

Given Dataset

Weight (X)	Price (Y)
2	35
4	60
5	20
3	50
6	50
5	55
7	60

Formula of Linear Regression

$$Y = MX + c$$

$$c = \bar{Y} - M\bar{X}$$

$$M = \frac{\bar{X} \cdot \bar{Y} - \overline{XY}}{(\bar{X})^2 - \overline{X^2}}$$

$$\bar{X} = \text{Mean } X$$

$$\bar{Y} = \text{Mean } Y$$

Calculation Table for Linear Regression

X	Y	XY	X <sup>2</sup>	$\bar{X}$	$\bar{Y}$	$\bar{X}\bar{Y}$	$(\bar{X})^2$	$\overline{X^2}$
2	35	70	4	$\frac{32}{7}$ $= 4.57$	$\frac{330}{7}$ $= 47.14$	$\frac{1555}{7}$ $= 222.14$	$(4.57)^2$ $= 20.88$	$\frac{164}{7}$ $= 23.43$
4	60	240	16					
5	20	100	25					
3	50	150	9					
6	50	300	36					
5	55	275	25					
7	60	420	49					

$$\text{Now, } M = \frac{\bar{X} \cdot \bar{Y} - \overline{XY}}{(\bar{X})^2 - \overline{X^2}}$$

$$= \frac{4.57 \times 47.14 - 222.14}{20.88 - 23.43}$$

$$= \frac{215.43 - 222.14}{20.88 - 23.43}$$

$$= \frac{-6.71}{-2.55}$$

$$\text{Slope, } M = 2.63$$

$$\text{Now, } C = \bar{Y} - M\bar{X}$$

$$= 47.14 - 2.63 \times 4.57$$

$$= 47.14 - 12.02$$

$$\text{Intercept, } C = 35.12$$

Now, predicted price for vegetable weight 6

$$\text{is, } Y = MX + C$$

$$= 2.63 \times 6 + 35.12$$

$$= 50.9$$

Now, we find the predicted value for the given dataset and also calculate the residuals:

weight	value	predicted_value	residuals
2	35	40.38	5.38
4	60	45.64	14.36
5	20	48.27	28.27
3	50	43.01	6.99
6	50	50.90	0.90
5	55	48.27	6.73
7	60	53.53	6.47

Now, Take another table for calculating MSE & MAE:

actual value ( $y_i$ )	predicted value ( $\hat{y}_i$ )	$y_i - \hat{y}_i$	$ y_i - \hat{y}_i $	$(y_i - \hat{y}_i)^2$
35	40.38	-5.38	5.38	28.94
60	45.64	14.36	14.36	206.21
20	48.27	-28.27	28.27	799.19
50	43.01	6.99	6.99	48.86
50	50.90	-0.9	0.9	0.81
55	48.27	6.73	6.73	45.29
60	53.53	6.47	6.47	41.86

## Mean Absolute Error (MAE):

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i|$$

$$= \frac{5.38 + 14.36 + 28.27 + 6.99 + 6.9 + 6.73 + 6.47}{7}$$

$$= \frac{69.1}{7}$$

$$= 9.87$$

## Mean Squared Error (MSE):

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$= \frac{28.94 + 206.21 + 799.19 + 48.86 + 0.81 + 45.29 + 41.86}{7}$$

$$= \frac{1171.16}{7}$$

$$= 167.31$$