

Heaven's Light is Our Guide

Rajshahi University of Engineering & Technology
(RUET)



Department of ECE

Course No.: ECE 4124

Course Title: Digital Signal Processing Sessional

LAB REPORT

Submitted by:

Name: Md. Rakibul Islam

Roll: 1810019

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Submitted to:

Hafsa Binte Kibria

Lecturer

Department of ECE, RUET

5.1 Experiment No: 05

5.2 Experiment Date: 22.05.2023

5.3 Experiment Name: Z-transform, zeroes, poles & ROC of Causal, Anti-causal, and Non-causal signal

5.4 Theory:

Casual Signal: In the context of the Z-transform, a causal signal is a sequence that is nonzero only for nonnegative indices or time instances. It is also as right handed signal. The Z-transform of a right-sided signal can be computed using the definition of the Z-transform.

The general formula for the Z-transform of a right-sided signal $x[n]$ is:

$$X(z) = \sum [x[n] * z^{(-n)}], \text{ for } n = 0 \text{ to infinity}$$

Anti-causal Signal: In the context of the Z-transform, a anti-causal signal is a sequence that is nonzero only for negative indices or time instances. It is also called as left handed signal. The Z-transform of a left-sided signal can be computed using the definition of the Z-transform.

The general formula for the Z-transform of a left-sided signal $x[n]$ is:

$$X(z) = \sum [x[n] * z^{(-n)}], \text{ for } n = -\text{infinity to } -1$$

Non-Causal Signal: Non-causal signal in the context of the Z-transform refers to a sequence that has nonzero values for both positive and negative indices or time instances. The Z-transform of a non-causal signal can still be computed using the definition of the Z-transform.

The general formula for the Z-transform of a non-causal signal $x[n]$ is:

$$X(z) = \sum [x[n] * z^{(-n)}], \text{ for all values of } n$$

5.5 Code & Output:

5.5.1.1 Code of Causal Signal:

```
x=[1 2 3 4 5]
b=0;
n=length(x);
y=sym('z');
for i=1:n
    b=b+x(i)*y^(1-i);
end
display(b)

z=[];
p=[0]
zplane(z,p)
```

5.5.1.2 Output:

```
>> z_transform  
  
x =  
  
    1    2    3    4    5  
  
b =  
  
 $\frac{2}{z} + \frac{3}{z^2} + \frac{4}{z^3} + \frac{5}{z^4} + 1$ 
```

Figure 5.1: Output of Causal Signal

5.5.1.3 Zeros and poles:

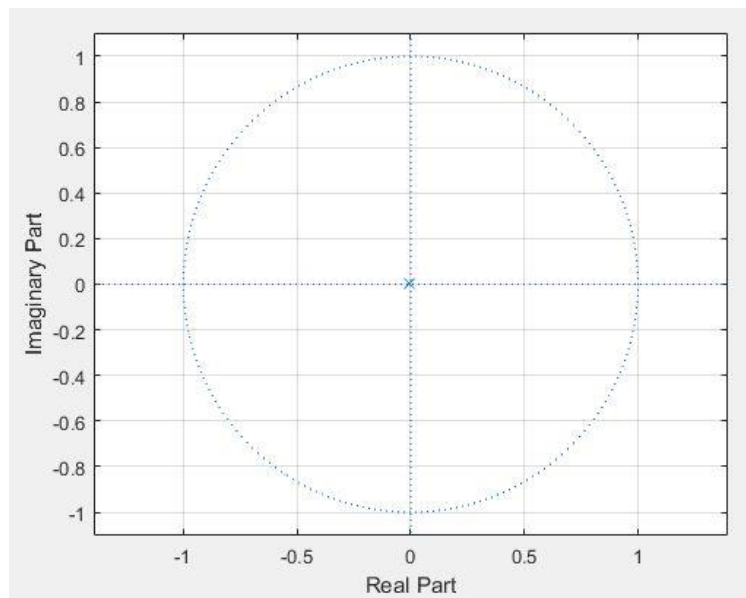


Figure 5.2: Zeros and Poles of Causal Signal

5.5.2.1 Code of Anti Causal signal:

```
x=[1 2 3 4 5]  
b=0;  
n=length(x);  
y=sym('z');  
for i=1:n  
    b=b+x(i)*y^(i-1);  
end  
display(b)  
z=[];  
p=[]  
zplane(z,p)
```

5.5.2.2 Output:

```
x =  
    1    2    3    4    5  
  
b =  
5*z^4 + 4*z^3 + 3*z^2 + 2*z + 1
```

Figure 5.3: Output of anti-causal Signal

5.5.2.3: Poles and Zeros:

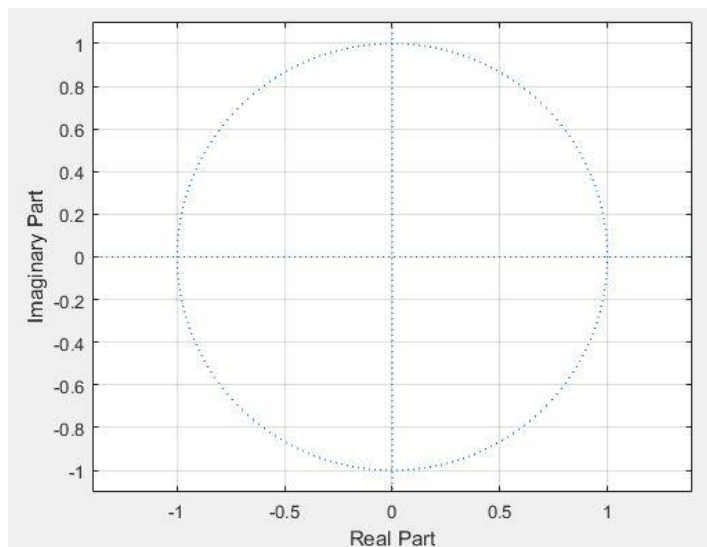


Figure 5.4: Zeros and Poles of anti-causal signal

5.5.3.1 Code of non causal signal:

```
x=[1 2 3 4 5]  
value=3;  
index=find(x==value);  
disp(index);  
  
b=0;  
n=length(x);  
y=sym('z');  
for i=1:n  
    b=b+x(i)*y^(index-i);  
end  
display(b)  
  
z=[];  
p=[0]  
zplane(z,p)  
grid
```

5.5.3.2 Output:

```
x =  
  
1      2      3      4      5  
  
3  
  
b =  
  
2*z + 4/z + 5/z^2 + z^2 + 3
```

Figure 5.3: Output of Non causal signal

5.5.3.3 Poles and Zeros:

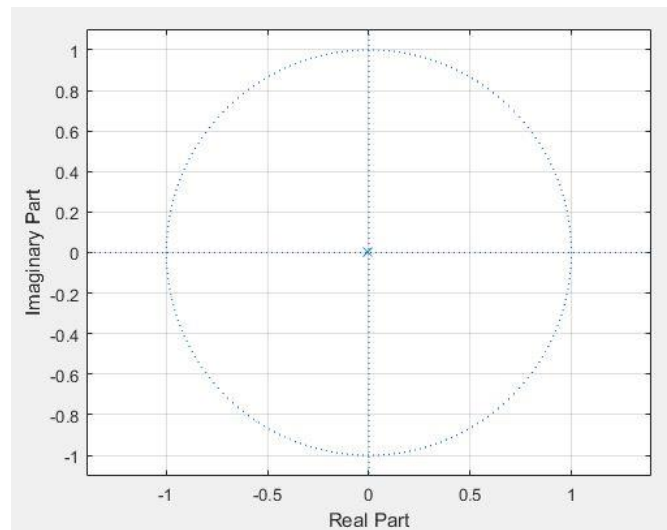


Figure 5.4: Poles and Zeros of non-causal signal

5.6 Discussion: In this experiment, we learnt about some signal like causal signal, anti causal signal and non causal signal. We saw the basic differences of these signals. A causal signal is a sequence that is nonzero only for nonnegative indices or time instances. The Z-transform of a causal signal is typically a rational function with a region of convergence (ROC) that includes the unit circle. An anti-causal signal is a sequence that is nonzero only for negative indices or time instances. The Z-transform of an anti-causal signal is typically a rational function with a region of convergence (ROC) that includes the exterior of the unit circle. A non-causal signal is a sequence that has nonzero values for both positive and negative indices or time instances. The Z-transform of a non-causal signal can still be computed, but the resulting expression may not be a rational function, and the ROC may be a ring or annulus in the Z-plane. We implemented the code for causal, anti causal, non-causal and finally we saw the poles and zeros of different signals.

5.7 Conclusion: We successfully completed the task as we got the exactly same result which we learnt from the theory.