

International Islamic University Chittagong
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Differential Equation
Ordinary Differential Equation
Group- A



Definition

1. Differential Equations
2. Ordinary Differential Equations
3. Partial Differential Equations
4. Order of Differential Equations
5. Degree of Differential Equations
6. Linear Differential Equations
7. Bernoulli's Differential Equations
8. Exact Differential Equations
9. Linear Differential Equations with Constant Coefficient
10. Integrating Factor
11. Bessel's Equation
12. Bessel's Function

Formation of Differential Equation

1. Form the differential equation whose solution is given by

- i. $y = A \cos (ax - b)$
- ii. $xy = pe^x + qe^{-x}$
- iii. $y = A \cos px + B \sin px$

Variables Separable

1. $x(y - 3)dy = 4y dx$
2. $\frac{dy}{dx} = e^{x-y} + x^2 e^{-y}$
3. $\frac{dy}{dx} = xy^3(1 + x^2)^{-\frac{1}{2}}, y(0) = 1$

Reducible Separable Variable

1. $\frac{dy}{dx} = (4x + y + 1)^2$
2. $\frac{dy}{dx} = (x + y) + \cos(x + y)$

Homogeneous Differential Equation

1. $y^2 + x^2 \frac{dy}{dx} = xy \frac{dy}{dx}$

$$2. \frac{dy}{dx} + \frac{y(x+y)}{x^2} = 0$$

Special case

$$1. \text{ Solve } (2x - 2y + 5) \frac{dy}{dx} = x - y + 3$$

$$2. \text{ Solve } \frac{dy}{dx} = \frac{6x-4y+3}{3x-2y+1}$$

Particular case

$$1. \text{ Solve } x \frac{dy}{dx} = \frac{2x-y+1}{x+2y-3}$$

$$2. \text{ Solve } \frac{dy}{dx} + \frac{ax+hy+g}{hx+by+7} = 0$$

Linear Differential Equation

$$1. (1 - x^2) \frac{dy}{dx} - xy = 1$$

$$2. y \log y \, dx + (x - \log y) dy = 0$$

Bernoulli's Differential Equation

$$1. \frac{dy}{dx} = x^3 y^3 - xy$$

$$2. x \frac{dy}{dx} + y = x^4 y^3$$

$$3. xy - \frac{dy}{dx} = y^3 e^{-x^2}$$

Exact Differential Equation

$$1. (x - 2e^y) dy + (y + x \sin x) dx = 0$$

$$2. \text{ Solve } (y^4 + 4x^3 y + 3x) dx + (x^4 + 4xy^3 + y + 1) dy = 0$$

If not exact,

$$1. ((x^2 + y^2) dx - 2xy \, dy = 0$$

$$2. (x^4 + 2y) dx + (xy^3 + 2y^4 - 4x) dy = 0$$

$$3. (2x \log x - xy) dy + 2y \, dx = 0$$

Higher Order Differential Equation with Constants Co-efficients

$$1. \frac{d^3 y}{dx^3} - 3 \frac{d^2 y}{dx^2} + 4 \frac{dy}{dx} - 2y = e^x + \cos x$$

$$2. \frac{d^3 y}{dx^3} + 3 \frac{d^2 y}{dx^2} + 3 \frac{dy}{dx} + y = e^{-x} + 1 + \sin 2x$$

Suggestion from

Rashed sir