

CSE204 : Offline 8 Report

Submitted by :

ID : 1805012

Complexity Analysis:

```
79 distance_index_pair calculate_distance2(point *points_x, point* points_y,int st,int en){
80     if( st > en )
81         return {inf,-1,-1,inf,-1,-1};
82     if( st == en ){
83         points_y[st] = points_x[st];
84         return {inf,-1,-1,inf,-1,-1};
85     }
86     if( en-st == 1 ){
87         for(int i=st;i<=en;i++)
88             points_y[i] = points_x[i];
89         merge_sort(points_y+st,2,cmp_ymajor);
90         return {distance(points_x[st],points_x[en]),points_x[st].index,points_x[en].index,inf,-1,-1};
91     }
92     if( en-st == 2){
93         for(int i=st;i<=en;i++)
94             points_y[i] = points_x[i];
95         merge_sort(points_y+st,3,cmp_ymajor);
96
97         distance_index dist_ind[3] ;
98         int id = 0;
99         for(int i=st;i<=en;i++)
100             for(int j=i+1;j<=en;j++)
101                 dist_ind[id++] = {distance(points_x[i],points_x[j]),points_x[i].index,points_x[j].index};
102         merge_sort(dist_ind,3,cmp_distance_index);
103         return {dist_ind[0],dist_ind[1]};
104     }
105
106     int mid = (st+en)/2;
107     distance_index_pair left = calculate_distance2(points_x,points_y, st, mid);
108     distance_index_pair right = calculate_distance2(points_x,points_y, mid+1, en);
109     distance_index dist_ind[4] = {left.di[0],left.di[1],right.di[0],right.di[1]};
110
111     merge_sort(dist_ind,4,cmp_distance_index);
112     double k = dist_ind[1].dist;
```

Let's say the time complexity of the function is $T(n)$.

The first 4 if blocks take $\Theta(1)$ time.

There are two recursive calls to the function, which costs $T(n/2)$ each.

```
113
114     int I = mid;
115     int J = en;
116     int i = st, j=mid+1;
117     int id = st;
118     int n = 0;
119     while( i<=I || j<=J ){
120         if( i>I )
121             points_y_aux[id++] = points_y[j++];
122         else if( j>J )
123             points_y_aux[id++] = points_y[i++];
124         else if( cmp_ymajor(points_y[i],points_y[j]))
125             points_y_aux[id++] = points_y[i++];
126         else points_y_aux[id++] = points_y[j++];
127     }
128     for(i=st;i<=en;i++)
129         points_y[i] = points_y_aux[i];
130
131     distance_index strip_min = {inf,-1,-1};
132     i = st;
133     while( i<=en ){
134         if( abs(points_y[i].x-points_x[mid].x) < k ){
135             strip[n] = points_y[i];
136             side[n] = (points_y[i].x<=points_x[mid].x) ;
137             n++;
138         }
139         i++;
140     }
141
142     for(i=0;i<n;i++){
143         for(j=i+1;j<n && (strip[j].y-strip[i].y) < k; j++){
144             if( (side[i]^side[j]) == 1 ){
145                 double temp_distance = distance(strip[i],strip[j]);
146                 if( strip_min.dist > temp_distance){
147                     strip_min.dist = temp_distance;
148                     strip_min.i = strip[i].index;
149                     strip_min.j = strip[j].index;
150                 }
151             }
152         }
153     }
154
155     if( strip_min.dist < dist_ind[3].dist ){
156         dist_ind[3] = strip_min;
157     }
158     merge_sort(dist_ind,4,cmp_distance_index);
159     return {dist_ind[0],dist_ind[1]};
160 }
```

Lines 114 – 129 merges the 'points_y' variables, which is $\Theta(n)$

Copying them to form valid strip takes $\Theta(n)$.

Lines 142 – 153 calculates the minimum distance in the strip. It takes $\Theta(n)$, though it has a nested loop. The value of $'j' - 'i'$ is at most 7, if the points are distinct. So it is $\Theta(n)$.

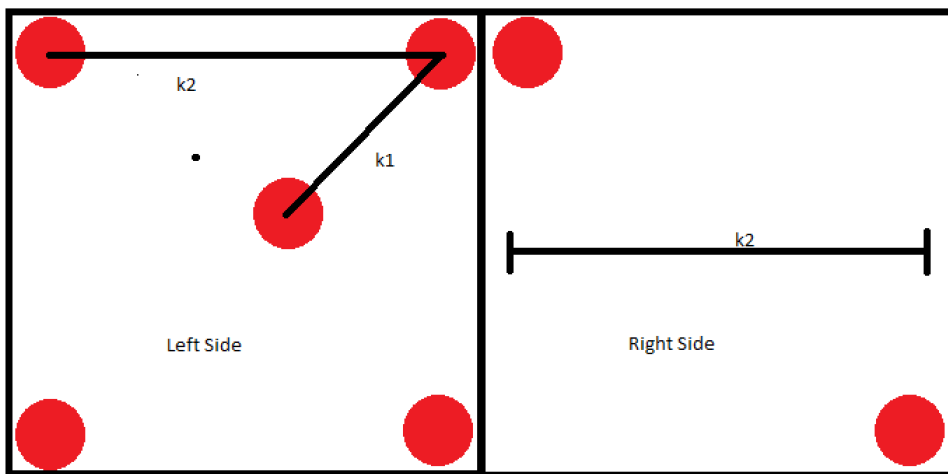
Let's say, the distances returned by left side is k_1, k_2 , where $k_1 < k_2$ and the distances returned by right side are k_3, k_4 , where $k_3 < k_4$.

Case 1: if k_1 is the minimum distance and k_2 is the second minimum value then

There is only one pair in left side whose distance is less than k_2 .

All the pair distances in the right side are greater than k_2 .

So, for a point common in left side and the strip,



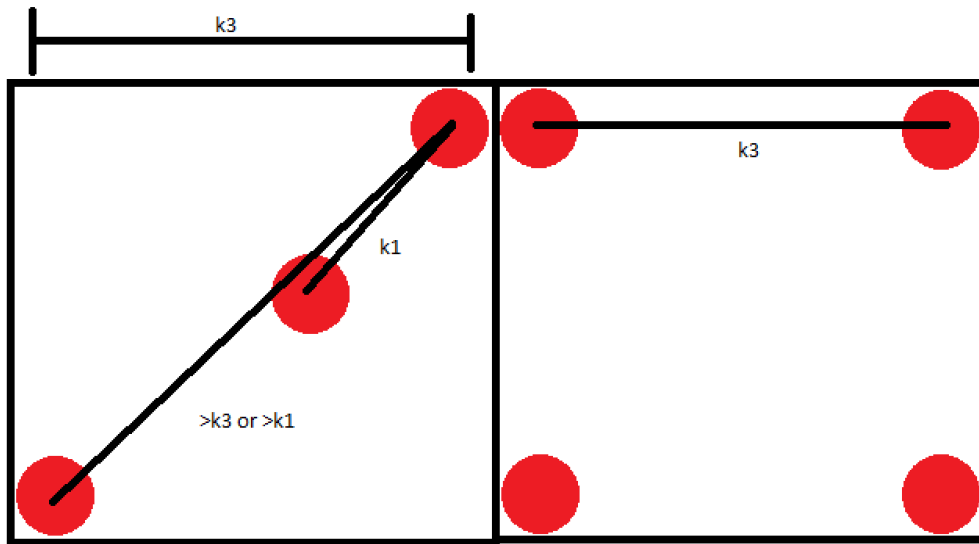
At most 7 points, 5 points on the left, and 2 on the right.

The same is valid for 2 smallest distances on the right side.

Case 2: if k_1 is the minimum and k_3 is the second minimum.

There is only one pair in left side whose distance is k_1 .

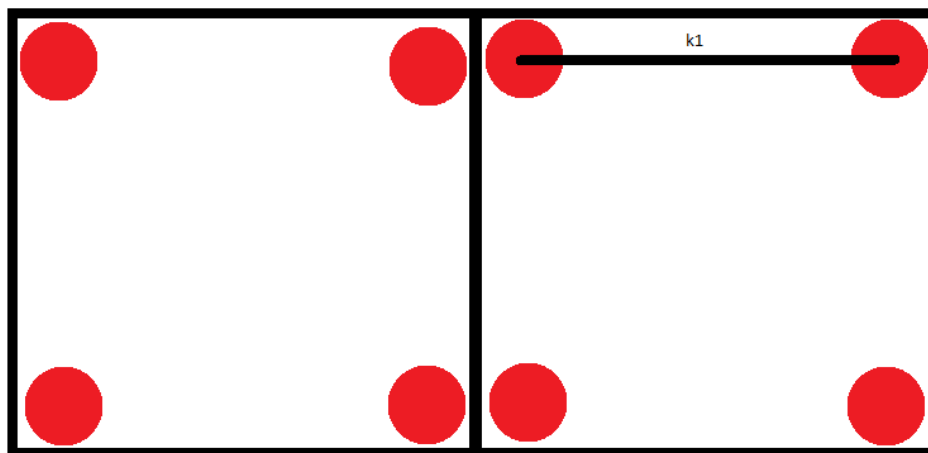
No pair distance of k_3 exist in the left side.



At most 7 points, 3 points on the left and 4 on the right.

The same also valid if k_1, k_2 is on the right and k_3, k_4 on the left.

Case 3: if k_1 and k_3 are equal.



Also at most 7 points.

Lines 155-159 takes $\Theta(1)$.

So, Total time complexity , $T(n) = \Theta(1) + 2T(n/2) + \Theta(n) + \Theta(n) + \Theta(n) + \Theta(1)$

or, $T(n) = 2T(n/2) + \Theta(n)$

Using Master method, $a = 2, b = 2, f(n) = \Theta(n)$, $n^{\log_2 2} = n$

So, $T(n) = \Theta(n \log n)$