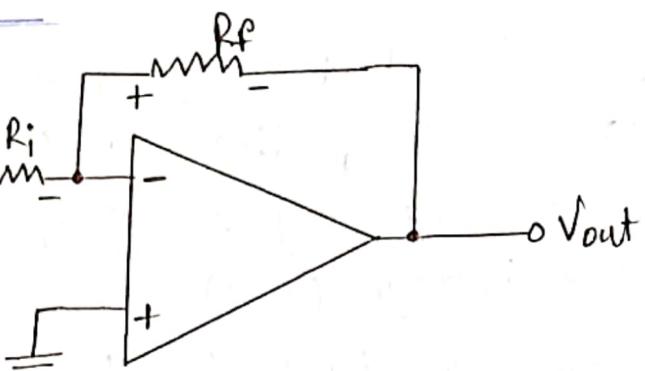


Properties of ideal op-amp are -

- (a) Since the voltage gain (A_v) of an ideal op-amp is infinite, it means that $V_{in} = 0V$.
- (b) Since the input impedance (Z_{in}) is infinite, an ideal op-amp has zero input current.
- (c) Since the output impedance (Z_{out}) of an ideal op-amp is zero, it means the output voltage does not depend on the value of load connected to op-amp.

Op-amp with negative feedback:

Inverting Amplifier: An Amplifier which has phase shift of 180° between input and output is called inverting amplifier.



$$\text{Here, } I_{in} = \frac{\text{Voltage across } R_i}{R_i}; \quad I_f = \frac{\text{Voltage Across } R_f}{R_f}$$

$$= \frac{V_{in} - V_A}{R_i}$$

$$= \frac{V_{in} - 0}{R_i}$$

$$= \frac{V_{in}}{R_i}$$

$$= \frac{V_{out}}{R_f}$$

$$= \frac{V_A - V_{out}}{R_f}$$

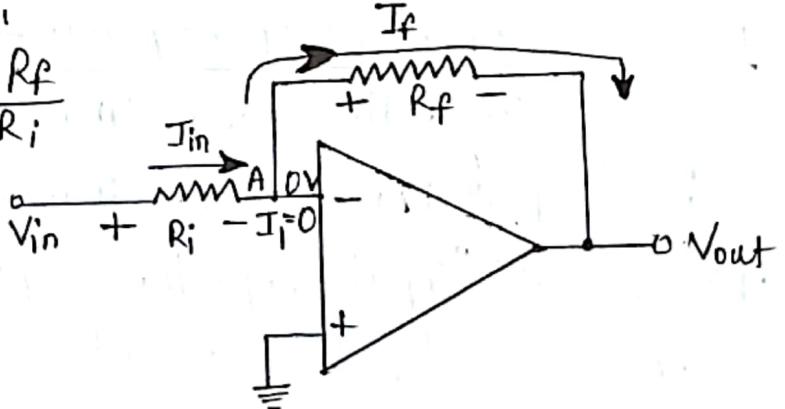
$$= \frac{0 - V_{out}}{R_f}$$

$$= \frac{-V_{out}}{R_f}$$

$$\text{Since, } I_f = I_{in}$$

$$\Rightarrow -\frac{V_{out}}{R_f} = \frac{V_{in}}{R_i}$$

$$\therefore \text{Voltage Gain, } A_{vL} = \frac{V_{out}}{V_{in}} = -\frac{R_f}{R_i}$$



Date: / /

Non inverting amplifier:

A non inverting amplifier

Produces an output signal V_{out}

that is in phase with the input signal

whereas an inverting amplifier's output V_{out}

is out of phase.

Voltage Across, $R_i = V_{in} - 0$

Voltage Across, $R_f = V_{out} - V_{in}$

Now, Current through R_i = Current through R_f

$$\Rightarrow \frac{V_{in} - 0}{R_i} = \frac{V_{out} - V_{in}}{R_f}$$

$$\Rightarrow V_{in} R_f = V_{out} R_i - V_{in} R_i$$

$$\Rightarrow V_{in} R_f + V_{in} R_i = V_{out} R_i$$

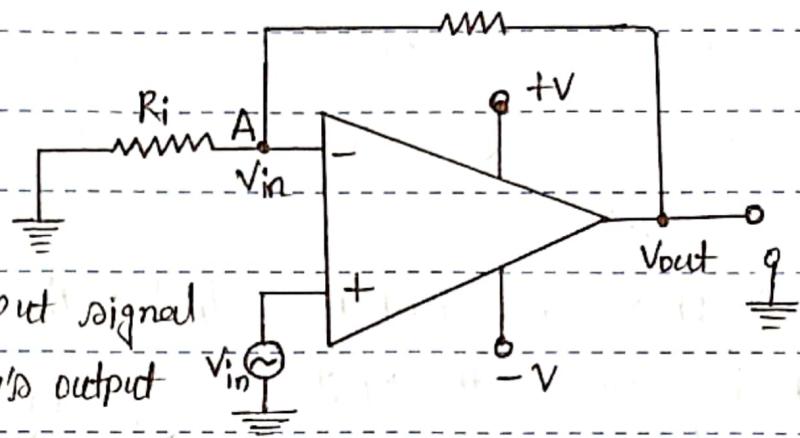
$$\Rightarrow V_{in} (R_f + R_i) = V_{out} R_i$$

$$\Rightarrow \frac{V_{out}}{V_{in}} = \frac{R_f + R_i}{R_i}$$

$$\Rightarrow \frac{V_{out}}{V_{in}} = 1 + \frac{R_f}{R_i}$$

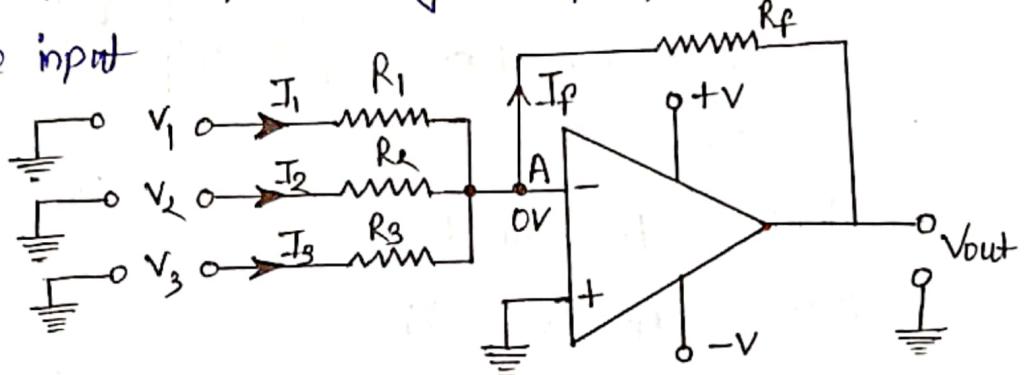
\therefore closed loop Voltage Gain, $A_{el} = \frac{V_{out}}{V_{in}} = 1 + \frac{R_f}{R_i}$

$$\therefore A_{el} = 1 + \frac{R_f}{R_i}$$



Summing Amplifier: A summing amplifier is an inverted op-amp that can accept two or more inputs. The output voltage of a summing amplifier is proportional to the negative of the algebraic sum of its input voltages.

{ Equations: } \Rightarrow Show that the output voltage is proportional to the algebraic sum of the input voltages.



$$I_f = I_1 + I_2 + I_3$$

when all the three inputs are applied, output voltage is,

$$\begin{aligned} V_{out} &= -I_1 R_f \\ &= -R_f (I_1 + I_2 + I_3) \\ &= -R_f \left(\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} \right) \end{aligned}$$

$$V_{out} = -R_f \left(\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} \right)$$

If, $R_1 = R_2 = R_3 = R$ then we have,

$$V_{out} = -\frac{R_f}{R} (V_1 + V_2 + V_3)$$

If, $R_f = R_1 = R_2 = R_3 = R$ then output voltage is,

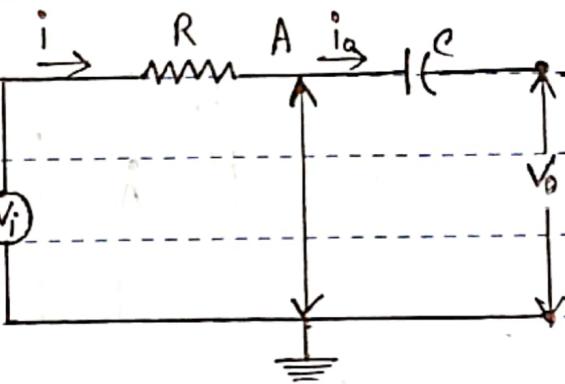
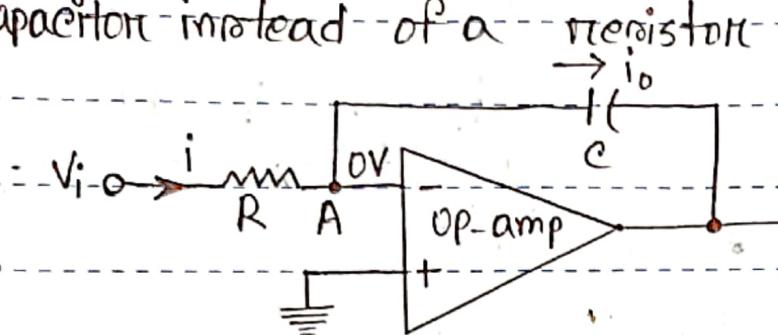
$$V_{out} = -(V_1 + V_2 + V_3)$$

Thus, when the gain of summing amplifier is unity the output voltage is the algebraic sum of the input voltages.

$$\therefore V_{out} = -\frac{R_f}{R} (V_1 + V_2 + V_3 + \dots)$$

Date: / /

Op-Amp Integration: An integrator is a circuit that performs integration of the input signal. Hence, feedback component is a capacitor instead of a resistor.



$$i = i_c$$

$$i = \frac{V_i - 0}{R} = \frac{V_i}{R} \quad \text{--- (1)}$$

Voltage across capacitor is $V_c = 0 - V_b = -V_b$

$$i_c = \frac{C dV_b}{dt} = -C \frac{dV_b}{dt} \quad \text{--- (2)}$$

From (1) and (2)

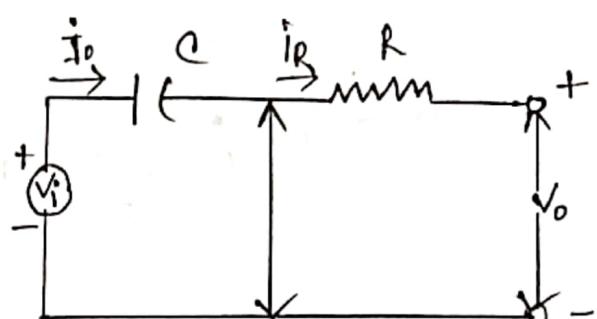
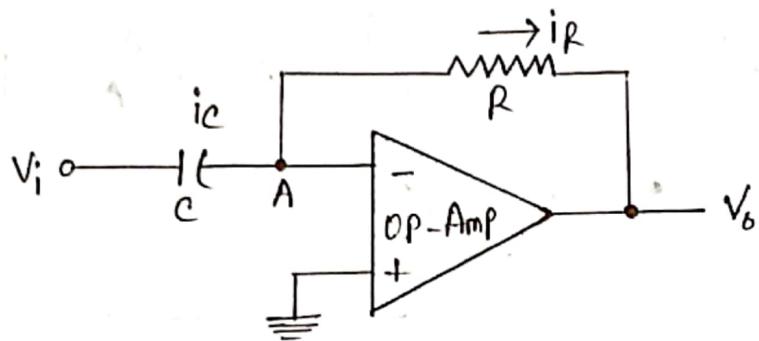
$$\frac{V_i}{R} = -C \frac{dV_b}{dt}$$

$$\frac{dV_b}{dt} = -\frac{1}{RC} V_i \quad \text{--- (3)}$$

Integrating both sides of eqn (3) we get,

$$V_b = -\frac{1}{RC} \int_0^t V_i dt$$

OP-Amp Differentiator: A differentiator is a circuit that performs differentiation of the input signal. A differentiator produces an output voltage that is proportional to the rate of change of the input voltage.



$$i_C = i_R$$

$$i_R = \frac{0 - V_o}{R} = -\frac{V_o}{R} \quad \text{and} \quad V_C = V_i - 0 = V_i$$

$$\Rightarrow i_C = C \frac{dV_C}{dt} = C \frac{dV_i}{dt}$$

$$\Rightarrow -\frac{V_o}{R} = C \frac{dV_i}{dt}$$

$$\therefore V_o = -RC \frac{dV_i}{dt}$$

Date: / /

25.1 A differential amplifier has an open-circuit voltage gain of 100. The input signals are 3.25 V and 3.15 V. Determine the output voltage?

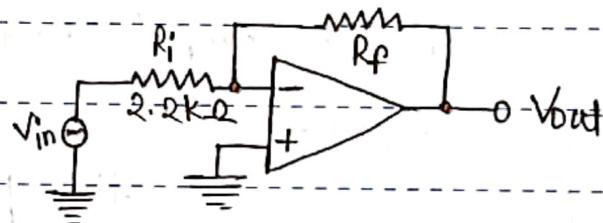
Solution: Here, $A = 100$, $V_1 = 3.25 \text{ V}$, $V_2 = 3.15 \text{ V}$

$$\begin{aligned}\text{Output voltage, } V_o &= A(V_1 - V_2) \\ &= 100(3.25 - 3.15) \\ &= 10 \text{ V}\end{aligned}$$

(Ans)

(Inverting Amplifier Math)

25.25 Given the op-amp configuration in Figure, determine the value of R_f required to produce a closed-loop voltage gain of -100.



Solution:

$$A_{CL} = -\frac{R_f}{R_i}$$

$$\Rightarrow -100 = -\frac{R_f}{2.2}$$

$$\Rightarrow R_f = 100 \times 2.2$$

$$\therefore R_f = 220 \text{ k}\Omega \quad (\text{Ans})$$

25.26 Determine the output voltage for the circuit. 200 kΩ

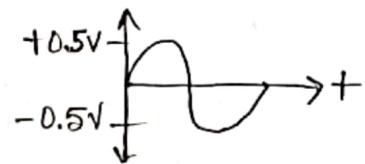
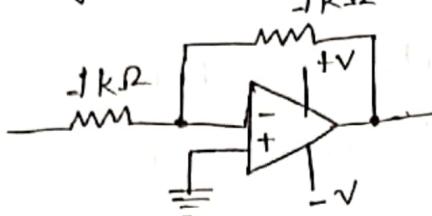
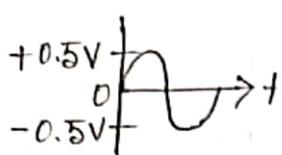
$$A_{CL} = -\frac{R_f}{R_L}$$

$$= -\frac{200 \text{ k}\Omega}{2 \text{ k}\Omega} = -100$$

$$\text{Output voltage, } V_{out} = A_{CL} \times V_{in}$$

$$\begin{aligned}&= (-100) \times (2.5 \text{ mV}) \\ &= -250 \text{ mV} \\ &= -0.25 \text{ V} \quad (\text{Ans})\end{aligned}$$

25.27 Find the output voltage for the circuit shown in figure.



Solution:

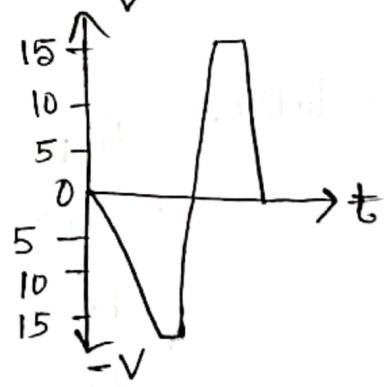
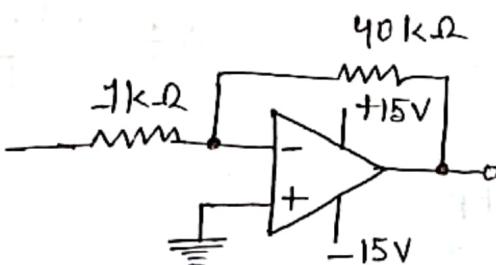
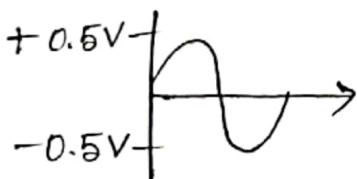
$$\text{Voltage gain, } A_{OL} = -\frac{R_f}{R_i}$$

$$= -\frac{1k\Omega}{1k\Omega}$$

$$= -1$$

Since, the voltage gain of the circuit is -1, the output will have the same amplitude but with 180° phase inversion.

25.28 Find the output voltage for the circuit shown in figure.



$$\text{Voltage gain, } A_{OL} = -\frac{R_f}{R_i}$$

$$= -\frac{40k\Omega}{1k\Omega}$$

$$= -40$$

Hence, voltage gain is -40. (Ans)

This means that the output will not have the same shape as input but will clip at the saturation voltage.

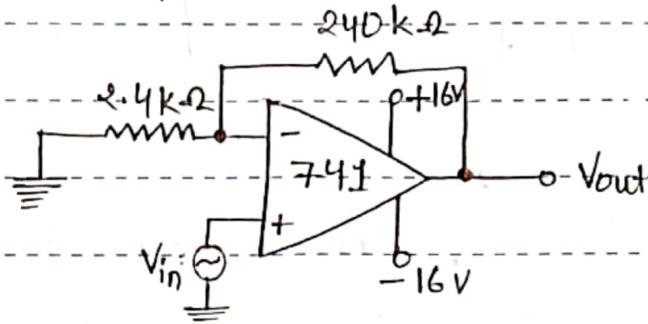
(Non-inverting amplifier Math)

Date: / /

25.32 Calculate the output voltage from the noninverting amplifier circuit shown in figure. for an input of 120 mV.

Solution:

$$\begin{aligned}\text{Voltage gain, } A_{cL} &= 1 + \frac{R_f}{R_i} \\ &= 1 + \frac{240\text{k}\Omega}{3.4\text{k}\Omega} \\ &= 1 + 100 \\ &= 101\end{aligned}$$



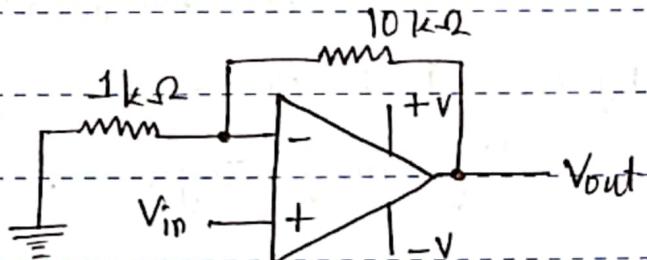
$$\text{output voltage, } V_{out} = A_{cL} \times V_{in} = (101) \times (120) = 12120 \text{ mV} = 12.12 \text{ mV}$$

(Ans)

25.33 For the noninverting amplifier circuit shown in figure. Find the output voltage for an input voltage of (i) 1V and (ii) -1V.

Solution:

$$\begin{aligned}\text{Voltage gain } A_{cL} &= 1 + \frac{R_f}{R_i} \\ &= 1 + \frac{10}{1} \\ &= 11\end{aligned}$$

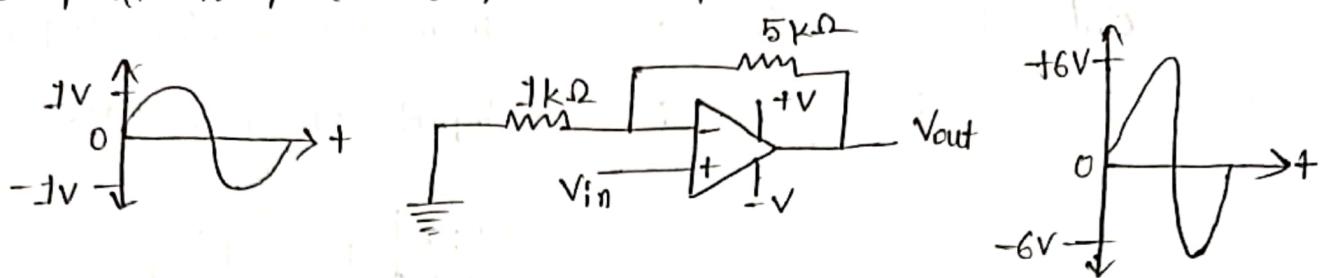


$$(i) \text{ For } V_{in} = 1\text{V}; \quad V_{out} = A_{cL} \times V_{in} = (11 \times 1)\text{V} = 11\text{V}$$

$$(ii) \text{ For } V_{in} = -1\text{V}; \quad V_{out} = A_{cL} \times V_{in} = 11 \times (-1) = -11\text{V}$$

(Ans)

25.34 For the noninverting amplifier circuit shown in figure, find peak to peak output voltage.



Solution: The input signal is 2V peak to peak.

$$\text{Voltage Gain, } A_{CL} = 1 + \frac{R_f}{R_i} = 1 + \frac{5\text{k}\Omega}{1\text{k}\Omega} = 1 + 5 = 6$$

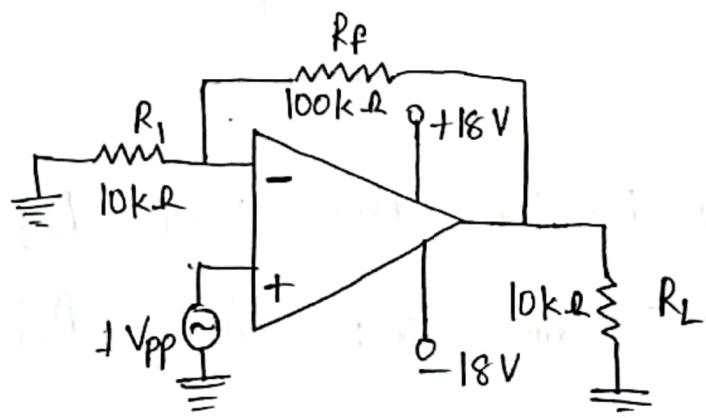
$$\begin{aligned} \therefore \text{Peak to peak output voltage} &= A_{CL} \times V_{in\text{pp}} \\ &= 6 \times 2 \\ &= 12\text{V}. \end{aligned}$$

(Ans)

25.35 For the noninverting amplifier circuit shown in figure, Find (i) closed loop voltage gain (ii) Maximum operating frequency. The slew rate is 0.5 V/μs.

Solution:

$$\begin{aligned} \text{(i) Voltage gain, } A_{CL} &= 1 + \frac{R_f}{R_i} \\ &= 1 + \frac{100}{10} \\ &= 1 + 10 \\ &= 11. \end{aligned}$$



Date: / /

(ii) To determine the value of maximum operating frequency (f_{max}), we need to calculate the peak output voltage for the amplifier. The peak-to-peak output voltage is,

$$V_{out} = A_{cl} \times V_{in} = 11 \times (1V_{pp}) = 11V_{pp}$$

Peak output voltage, $V_{pk} = 11/2 = 5.5 \text{ V}$

$$f_{max} = \frac{\text{Stem rate}}{2\pi V_{pk}} = \frac{0.5 \text{ V}/\mu\text{s}}{2\pi \times 5.5} = \frac{500 \text{ kHz}}{2\pi \times 5.5}$$

[$0.5 \text{ V}/\mu\text{s} = 500 \text{ kHz}$]

$$= 14.47 \text{ kHz}$$

(Ans)

(Summing Amplifier Math)

25.44 Determine the output voltage for the summing amplifier in the figure.

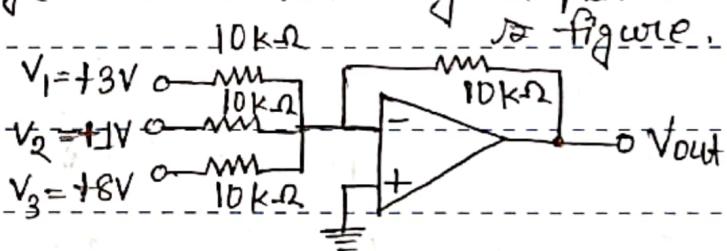
Solution:

$$V_{out} = -(V_1 + V_2 + V_3)$$

$$= -(3 + 1 + 8)$$

$$= -12 \text{ V}$$

(Ans)



25.45 Determine the output voltage for the summing amplifier shown in figure.

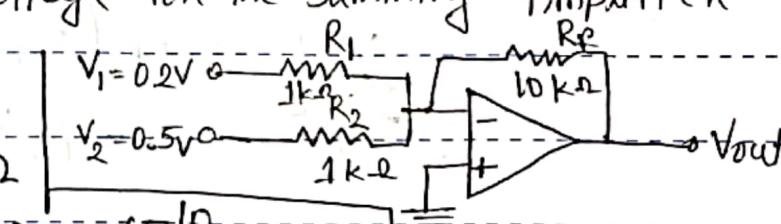
Solution: $R_f = 10k\Omega$, $R_1 = R_2 = R = 1k\Omega$

$$\text{Gain of Amplifier} = -R_f/R = \left(\frac{-10}{1}\right) = -10$$

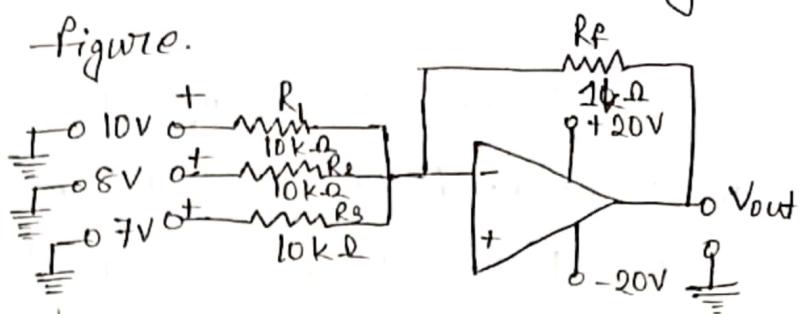
$$V_{out} = -\frac{R_f}{R} (V_1 + V_2)$$

$$= -\frac{10k\Omega}{1k\Omega} (0.2 + 0.5)$$

$$= -7 \text{ V} \quad \text{(Ans)}$$



25.46 Determine the output voltage for the summing amplifier shown in figure.



Solution: $R_p = 1\text{k}\Omega$

$$R_1 = R_2 = R_3 = R = 10\text{k}\Omega$$

$$\text{gain of amplifier} = - \frac{R_f}{R} = - \frac{1}{10} = - \frac{1}{10}$$

$$\begin{aligned} V_{\text{out}} &= - \frac{R_f}{R} (V_1 + V_2 + V_3) \\ &= - \frac{1}{10} (10 + 8 + 7) \\ &= - 2.5 \text{ V} \quad (\text{Ans}) \end{aligned}$$

25.47 Two voltages of $+0.6\text{V}$ and -1.4V are applied to the two input resistors of a summing amplifier. The respective input resistors are $400\text{k}\Omega$ and $100\text{k}\Omega$ and feedback capacitor resistor is $200\text{k}\Omega$. Determine the output voltage.

Solution:

$$\begin{aligned} V_{\text{out}} &= - R_f \left(\frac{V_1}{R_1} + \frac{V_2}{R_2} \right) \\ \therefore V_{\text{out}} &= - 200\text{k}\Omega \left(\frac{0.6}{400} + \frac{-1.4}{100} \right) \\ &= 2.5 \text{ V} \quad (\text{Ans}) \end{aligned}$$

Here,

$$R_f = 200\text{k}\Omega$$

$$R_1 = 400\text{k}\Omega$$

$$R_2 = 100\text{k}\Omega$$

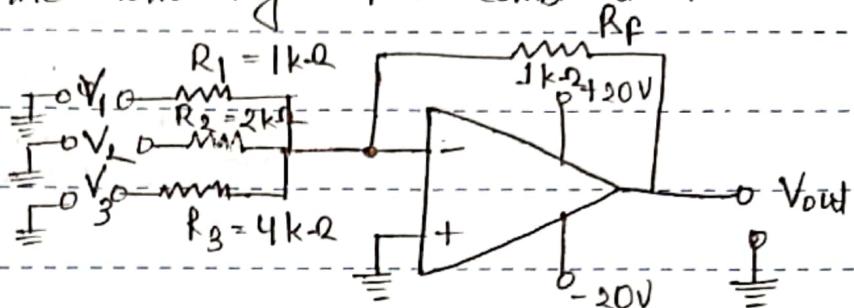
$$V_1 = +0.6\text{V}$$

$$V_2 = -1.4\text{V}$$

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25.48 Determine the output voltage from the circuit shown in figure for each of the following input combinations.

$V_1(V)$	$V_2(V)$	$V_3(V)$
+10	0	+10
0	+10	+10
+10	+10	+10



Solution: $V_{out} = -\frac{R_f}{R_1} (V_1 + V_2 + V_3)$

$$= -\left(\frac{R_f}{R_1} V_1 + \frac{R_f}{R_2} V_2 + \frac{R_f}{R_3} V_3\right)$$

$$= -\left(\frac{1}{1} V_1 + \frac{1}{2} V_2 + \frac{1}{4} V_3\right)$$

$$V_{out} = -(V_1 + 0.5V_2 + 0.25V_3)$$

The output voltage for the first set of input is

$$V_{out} = -(10 + 0.5 \times 0 + 0.25 \times 10) = -1.25 \text{ V}$$

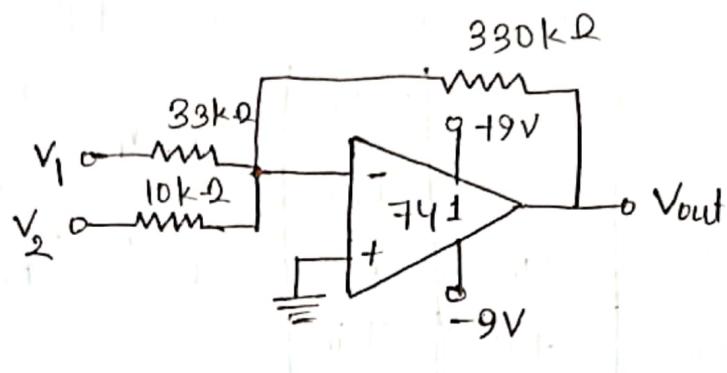
For the 2nd set of input is

$$V_{out} = -(0 + 0.5 \times 10 + 0.25 \times 10) = -7.5 \text{ V}$$

For the 3rd set of input is

$$V_{out} = -(10 + 0.5 \times 10 + 0.25 \times 10) = -17.5 \text{ V.}$$

25.49 Calculate the output voltage for the circuit of figure. The inputs are $V_1 = 50 \sin(1000t) \text{ mV}$ and $V_2 = 10 \sin(3000t) \text{ mV}$.



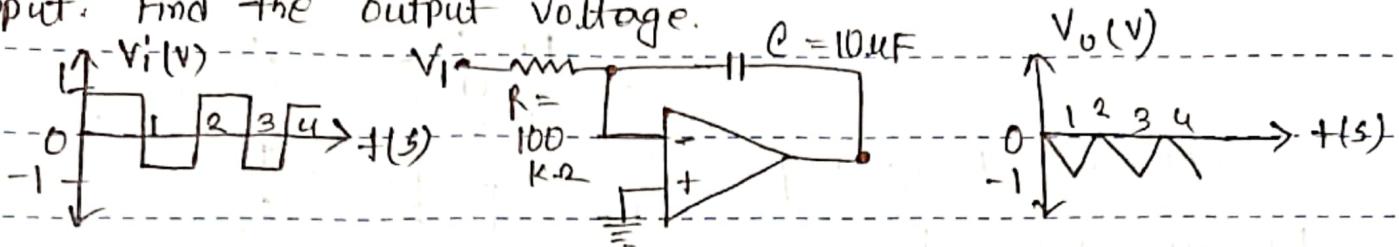
Solution: The output voltage for the circuit is,

$$\begin{aligned}
 V_{\text{out}} &= - \left(\frac{R_f}{R_1} V_1 + \frac{R_f}{R_e} V_2 \right) \\
 &= - \left(\frac{330\text{k}\Omega}{33\text{k}\Omega} V_1 + \frac{330\text{k}\Omega}{10\text{k}\Omega} V_2 \right) \\
 &= - (10V_1 + 33V_2) \\
 &= - [10 \times 50 \sin(1000t) + 33 \times 10 \sin(3000t)] \text{ mV} \\
 &= - [0.5 \sin(1000t) + 0.33 \sin(3000t)] \text{ V}
 \end{aligned}$$

(Op-amp Integrator meth)

Date: / /

Q5.50 Shows the op-amp integrator and the square wave input. Find the output voltage.



Solution: The output voltage of this circuit is given by,

$$V_o = -\frac{1}{RC} \int_0^t V_i dt$$

$$\begin{aligned} RC &= (100) \text{k}\Omega \times (10) \mu\text{F} \\ &= (100 \times 10^3 \text{k}\Omega) (10 \times 10^{-6} \text{F}) \\ &= 1\text{s} \end{aligned}$$

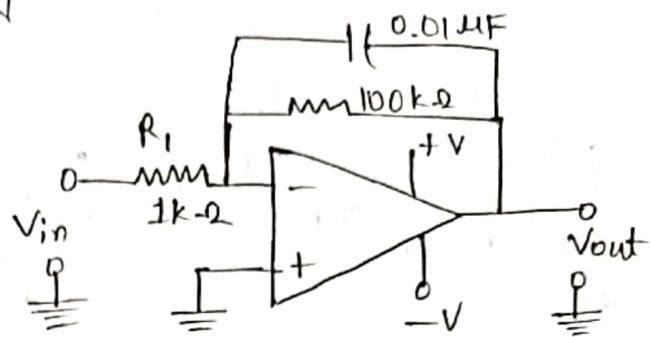
$$V_o = - \int_0^t V_i dt$$

When we integrate a ~~time~~ constant, we get a straight line, when input voltage to an integrator is constant, the output is a linear ramp. Then input to the integrator is applied to the inverting input, the output of the circuit will be 180° out of phase with the input. When input goes positive, the output will be a negative ramp. When the input is negative, the output will be a positive ramp.

25.51 Determine the lower frequency limit (critical frequency) for the integrator circuit shown in figure.

Solution:

The critical frequency for the integrator circuit shown in figure.



$$f_c = \frac{1}{2\pi R_f C}$$

$$= \frac{1}{2\pi \times (10^5) \times (0.01 \times 10^{-6})}$$

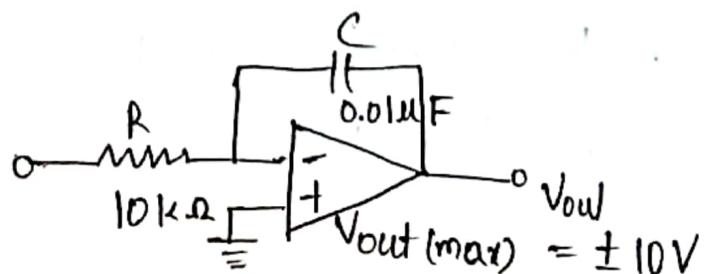
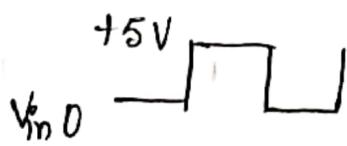
$$= 159 \text{ Hz}$$

Hence, $R_f = 100\text{k}\Omega$
 $= 105\Omega$
 $C = 0.01\mu\text{F}$
 $= 0.01 \times 10^{-6}\text{F}$

(Ans)

25.52 (i) Determine the rate of change of the output voltage in response to a single single pulse input to the integrator circuit in shown in figure.

(ii) Show the output waveform.



Date: / /

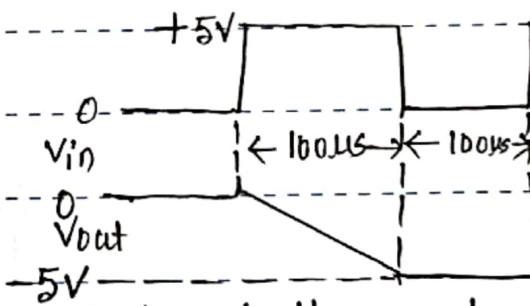
Solution: (i) Output voltage, $V_{out} = -\frac{1}{RC} \int_0^t V_{in} dt$

The rate of change of output voltage is,

$$\begin{aligned}\frac{\Delta V_{out}}{dt} &= -\frac{V_{in}}{RC} = -\frac{5V}{(10k\Omega)(0.01\mu F)} \\ &= -50 \text{ kV/s} \\ &= -50 \text{ mV/}\mu\text{s}\end{aligned}$$

(ii) The rate of change of output voltage is $-50 \text{ mV/}\mu\text{s}$. When the input is at +5V, the output is a negative-going ramp. When the input is at 0V, the output is a constant level. In 100μs, the output voltage decreases.

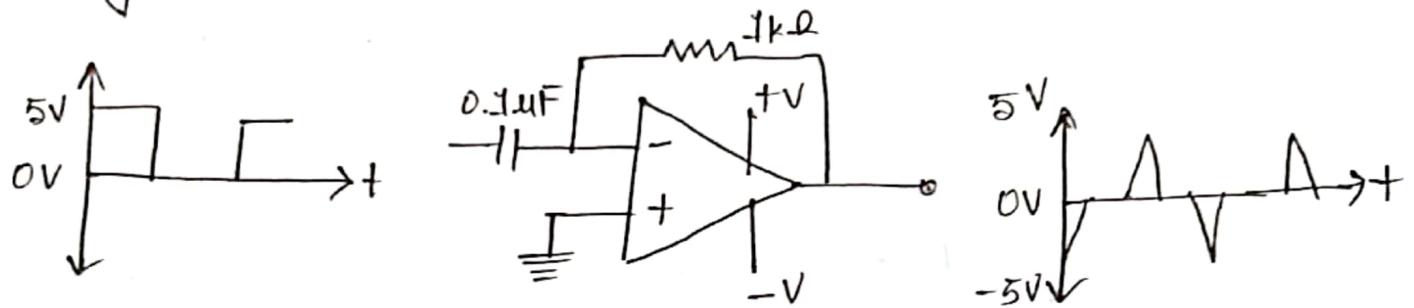
$$\begin{aligned}\Delta V_{out} &= \frac{\Delta V_{out}}{dt} \times dt \\ &= \frac{-50 \text{ mV}}{\mu\text{s}} \times 100\mu\text{s} \\ &= -5V\end{aligned}$$



The negative going ramp reaches $-5V$ at the end of the pulse. The output voltage then remains constant at $-5V$ for the time the input is 0V.

Op-Amp differentiator (Math)

25.54 This figure shows the square wave input to a differentiator circuit. Find the output voltage if input goes from 0V to 5V in 0.1ms.



Solution: Output voltage, $V_o = -RC \frac{dV_i}{dt}$

$$\begin{aligned} RC &= (1\text{k}\Omega) \times (0.1\mu\text{F}) \\ &= (10^3\Omega) (0.1 \times 10^{-6}\text{F}) \\ &= 0.1 \times 10^{-3}\text{s} \end{aligned}$$

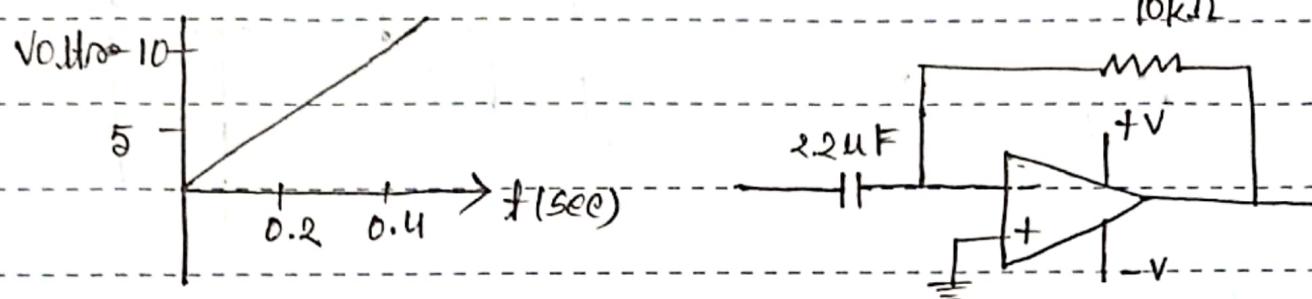
$$\text{At } t=0, \quad \frac{dV_i}{dt} = \frac{5\text{V}}{0.1\text{ms}} = \frac{5 \times 10^4\text{V}}{\text{s}} = 5 \times 10^4\text{V/s}$$

$$\begin{aligned} V_o &= -(0.1 \times 10^{-3})(5 \times 10^4) \\ &= -5\text{V} \end{aligned}$$

(Ans)

Date: / /

25.55 For the differentiator circuit shown in figure. determine the output voltage if the input goes from 0V to 10V in 0.4s. Assume the input voltage changes at constant rate.



Solution: Output voltage, $V_o = -RC \frac{dv_i}{dt}$

$$\text{Now, } RC = (10k\Omega) \times (2.2\mu F) = (10^4\Omega) (2.2 \times 10^{-6} F)$$

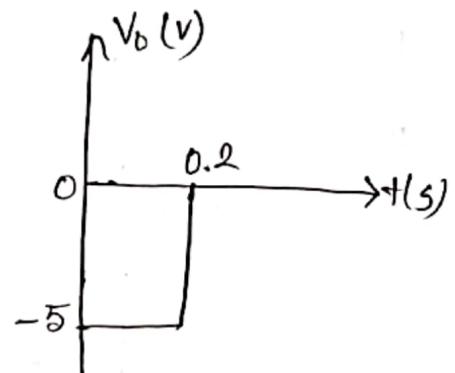
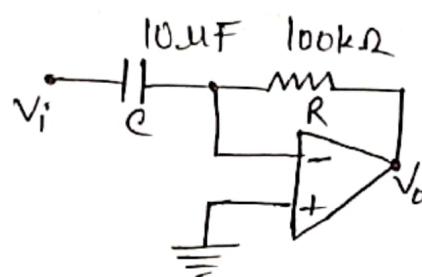
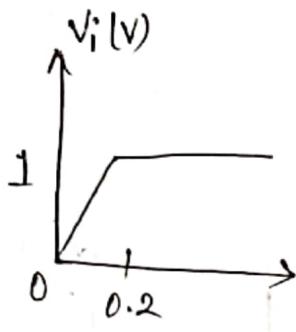
$$= 2.2 \times 10^{-2} s$$

$$\text{Also, } \frac{dv_i}{dt} = \frac{(10-0)V}{0.4s} = \frac{10V}{0.4s} = 25 V/s$$

$$V_o = -(2.2 \times 10^{-2}) \times 25 = -0.55 V$$

The output voltage stays constant at -0.55V.

- 25.56 For the differentiator circuit shown in figure
 (i) determine (i) the expression for the output voltage
 (ii) the output voltage for the given input.



Solution: (i) For the differentiator

$$\begin{aligned}
 V_o &= -RC \frac{dv_i}{dt} \\
 &= -(100k\Omega) \times (10\mu F) \frac{dv_i}{dt} \\
 &= -(100 \times 10^3 \Omega) \times (10 \times 10^{-6} F) \frac{dv_i}{dt} \\
 &= - \frac{dv_i}{dt}
 \end{aligned}$$

(ii) Input voltage is a straight line between 0 and 0.2s. The output voltage is

$$\begin{aligned}
 V_o &= - \frac{dv_i}{dt} \\
 &= - \frac{(1-0)}{0.2} \\
 &= -5V
 \end{aligned}$$

Between 0 to 0.2s, the output voltage is constant at -5V. For $t > 0.2s$, the input is constant so that output voltage is zero.