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Autumn : 2016

Answer to the Question No: 1 (a)

Now the addition of two numbers using BCD code is

$$46 = 0100\ 0110$$

$$55 = 0101\ 0101$$

$$= 1001\ 1011$$

$$\therefore \text{if invalid add } 6 = 0110$$

$$1010\ 0001$$

$$\therefore \text{if invalid add } 6 = 0110$$

$$10000001$$

$$\therefore \text{More precisely} = \frac{0001}{1} \frac{0000}{0} \frac{0001}{1}$$

So the BCD addition of

$$46 + 55 \text{ is } = 101$$

$$\begin{aligned} 01\ 10 &= 6 \\ 01\ 00 &= 4 \\ 01\ 01 &= 5 \end{aligned}$$

Answer to the Question No: 1(b)

(2)

Binary codes are those codes which depend on the binary number system to represent its meaning. Binary codes are two base codes. They are '0' and '1'.

Advantages of Excess 3 codes over BCD codes are:-

- ① Excess 3 code has no limitation
- ② It considerably simplifies arithmetic operations.

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Answer to the Question NO:1c)

A gray code is an encoding of numbers so that adjacent numbers have a single bit digit differing by 1.

Three gray codes for 3 variables

Decimal	BCD	gray
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1	0001	0001
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5	0101	0111
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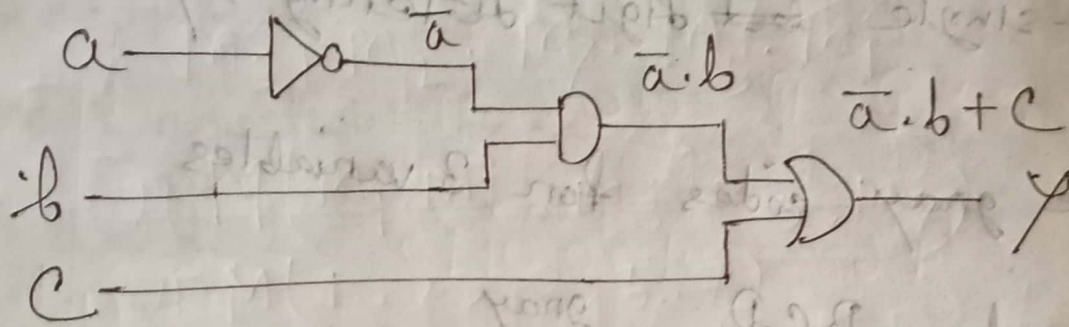
6	0110	0101
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process had been provided in the previous number system P&P.

~~process in has been~~

Q1: Answer to the Question 2(a)

So the given circuit



So the boolean expression is

$$Y = \bar{a} \cdot b + c$$

Truth Table: $1110 = 1010 = 1$

	a	b	c	\bar{a}	$\bar{a} \cdot b$	$\bar{a} \cdot b + c$
1	0	0	0	1	0	0
2	0	0	1	1	0	1
3	0	1	0	1	1	1
4	0	1	1	1	1	1
5	1	0	0	0	0	0
6	1	0	1	0	0	1
7	1	1	0	0	0	0
8	1	1	1	0	0	1

Answer to the Ques NO: 2(b)

So the above expression is

$$y = \bar{a}b + c$$

$$= \bar{a}b(c + \bar{c}) + c(a + \bar{a})(b + \bar{b})$$

$$= \bar{a}bc + \bar{a}b\bar{c} + abc + \bar{a}\bar{b}c + \bar{a}\bar{b}\bar{c} + abc + \bar{a}b\bar{c}$$

$$\therefore Y_1 = \bar{a}bc + \bar{a}b\bar{c} + abc + \bar{a}\bar{b}c + \bar{a}\bar{b}\bar{c}$$

$$= m_3 + m_2 + m_7 + m_5 + m_1$$

$$= m_1 + m_2 + m_3 + m_5 + m_7$$

\therefore Sum of Minterms,

$$= \sum m(1, 2, 3, 5, 7)$$

\therefore We can express POS or Product of Max-terms,

$$\begin{aligned} \bar{Y}_1 &= \bar{a}bc + \bar{a}b\bar{c} + abc + \bar{a}\bar{b}c + \bar{a}\bar{b}\bar{c} \\ &= (\bar{a}bc) \cdot (\bar{a}b\bar{c}) \cdot (abc) \cdot (\bar{a}\bar{b}c) \cdot (\bar{a}\bar{b}\bar{c}) \end{aligned}$$

Q. 10) ON each set of numbers

$$= (a + \bar{b} + \bar{c}) \cdot (a + b + c) \cdot (\bar{a} + \bar{b} + \bar{c}) \cdot (\bar{a} + b + \bar{c})$$

$$= (a + \bar{b} + \bar{c}) \cdot (a + b + c) \cdot (\bar{a} + \bar{b} + \bar{c}) \cdot (\bar{a} + b + \bar{c})$$

$$= \pi M(m_1, m_2, m_3, m_4, m_5, m_6, m_7)$$

$$= \pi M(1, 2, 3, 5, 7)$$

It is the Product of minterms

$$= \sum m(1, 2, 3, 5, 7)$$

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Answer to the Question No: 2(c)

$$F1 = (A+C)(AD+AD)+AC+C$$

$$= (A+C)(AD) + C(A+1)$$

$$= AAD + ADC + C$$

$$= AD + ADC + C$$

$$= AD + C(AD+1)$$

$$= AD + C$$

Ans

$$F2 = (A'(A+B)')' + (B+AA)(A+B)$$

$$= (A'(A+B'))' + (A+B)(A+B)$$

$$= (A'B')' + (A+B)$$

$$= (A'' + B'') + (A+B)$$

$$= (A+B) + (A+B)$$

$$= A+B$$

Ans

(8)

Answer to the Question No: 3(a)

$$F = (A' + B' + D)(A' + D')(A + B + D')(A + B' + C + D)$$

$$= (A' \cdot B' \cdot D') + (A' \cdot D') + (A' \cdot B' \cdot D') + (A' \cdot B' \cdot C \cdot D')$$

$$= (\overline{A} \overline{B} \overline{D}) + (\overline{A} \overline{D}) + (\overline{A} B' D) + (\overline{A} B' C \overline{D})$$

$\overline{A} \overline{B}$	0	1	2	3
$\overline{A} B$	4	5	6	7
$A B$	12	13	14	15
$A \overline{B}$	8	9	10	11

Karnaugh map showing the function F. The map is a 4x4 grid with rows labeled $\overline{A} \overline{B}$, $\overline{A} B$, $A B$, and $A \overline{B}$ and columns labeled 0, 1, 2, 3. The cells are numbered 0 through 15. The function F is represented by the following cells containing 1s: (1,1), (1,2), (1,3), (1,4), (2,0), (2,1), (2,2), (2,3), (3,1), (3,2), (3,3), (3,4). The cells (0,0), (0,1), (0,2), (0,3), (1,0), (1,1), (1,2), (1,3), (2,0), (2,1), (2,2), (2,3), (3,0), (3,1), (3,2), (3,3) are marked with 0.

⑨

$$\therefore F = AD + AB + B\bar{C}\bar{D} + \bar{B}D$$

Ans:

Answer to the Question No. 3 (b)

$$F = AB'C + B'C'D' + BCD + ACD' + A'B'C + A'BC'D$$

	$\bar{C}\bar{D}$	$\bar{C}D$	CD	$C\bar{D}$
$\bar{A}\bar{B}$	1	0	1	1
$\bar{A}B$	0	1	1	0
AB	0	0	1	1
$A\bar{B}$	1	0	1	1

(10)

$$F = \overline{A}BD + \overline{B}\overline{D} + AC + CD$$

AnsAns

(d) 8.0. Note 22 out of 200 A

$$F = \overline{A}BD + \overline{B}\overline{D} + AC + CD$$

$\overline{C}D$	CD	$\overline{C}\overline{D}$	$\overline{C}D$	
1	1	0	1	$\overline{A}B$
0	1	1	0	$A\overline{B}$
1	1	0	0	$\overline{A}B$
1	1	0	1	$\overline{A}B$

(11)

Answer to the Question NO: 3(c)

$$F_0(A, B, C, D) = \sum (0, 4, 5, 8, 10, 15)$$

$$J(A, B, C, D) = \sum (2, 7, 9, 13)$$

	$\bar{C}\bar{D}$	$\bar{C}D$	CD	$C\bar{D}$
$\bar{A}\bar{B}$	1 0			X 2
$\bar{A}B$	1 4	1 5	X 6	
AB	0 12	X 13	1 15	14
$A\bar{B}$	1 4	X 9	0 11	1 10

$$F = \bar{B}\bar{D} + BD + \bar{A}\bar{C}\bar{D}$$

Ans:

(12)

(11)

Answer to the question No: 3(c)

Implementing F equation using
NAND Gate

The given equation

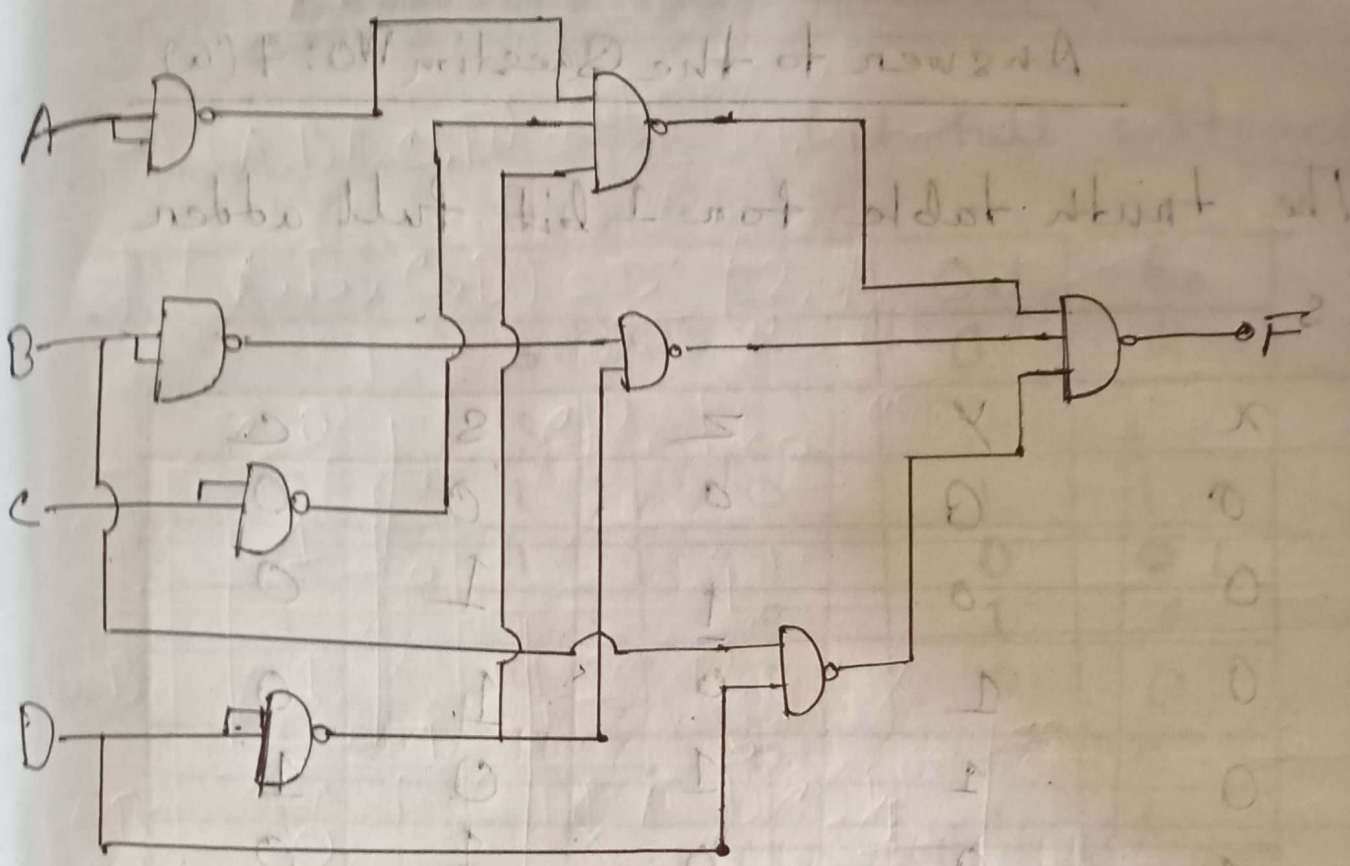
$$F = \bar{B}\bar{D} + BD + \bar{A}\bar{C}\bar{D}$$

$$= \bar{B}\bar{D} + BD + \bar{A}\bar{C}\bar{D}$$

$$= \bar{B}\bar{D} + BD + \bar{A}\bar{C}\bar{D}$$

$$\bar{C}\bar{D}\bar{A} + BD + \bar{D}\bar{B}$$

Ans.



$$F = \overline{B} \overline{D} + B \overline{D} + \overline{A} \overline{C} \overline{D}$$

Ans

Answer to the Question No: 4(a)

The truth table for 1 bit full adder is

x	y	z	s	c
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

(31)

(15)

(2) Answer to the Question NO: 4(b)

The truth table for 1 bit full subtractor

x	y	z	Out	Bo
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

Many seemed to be confused with this. The confusion is where to start from. Let us consider a practical case where you are actually walking up and down the stairs and real situations were you need to turn on and off the light in a sequential manner.

Let S_1 , S_2 represent the status of switches on first floor and second floor respectively. Let Y be the status of bulb. 1 represents on condition and 0 represents off condition.

You are climbing up from first floor to second floor.

Both switches are off and the light is also off, now its $S_1=0$, $S_2=0$ and $Y=0$.

You need light to walk up the staircase. So you switch on S_1 on the first floor, the light should get switched on. Hence now $S_1=1$, $S_2=0$ and $Y=1$.

After climbing the stairs, you reached S_2 and now you want to switch off the light as you no longer need it as you have crossed the stairs, so you press switch S_2 (you actually turn S_2 on to switch off the light). Now, $S_1=1$, $S_2=1$, $Y=0$

Similarly if you start the other way round - i.e. you are moving down from second floor to first floor, you will observe that when $S_1=0$, $S_2=1$, $Y=1$

From the above observations, we can conclude that the output is on whenever either of the switches are on and off when both the switches are together on and off. The only truth table that matches with this is that of the XOR gate.