

International Islamic University Chittagong
Department of Electrical and Electronic Engineering

Final Examination Spring 2020

Course Code: **Math-1107**

Time: **5 hours** (Writing - **4 hours 30 minutes** + **30 minutes** submission time)

Program: B.Sc. Engg. (EEE)

Course Title: **Mathematics I**

Full Marks: **50** (Written 30 + Viva/Viva-Quiz-20)

[Answer each of the questions (1-5) from the followings; Figures in the right margin indicate full marks.]

SET-E

- | | | | |
|--|-----|----|----|
| <p>1(a). Investigate the maximum and minimum values of $f(x) = (x + p)^6 \cdot (x - Q)^5$ by using first time derivative, where P is the last two digits and Q is the reverse order of last two digits of your ID number.</p> | CO2 | Cr | 2 |
| <p>1(b). If $V = (x^2 + y^2 - z^2)^{\frac{1}{M}}$ then evaluate $V_{xx} + V_{yy} + V_{zz}$, where M the sum of all digits of your ID number is.</p> | CO1 | E | 2 |
| <p>1(c). Verify Euler's theorem to consider a homogeneous function of x, y, r whose degree is the sum of all digits of your ID number.</p> | CO2 | E | 2 |
| <p>2(a). Evaluate the following Integrals :</p> <p style="margin-left: 40px;">(i) $\int \frac{dx}{x(x+n)(x^n+2)}$ (ii) $\int \frac{dx}{a+b\cos x}$</p> <p style="margin-left: 40px;">Where n is the sum of all digits of your ID number.</p> | CO2 | An | 4 |
| <p>2(b). Explain the physical meaning of $\int f(x)dx$ and also its effect in EEE.</p> | CO1 | An | 2 |
| <p>3(a). Establish the reduction formula for $\int \tan^m x x^n dx$ and hence evaluate I_5.</p> | CO1 | Ap | 2 |
| <p>3(b). Write two properties of definite integral and verify it with considering an example which degree is sum of last two digit of your ID number</p> | CO2 | Ap | 2 |
| <p>3(c). Evaluate $\int_0^{\pi/2} \sin^5 \theta \cos^4 \theta d\theta$ by using Gamma-Beta function and also verify the result.</p> | CO1 | E | 2 |
| <p>4(a). Evaluate $\iiint_R (Ax^2 + By - Cz^2x) dx dy dz$, where $R: 0 \leq x \leq A, 0 \leq y \leq B, 0 \leq z \leq C$ where A be the first, B be the third digit of your ID number and C is the square root of sum of all digits of course code.</p> | CO1 | E | 3 |
| <p>4(b). Apply the limit of a sum to find $\int_a^b x^3 dx$.</p> | CO2 | Ap | 3 |
| <p>5(a). Evaluate the area of the region bounded by the parabolas $y^2 = 4ax$ and $x^2 = Kay$, where K is the sum of largest two digits of your ID number.</p> | CO2 | E | 3 |
| <p>5(b). Obtain the volume of $r = a(1 + \cos\theta)$, Also write the name of the curve and explain a, r.</p> | CO1 | Ap | 3 |
| <p>6. Viva/Viva-Quiz: The time of viva/viva-quiz will be declared in Google classroom.</p> | | | 20 |