

Discrete Mathematical Structures (CS330)

nowledge of the concepts needed to test the

Course Outcomes

Course

Outcomes

logic of the program.

CO2 : Demonstrate the understanding of relations and

able to determine the properties.

CO3 : Perceive, construct and decode group codes

ties.

based on the various methods.

CO4 : Demonstrate different traversal methods for



Course Contents

Fundamental of Logic: Basic Connectives and Truth Tables, Logical Equivalence: The Laws of Logic, Logical Implication: Rules of Inference, The Use of Quantifiers, Quantifiers, Definitions and the Proofs of Theorems.

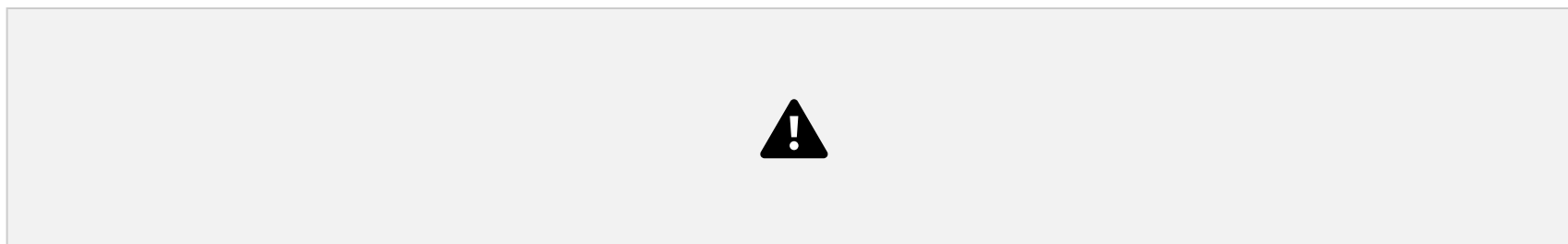
08

	Relations: Properties of relations, Computer Recognition: Zeros-One Matrices and Directed Graphs, Partial; orders: Hasse diagrams , Equivalence Relations and Partitions , Lattices.	08
	Elements of coding theory and Hamming Metric, generation of codes using Parity check and Generator matrices.	08
	Graph theory: Definitions and Examples, Subgraphs, Complements, and Graph Isomorphism, Vertex degree, Euler trail and circuits, Planar Graphs, Hamiltonian Paths and cycles.	08
	Trees: Definitions, Properties and Examples, Rooted trees, trees and sorting weighted trees and prefix Codes.	07



Text and Reference Books

- 1.

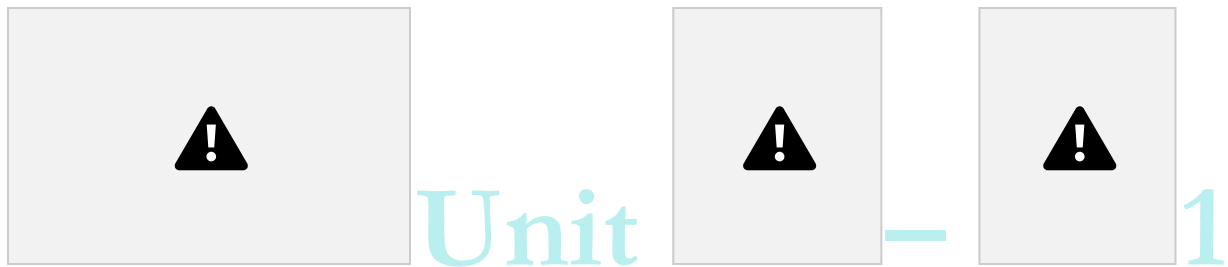
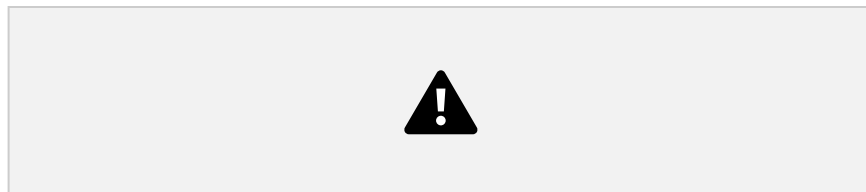
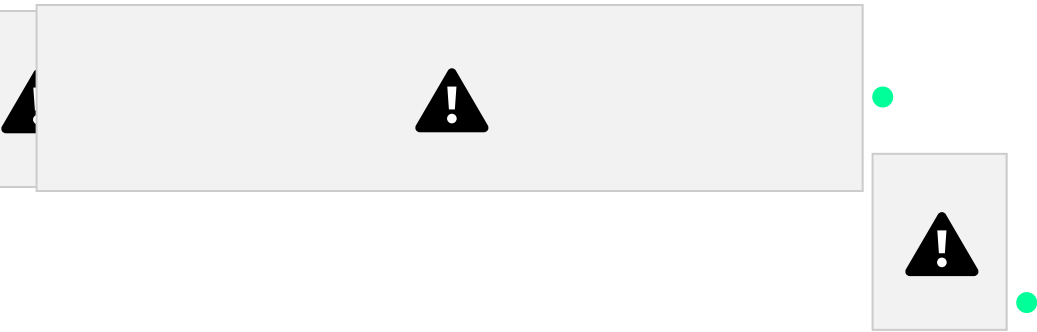


What is Discrete Mathematics?



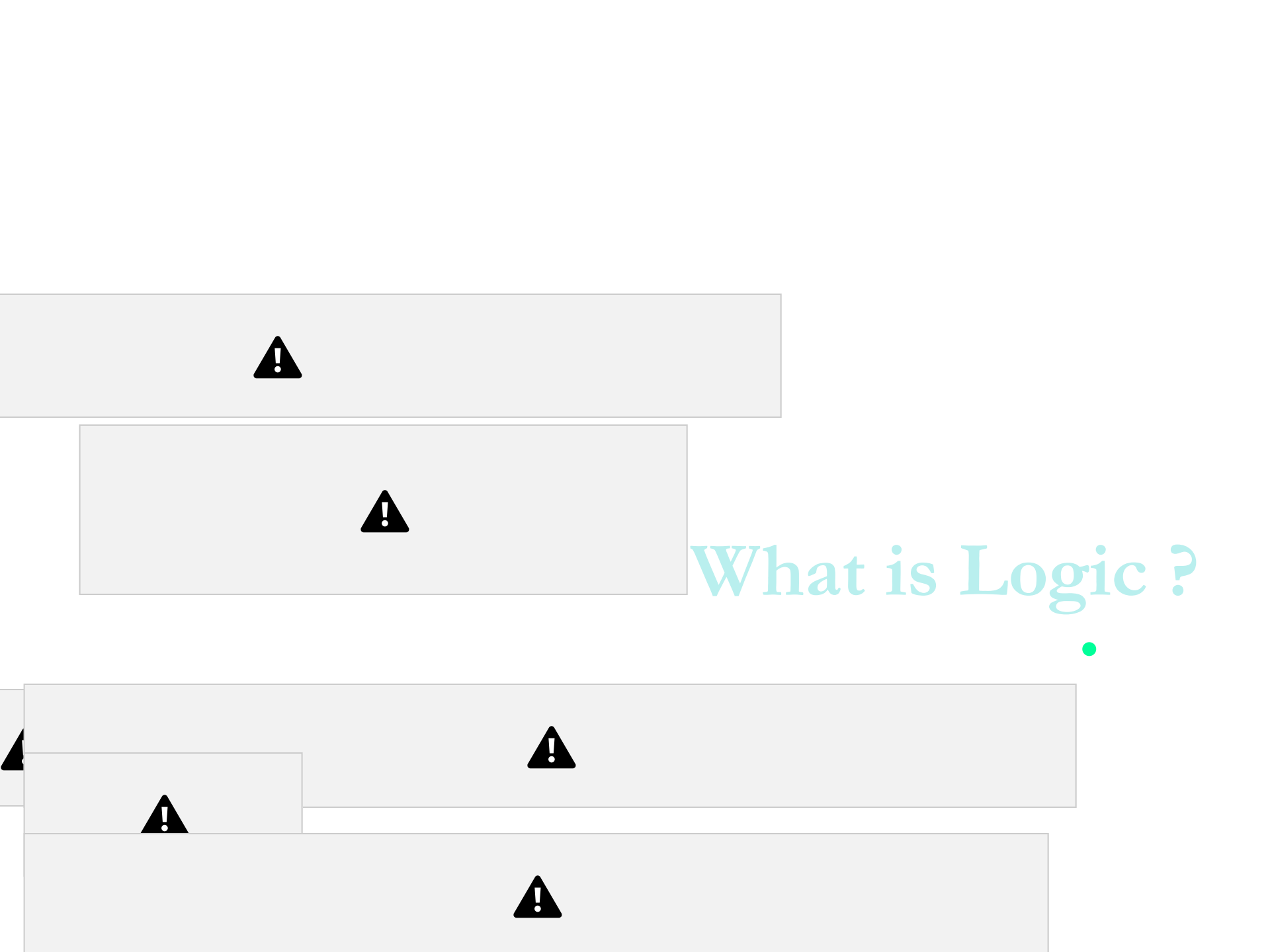
Applications of Discrete Mathematics •







Fundamentals of Logic

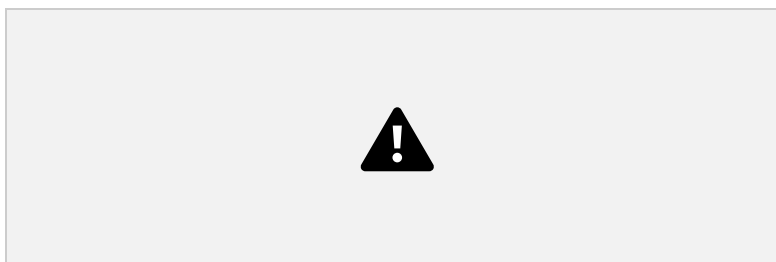
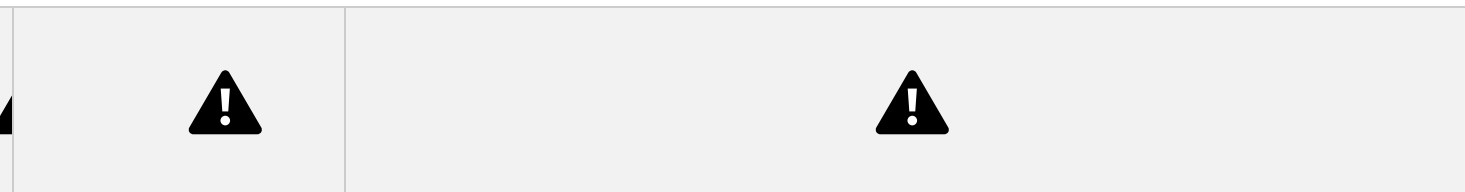


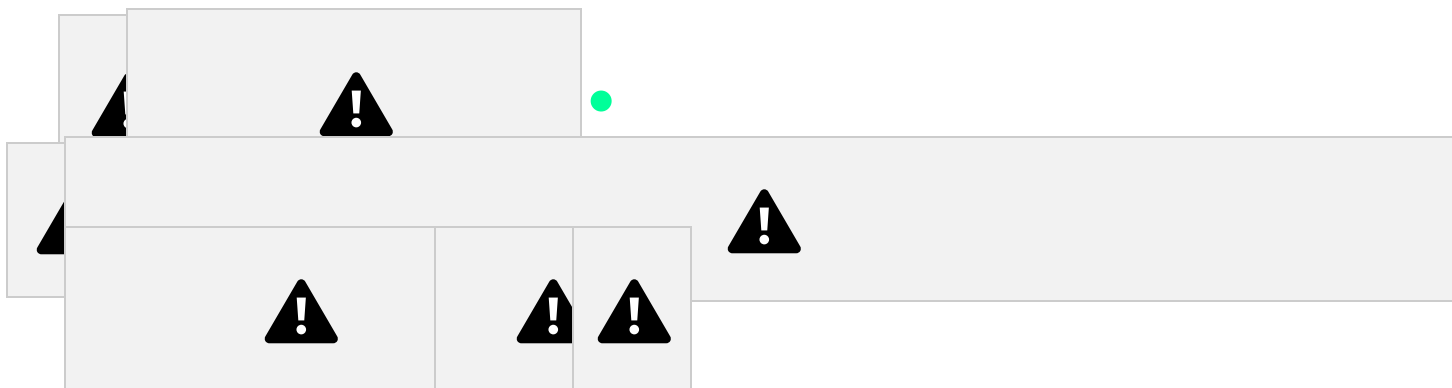
What is Logic ?





for Artif





True

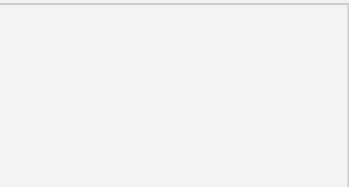
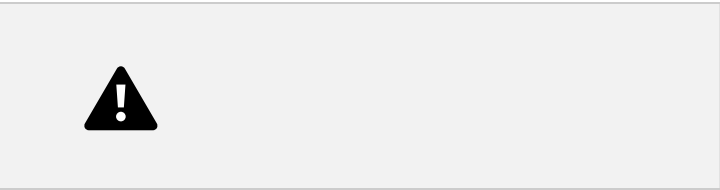
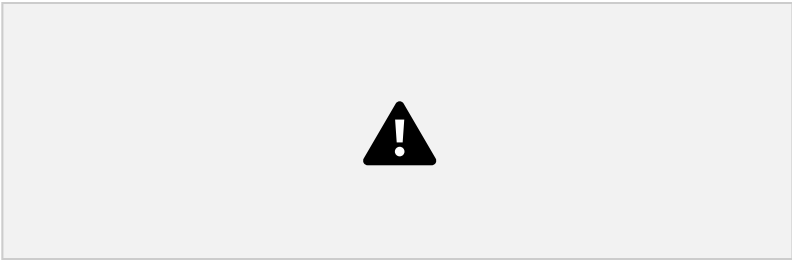


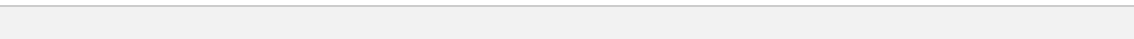
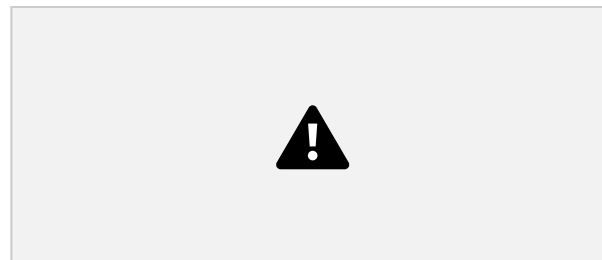
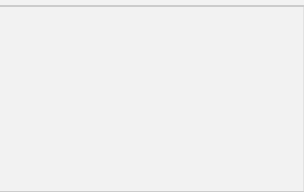
False



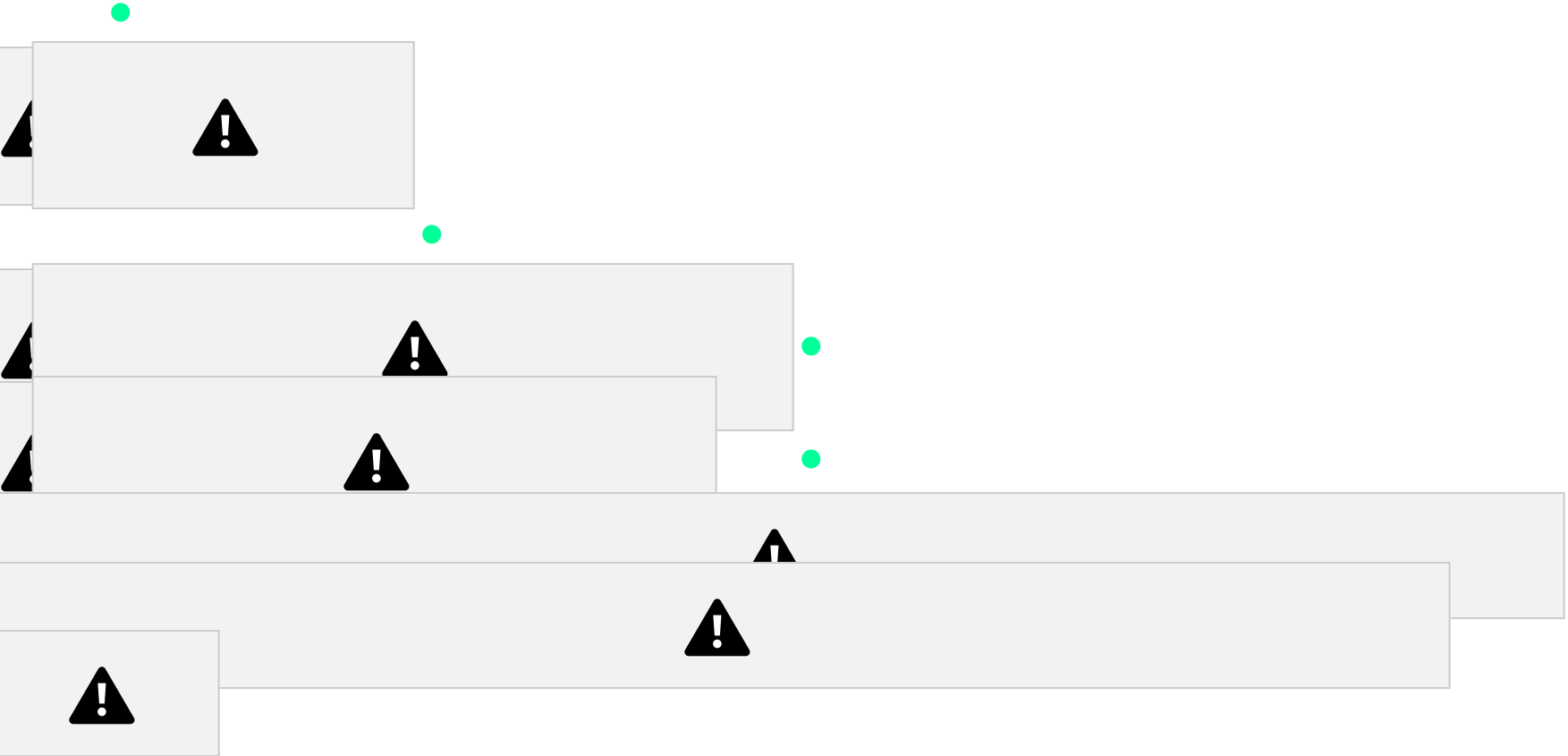


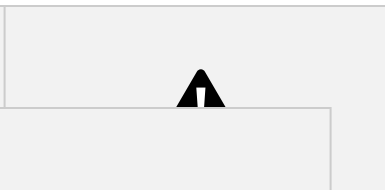
True or False



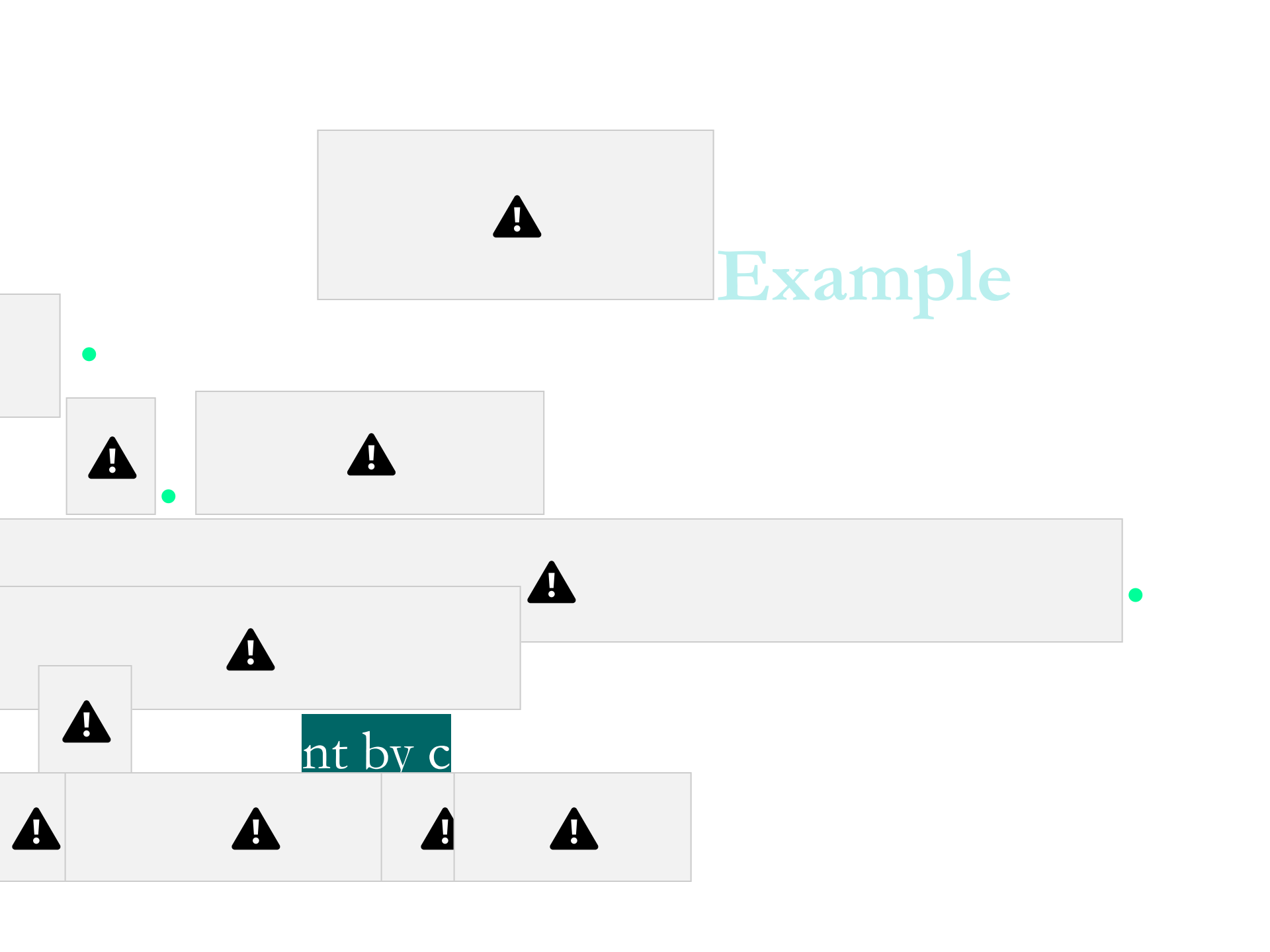


Example





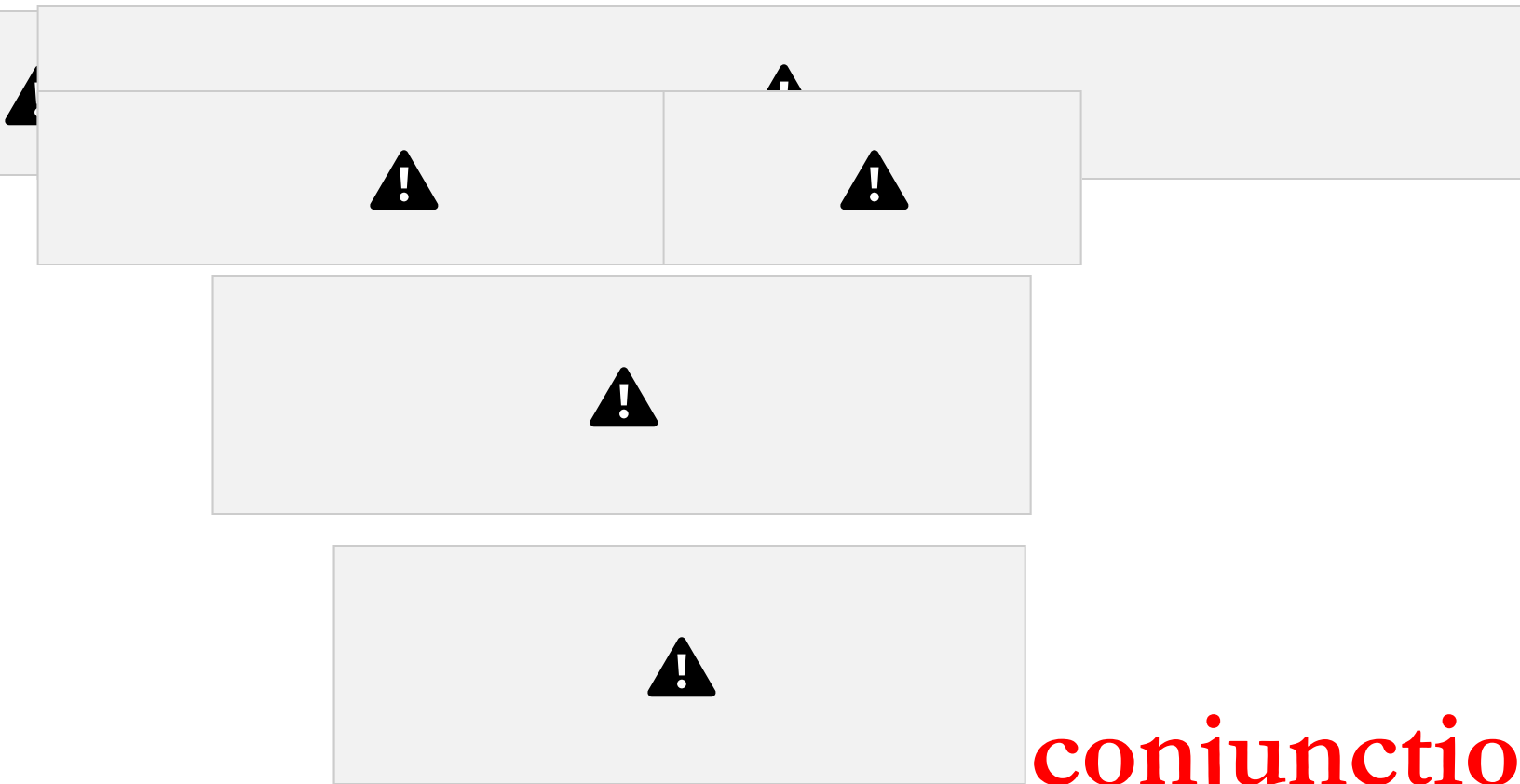




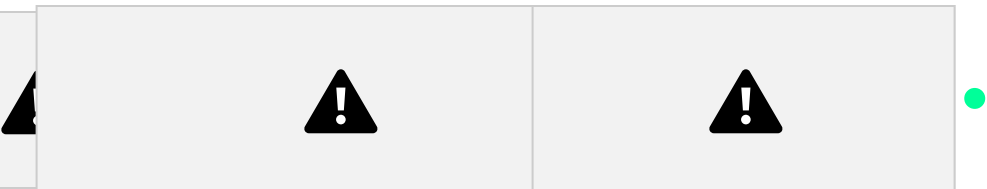
Example

nt by c

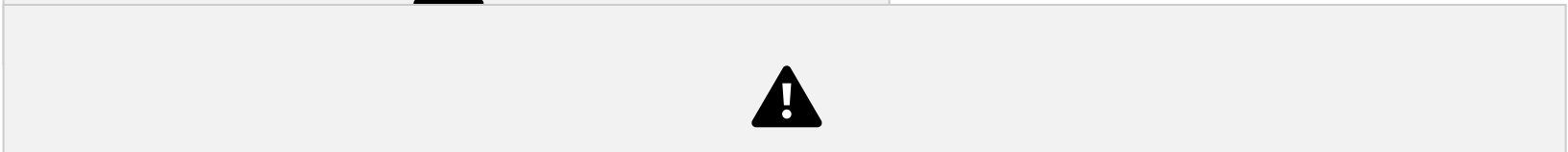
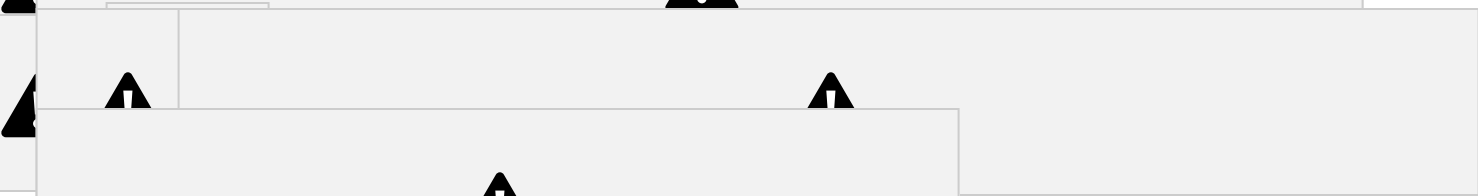
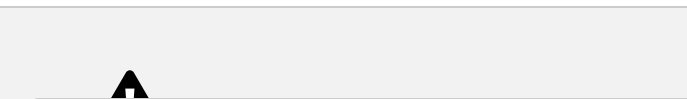
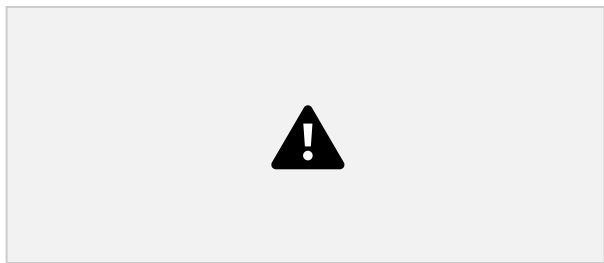




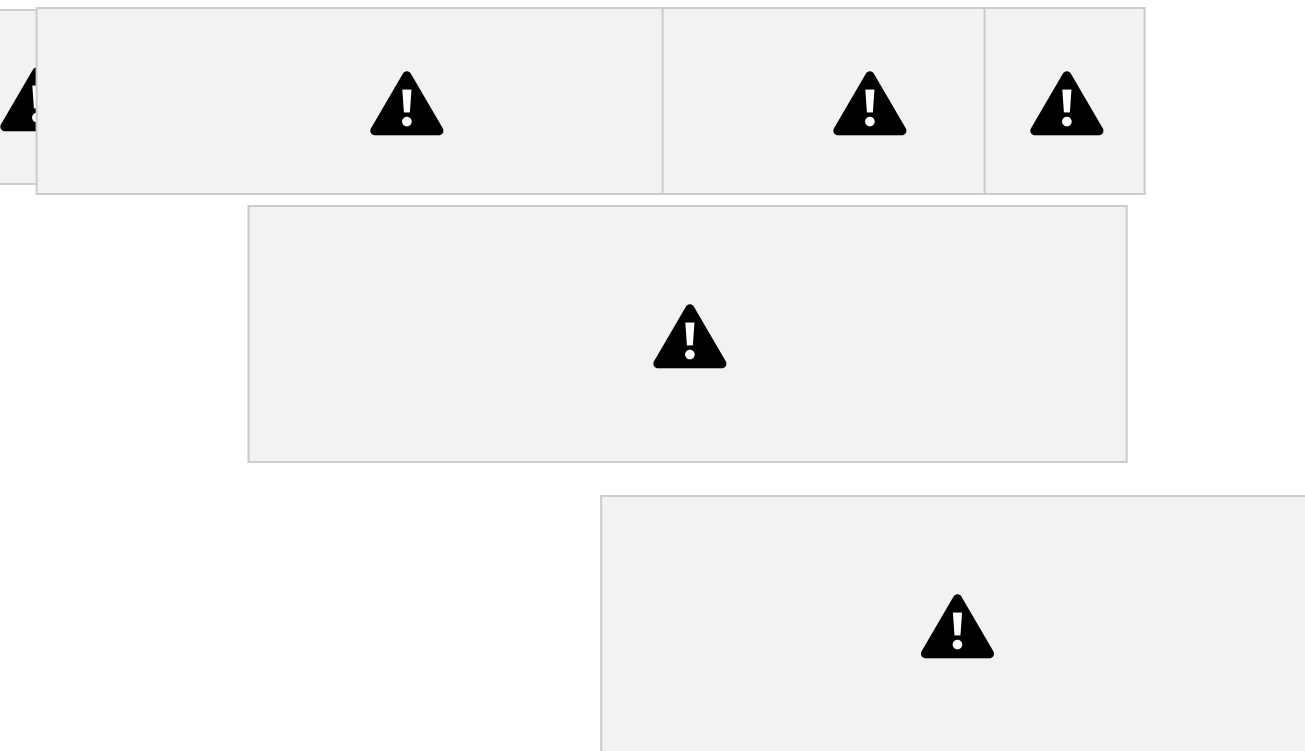
conjunction •



T







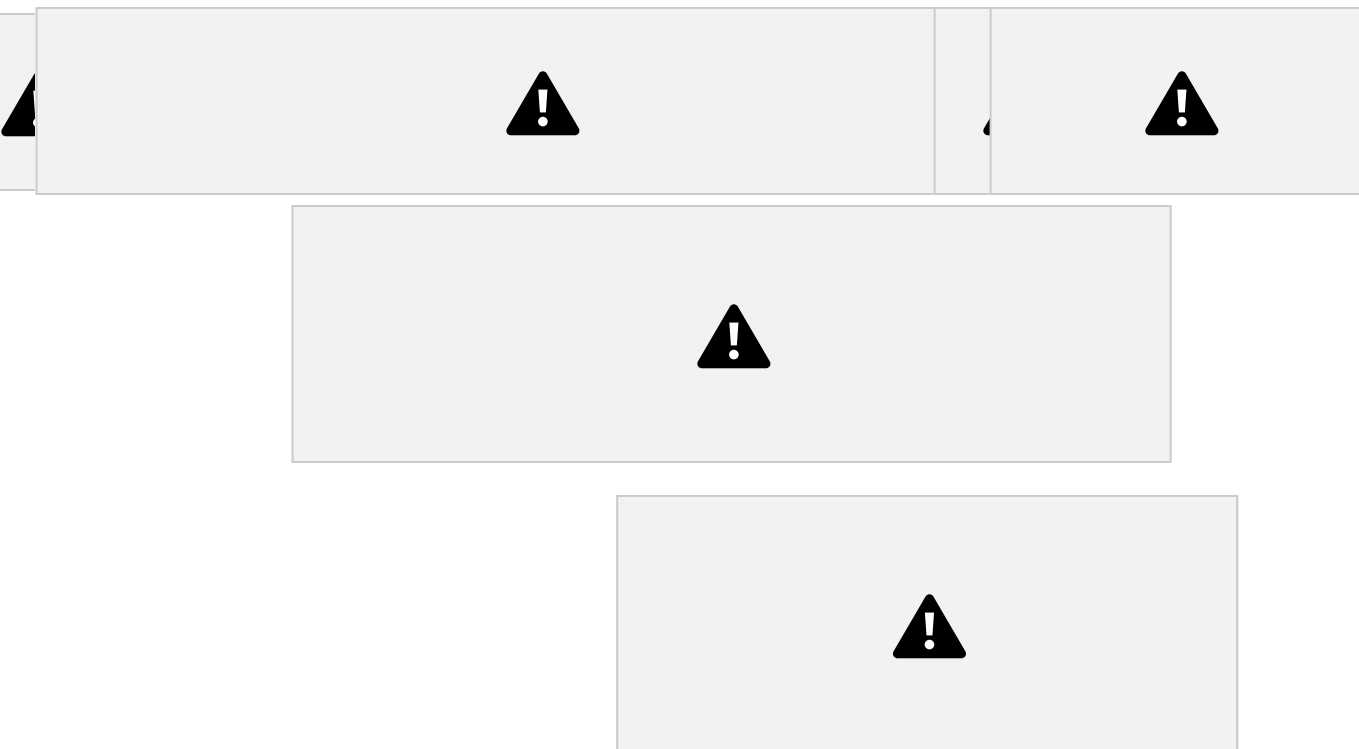
disjunction •

disjunction

F







Negation •

~

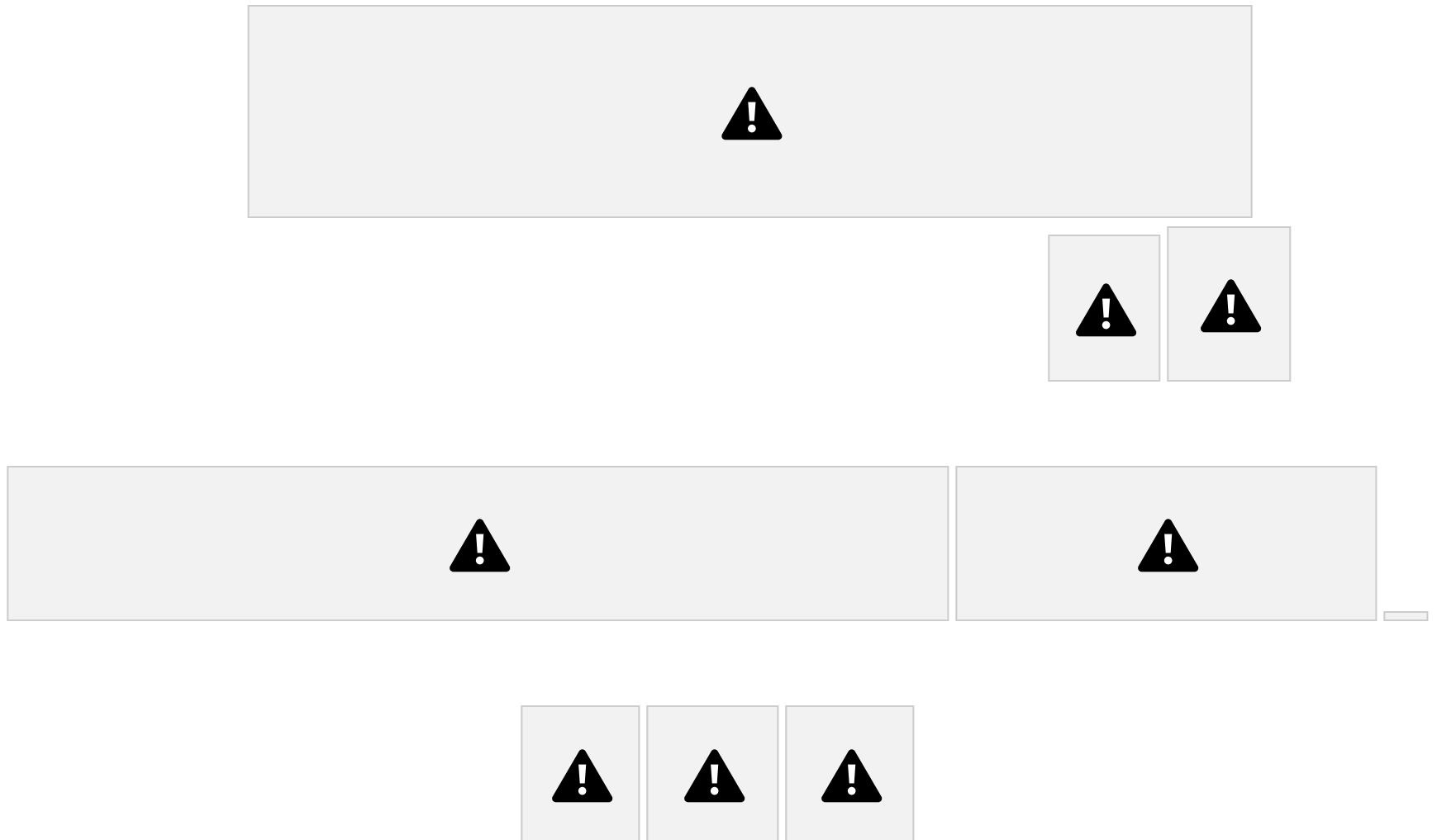




Negation Continued... •



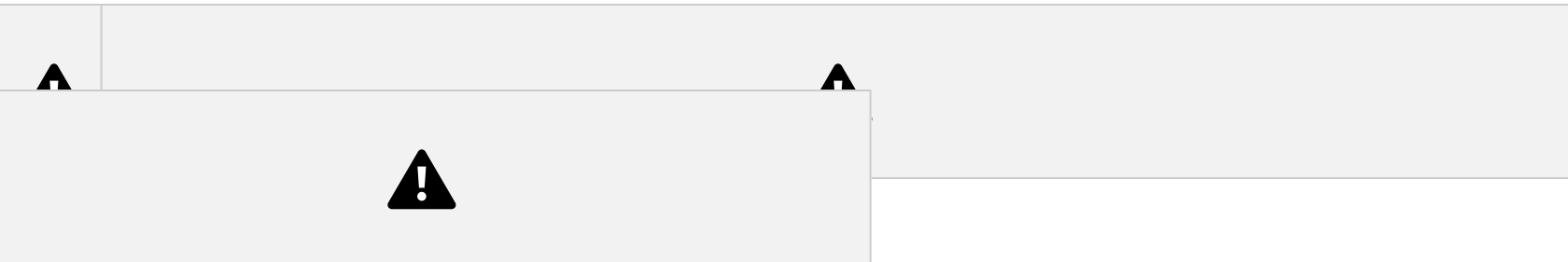




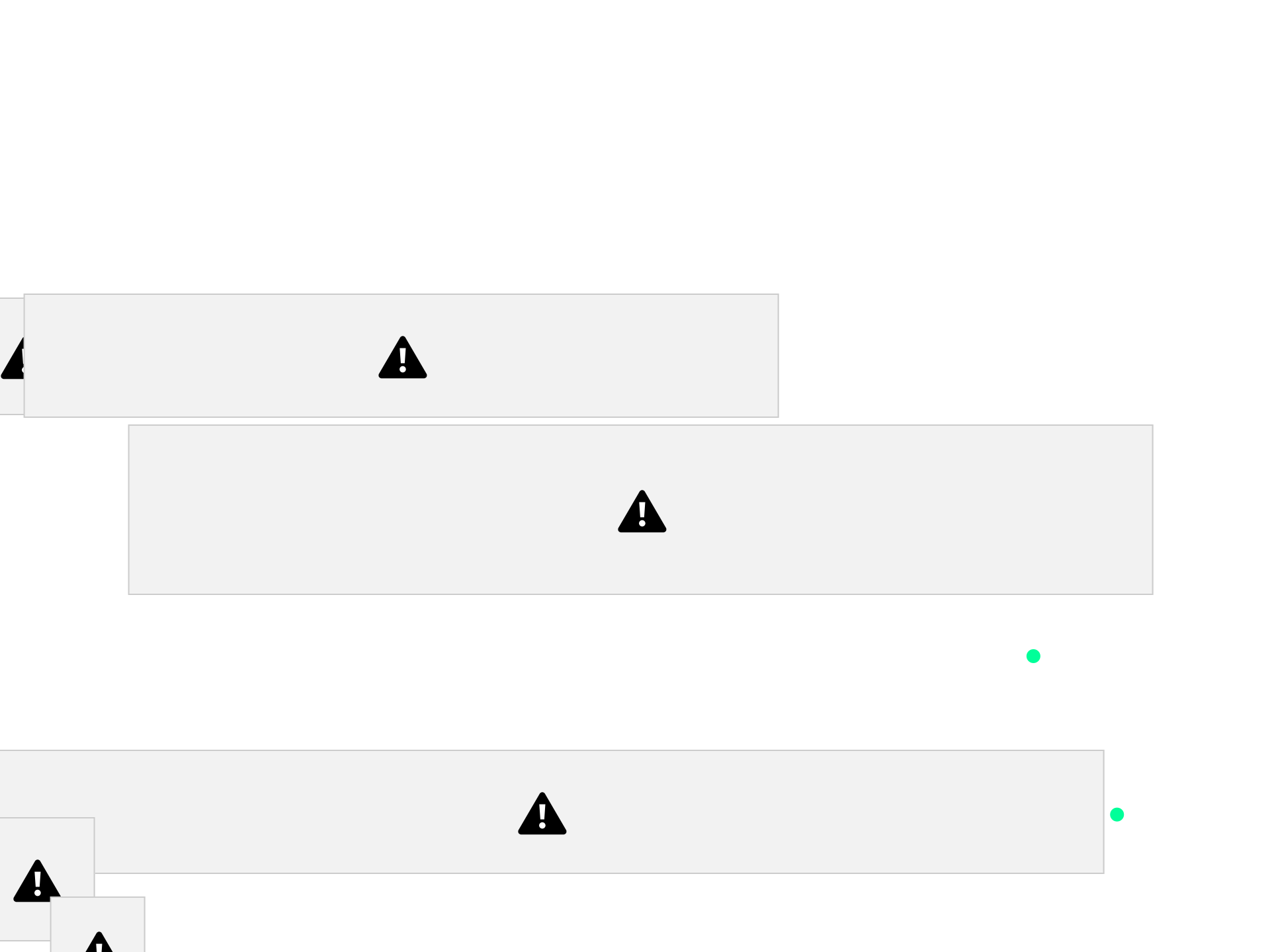
- Either P or Q' (but not both),

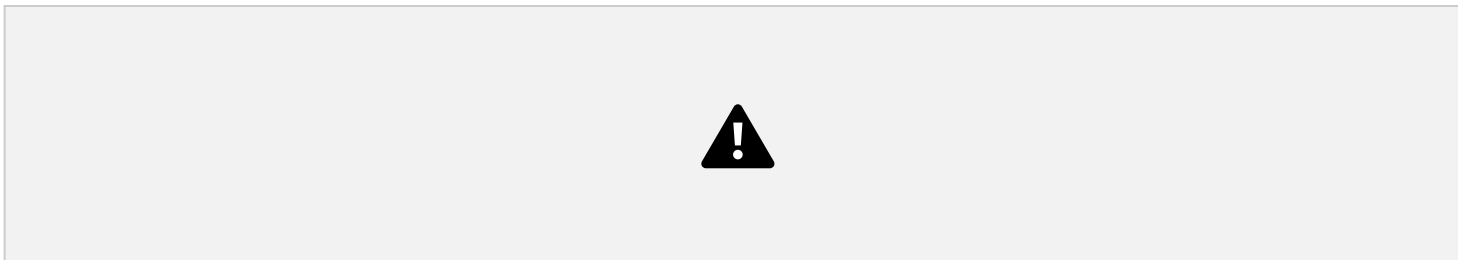
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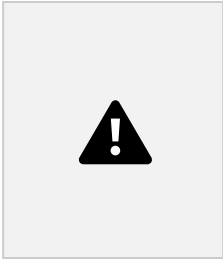
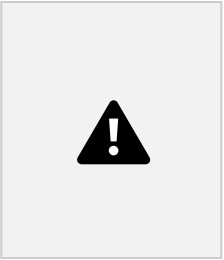
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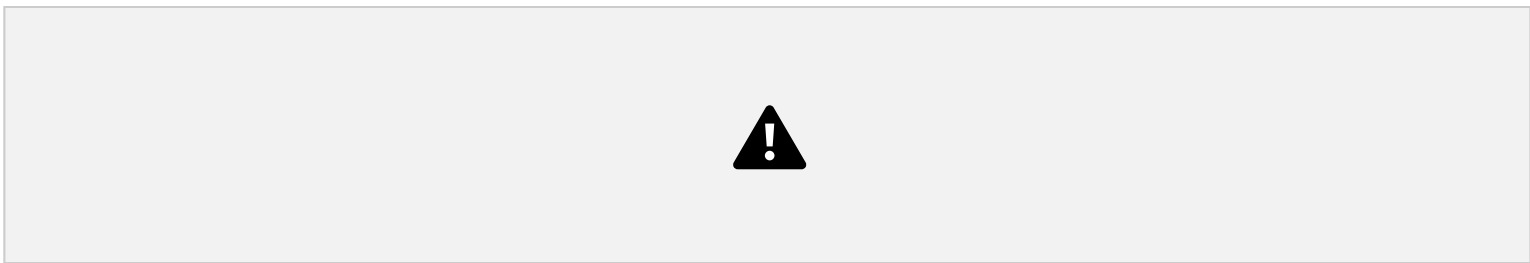
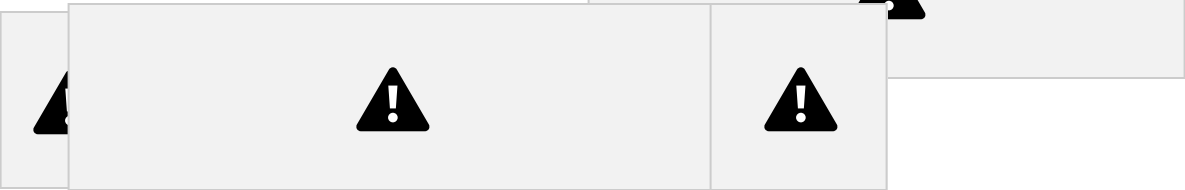
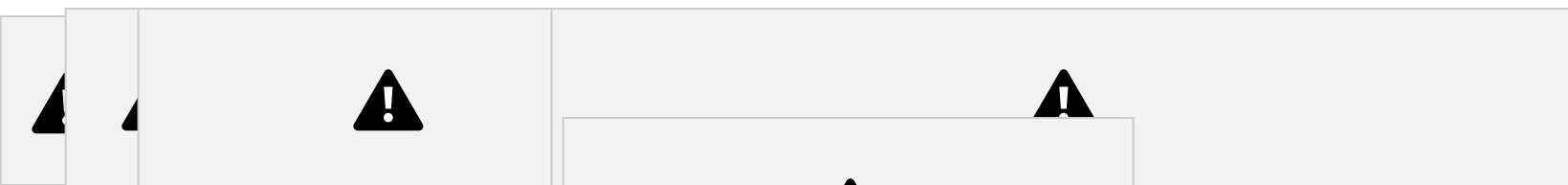


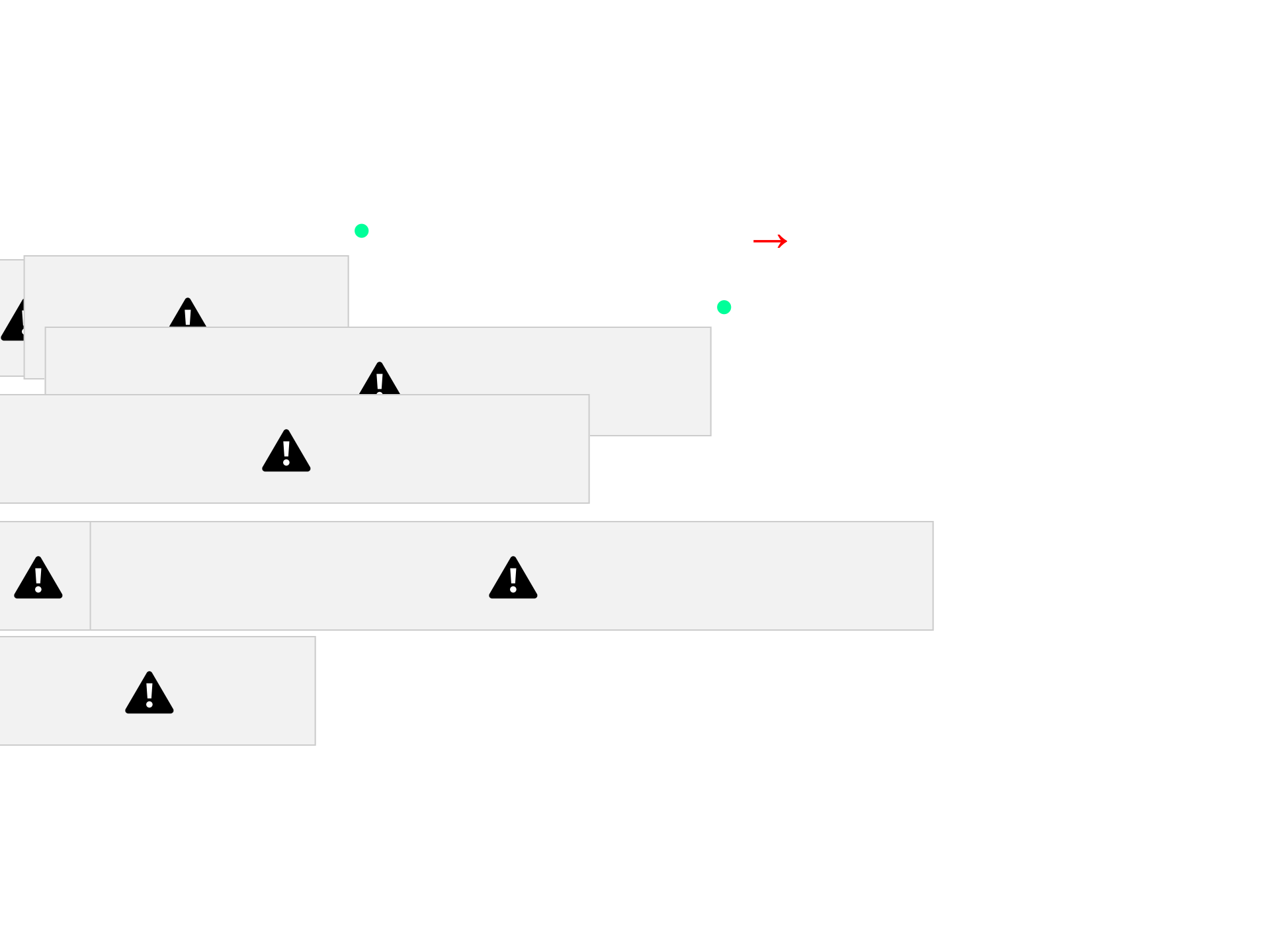


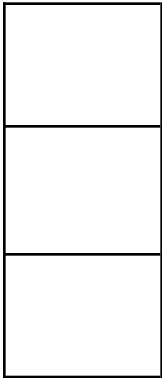
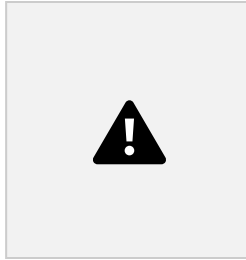
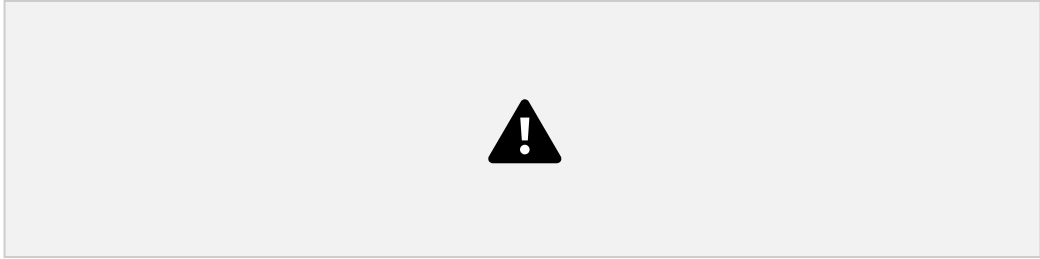






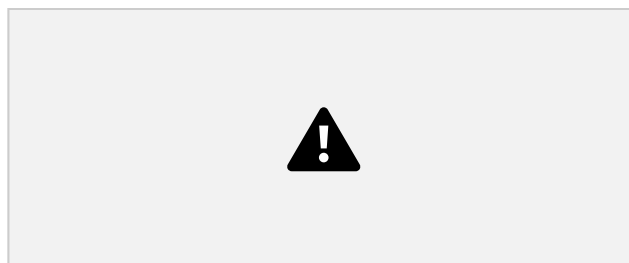
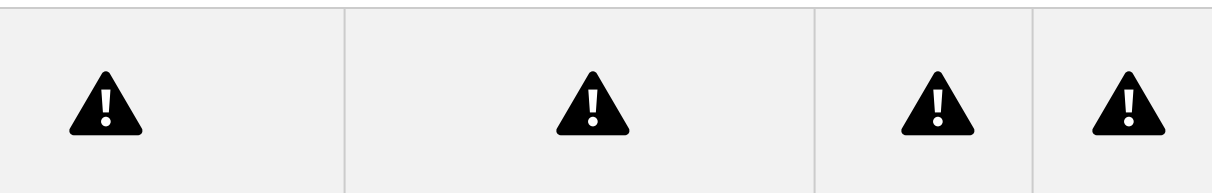




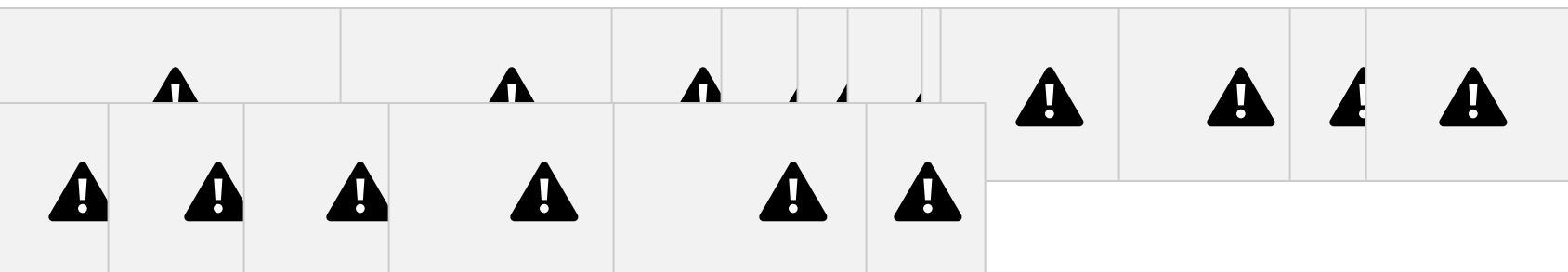


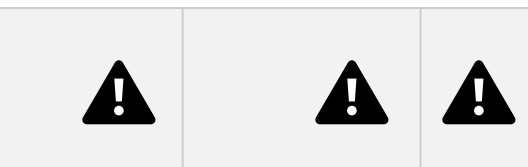
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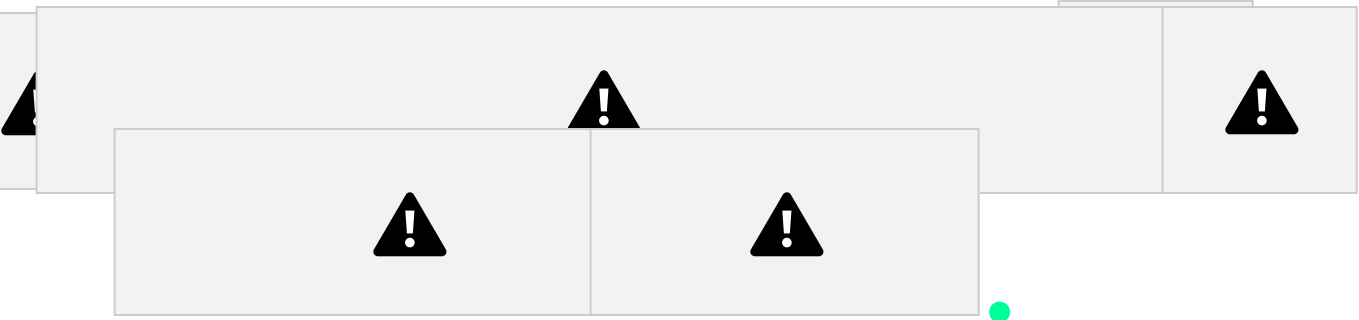
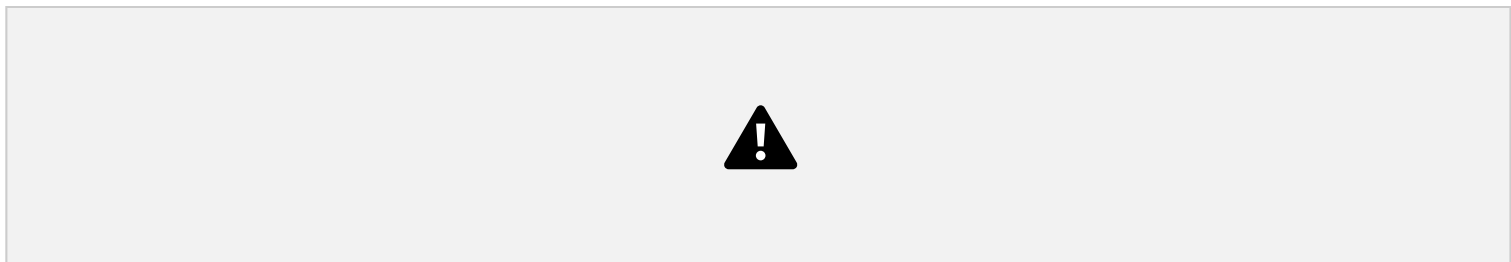


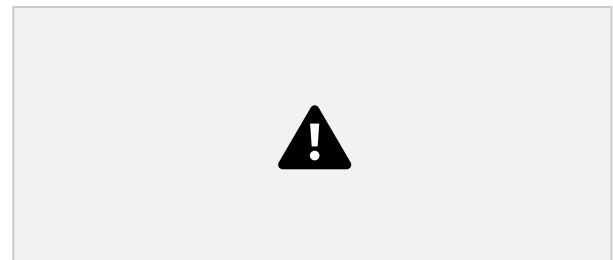
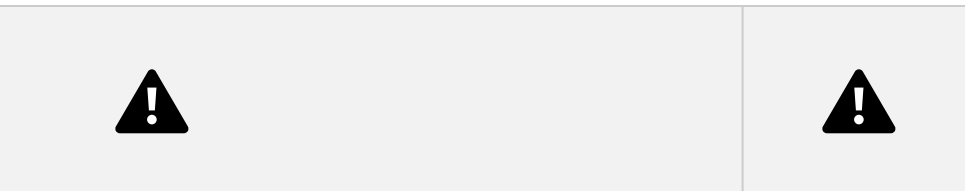


Example

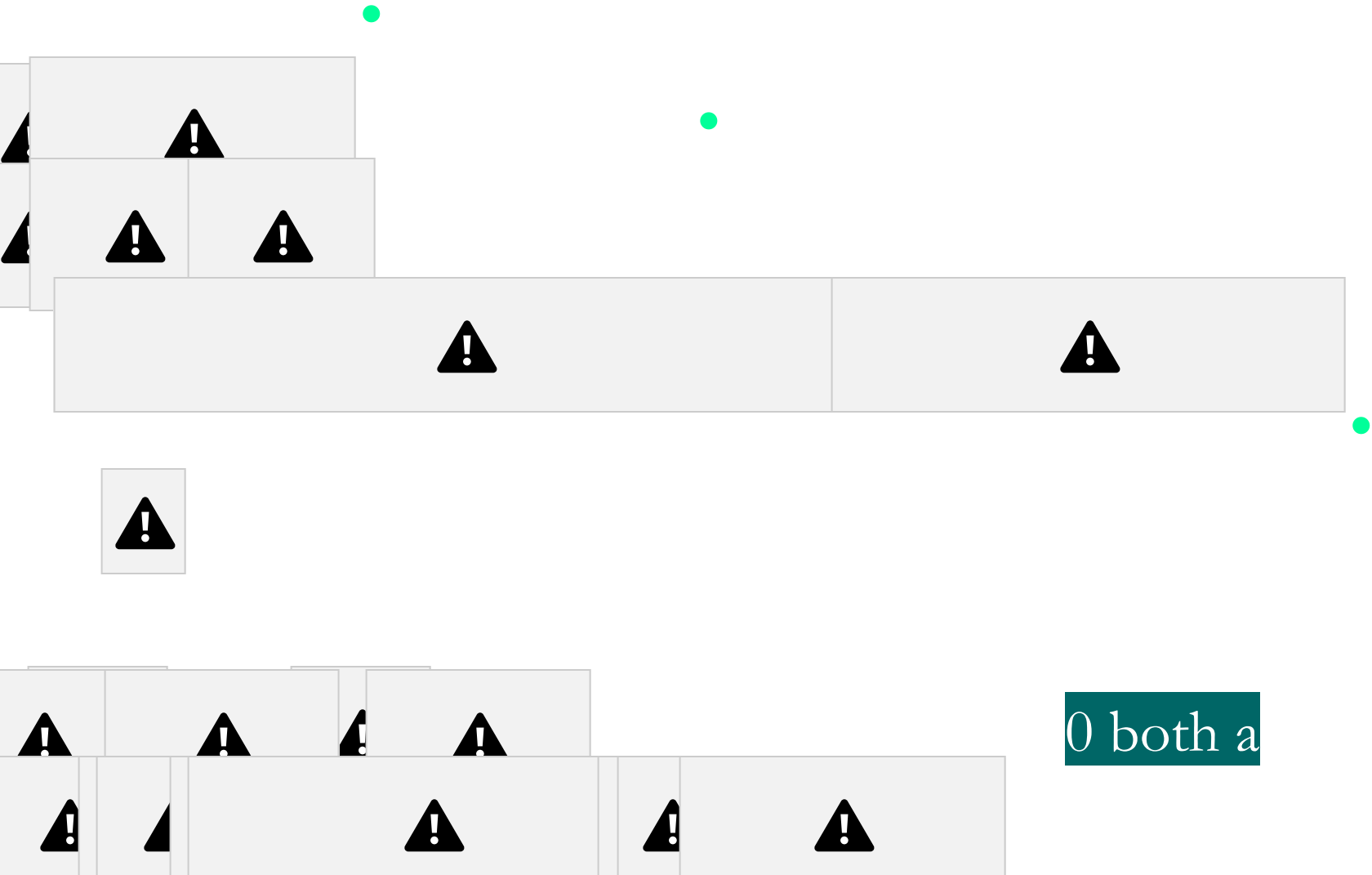


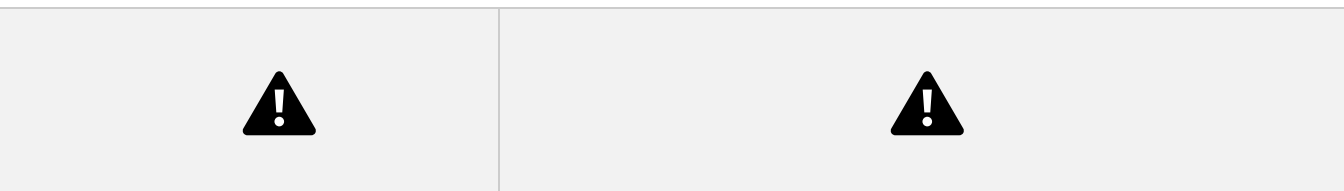
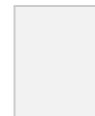


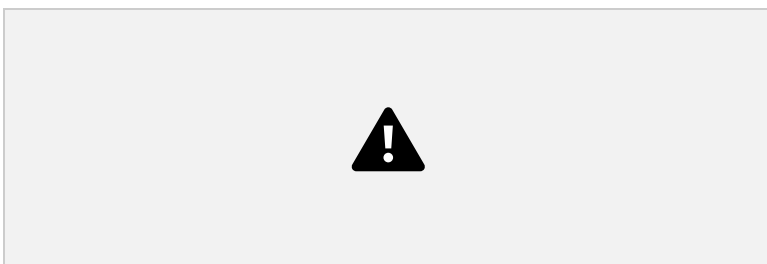
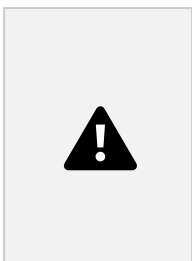




Example







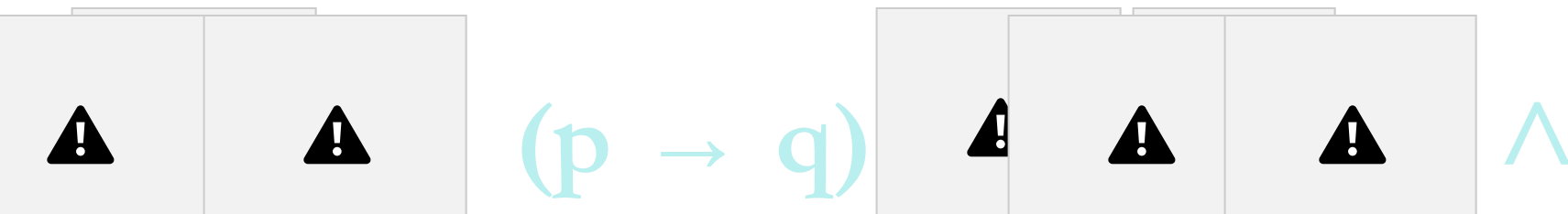






Exercise

Problems

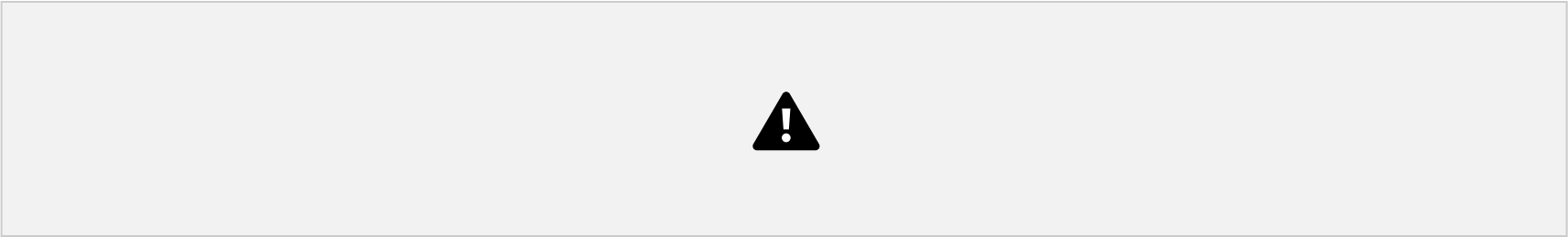




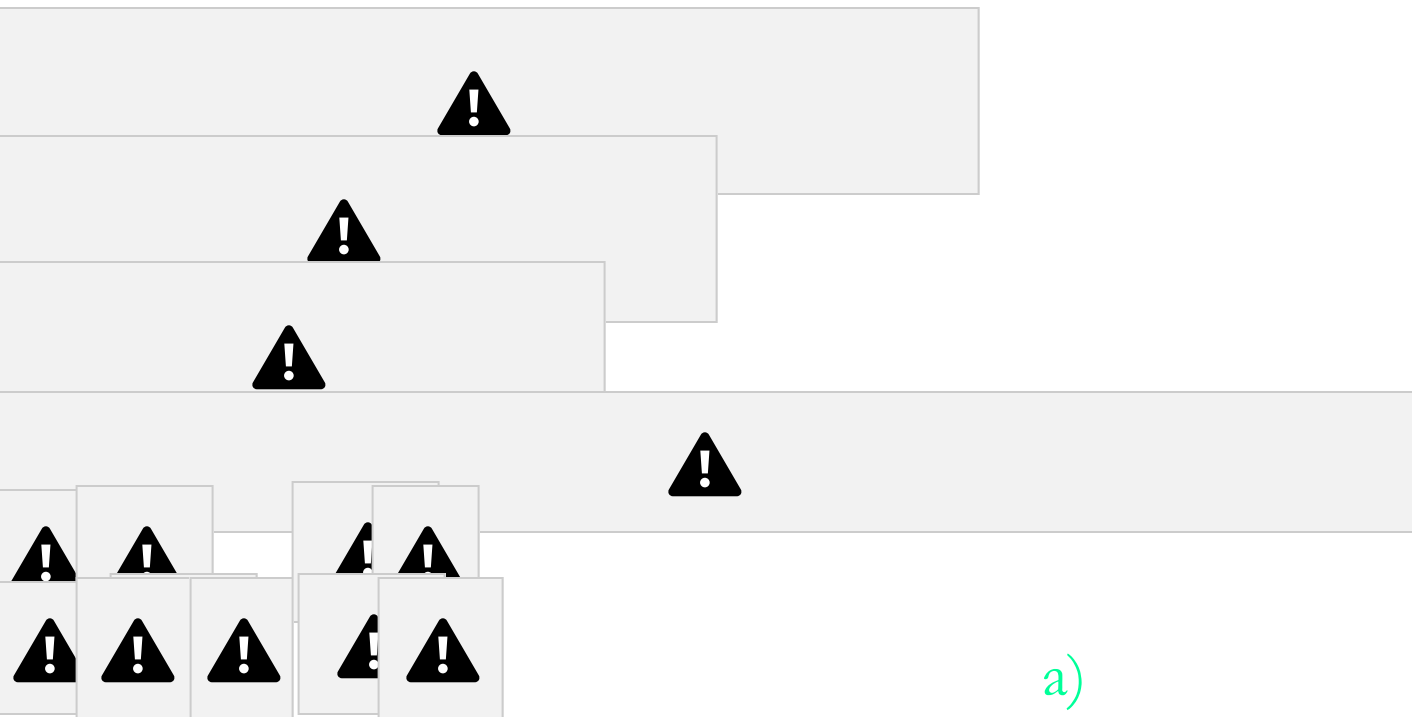
$$[(q \wedge \neg r) \rightarrow (p \vee r)]$$

p	q	r	$p \rightarrow q$ (a)	$q \wedge \neg r$	 $p \vee r$	$[(q \wedge \neg r) \rightarrow (p \vee r)]$ (b)	$a \wedge$  b
0	0	0	1	0	0	1	1
0	0	1	1	0	1	1	1
0	1	0	1	1	0	0	0
0	1	1	1	0	1	1	1
1	0	0	0	0	1	1	0
1	0	1	0	0	1	1	0

1	1	0	1	1	1	1	1
1	1	1	1	0	1	1	1



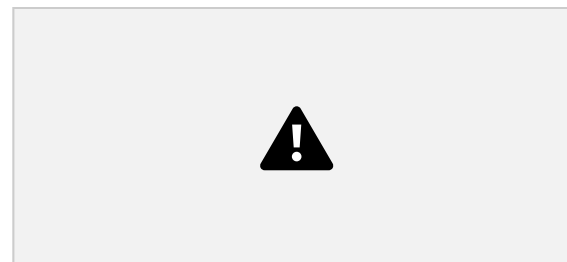
Exercise Problems continues...



a)

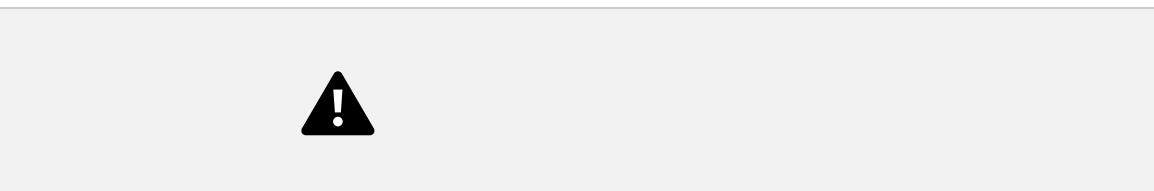
b)

c)



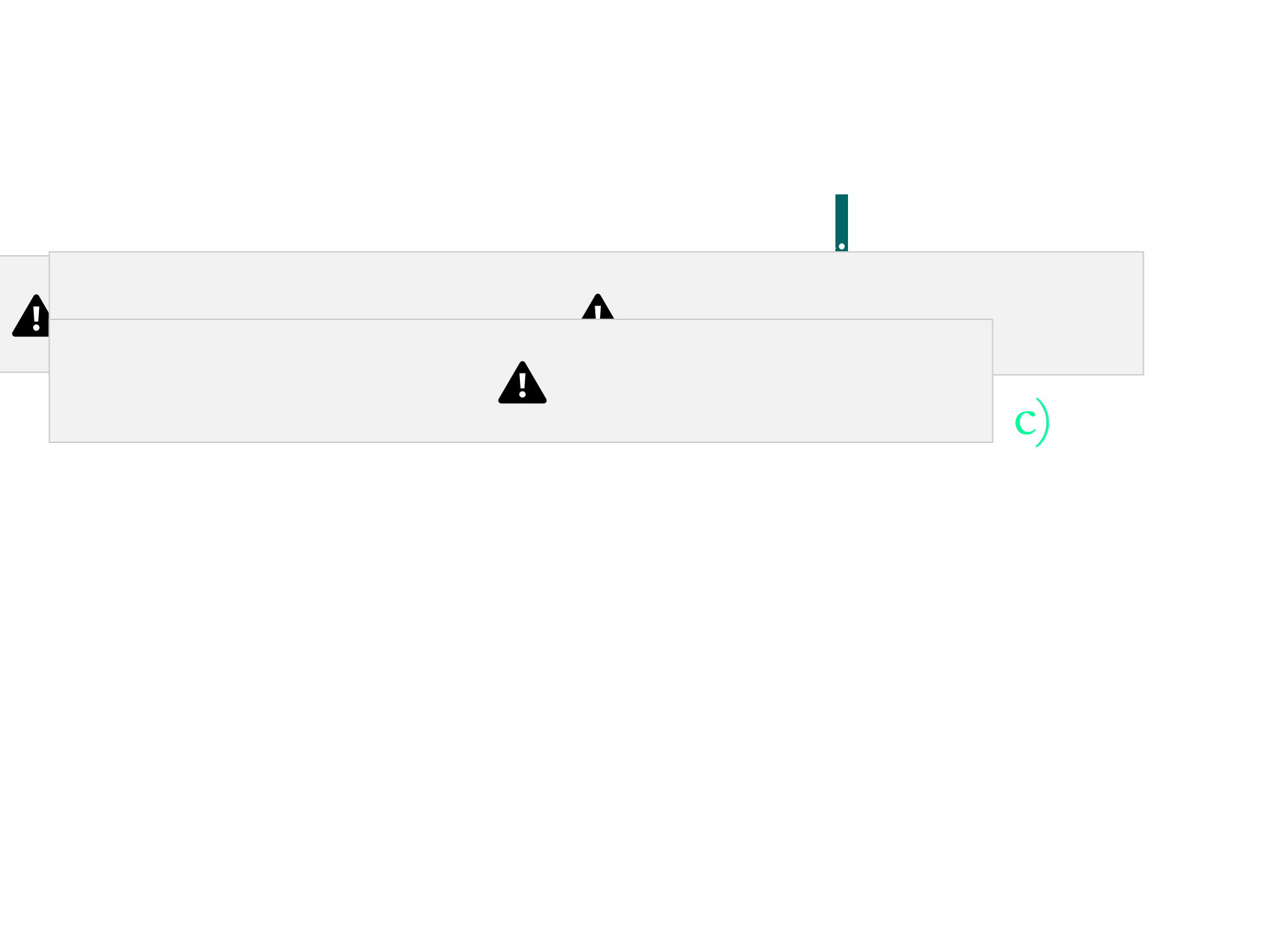
Solution

a)



b)







Exercise problems continues...



$s \leftrightarrow t$



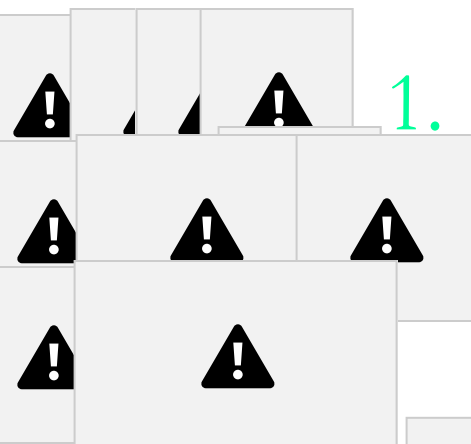
$u \wedge$

$\neg t \rightarrow \neg s$

$u \wedge s$



Exercise problems continues...



1.

2.

3.



4.





Exercise problems continues...

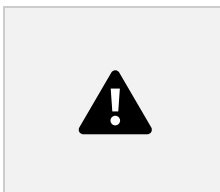
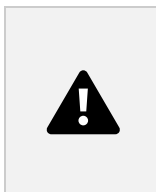
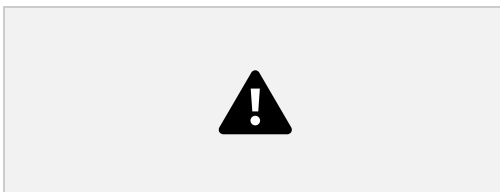
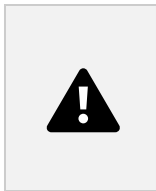




Exercise problems

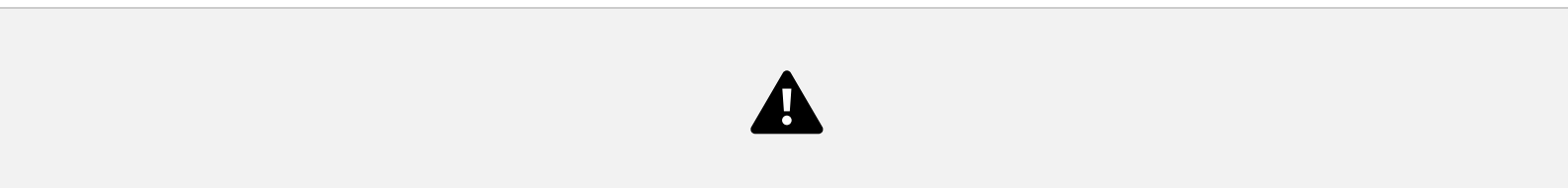
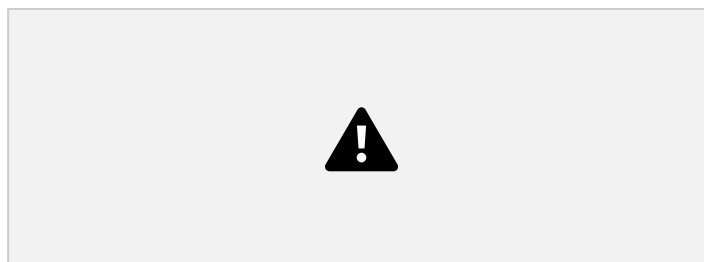
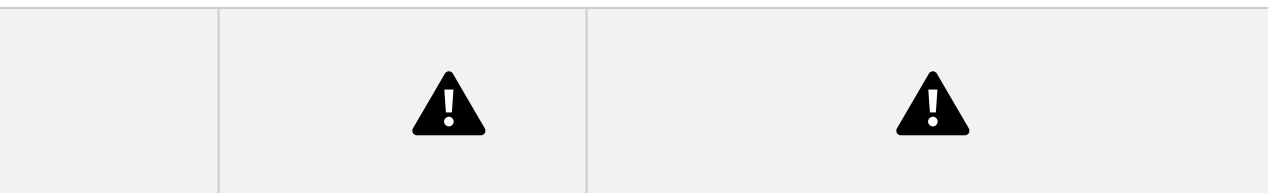
continues...





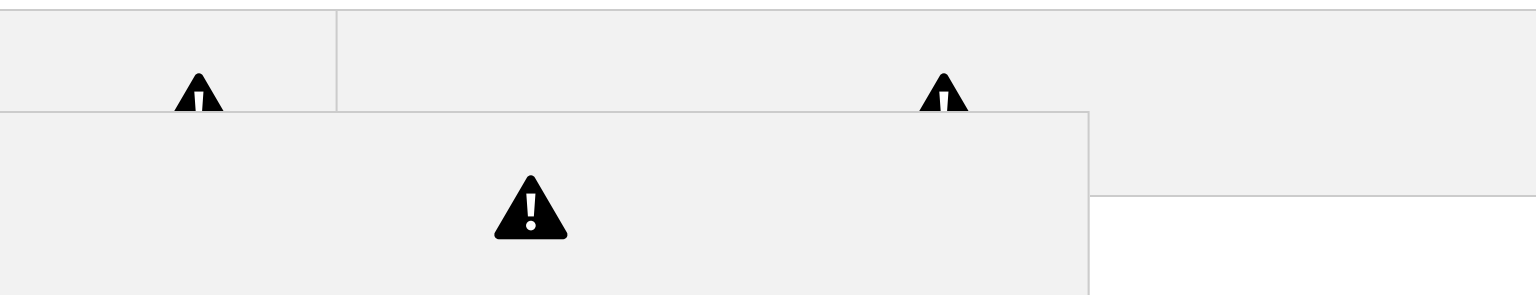
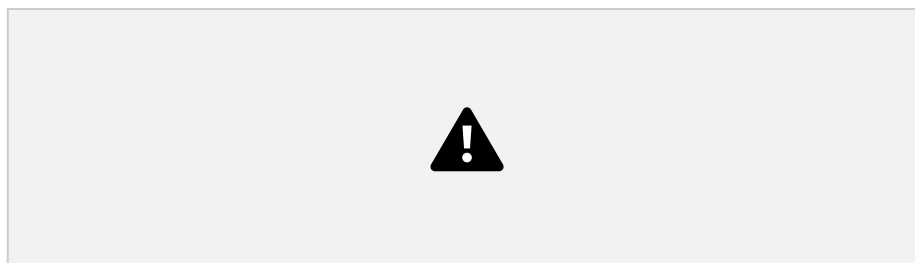






tautology

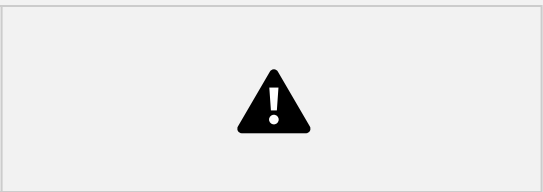
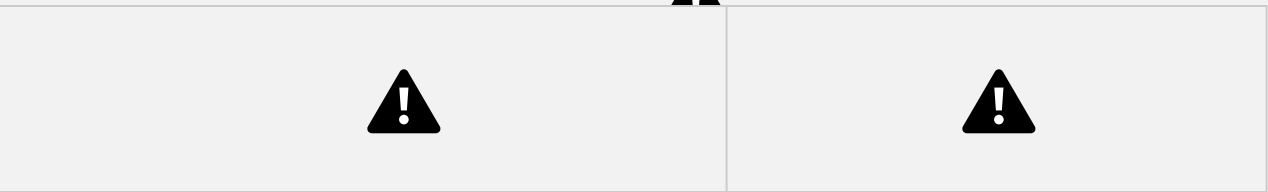
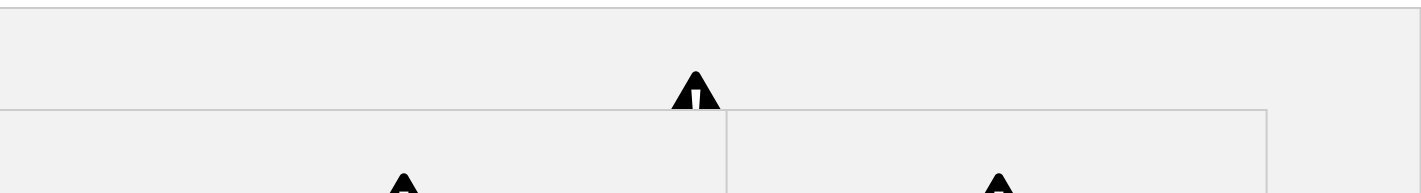
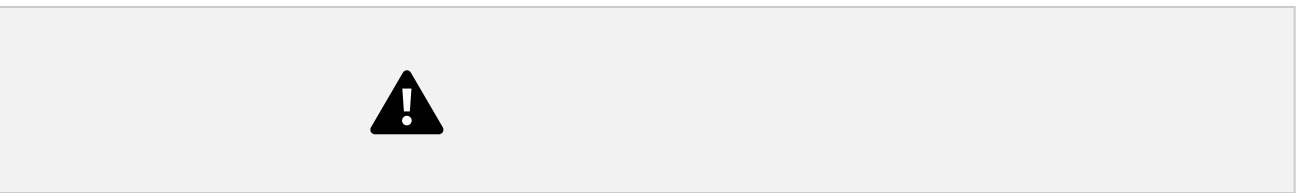




Contradiction

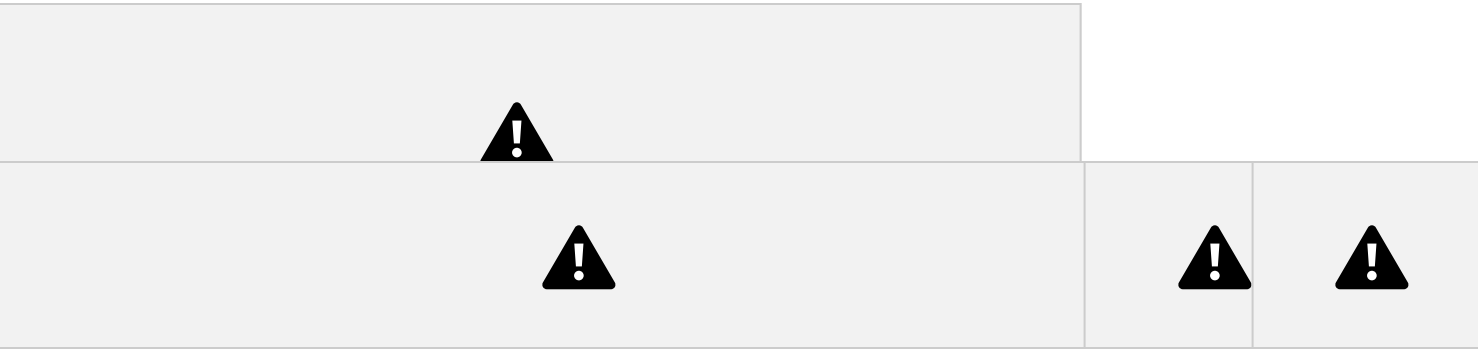
absurdity





Contingency.





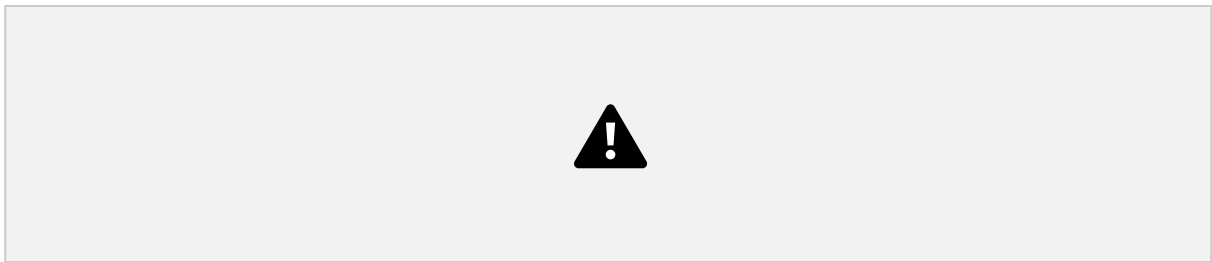
Exercise problems :



a)

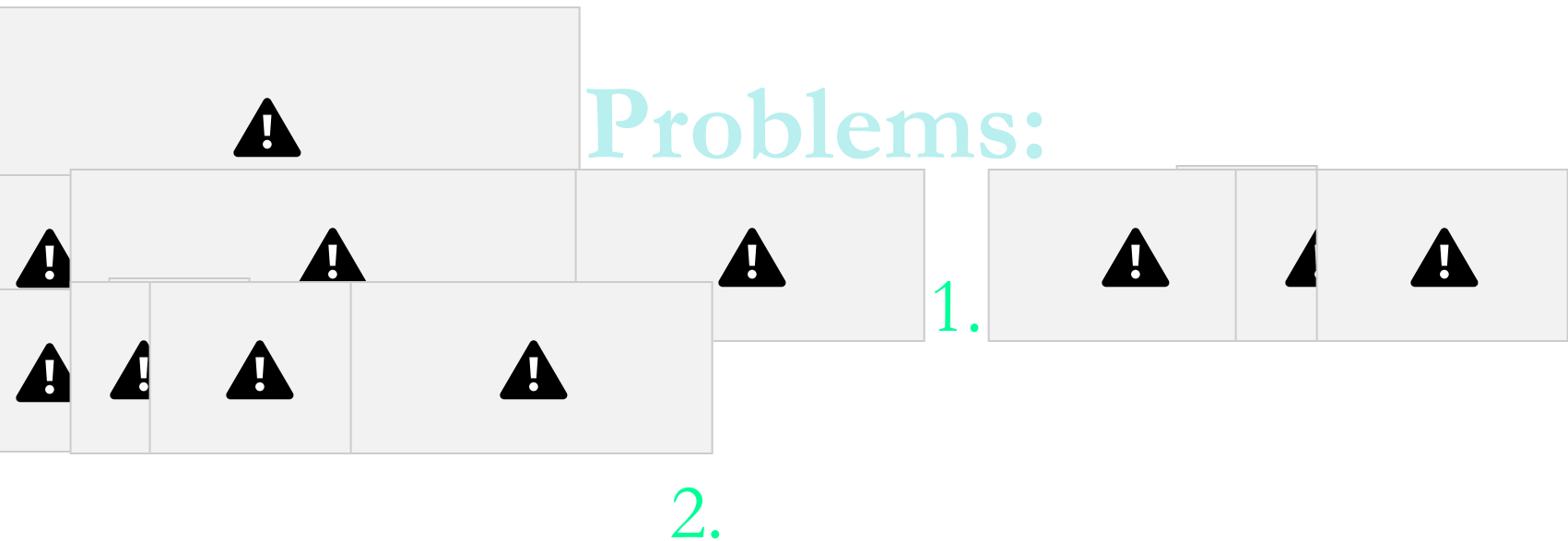
b)





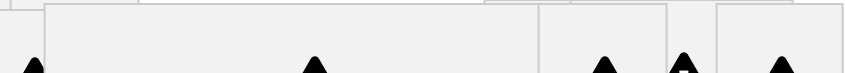


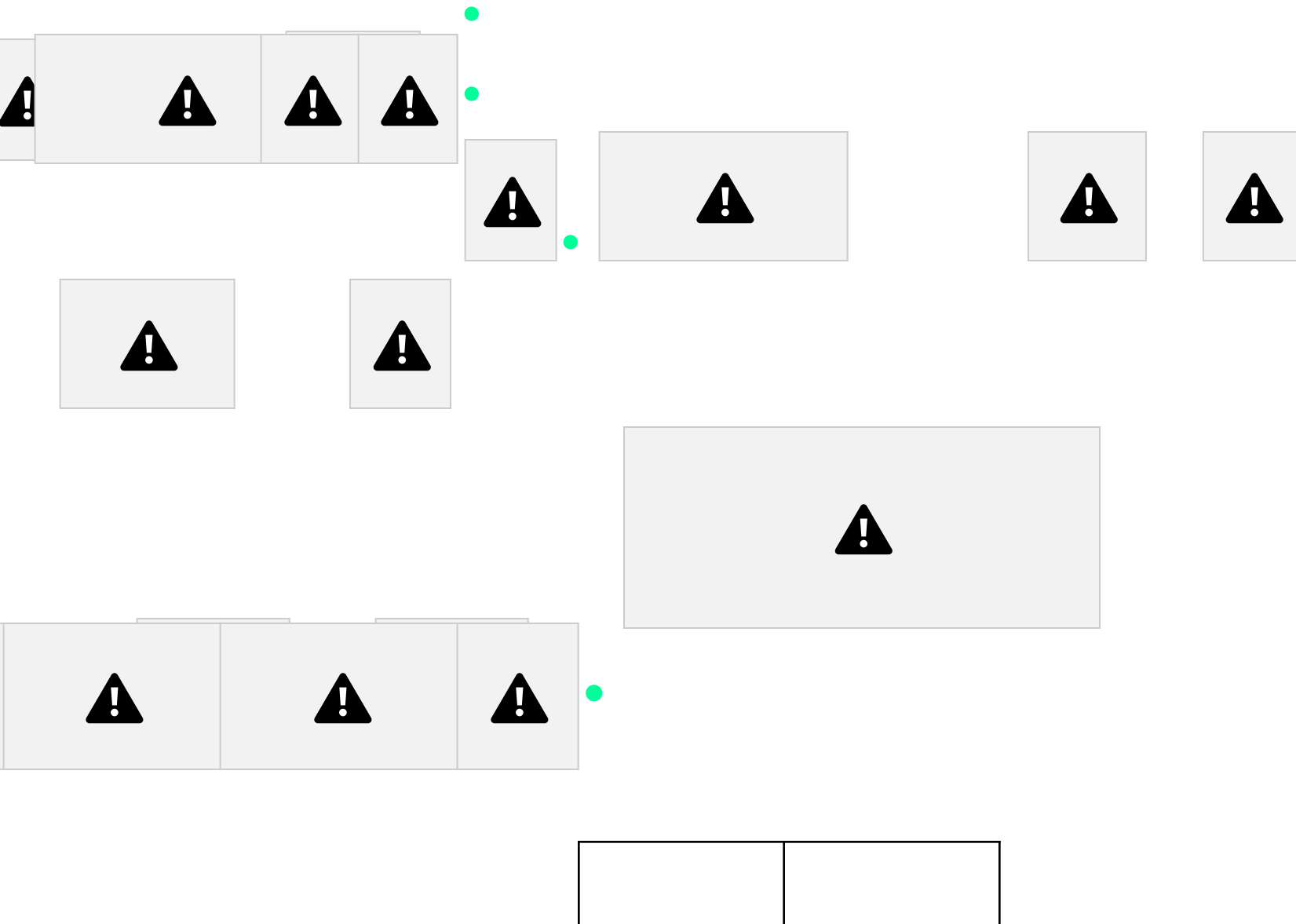






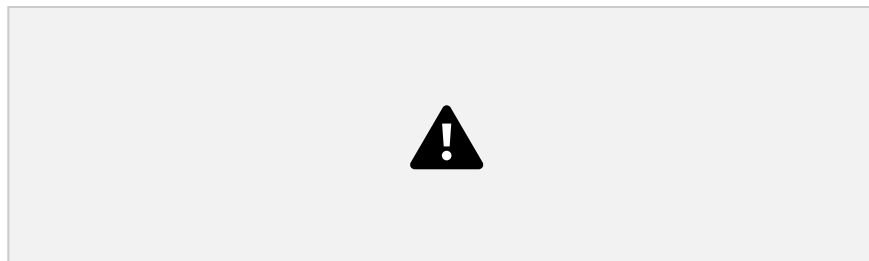
Definitions





T





→ ~p

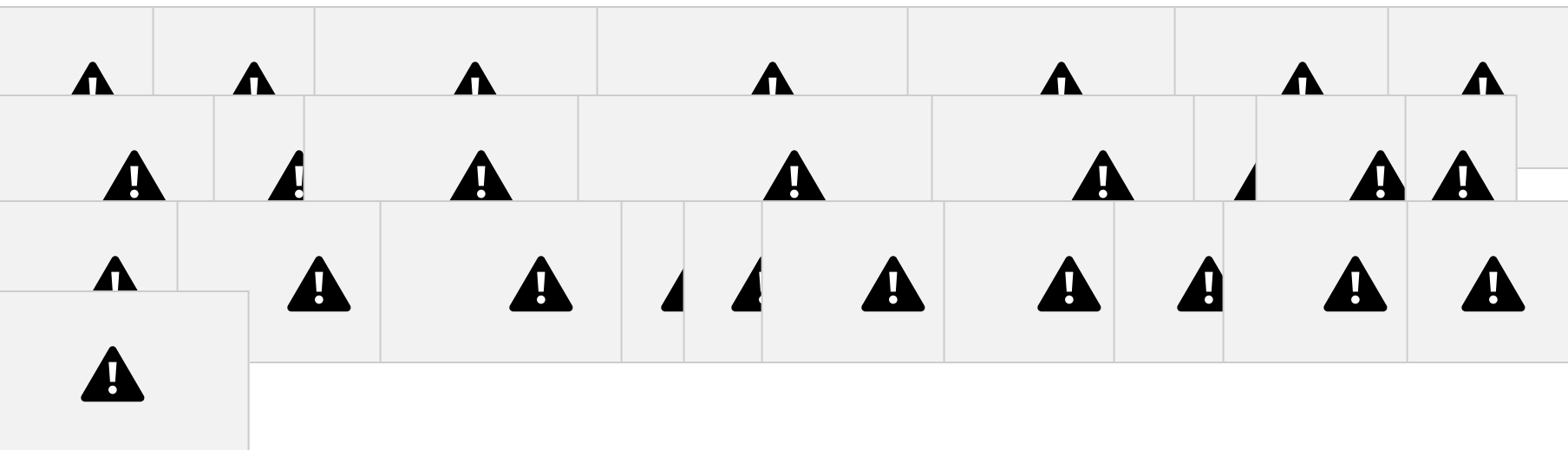
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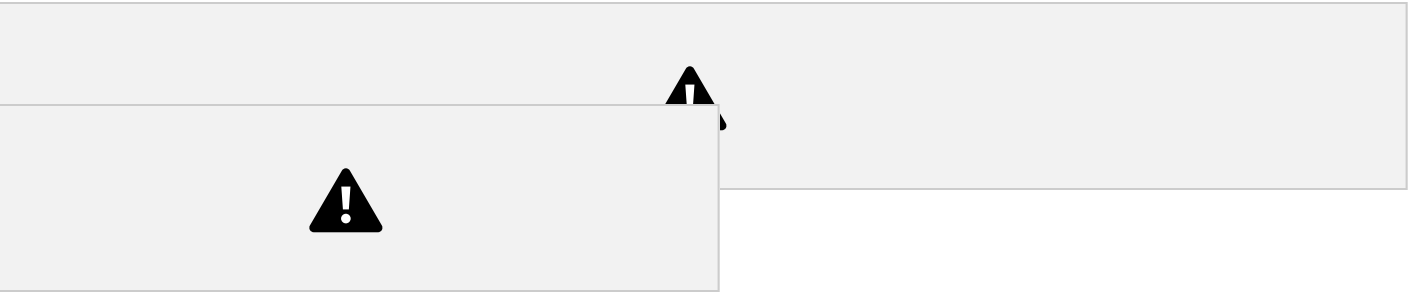
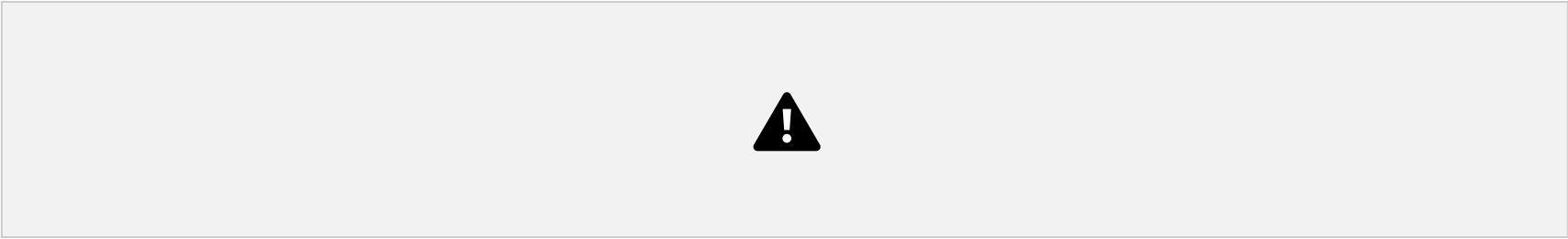


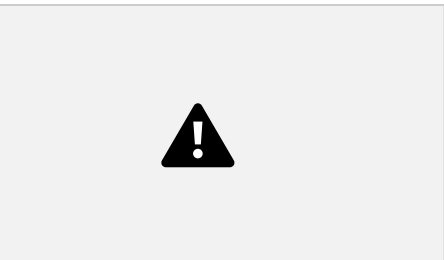


The Laws of Logic

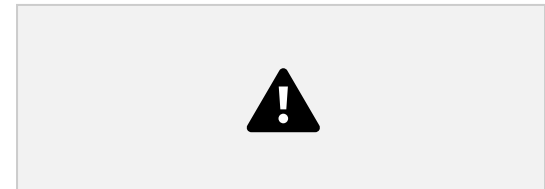
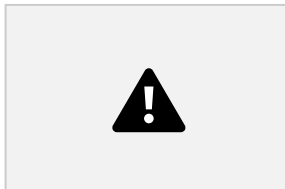








Proof :





P	q	$P \vee q$	$\sim(p \vee q)$	$\sim p$	$\sim q$	$\sim(p) \wedge \sim(q)$
0	0	0	1	1	1	1
0	1	1	0	1	0	0
1	0	1	0	0	1	0
1	1	1	0	0	0	0

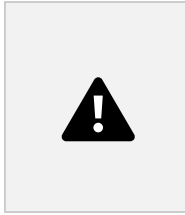
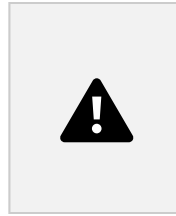
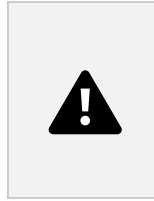




2.

Distributive Law





Laws of Logic



Law of double negation



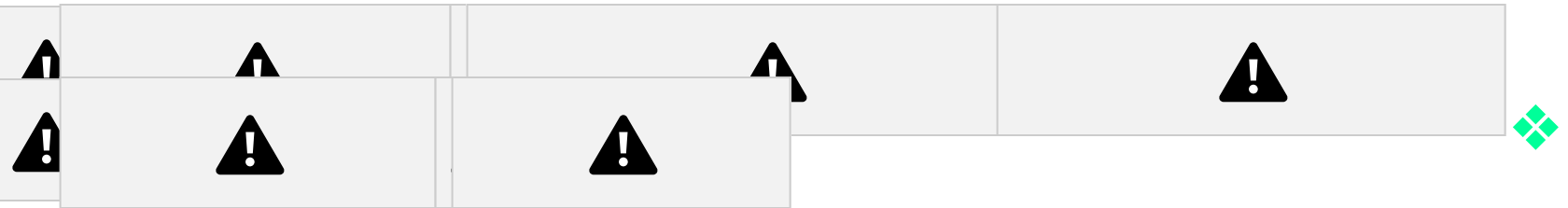
De Morgan's



laws ❖



Commutative Laws ❖

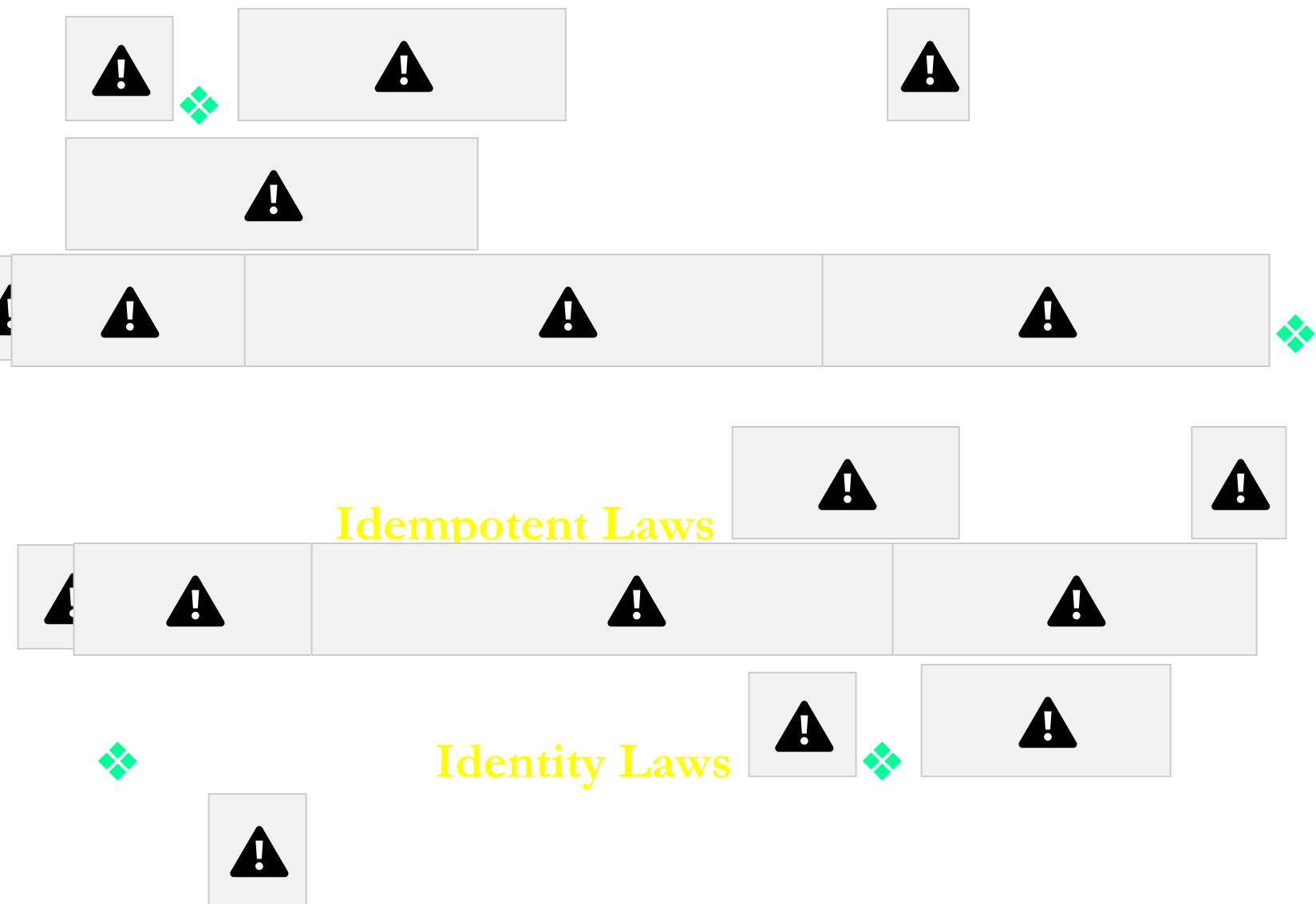


Associative Laws ❖



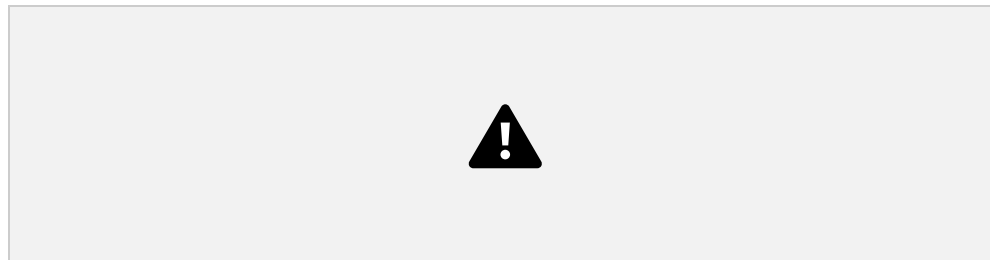
Distributive Laws

Laws of Logic....





Inverse Laws



Laws of
Logic...



Domination Laws





Absorption Laws



Implication Law



Exercise Problems



1.



Exercise Problems





Exercise Problems



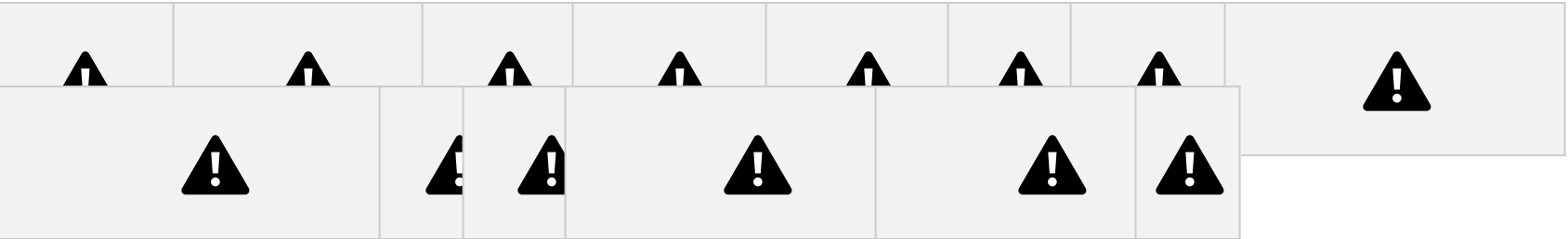
Exercise Problems

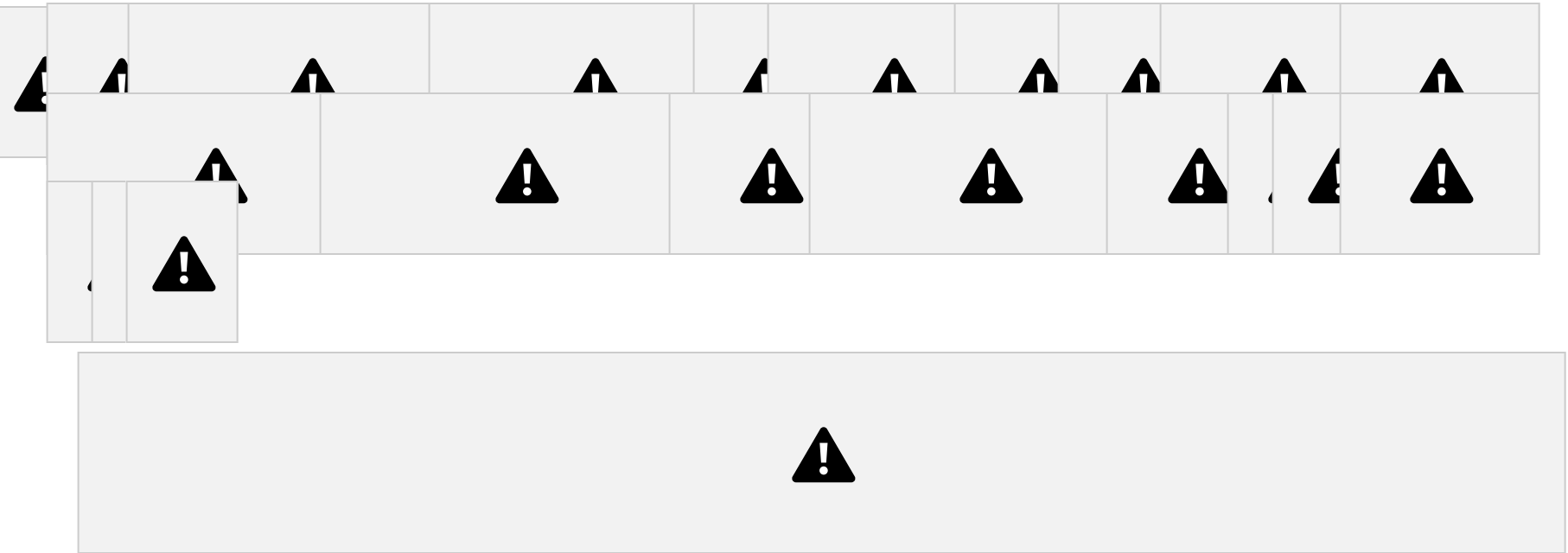


Exercise Problems

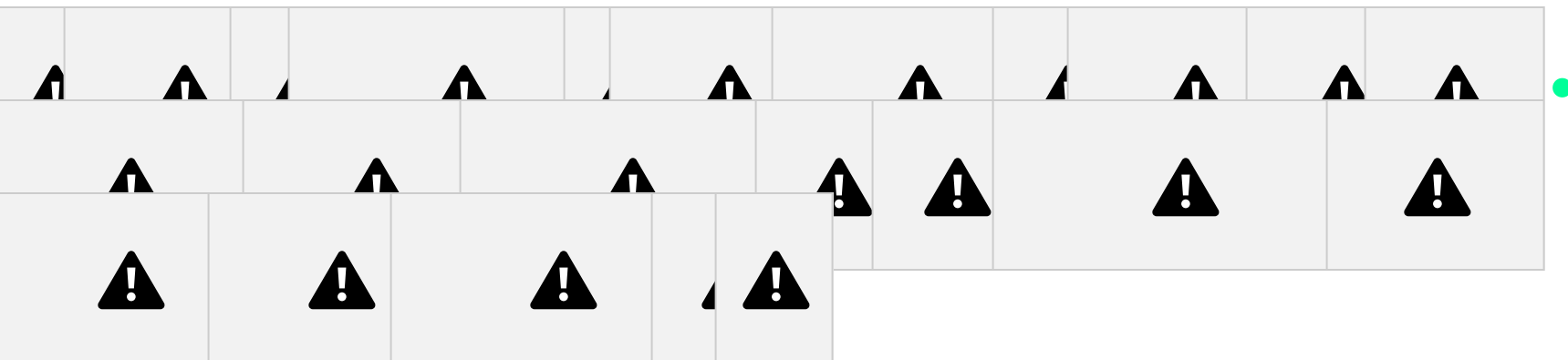


Exercise Problem :

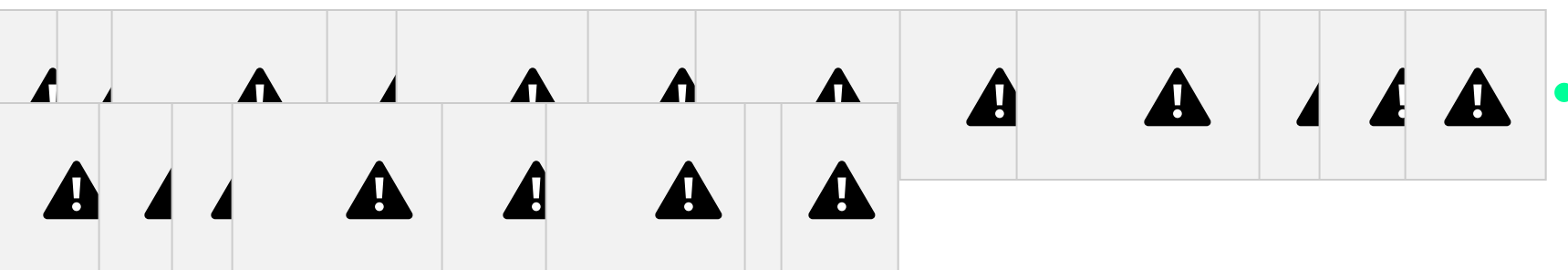


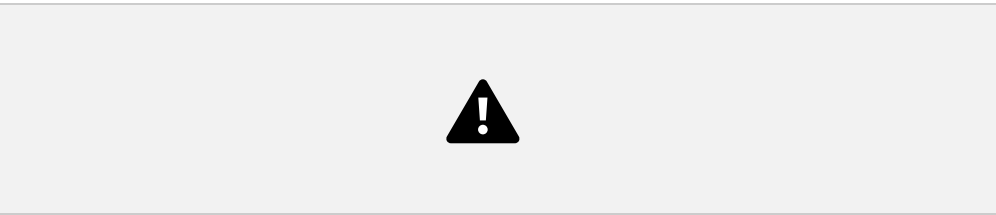


Application to Switching Networks •

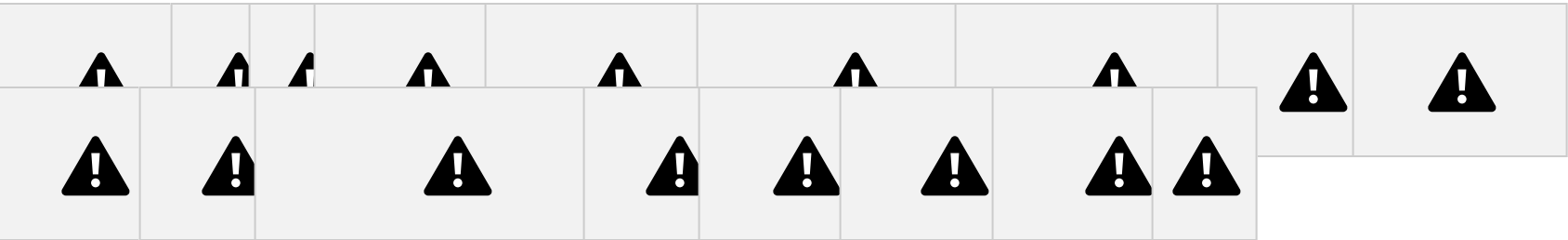


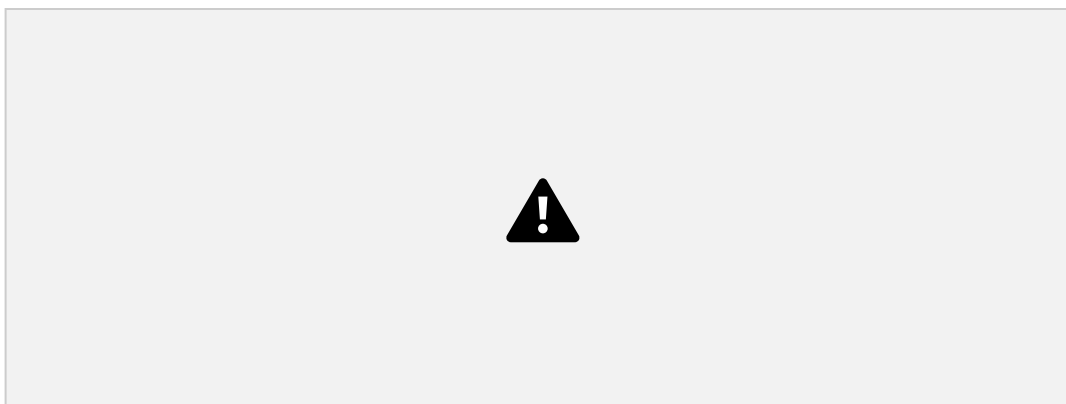
h is op





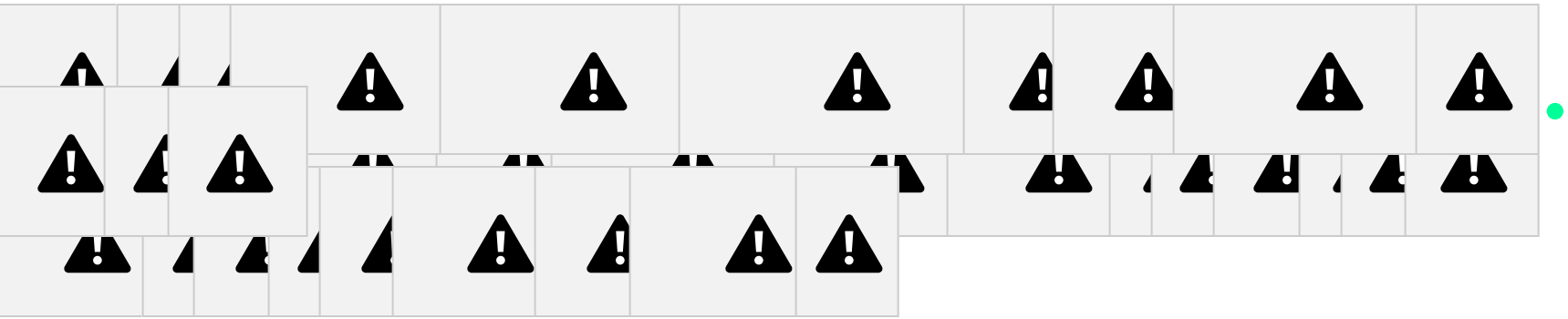
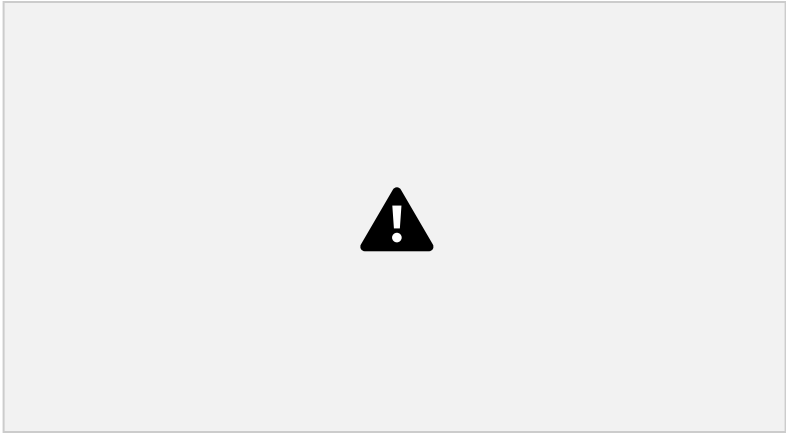
Switching
Networks...



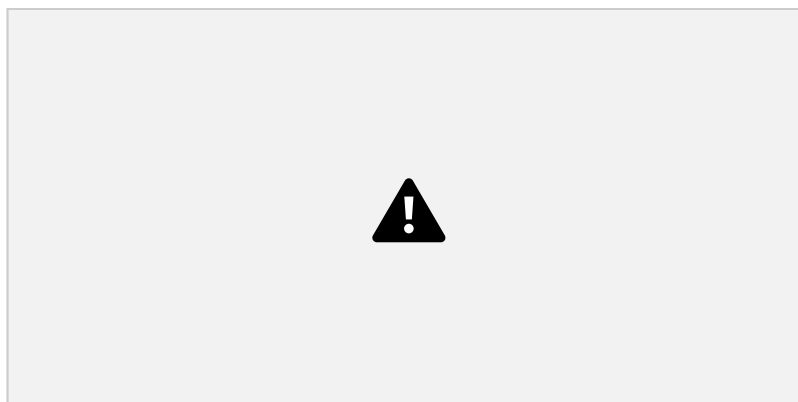


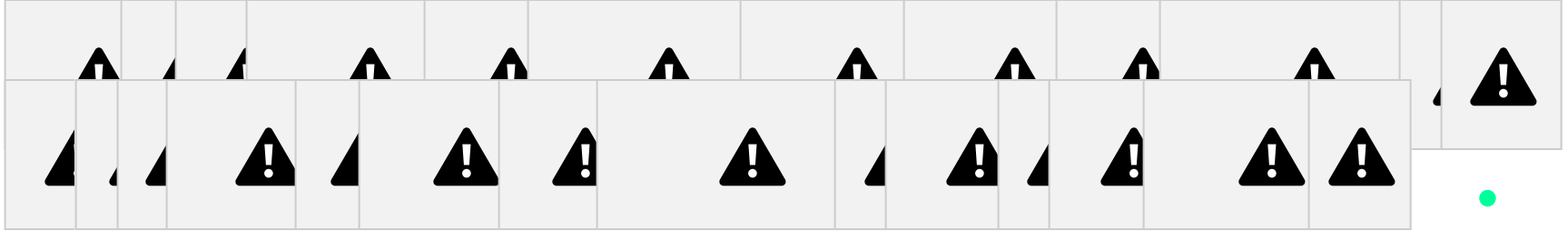


Switching
Networks...





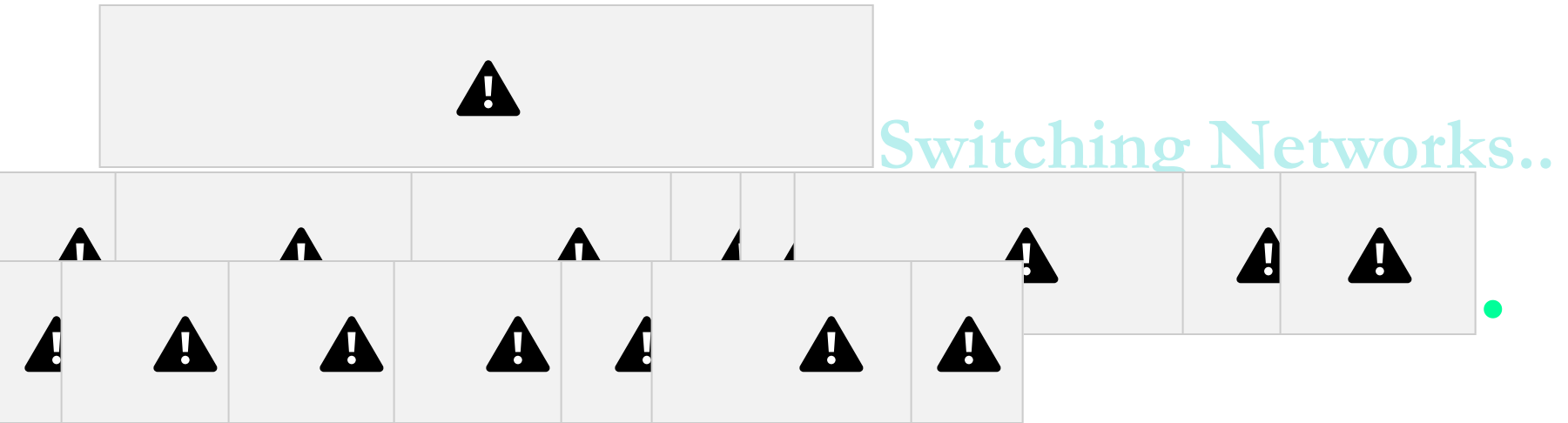




of two



p



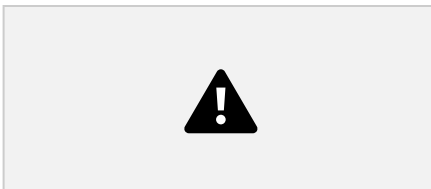
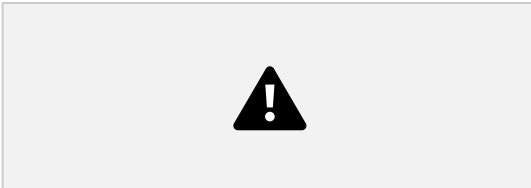
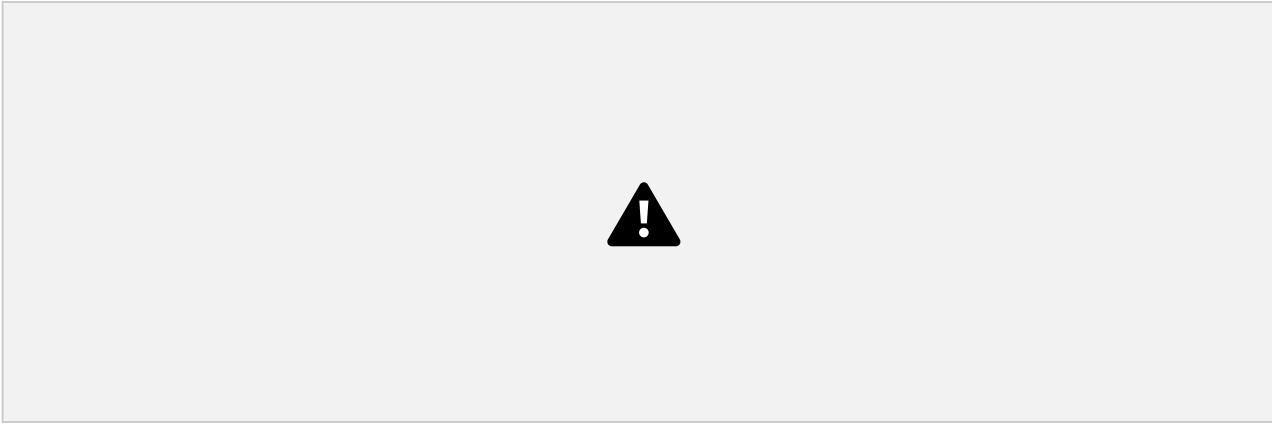


etwork

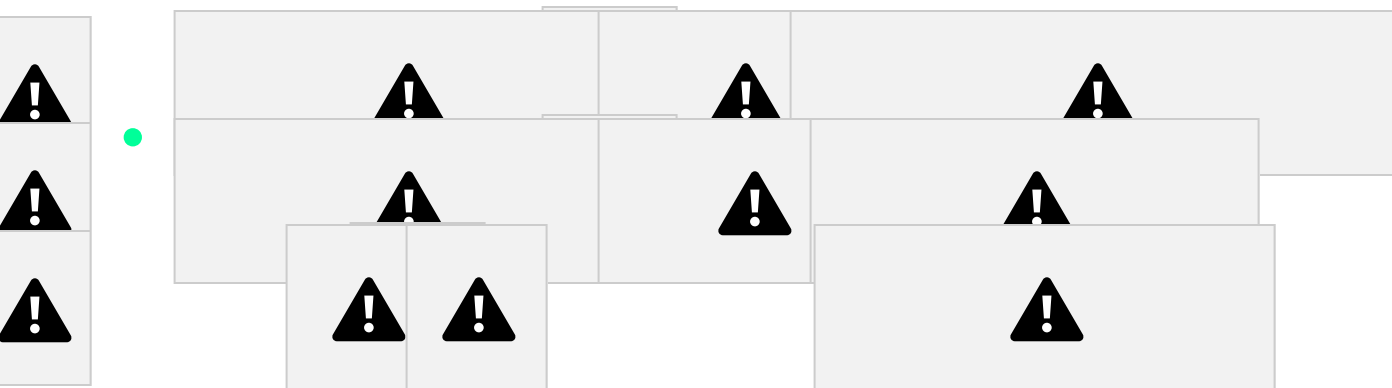


Examples:





Solution



commutative Law •

Inverse

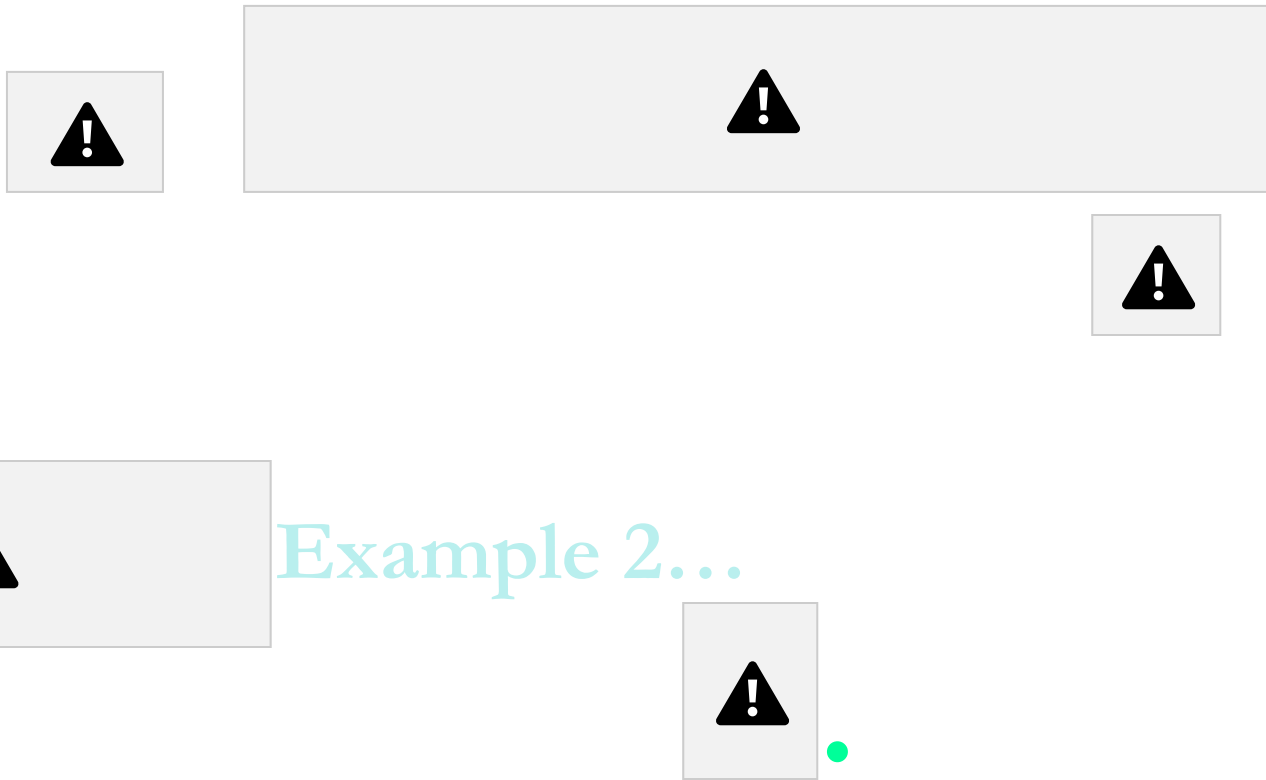
Law

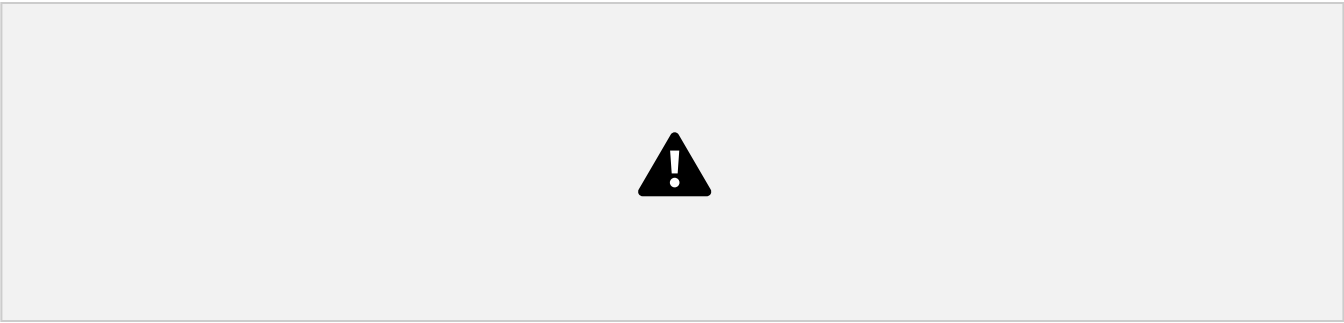


Identity Law

This shows that the given network with 4 switches is

equivalent to a network that contains only one switch.











Example 3 & 4





Solution 3



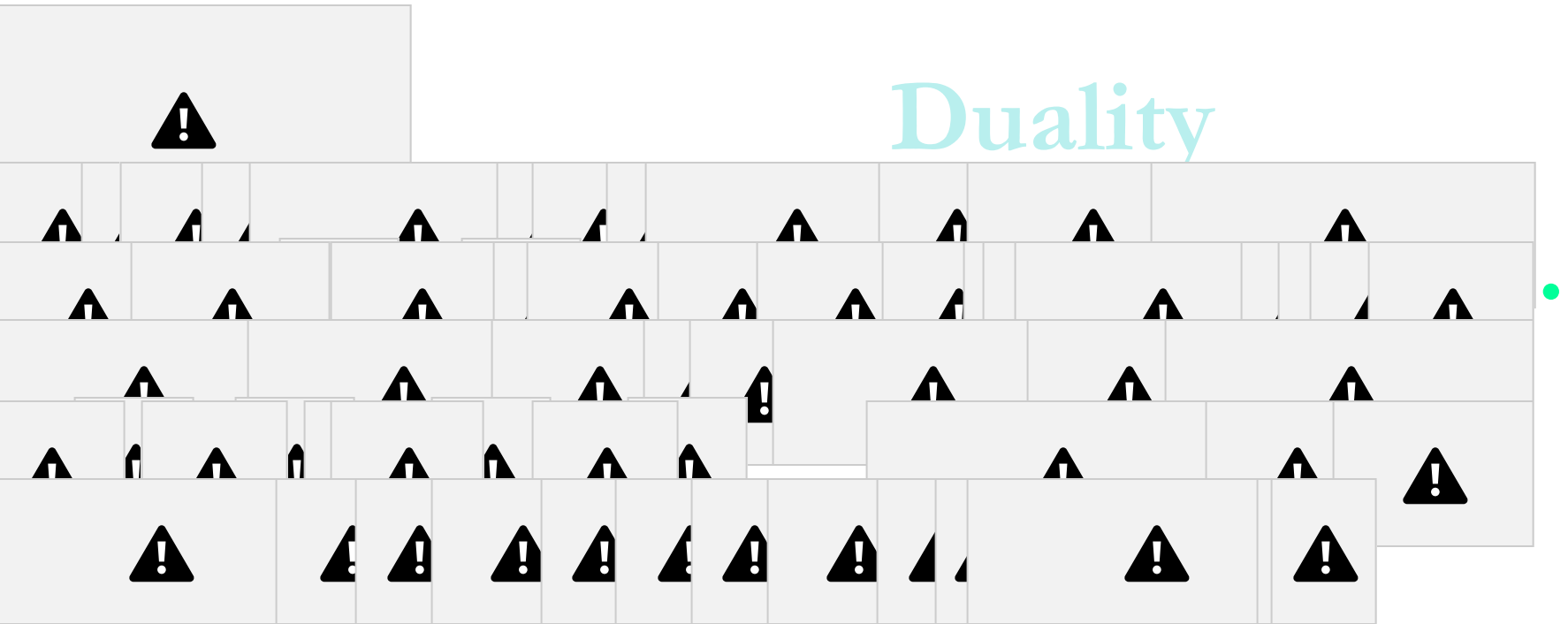


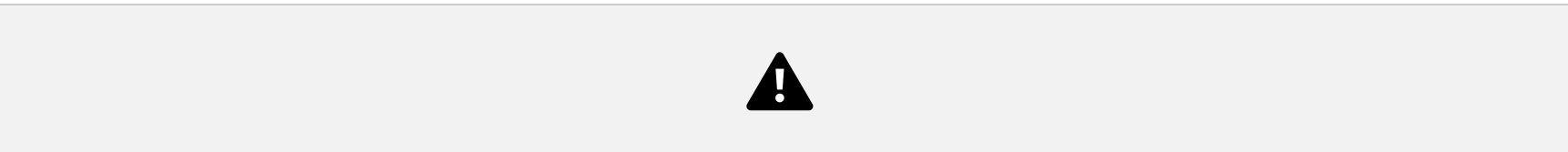
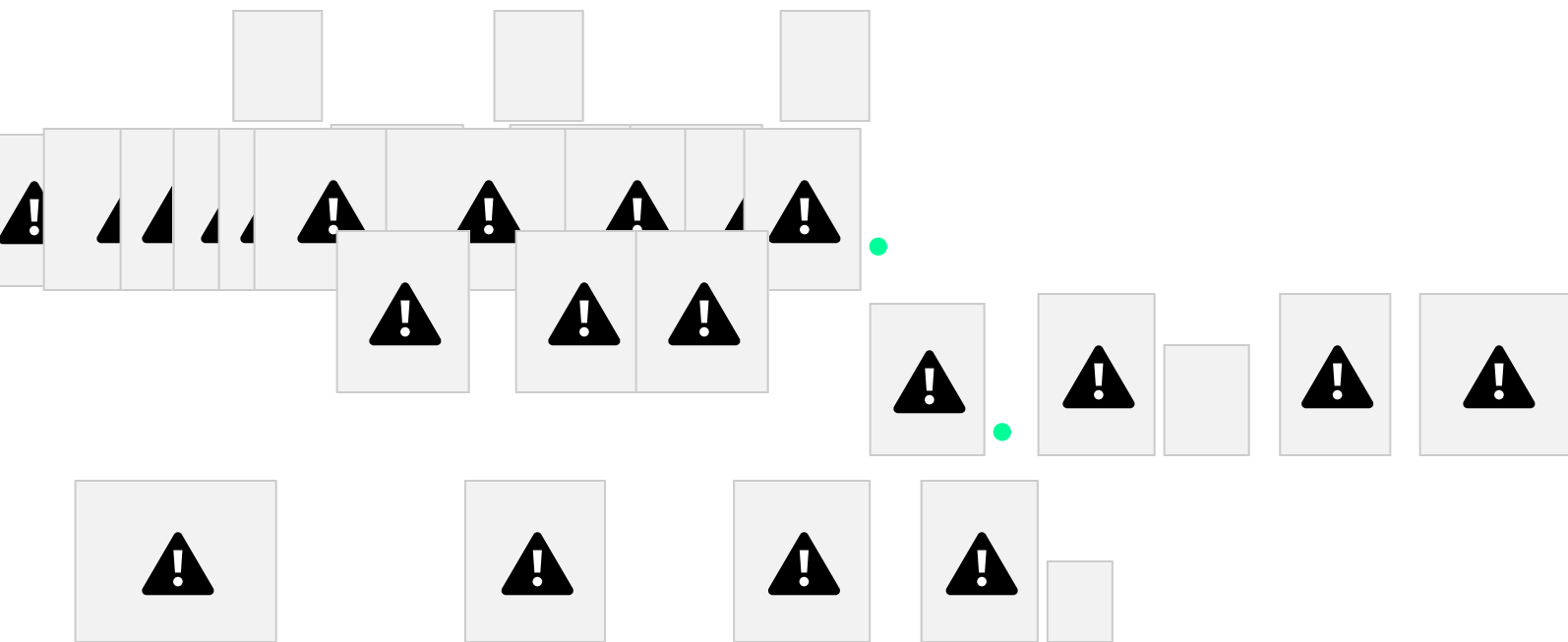


Try It Yourself



Duality



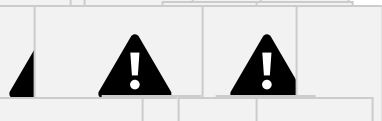




1.



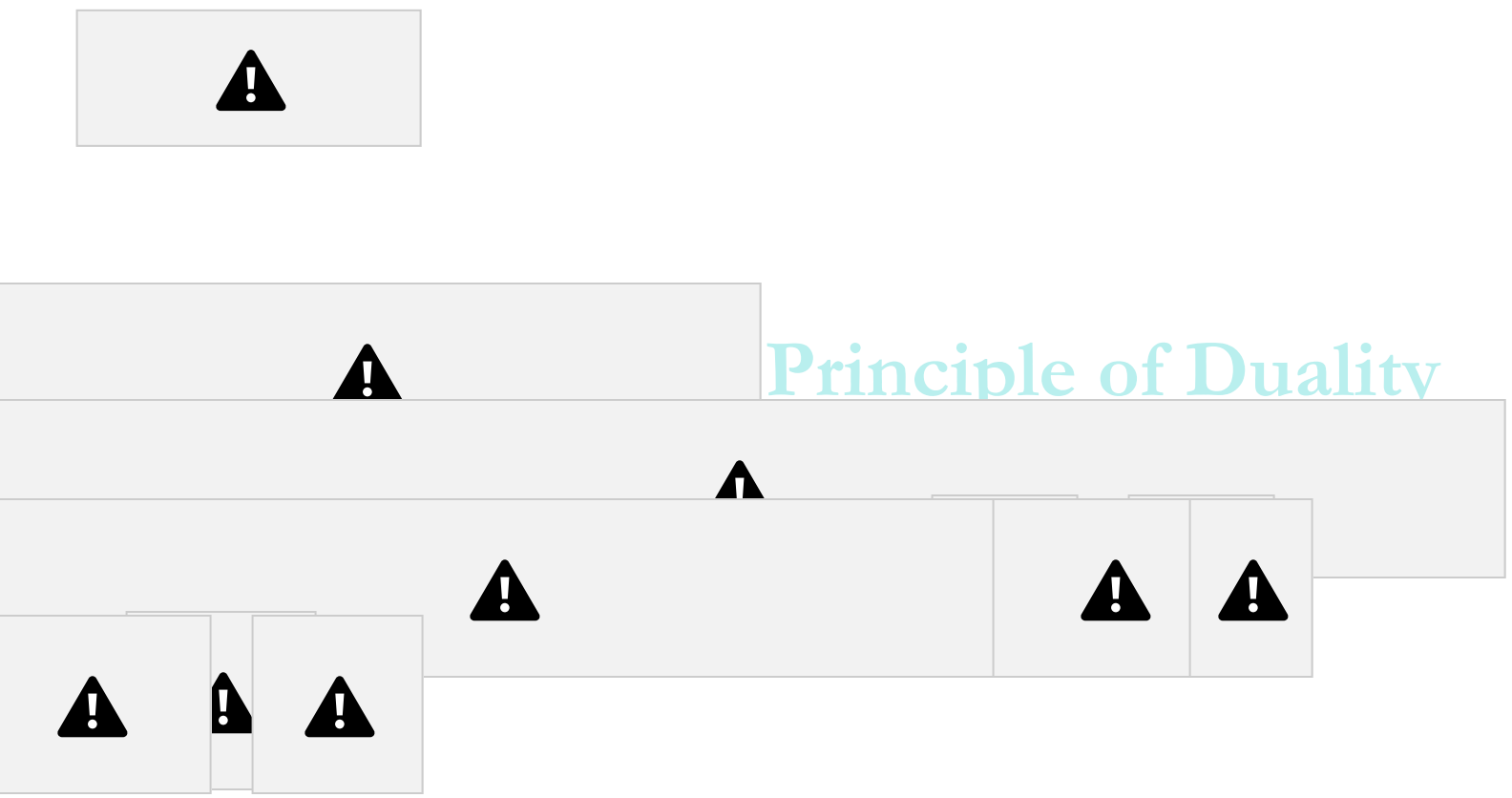
$\neg p \wedge q$



$p \vee \neg q \wedge r$

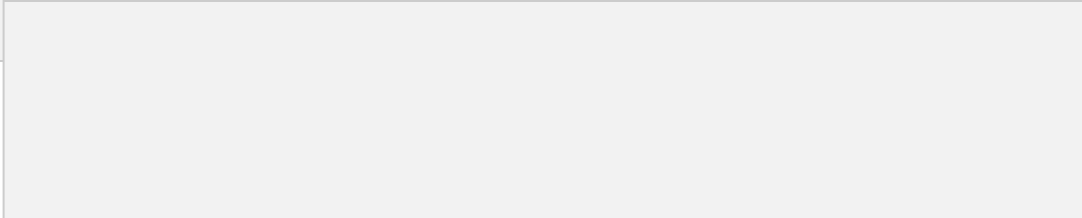
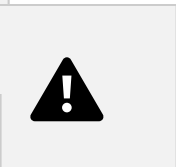
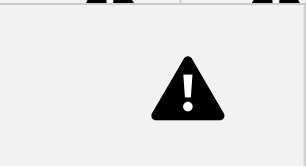


Principle of Duality





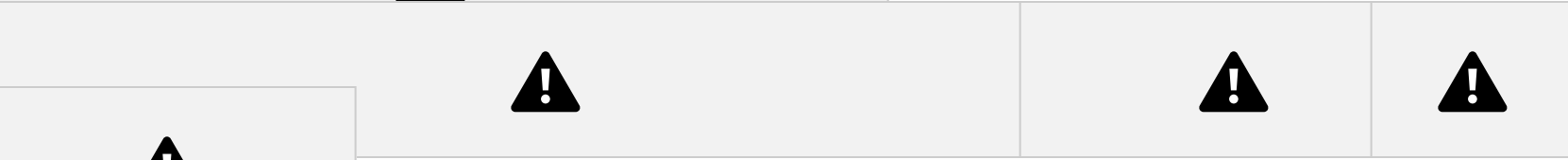
Example







Other Connectives : ↑ ↓



Not

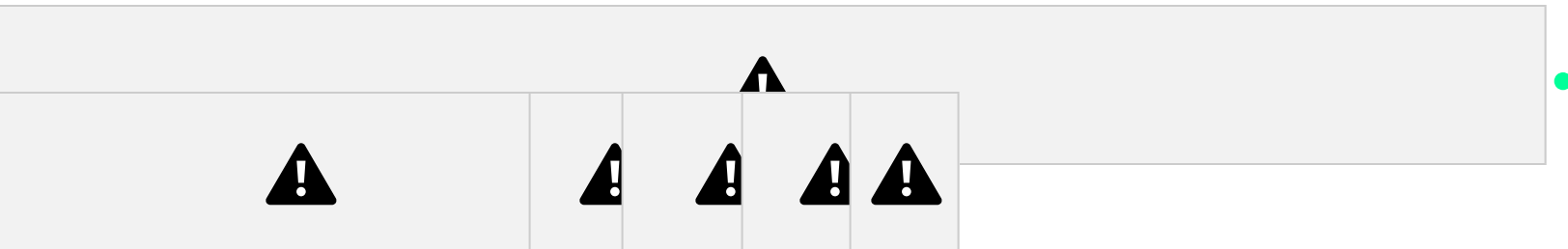
of p and q”

$(p \uparrow q)$



“Not of p or q”

$(p \downarrow q)$



!

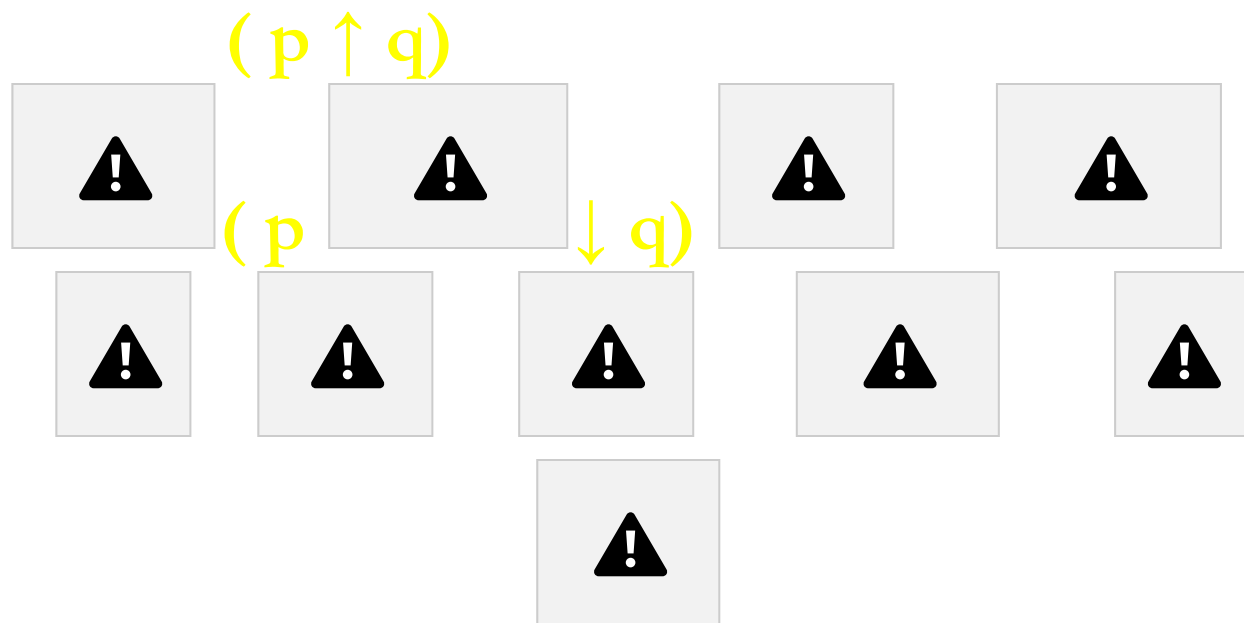
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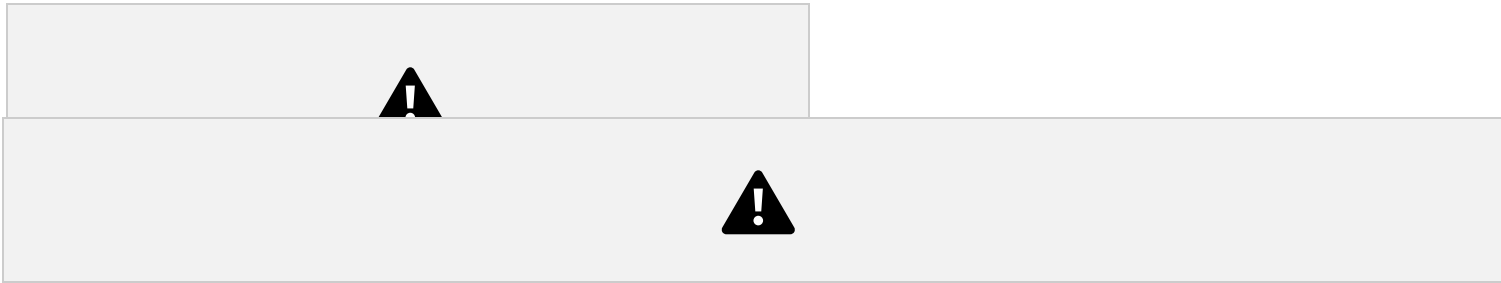
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!

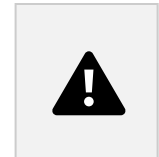
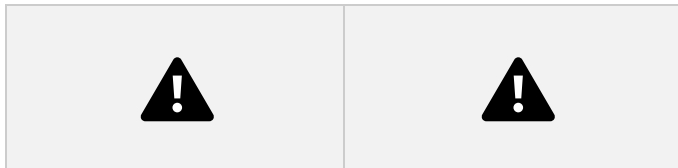
!

p	q	$\neg p$	$\neg q$	$\neg p \vee \neg q$	$\neg(p \wedge q)$ ↑	
0	0	1	1	1	1	
0	1	1	0	1	1	
1	0	0	1	1	1	
1	1	0	0	0	0	





Exercise problems:



1.

