

Page fault

$$EAT = (1-p) \times \text{mem. access time} + p \times \text{Pg. fault overhead}$$

↓
swap out
swap in
relatching with

$0 < p < 1 \leftarrow$ pg. fault for every reference
 $\uparrow \quad \uparrow$
 no pg. fault probability of occurrence of
 pg. fault

$p = 0.6$
 \downarrow
 fault \rightarrow hard disk (ms)

$(1-p) = 0.4$
 \hookrightarrow hit \rightarrow M.M
 \downarrow
 ms/ns

Ex. :- mem. access time = 200 ns
avg. pg. fault overhead = 8 ms
if 1 access out of 1000 causes pg. fault

$$p = \frac{1}{1000} = 0.001$$

$$EAT = (1 - \frac{0.001}{1000}) \times 200 \frac{\eta s}{\times 10^{-9}} + (0.001) \times 8m \times 10^3$$

$$E_{AT} = 82 \mu A$$

FIFO — process — 8 pages — 4 frames

→ ref. string

1	2	3	4	2	5	6	2	1	2	3	7	6	3	2	1	2	3	6
1	1	1	1*		5	5	5	5*		3	3	3		3*	1		3	
	2	2	2		2*	6	6	6		6*	7	7		7	7*		3	
		3	3		3	3*	2	2		2	2*	6		6	6		6*	
			4		4	4	4	1		1	1	1*		2	2		2	

$$H_i K = 6$$

$$\text{faults} = 20 - 6 = 14$$

$$\text{Pg. fault ratio} = \frac{14}{20} \times 100 = 70\%$$

Optimal pg. replacement —

+ future pg. references

* replace the page that is not used for the longest period of time

1	2	3	4	2	1	5	6	2	1	2	3	7	6	3	2	①	2	3	6
1	1	1	1			1	1					7				1			
	2	2	2			2	2					2				2			
		3	3			3	3					3				3			
			4			5	6					6				6			

$$H_i K = 12$$

$$\text{faults} = 20 - 12 = 8$$

$$\text{Pg. fault ratio} = \frac{8}{20} \times 100 = 40\%$$

* difficult to implement
* to predict

Least Recently used (LRU)

1 2 ③ 4 2 1 5 6 2 1 2 3 7 6 3 2 1 2 3 6

↓

1	1	1	1			1	1				1	1	6			6		
	2	2	2			2	2				2	2	2			2		
		3	3			5	5				3	3	3			3		
			4			4	6				6	7	7			1		
				✓	✓			✓	✓	✓				✓	✓		✓	✓

hits = 10 = faults

pg. fault ratio = $\frac{10}{20} \times 100 = 50\%$

LRU ← Stack
Counter

1 2 3 4 2 1 ⑤ 6 2 1 2 3 7 6 3 2 1 2 3 6

✓

1	2	3	4	2	1	5	6	2	1	2	3	7	6	3	2	1		
	1	2	3	4	2	1	5	6	2	1	2	3	7	6	3	2		
		1	2	3	4	2	1	5	6	6	1	2	3	7	6	3		
			1	2	3	4	2	1	5	5	6	1	2	2	7	6		
				1	1	3	4	2	1	5	5	6	1	2	2	7	6	
																	✓	✓
																	✓	✓

hits = 10 = faults

Counters — pg.
1
2
3
4
5

Counter 2 bit — 0, 1, 2, 3
x 2 3 4 7
x 2 3 4
x 2 3
x 2
1

