

## Unit-1 : Circuit Analysis

### # Basics

1) Electrical - things operate in greater than 12V (ex: fan)

2) Electronics - things operate in lesser than 12V

Hardware  
waste

Software waste  
(CS)

(ex- phones)

- important parameters that must be balanced :-  
power, area, speed  
to increase its performance.

- diode, BJT [bipolar junction transistors], FET
- analog → varies with time instantly (Ex- 29, 30)
- digital → varies with time but not periodical  
(discrete values, ex- voice over transmission)

field effect transistors

Transmission → Channel → Receiver  
hacking is possible here

→ Components :

1) Active

- anything that needs power supply

2) Passive

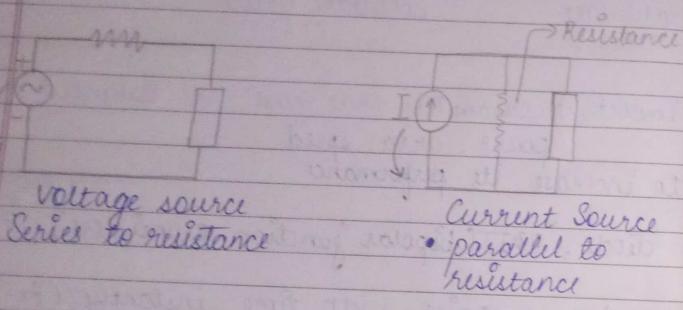
- components that don't require power.

- ex - IC (integrated circuit)
- ex (detector, resistor, capacitor)

→ The resistor must be connected in series with voltage source & in parallel with current source.

# Relation b/w current & voltage

$$V=IR \rightarrow \text{Ohm's law}$$



the circuits are connected to each other too

Kirchoff's Law

KCL: all the incoming current = all the outgoing

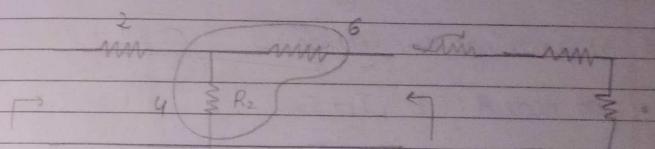
VL: The algebraic sum of all voltages = 0  
 $\sum V = 0$   
 drops & emf sources  
 in any closed path.

# Series & parallel resistance

$$R_p = R_1 + R_2 + \dots + R_n$$

$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}$$

$$R_p = \frac{R_1 R_2}{R_1 + R_2}$$



voltage → short circuit  
 current → open circuit

equivalent resistance →  $R_p = R_1 + (R_2 // R_3)$

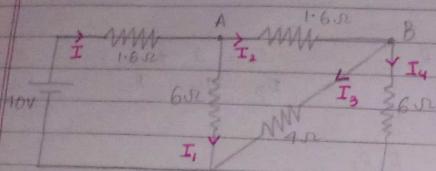
$$\rightarrow R_p = \frac{R_2 R_3}{R_2 + R_3}$$

10/3/04

# Nodal Analysis: Use KCL

Ques Find current through the 4Ω resistor of the

following circuit.



earthing

Sol $\Rightarrow$  at earthing, the voltage = 0

- At node A:  $I = I_1 + I_2$

$$\frac{V}{R} = \frac{V_1}{R_1} + \frac{V_2}{R_2}$$

$$\frac{40 - V_A}{1.6} = \frac{V_A - 0}{6} + \frac{V_A - V_B}{1.6} \quad \text{--- (i)}$$

- At node B:  $I_2 = I_3 + I_4$

$$\frac{V_2}{R_2} = \frac{V_3}{R_3} + \frac{V_4}{R_4}$$

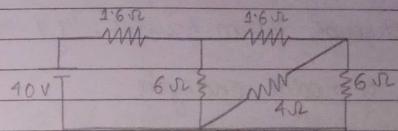
$$\frac{V_A - V_B}{1.6} = \frac{V_B - 0}{4} + \frac{V_B - 0}{6} \quad \text{--- (ii)}$$

- at the potential 40V, it is +ve up & -ve down so take it +ve.

→ if it is -ve terminal at top & +ve below, the voltage is -ve.

$$+40V \quad -40V$$

→ Solving the circuit :-



- 1)  $6\Omega \times 4\Omega \text{ in parallel} = \frac{6 \times 4}{6+4} = \frac{24}{10} = 2.4\Omega$

- 2)  $1.6\Omega \text{ & } 2.4\Omega \text{ in series} = 1.6 + 2.4 = 4\Omega$

- 3)  $6\Omega \text{ & } 4\Omega \text{ in parallel} = 2.4\Omega$

- 4)  $1.6\Omega \text{ & } 2.4\Omega \text{ in series} = 4\Omega$

$$\text{Ohm's law } V=IR \quad = \quad 40 = I \times R \\ I = 10A$$

# From (i)  $\rightarrow \frac{40 - V_A}{1.6} = 10, \quad 40 - V_A = 16$   
 $V_A = 40 - 16 = 24V$

$$I_1 = \frac{24}{6} = 4A \quad I_2 = I - I_1 \\ = 10 - 4 = 6A$$

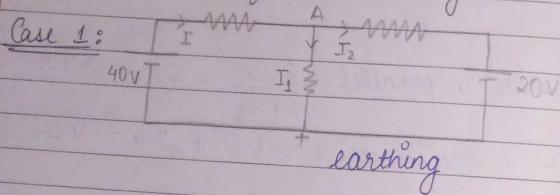
- $I = 10A, I_1 = 4A, I_2 = 6A$

# From (ii)  $I_2 = I_3 - I_4 \rightarrow \frac{V_A}{6} - \frac{V_B}{6} = 14.4$

 $\downarrow$ 
 $\frac{V_B}{4} = 14.4$

Ans: current through  $4\Omega$  resistor,  $\frac{14.4}{4} = 3.6A$

### Different cases of nodal analysis



connected to earth:

and  $\frac{V_A - 20}{R}$

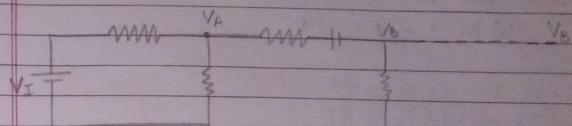
$\frac{V_A + 20}{R}$

i.e. if we come across the +ve terminal first we take -ve.

$\frac{V_A - 20}{R}$

but if we come across the -ve terminal first we take +ve  $\rightarrow \frac{V_A + 20}{R}$

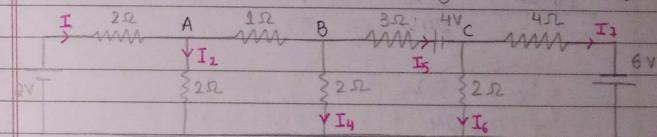
Case 2:



$$\frac{V_A - V_B - V_0}{R}$$

- not connected to earth instead connected to more circuit.

Ques: Find the value of current flowing through  $3\Omega$  resistance in given circuit using nodal analysis.



Sol: At node A:  $I = I_2 + I_3$

$$\frac{2-V_A}{2} = \frac{V_A-0}{2} + \frac{V_A-V_B}{1}$$

$$\rightarrow 2-V_A = V_A + 2V_A - 2V_B ; \quad 2 = 4V_A - 2V_B$$

$$1 = 2V_A - V_B$$

now find  $V_A, V_B, V_C$

$$\rightarrow 2V_A - 1 = V_B$$

$$\rightarrow 6V_A - 11(2V_A - 1) + 2V_C = -8$$

$$\rightarrow 6V_A - 22V_A + 11 + 2V_C = -8$$

$$-16V_A + 2V_C = -8 - 11$$

$$-16V_A + 2V_C = -19$$

$$\rightarrow 4(2V_A - 1) - 13V_C = 31$$

$$8V_A - 4 - 13V_C = 31$$

$$-16V_A + 2V_C = -19$$

$$(8V_A - 13V_C = 35) \times 2$$

$$\begin{aligned} 16V_A' - 26V_C &= 70 \\ -16V_A + 2V_C &= -19 \\ -24V_C &= 51 \end{aligned}$$

$$V_C = \frac{-51}{24}$$

$$-16V_A = -19 - \left(\frac{-51}{24}\right) \times 2$$

$$-16V_A = -19 + \frac{51}{12} = \frac{-228 + 51}{12} = \frac{59}{64}$$

$$8 \times \frac{59}{64} - 1 = V_B \rightarrow \frac{59}{32} - 1 = V_B$$

$$\frac{59 - 32}{32} = V_B$$

$$\therefore V_B = \frac{27}{32}$$

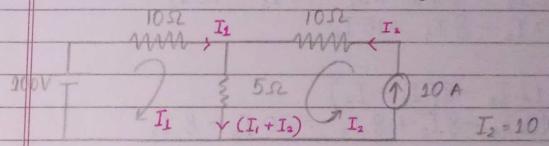
$$\therefore V_A = \frac{59}{64} = V_B = \frac{27}{32}, V_C = \frac{-51}{24}$$

Current flowing through  $I_1$

$$\frac{27}{32} - 4 + 51 = 3$$

# Loop/Mesh Analysis :-

Ques Find the current in all the resistive branches of the circuit using loop analysis.



(Loop)

$$100 = 10I_1 + 5(I_1 + I_2)$$

$$100 + (-10)I_1 - 5(I_1 + I_2) = 0$$

$$100 - 10I_1 - 5I_1 - 50 = 0$$

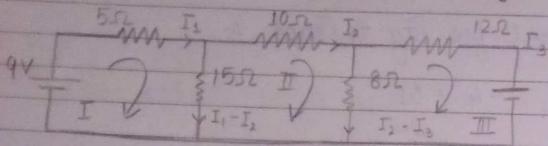
$$50 - 15I_1 = 0$$

$$I_1 = \frac{50}{15} = \frac{10}{3} = 3.33A$$

$$I_1 = 3.33A$$

$$I_2 = 10A$$

Ques Determine the value of current in 8Ω resistor in the network shown below using mesh method.



$$\text{loop 1: } 9 = 5I_1 + 15(I_1 - I_2)$$

$$9 = 5I_1 + 15I_1 - 15I_2 = 20I_1 - 15I_2$$

$$\text{loop 2: } 0 = 10I_2 + 8(I_2 - I_3) - 15(I_1 - I_2)$$

$$= 10I_2 + 8I_2 - 8I_3 - 15I_1 + 15I_2$$

$$= 33I_2 - 8I_3 - 15I_1$$

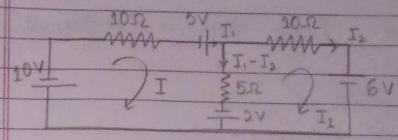
$$\text{loop 3: } 6 = 12I_3 - 8(I_2 - I_3)$$

$$6 = 12I_3 - 8I_2 + 8I_3 = 20I_3 - 8I_2$$

$$I_1 = \frac{9 + 15I_2}{20}$$

Calculations needed to be done

Ques



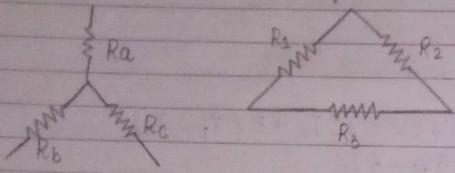
$$\text{loop 1: } -10V + 5V + 2V = 10I_1 + 5(I_1 - I_2)$$

$$-3V = 15I_1 - 5I_2$$

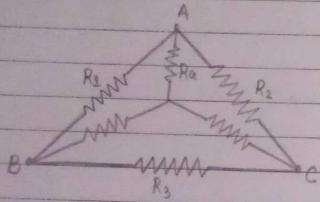
$$\text{loop 2: } -6V - 2V = 10I_2 - 5(I_2 - I_3)$$

$$-8V = 15I_2 - I_3$$

## # Star - Delta, and Delta - Star Transformation



## # Delta - Star

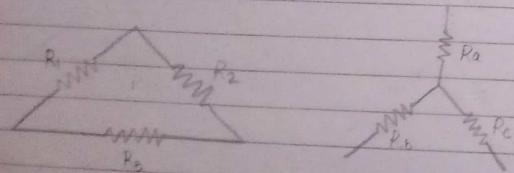


$$R_a = \frac{R_1 \cdot R_2}{R_1 + R_2 + R_3}$$

$$R_b = \frac{R_1 R_3}{R_1 + R_2 + R_3}$$

$$R_c = \frac{R_2 R_3}{R_1 + R_2 + R_3}$$

## # Star - Delta



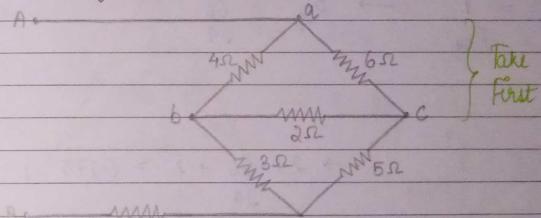
$$R_1 = R_a + R_b + \frac{R_a R_b}{R_c}$$

$$R_2 = R_a + R_c + \frac{R_a R_c}{R_b}$$

$$R_3 = R_b + R_c + \frac{R_b R_c}{R_a}$$

Ques

Find the resistance b/w terminals A & B for the circuit given below use ( $\Delta - Y$ )

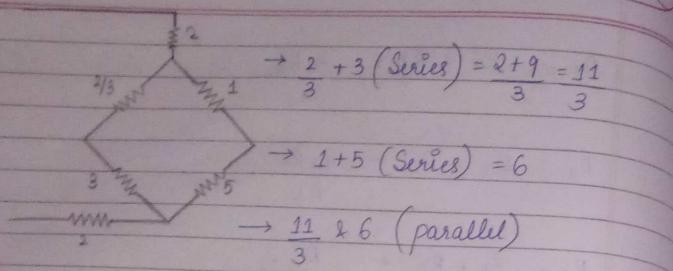


Sol

$$R_a = \frac{R_1 R_2}{R_1 + R_2 + R_3} = \frac{4 \times 6}{12} = 2$$

$$R_b = \frac{4 \times 2}{12} = \frac{2}{3}$$

$$R_c = \frac{6 \times 2}{12} = 1$$



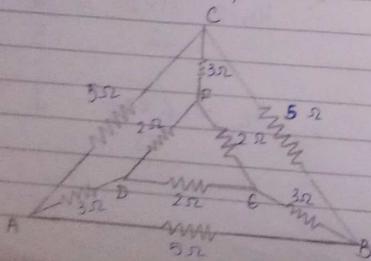
$$\rightarrow \frac{1}{\frac{11}{3}} + \frac{1}{6} = \frac{1}{R_{eq}} \rightarrow \frac{3}{11} + \frac{1}{6} = \frac{1}{R} \rightarrow \frac{18+11}{66} = \frac{1}{R_{eq}}$$

$$\rightarrow \frac{29}{66} = \frac{1}{R_{eq}} \rightarrow R_{eq} = \frac{66}{29}$$

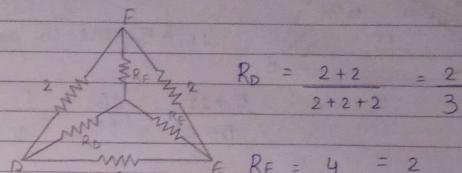
$$\rightarrow 2 + \frac{66}{29} + 2 = 6.275 \Omega$$

### Assignment Questions

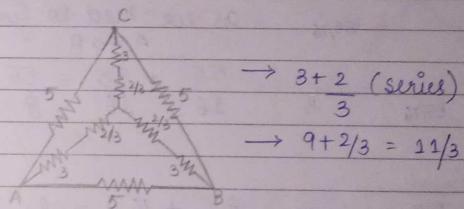
Find resistance b/w points A & B.



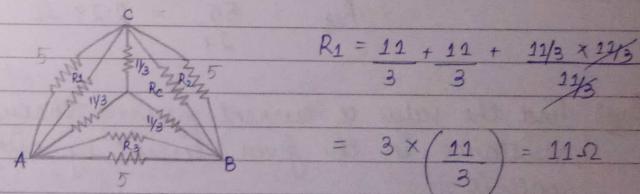
# delta to star :-



$$R_F = \frac{4}{6} = \frac{2}{3}$$

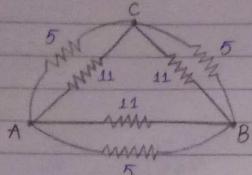


→ Convert star into delta



$$R_2 = 11 \Omega$$

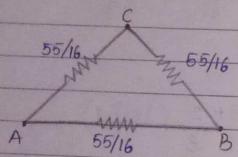
$$R_3 = 11 \Omega$$



$I_1$  &  $I_5$  are in parallel

$$\frac{5+11}{55} = \frac{16}{55} = \frac{1}{Req}$$

$$\frac{55}{16} = Req$$



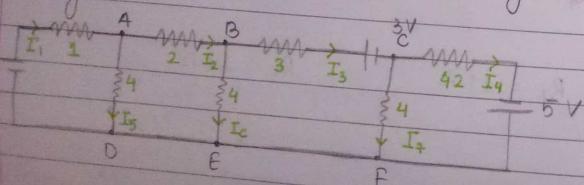
as we need to find  
 $A \rightarrow B$

$$\frac{55}{16} + \frac{55}{16} = \frac{55}{8}$$

$$\frac{8}{55} + \frac{16}{55} = \frac{1}{Req}$$

$$Req = \frac{55}{24} = 2.29 \Omega$$

Find the value of current flowing through  $3\Omega$  resistance in the given circuit by using nodal analysis.



Sol Applying KCL:

# at node A:  $I_1 = I_2 + I_5$

$$\rightarrow \frac{V_A - V_B}{1} = \frac{V_A - V_B}{2} + \frac{V_A - \infty}{4},$$

$$\rightarrow 4V_A = \frac{2V_A - 2V_B + V_A}{4}$$

$$16 - 4V_A = 3V_A - 2V_B \rightarrow 16 + 2V_B = 7V_A$$

$$V_A = \frac{16 + 2V_B}{7}$$

# at node B:  $I_2 = I_3 + I_6$

$$\frac{V_A - V_B}{2} = \frac{V_B - V_C - 3}{3} + \frac{V_B}{4}$$

$$\frac{V_A - V_B}{2} = \frac{4V_B - 4V_C - 12 + 3V_B}{12}$$

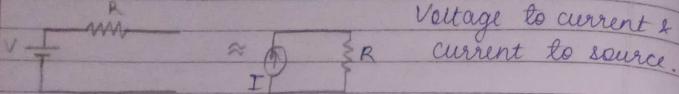
$$\rightarrow 6(V_A - V_B) = 4V_B - 4V_C - 12 + 3V_B$$

$$6V_A - 6V_B = 7V_B - 4V_C - 12$$

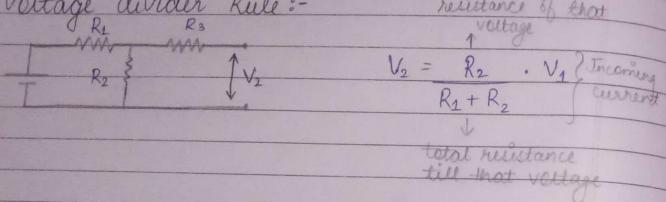
$$\Rightarrow 6V_A - 13V_B + 4V_C = -12 \checkmark$$

30/11/24

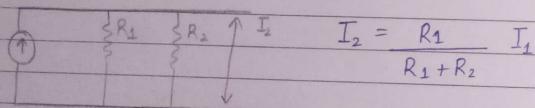
## 1) Source Conversion :-



## 2) Voltage divider Rule :-

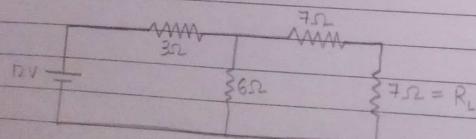


## 3) Current division Rule :-

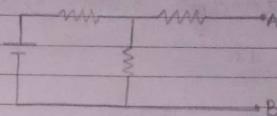


## # Thevenin's Theorem

Find the current in load resistance  $R_L$  using Thevenin's Theorem.



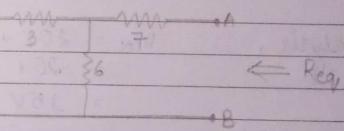
Step 1: Remove the load network & mark the 2 terminals A & B.



Step 2: Calculate the thevenin equivalent voltage ( $V_{TH}$ ) across terminals A & B.

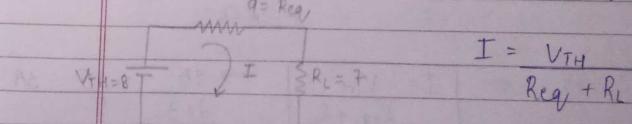
Using voltage divider case Rule  $\rightarrow V_{TH} = \frac{6}{3+7} \times 12 = 8V$  (only in some cases)

Step 3: Find the thevenin equivalent resistance by short circuiting voltage source & open circuiting current source across the two terminals (A) (B).



$$R_{eq} = 7 + \left( \frac{6}{3+6} \parallel 3 \right) = 7 + \frac{(6 \times 3)}{6+3} = 7 + \frac{18}{9} = 9\Omega$$

Step 1: Replace the network by thevenin equivalent circuit & connect the load resistance back to it.

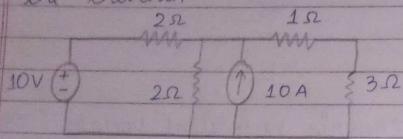


$$\frac{8}{9+7} = \frac{8}{16} = \frac{1}{2}$$

$$I = D \cdot S \cdot A$$

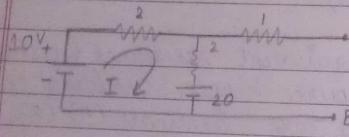
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Ques Find the current through 3 ohm resistor using the thevenin



Sol  $\Rightarrow$

$$\begin{aligned} V &= 10 - 2I \\ R &= 4 \Omega \end{aligned} \quad \left\{ \begin{aligned} V &= IR \\ I &= \frac{V}{R} = \frac{-10}{4} = -2.5 \text{ A} \end{aligned} \right.$$



Using loop analysis,

$$\begin{aligned} 10 - 2I &= 2I + 2I \\ -10 &= 4I \\ I &= \frac{-10}{4} = -2.5 \text{ A} \end{aligned}$$

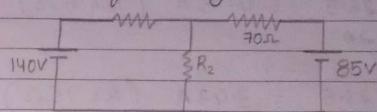
$$\begin{aligned} V_{TH} &= 20V + 2I \\ &= 20 + 2(-2.5) \\ &= 15V \end{aligned}$$

$$\begin{aligned} \text{Req} &= 1 + (2 \text{ parallel } 2) \\ &= 1 + \frac{2 \times 2}{4} = 1+1 \\ &= 2\Omega \end{aligned}$$

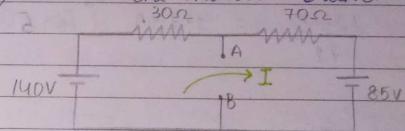
$$\begin{aligned} \text{Req} &= 2 \\ R_L &= 3\Omega \end{aligned} \quad \left| \begin{array}{l} I = \frac{V_{TH}}{\text{Req} + R_L} \\ \rightarrow 15 = \frac{15}{2+3} = 3A \end{array} \right.$$

Ques

In the circuit given below find the branch current  $I_2$  which flows through the resistance  $R_2$  where  $R_2$  has following values :  $5\Omega, 15\Omega, 10\Omega$



Sol  $\Rightarrow$  1) remove the middle branch i.e. short circuit



$$\rightarrow \frac{1}{\text{Req}} = \frac{1}{70} + \frac{1}{30} \quad (\text{they are in } \parallel \text{ due to } A)$$

$$\rightarrow \text{Req} = \frac{70 \times 30}{70 + 30} = \frac{2100}{100} = 21\Omega$$

$$\rightarrow \text{according to loop} = I = \frac{V}{R} = \frac{140 - 85}{21} = \frac{55}{21} = 2.65 \text{ A}$$

$$\rightarrow V_A = V_{TH}$$

(using nodal analysis)

$$\begin{aligned} I &= \frac{140 - V_A}{30} ; \quad 30(0.55) = 140 - V_A \\ 16.5 &= 140 - V_A \\ V_A &= 123.5 \text{ V} \end{aligned}$$

$$I = \frac{V_{TH}}{R_{eq} + R_L}$$

$$\rightarrow I = \frac{123.5}{21+5} = \frac{123.5}{26} = 4.75 \text{ A (For } 5\Omega)$$

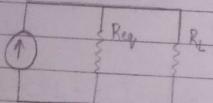
$$\rightarrow I = \frac{123.5}{21+15} = \frac{123.5}{36} = 3.43 \text{ A (For } 15\Omega)$$

$$\rightarrow I = \frac{123.5}{21+50} = \frac{123.5}{71} = 1.73 \text{ A (For } 50\Omega)$$

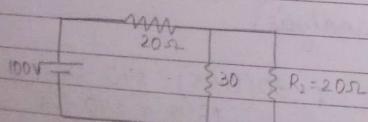
### # Norton's Theorem

- $R_{eq} / I_n$

$I_n = I_{sc}$  (short circuit current)

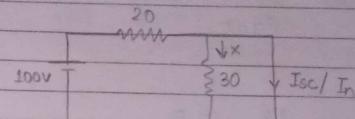


Find the current in  $20\Omega$  resistor using norton's theorem



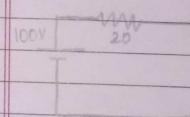
P1: Remove the lead resistance & short circuit

the two terminals & calculate this short circuit current ( $I_n / I_{sc}$ ).



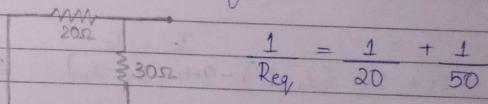
$\rightarrow$  Current doesn't flow through  $30\Omega$  as there is better path which doesn't have any resistance i.e. directly to path of short circuit.

If resistance is there on other branches  
ex: then it flows through both the resistors.



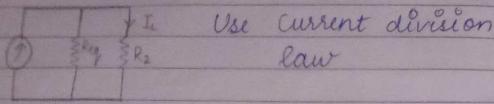
$$V = IR \rightarrow I_n = \frac{V}{R} = \frac{100}{20} = 5 \text{ A}$$

Step 2: Find the value of  $R_{eq}$  across the terminal



$$R_{eq} = \frac{30 \times 20}{50} = \frac{600}{50} = 12 \Omega$$

Step 3 → Find the Norton equivalent circuit



$$I_L = \frac{R_{eq}}{R_{eq} + R_2} \cdot I_{in} = \frac{12}{12+20} \times 5 \text{ mA}$$

$$= \frac{12 \times 5}{32} = \frac{60}{32} = 1.875 \text{ A}$$

Use current division law

$$\text{II) } -2.4(I_1 - I_2) = 120$$

$$-2.4I_1 + 2.4I_2 = 120$$

~~$$-18.4I_1 - 2.4I_2 = -26$$~~

~~$$-2.4I_1 + 2.4I_2 = 120$$~~

$$16I_1 = 94$$

$$\therefore I_1 = 5.875 \text{ mA}$$

# Maximum Power Transfer :-

- 1) Maximum power transfer theorem is used to determine the conditions under which maximum power can be transferred from source to load.
- 2) Maximum power will be transferred if equivalent resistance = load resistance. ( $R_{eq} = R_L$ )
- 3) For the Thevenin equivalent circuit is given

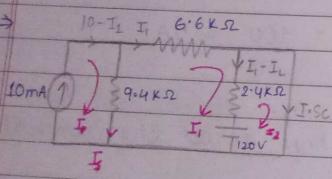
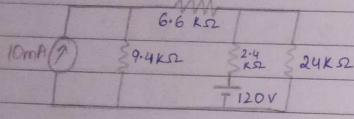
$$I_L = \frac{V_{TH}}{R_{eq} + R_L}$$

• L for max power  $I_{Lmax} = \frac{V_{TH}}{2R_{eq}}$  ? max current

4) Maximum power is given by

$$P_{max} = I^2_{max} R_{eq}$$

Ques For the network shown in the figure derive the Norton equivalent circuit & find the current through  $24\text{ k}\Omega$  resistor.



$$I_{in} = I_{sc}$$

$$R_{eq} = 6.6I_1 + 2.4(I_1 - I_2) - 9.4(10 - I_1) = -120$$

$$6.6I_1 + 2.4I_1 - 2.4I_2 - 94 + 9.4I_1 = -120$$

$$18.4I_1 - 2.4I_2 = -120 + 94$$

$$18.4I_1 - 2.4I_2 = -26$$

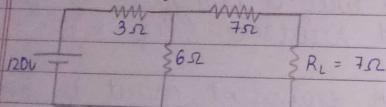
$$P = \frac{V_{TH}}{2R_{eq}} \times \frac{V_{TH}}{2R_{eq}} \times R_{eq} = \left[ \frac{V_{TH}^2}{4R_{eq}} \right]$$

Total power delivered from source under this condition is :

$$P_T = V_{TH} \cdot I_{max}$$

$$P_T = \frac{V_{TH}}{2R_{eq}} \times \frac{V_{TH}}{2R_{eq}} \times 2R_{eq} = \left[ \frac{V_{TH}^2}{4R_{eq}} \right]$$

Ques Find the current in load resistance. What is max power of  $R_L$  if it varies. Also find power absorbed by load if  $R_L = 7 \Omega$  &  $11 \Omega$



\* consider  $R_{eq}$  only, don't use  $R_L$ 's value

Sol-1) Remove load resistance

$$V_{TH} = \frac{6}{3+6} \times 12 = \frac{2 \times 6}{9} \times 12 = 8V.$$

$$2) R_{eq} = 7 + \left( \frac{6}{6+3} \right) = 7 + \left( \frac{6 \times 3}{6+3} \right) = 9\Omega$$

$$3) I_{max} = \frac{8}{9+9} = \frac{8}{18} = 0.44A$$

$$(ii) R_L = 7\Omega \quad \& \quad R_L = 11\Omega$$

$$\rightarrow I_{max} = \frac{8}{9+7} = \frac{8}{16} = 0.5A$$

$$\rightarrow P_{Lmax} = I_{max}^2 \times R_L$$

$$= \frac{0.5^2}{10} \times 7 \times \frac{0.5^2}{10} = \frac{7}{4} = 1.75A$$

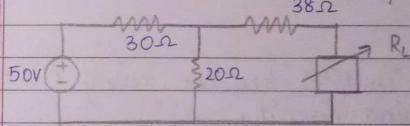
$$D) R_L = 11\Omega$$

$$I_{max} = \frac{8}{9+11} = 0.4A$$

$$P_{Lmax} = I_{max}^2 \times R_L$$

$$= 0.4 \times 0.4 \times 11 = 1.76A$$

Ques Find the value of  $R_L$  for max power transferred also determine the max power transferred.



$$\rightarrow V_{TH} = \frac{20}{20+30} \times 50 = \frac{20}{50} \times 50 = 20V$$

$$\rightarrow R_{eq} = 38 + \left( \frac{30 \times 20}{30+20} \right) = 38 + \left( \frac{600}{50} \right) = 50\Omega$$

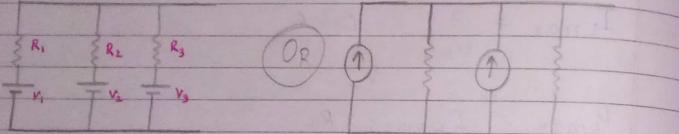
$$R_{eq} = R_L$$

$$\hookrightarrow I_{Lmax} = \frac{20}{50+50} = \frac{20}{100} = 0.2A$$

$$P_{Lmax} = 0.2 \times 0.2 \times 50 = 2V$$

$$= \frac{0.2}{10} \times \frac{0.2}{10} \times 50 + 0$$

# Millman's Theorem :-



$$V_m = \frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3}$$

$$R_m = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}}$$

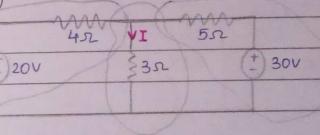
$$Sol \Rightarrow R_m = \frac{1}{\frac{1}{1} + \frac{1}{2} + \frac{1}{3} + \frac{1}{10}} = \frac{1}{1 + 0.5 + 0.3 + 0.1} = 0.52 \Omega$$

$$= 0.52 \Omega$$

$$V_m = \frac{1 + \frac{2}{2} + \frac{3}{3} + 0}{1 / 0.52} = \frac{1 + 1 + 1}{0.52} = \frac{3}{0.52} = 1.54V$$

7/12/24

Ques Calculate the current  $I$  shown in the figure below using millman's theorem.



\* convert into millman form.

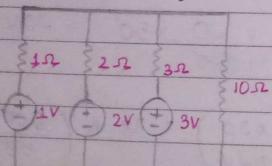
$$Sol \Rightarrow V_m = \frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3}$$

$$R_m = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}}$$

$$R_m = \frac{1}{\frac{1}{4} + \frac{1}{3} + \frac{1}{5}} = \frac{1}{0.783}$$

$$= 1.277$$

Calculate current in  $10\Omega$  resistor using Millman's Theorem for following circuit.



$$V_m = \frac{20}{4} + \frac{30}{5} = \frac{5+6}{1} \times 1.277$$

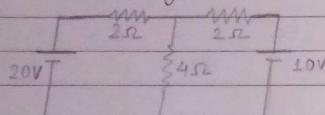
$$\frac{1}{1.277} = \frac{11}{0.783} = 14.048$$

$V_m = IR$  ( $R = \frac{V}{I}$  resistance question mein nikalne ko bura hoga)

$$\frac{14.048}{3} = I \rightarrow [4.68 A]$$

### # Super Position Theorem (V.V. Imp)

Ques Calculate the current in each branch in the figure given below using super position theorem.



Step 1: □ S.P.T is applicable to circuit having more than one source (ya I ya voltage)

□ Short voltage source / open the I source, one at a time.

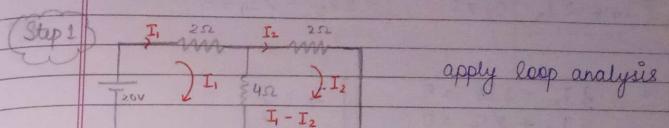
2: □ Calculate the current in each branch / required branch.

$$I_3 = 3A \quad I_4 + 1.11 = 0$$

$$I_4 = 2A$$

$$I_B = (I_1 - I_2) + (I_3 - I_4) \quad I_c = I_2 - I_3$$

$$I_a = I_1 - I_4$$



$$2I_1 + 4(I_1 - I_2) = 20 \quad | \quad 2I_2 - 4(I_1 - I_2) = 0$$

$$2I_1 + 4I_1 - 4I_2 = 20 \quad | \quad 2I_2 - 4I_1 + 4I_2 = 0$$

$$6I_1 - 4I_2 = +20 \quad | \quad 6I_2 - 4I_1 = 0$$

$$3I_1 - 2I_2 = +10 \quad | \quad 3I_2 - 2I_1 = 0$$

$$(3I_1 - 2I_2 = 10) \times 2$$

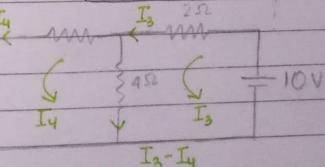
$$(-2I_1 + 3I_2 = 0) \times 3$$

$$6I_1 - 4I_2 = 20 \quad | \quad 3(4) - 2I_1 = 0$$

$$-6I_1 + 9I_2 = 0 \quad | \quad \frac{12}{2} = I_1$$

$$5I_2 = 20 \quad | \quad I_1 = 6A$$

$$I_2 = 4A \quad | \quad$$



$$\begin{array}{l|l}
 2I_4 - 4(I_3 - I_4) = 0 & 2I_3 + 4(I_3 - I_4) = 10 \\
 2I_4 - 4I_3 + 4I_4 = 0 & 2I_3 + 4I_3 - 4I_4 = 10 \\
 -2I_4 = 4I_3 & 6I_3 - 4I_4 = 10 \\
 -2I_4 - 4I_3 = 0 & 2(3I_3 - 2I_4) = 10 \\
 -2(I_4 + 2I_3) = 0 &
 \end{array}$$

$(I_4 + 2I_3 = 0) \times 2$

$$3I_3 - 2I_4 = 5$$

$$\begin{array}{l}
 3I_3 - 2I_4 = 5 \\
 4I_3 + 2I_4 = 0 \\
 7I_3 = 5
 \end{array}
 \quad \boxed{I_3 = \frac{5}{7}}$$

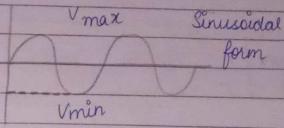
$$3I_3 - 2I_4 = 5$$

$$\boxed{I_3 = \frac{5}{7}}$$

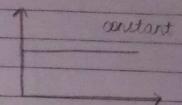
## Unit-2 : A.C. Circuits & CRO

# Notes :

- AC (alternating current)

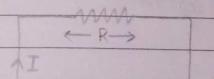


- Direct Current



Co-sinusoidal

# AC through pure Resistor :-



→ wave form

always in  
pure  
resistor

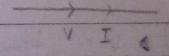


$$V = V_{\max} \sin \omega t$$

$$I = I_{\max} \sin \omega t$$

$$\omega = 2\pi f$$

→ Phasor form



$$V = V_m < 0$$

(inline)

$I = I_m < 0$   $\triangleright$  Voltage & current are inline & the angle b/w them is zero

\*  $|V=IR|$ , power absorbed is given by  $[P=VI]$

$$V_{rms} = \frac{V_{max}}{\sqrt{2}}$$

$$I_{rms} = \frac{I_{max}}{\sqrt{2}}$$

Ques At 250V, 50Hz voltage is applied across a circuit consisting of pure resistance of  $20\Omega$ .

Determine the following :-

- 1) Current through the circuit
- 2) Power absorbed by circuit
- 3) Give expression for voltage & current
- 4) Give the wave & phasor diagram.

13th Feb

$$\Rightarrow 1) V=IR$$

$$250V = I \times 20\Omega$$

$$\frac{250}{20} = I \Rightarrow I = 12.5A$$

$$2) P=VI$$

$$= 250 \times \frac{12.5}{10} = 3125$$

$$3) \bullet V = \frac{V_{max}}{\sqrt{2}} \rightarrow V_{max} = V \times \sqrt{2}$$

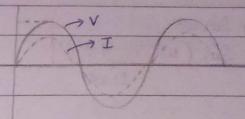
$$V_{max} = 250 \times \sqrt{2}$$

$$= 353.553V$$

$$\bullet I_{max} = I \times \sqrt{2} = 12.5 \times \sqrt{2}$$

$$= 17.67A$$

4)  $V_{max}$



$$\omega = 2\pi f$$

$$= 2 \times 3.14 \times 50 = \frac{2 \times 3.14 \times 50}{20\pi} = 314$$

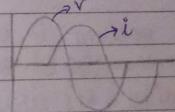
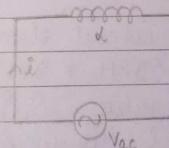
$$V \quad I$$

# AC through pure Inductor

$$V-I=DC$$

$$V-i=AC$$

$$V_{ac}$$

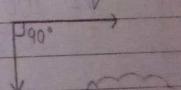


→ phasor form

$$V = V_{max} \sin \omega t$$

$$i = I_{max} \sin (\omega t + 90^\circ)$$

lags



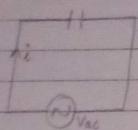
?  $P_a = 0$

$$V = IR \quad X_L \quad \therefore V = I X_L$$

$$X_L = \omega \times L$$

$$\omega = 2\pi f$$

# AC through pure capacitor



$$V = V_{max} \sin \omega t$$

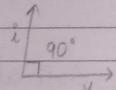
$$I = I_{max} \sin(\omega t + 90^\circ)$$

leads

$$X_C = \frac{1}{\omega C}, \quad \omega = 2\pi f \rightarrow \text{wave form}$$

$$V = I X_C$$

$\rightarrow$  Phasor form



The voltage & current through circuit elements are  $V = 100 \sin 314t$  and  $I = 10 \sin(314t + 315^\circ)$ . Identify the circuit element. Find value of inductive reactance, value of inductance & frequency.

$$V = 100 \sin 314t$$

$$I = 10 \sin(314t + 315^\circ)$$

$$\text{angle} = 315^\circ$$

lies in 4th quad

$\therefore$  inductor

$$\rightarrow \omega = 314, \quad V_{max} = 100, \quad I_{max} = 10$$

$$X_L = \omega \times L$$

$$10 = 314 \times L$$

$$\frac{10}{314} = L$$

$$\downarrow$$

$$V_{max} = I_{max} \times X_L$$

$$100 = 10 \times X_L$$

$$\frac{100}{10} = X_L \rightarrow 10$$

$$d = 0.031$$

$$\omega = 2\pi f \rightarrow 2 \times 3.14 \times f = 314$$

$$f = \frac{314}{2 \times 3.14} \times \frac{100}{50}$$

$$f = 50 \text{ Hz}$$

$m \leftarrow 10^{-3}$	$10^3 \rightarrow \text{kilo}$
(micro) $\mu \leftarrow 10^{-6}$	$10^6 \rightarrow M$
(nano) $n \leftarrow 10^{-9}$	$10^9 \rightarrow G$
pico $\leftarrow 10^{-12}$	$10^{12} \rightarrow$

Ques 50 Hz / 230V is applied across a pure capacitive circuit having capacitance of  $26.5 \mu F$ . Show voltage & I in a time diagram (wave form), also calculate the reactive capacitance in circuit.

$$\text{Sol} \Rightarrow f = 50 \text{ Hz}, \quad V_{rms} = 230 \text{ V}, \quad C = 26.5 \mu F = 26.5 \times 10^{-6} \text{ F}$$

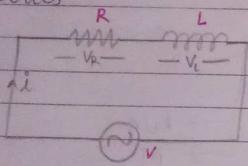
$$\rightarrow \omega = 2\pi f \\ = 2 \times \frac{314}{100} \times 50 = 314$$

$$\rightarrow X_C = \frac{1}{\omega C} \rightarrow \frac{1}{314 \times 265 \times 10^{-6}} = \frac{10^6 \times 10}{314 \times 265} \\ = 120.17 \Omega$$

14th Feb

# AC through R, L circuit

→ Series



$$V = V_{max} \sin \omega t$$

$$I = I_{max} \sin(\omega t - \phi)$$

$$V = IZ \rightarrow \text{impedance}$$

→ phasor diagram:

$$Z = R + jX_L \quad \text{Imaginary term}$$

$$|Z| = \sqrt{R^2 + X_L^2}$$

$$V^2 = V_R^2 + V_L^2$$

$$\phi = \tan^{-1} \left( \frac{X_L}{R} \right)$$

► Power Factor =  $\cos \phi = \frac{R}{Z} \rightarrow$  resistance  
 $\rightarrow$  impedance

► apparent power =  $VI$

►  $P_r$  (True/Real Power) =  $VI \cos \phi$

►  $P_r$  (reactive power) =  $VI \sin \phi$

► Q-Factor =  $\frac{1}{\text{power factor}} = \frac{Z}{R}$  or  $\frac{1}{R} \sqrt{\frac{L}{C}}$

Ques A  $4\Omega$  resistor is connected to a  $10mH$  inductor across a  $100$  volts  $50$  Hz voltage source. Find input current, voltage drop across resistor & inductor, power factor of the circuit & the real power consumed in the circuit?

Sol  $\Rightarrow R = 4\Omega, L = 10 \times 10^{-3}, V_{rms} = 100, f = 50 \text{ Hz}$ ,  
 $I = ?$ ,  $V_R = ?$ ,  $V_L = ?$ ,  $P.f. = ?$ ,  $P.t. = ?$

$$V = IZ \quad Z = \sqrt{R^2 + X_L^2} \quad V = IZ$$

$$100 = I \cdot 5.08$$

$$X_L = \omega L \quad \omega = 2\pi f = 2 \times \frac{314 \times 50}{100} = 314$$

$$X_L = \frac{314 \times 10}{100} = 31.4$$

$$\rightarrow Z = \sqrt{(4)^2 + (3\pi 4)^2} = \sqrt{16 + 9 \cdot 859} = \sqrt{25.859}$$

$$= 5.08$$

19.68

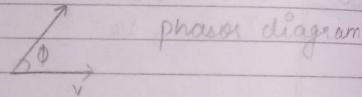
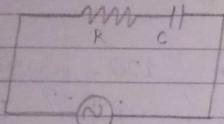
$$\rightarrow V_R = I \times R = 19.6 \times 4 = 78.4$$

$$\rightarrow V_L = I \times X_L = 19.6 \times 3\pi 4 = 61.79$$

$$\rightarrow P.F. = \frac{R}{Z} = \frac{4}{5.08} = 0.78$$

$$\rightarrow P.t = VI \cos \phi = \frac{100 \times 19.68}{100} \times \frac{0.78}{100}$$

- # AC through RC circuit
- phasor diagram (wrt I)
  - phasor diagram of voltage in opposite direction.



$$V = IZ$$

$$\phi = \tan^{-1} \left( -\frac{X_C}{R} \right)$$

$$Z = \sqrt{R^2 + (X_C)^2}$$

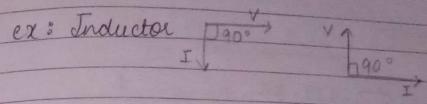
$$Z = R - j X_C$$

$$V = V_{max} \sin \omega t$$

$$I = I_{max} \sin (\omega t + \phi)$$

$$V^2 = V_R^2 + V_C^2$$

# Phasor diagram for voltage is exactly opposite to the phasor diagram we have drawn.



16th Feb

Ques

A supply of 400V, 50 Hz is applied to a series RC circuit. Find the value of capacitor if the power absorbed by the resistor is 500W at 150V. Also find what is energy stored in the capacitor.

Sol ⇒

$$V = 400V$$

$$F = 50 \text{ Hz}$$

$$C = ?$$

$$P_a = V_R I \rightarrow V_R = 150V \\ (\text{resistor})$$

$$\rightarrow I = \frac{P_a}{V_R} = \frac{500}{150} = 3.33A$$

$$\rightarrow V^2 = V_R^2 + V_C^2 \\ = (400)^2 = (150)^2 + V_C^2$$

$$V_C = \sqrt{137500} = 370.80$$

$$\rightarrow V_C = I X_C \\ 370.80 = 3.33 \times X_C$$

$$\frac{370 \cdot 80}{3.33} = X_C$$

$$\Rightarrow X_C = 111.35$$

$$\Rightarrow X_C = \frac{1}{\omega C} \rightarrow 111.35 = \frac{1}{2 \times 3.14 \times 50 \times C}$$

$$\Rightarrow 111.35 = \frac{1}{314 \times C}$$

$$\Rightarrow 111.35 \times 314 \times C = \frac{1}{111.35 \times 314}$$

$$C = 0.0000286009$$

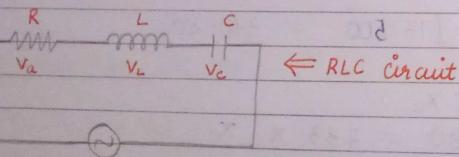
$$C = 0.286 \times 10^{-3} \text{ m}\mu\text{F}$$

$$= 28.60 \mu\text{F}$$

Q) Energy stored in capacitor is =  $\left[ \frac{1}{2} C V_C^2 \right]$

$$= \frac{1}{2} \times (370.8)^2 \times 0.0000286009 = 1.966 \text{ J}$$

# AC through RLC Circuit



Date \_\_\_\_\_  
Page \_\_\_\_\_

classmate  
Date \_\_\_\_\_  
Page \_\_\_\_\_

$$V = V_{\max} \sin \omega t$$

$$i = I_{\max} \sin (\omega t \pm \phi)$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$\phi = \tan^{-1} \left( \frac{X_L - X_C}{R} \right)$$

$$V^2 = V_R^2 + (V_C - V_L)^2$$

\* Note

- 1) If  $X_L$  is greater than  $X_C \rightarrow$  lags  
 $X_L < X_C \rightarrow$  leads  
 $X_L = X_C \rightarrow$  in-line

Ques (Imp) A coil of resistance  $20\Omega$  and inductance  $100\text{mH}$  is connected in series with a capacitance of  $40\text{micro farad}$  across  $100\text{V}, 50\text{Hz}$  AC supply. Calculate:

- (a) Current in the circuit
- (b) Power factor
- (c) Phase angle
- (d) Voltage across each element.

Sol  $\Rightarrow$

$$V = 100 \text{ V}$$

$$f = 50 \text{ Hz}$$

$$R = 20 \Omega$$

$$L = 100 \text{ mH} = 0.100 \text{ H}$$

$$V = IZ$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$X_L = \omega L$$

$$X_L = \frac{2\pi f L}{7} = \frac{2 \times 22}{7} \times 50 \times 0.100$$

$$X_L = 31.428$$

$$X_C = \frac{1}{\omega C}$$

$$= \frac{1}{2\pi f \times 40}$$

$$= \frac{1}{2 \times 3.14 \times 50 \times 40}$$

$$X_C = 79.61$$

$$Z = \sqrt{(20)^2 + (31.4 - 79.61)^2}$$

$$= \sqrt{400 + (2323.24)}$$

$$= \sqrt{2723.24}$$

$$Z = 52.19$$

$$\begin{aligned} V &= IZ \\ 100 &= I \times 52.19 \end{aligned}$$

$$(a) I = 1.91$$

$$(b) \frac{R}{Z} = P.F$$

$$\frac{20}{52.19} = 0.38$$

$$P.F = 0.38$$

$$(c) \cos \phi = P.F$$

$$\cos^{-1}(0.38) = 67.66^\circ$$

$$\phi = 67.66^\circ$$

$$(d) V_R = \frac{I \times R}{I \cdot 91 \times 20} = 38.2 V$$

$$\begin{aligned} V_L &= I \times X_L \\ &= 1.91 \times 20 = 59.97 V \end{aligned}$$

$$\begin{aligned} V_C &= I \times X_C \\ &= 1.91 \times 79.61 = 152.05 V \end{aligned}$$

Ques A coil with resistance 50 ohms is connected with a capacitor in series across 220 volt supply. The circuit has the capacitance of  $20 \mu F$ . Calculate the inductive reactance of 3.5.

- Frequency in the circuit if  $W = 75$ .
- The voltage across capacitor if voltage across inductor is 100 volts ( $V_L = 100V$ ).
- power factor

23rd Feb 2024

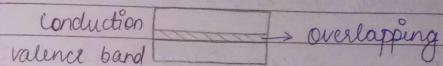
### Unit-3 : Semiconductor

# Energy band gap in materials :-

conductor      insulators      semi-conductor

#### D [Conductor]

→ The valence band & conductor band overlap each other & has no band gap energy & thereby has maximum conduction.

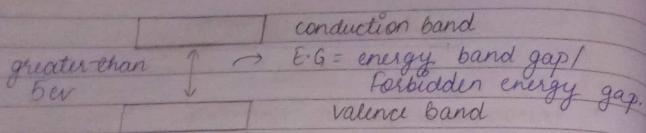


→ The electrons are free to move without any external energy source

→ Ex: metals

#### D [Insulator]

→ The valence band & conduction band has a large energy band gap (generally  $> 5eV$ ) such that electrons from valence band can't jump to conduction band whatever is possible.



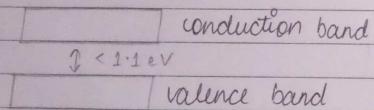
Ex: wood

#### D) Semi-conductor

→ A material which acts as an insulator as well as a conductor depending upon certain parameters like external energy is known as a semi-conductor.

→ Energy band gap b/w valence band & conduction band is less than ( $< 1.1 \text{ eV}$ ).

→ By applying some external energy electrons from valence band can jump to the conduction band & the material can act like a conductor.



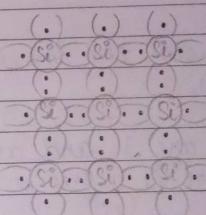
A semi-conductor acts as an insulator at absolute zero temperature i.e.  $[0^\circ \text{K}]$

Ex - silicon, germanium etc.

#### # Types of semi-conductors.

##### D) Intrinsic Semi-conductor

- 1) A semi conductor which is ~~purely~~ formed purely from the carbon family (group 4 elements) without any mixture is an intrinsic s.c.
- 2) Silicon is the most used semi-conductor because of its vast & free availability than germanium.



##### D) Extrinsic Semi Conductor

~ Doping = The process of adding impurity is known as doping.

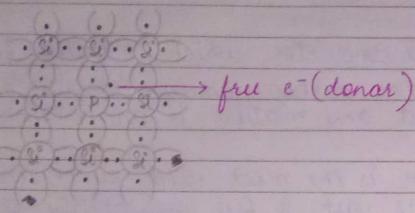
1) There are 2 types of extrinsic semi-conductor :

a) n-type extrinsic semi conductor

→ In N-type extrinsic semi conductor the impurity is added from group 5 elements.

→ The valence e<sup>-</sup>s are 5 and are known as

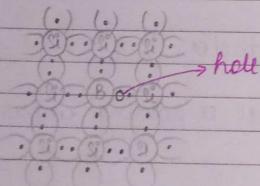
penta-valent. Therefore, an extra electron is available (extra  $e^-$  for conductivity).



### b) P-type semi-conductor

→ In p-type semi-conductor the impurity is added from group 3 elements.

→ The valence electrons are 3 and are known as trivalent. Therefore there is a free space.



\* hole is the free space

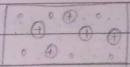
\* it is an acceptor

### # Elemental vs Compound Semiconductor

→ Semiconductor made of single elemental such as silicon, germanium are known as elemental semi-conductors.

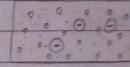
→ Semiconductors made of several elements such as the combination of group 3 or 5 / group 2 & 6 elements are known as compound semi-conductors.  
Eg - GaAs

### # N-type



Majority  $\rightarrow \cdot$  (-ve)  
Minority  $\rightarrow \circ$  (+ve)

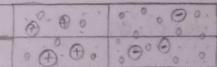
### P-type



Majority  $\rightarrow \oplus$  (+ve)  
Minority  $\rightarrow \ominus$  (-ve)

$\oplus \rightarrow$  Donor ions (fixed)  
(In mobile)

$\ominus \rightarrow$  Acceptor ions

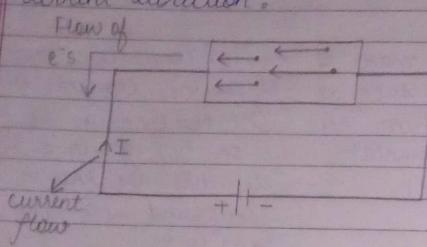


p-n junction

### # Flow of $e^-$ / Current in semi-conductor

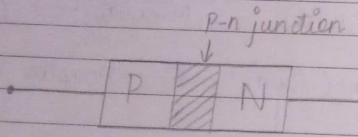
① The flow of  $e^-$  is always opposite to the conventional

current direction.



### # P-N Junction

- ① When a p & n-type material are brought together a junction is formed between the two known as p-n junction and a basic diode is created.
- ② A diode is a device that conducts current in only one direction.

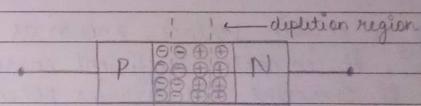


### \* Practical Vs Ideal Junction

- ① Ideal diode draws no current when reverse biased.
- ② Ideal diode offers infinite resistance when reverse biased.
- ① Practical diode draws very low current when reverse biased.
- ② Practical diode offers very high resistance when reverse biased.

### # Formation of depletion region

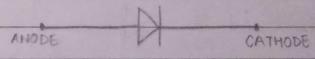
- ① Free electrons near the junction begin to diffuse with holes.
- ② The N-region loses electrons and creates a positively charged layer near the junction.
- ③ The P-region loses holes and creates a negatively charged layer near the junction.
- ④ The two layers forms the depletion region.



- ⑤ The depletion layer acts as a potential barrier for further movement of electrons across the junction.

→ The barrier potential for  $Si = 0.7V$  &  $Ge = 0.3V$

- ⑥ The component form is known as a p-n junction diode.

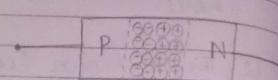


DIODE SYMBOL

## # Biasing a diode

→ No-Bias

Add equilibrium or no-bias :



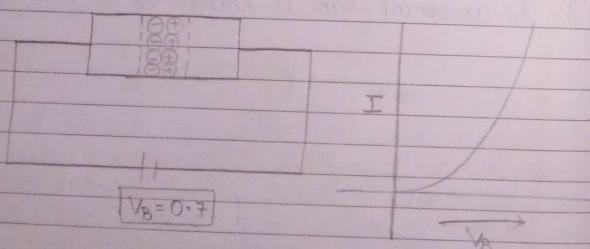
→ Forward-Bias

① In forward bias condition P-type is connected to +ve terminal & N-type to -ve terminal of the battery.

② On applying a certain voltage, known as bias voltage ( $V_B$ ), it imparts sufficient energy to free electrons to overcome the barrier potential and move through their p-region.

③ The depletion region narrows.

④ On increasing the voltage, huge current flows through the diode.

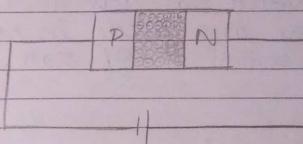


→ Reverse Biasing

① In reverse bias condition, n-type is connected to positive terminal & p-type is connected to negative side of battery.

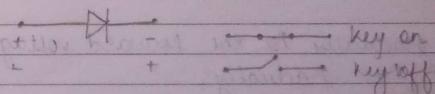
② On applying voltage, diode exhibits negligible energy & the movement of e-s are ideally blocked.

③ The depletion region widens

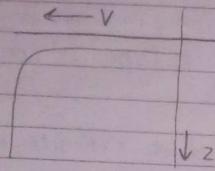


④ There are few thermally generated minority carriers in both p and n region. These minority carriers are drifted towards p-n junction & a very small amount of current flows through a diode.

This current is known as reverse saturation current.



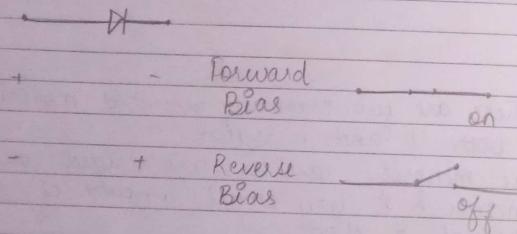
### → Reverse characteristics



### \* Note:

Diode as a switch.

A diode in forward bias acts as a switch in on state where as a diode in reverse bias acts as a switch in off state.



### # Effect of temperature on VI characteristics of diode

#### ① Forward characteristics

- As we gradually increase the forward voltage, a forward current increases gradually.

- b) When the forward voltage is increased to a value known as knee voltage, the forward current begins to increase rapidly.

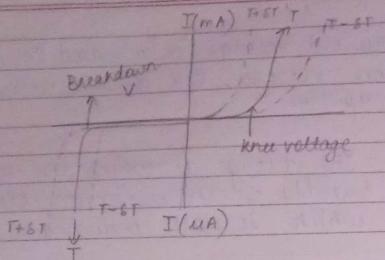
Knee Voltage : The voltage at which the current starts to increase rapidly or the minimum voltage applied to a diode for which it starts conducting.

#### ② Reverse characteristics

- As we gradually increase the reverse bias voltage, a very small reverse current flows across the diode.
- When the applied reverse bias voltage is increased to a value where the reverse voltage across the diode reaches breakdown value, the reverse current increases rapidly.

#### ③ Effect of Temperature

- If temperature increases the conductivity also increases and the resistance of diode decreases, whereas if the temperature decreases the conductivity decreases and the resistance of the diode increases.



## # Diode equation (Shockley's Equation)

The diode equation:

$$I_D = I_s (e^{\frac{V_D}{nV_T}} - 1)$$

where,

$I_D = I$  → It is the diode current

$I_s = I_0$  → It is the reverse saturation current

$V_D = V$  → It is the diode voltage (applied voltage)

$n \rightarrow$  It is the Ideality factor

For Silicon  $n = 2$

Germanium  $n = 1$

$V_T \rightarrow$  It is the thermal voltage given by

$V_D = +$  (forward bias)  
 $V_D = -$  (reverse bias)

$$V_T = \frac{kT}{q}$$

where  $k$  is the Boltzmann's Constant and it's value is  $k = 1.38 \times 10^{-23} \text{ J/K}$ .

$T$  is the Temperature and  $q$  is the charge given by  $q = 1.61 \times 10^{-19} \text{ C}$

\* Note

At room temperature  $V_T = 26 \text{ mV}$

\* Ques: A Germanium diode carries a current of one mA at room temperature, when a forward bias voltage of 0.15 V is applied. Estimate the reverse saturation current at room temperature.

Sol = Germanium

$$\eta = 1$$

$$I_D = 1 \times 10^{-3}$$

$$V_T = 26 \times 10^{-3}$$

$$V_D = 0.15$$

$$I_0 = ?$$

$$I_D = I_s (e^{\frac{V_D}{nV_T}} - 1)$$

$$1 \times 10^{-3} = I_s (e^{0.15 / 1 \times 26 \times 10^{-3}} - 1)$$

$$\frac{1 \times 10^{-3}}{(e^{V_D/26 \times 10^{-3}} - 1)} = I_S$$

$$\Rightarrow \frac{1 \times 10^{-3}}{319.291} = I_S$$

$$\Rightarrow 3.13 \times 10^{-6} = I_S$$

Ques For what voltage will the reverse current of a Germanium diode reach 99% of its saturation value at room temperature.

Sol \* For Ge

$$n = 1$$

$$V_T = 26 \times 10^{-3}$$

$$I_0 = ?$$

$$I = 99\% \text{ of } I_0 = -99 \times I_0 / 100$$

$$\Rightarrow I_D = I_S (e^{V_D/n V_T} - 1)$$

$$\Rightarrow \frac{-99}{100} \times I_0 = I_0 (e^{V_D/1 \times 26 \times 10^{-3}} - 1)$$

$$\Rightarrow \frac{-99}{100} = e^{V_D/1 \times 26 \times 10^{-3}} - 1$$

$$\Rightarrow 0.01 = e^{V_D/26 \times 10^{-3}}$$

Take log on both sides

$$\log(0.01) = \log \frac{V_D}{26 \times 10^{-3}}$$

$$\log(-2 \times 26 \times 10^{-3}) = V_D$$

$$\boxed{V_D = -0.052}$$

After taking log on both sides left side will remain as it is  
right side will change sign  
i.e.  $(e)$  cut jayega

Ques What is the ratio of current for a forward bias of 0.05 V to the current for the same magnitude of reverse bias.

→ If diode isn't given, assume either germanium or silicon. (Do this question in assignment)

Ques If a silicon diode is operating at a temperature of  $95^\circ C$  & operating voltage of 0.8 V. Calculate the forward current if the reverse current is  $2.5 \text{ mA}$ .

Sol  $\Rightarrow I_0 = 2.5 \times 10^{-6}$

$$I = I_0 (e^{V_D/n V_T} - 1)$$

$$I = 2.5 (e^{0.8/2 \times 10^{-6}} - 1)$$

$$V_T = \frac{kT}{q}$$

$$V_T = \frac{1.38 \times 10^{-23} \times 300}{1.62 \times 10^{-19}}$$

$$V_T = 0.0269$$

$$V_T = 2.64 \times 10^{-9}$$

$$I = 2.5 \times 10^{-6} (e^{2.64/2 \times 2.64 \times 10^{-9}} - 1)$$

$$I = 2.5 \times 10^{-6} (38,03,815.315 - 1)$$

$$I = 9.50$$

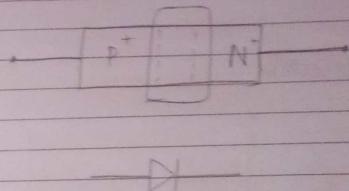
### # Zener Diode

① If it is fabricated to be operated in breakdown region.

When operated in breakdown it maintains a constant voltage.

⑥ The diode is formed by heavily doping n-type & p-type materials or both.  $p^n$

⑦ The depletion region narrows and the electric field is very high, doped material, by using heavily.



### # Breakdown Mechanism

Breakdown are of two types :

- 1) Avalanche breakdown
- 2) Zener Breakdown

#### ▷ Avalanche Breakdown

- a) It is observed in p-n junction diode as well as Zener diode, generally for a reverse voltage of  $> 6V$ , ie.  $V_R > 6V$ .
- b) The carrier increase is the result of collisions, the result of electric field

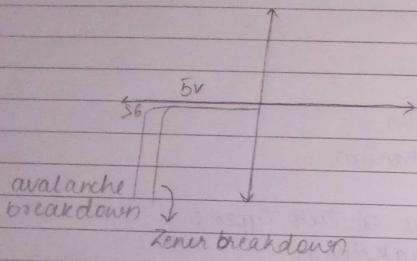
#### ▷ Zener Breakdown

- a) It is observed in zener diodes at a voltage  $\leq 6V$ .
- b) The carrier increase is the result of collisions, the result of electric field

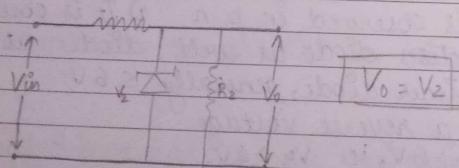
(e<sup>-</sup> collide with crystal atom and knocks it off, forming/creating e<sup>-</sup> holes. Carrier multiplication takes place).

- c) It destroys the diode.  
(burnt off).      c) The diode is discovered.

#### # V-I characteristics

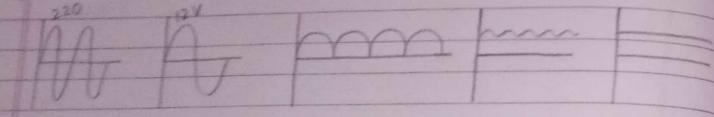
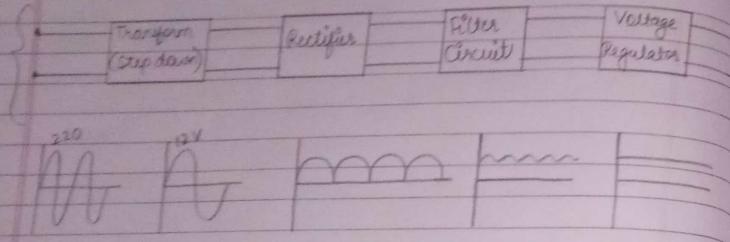


#### # Zener diode as Voltage regulator



~ A Zener diode can be used as a voltage regulator by placing it in parallel to the output and in reverse bias condition.

## # AC to DC Generator

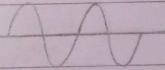
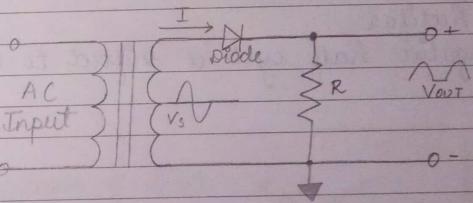


3rd April

## # Rectifier

- ① Rectifier is a device / circuit which converts AC input to pulsating DC.
- ② all the negative cycles are eliminated either by zero value or by a +ve value.
- ③ Rectifiers are of two types :
  - a) Half wave Rectifier

- i) It uses a single diode.
- ii) The negative half cycle is clipped and only the +ve half cycle remains

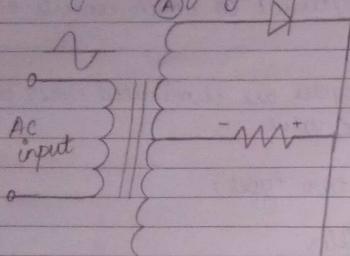


## (b) Full Wave Rectifier

They are of two types :

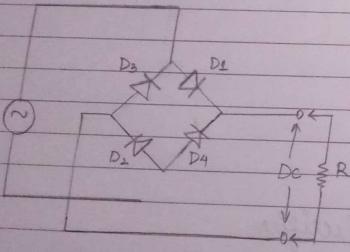
### i) Center Tap Full Wave Rectifier

→ The negative half cycle is shifted to the positive half.



### ii) Bridge Rectifier

→ The negative half cycle is shifted to the positive half.



→ For positive half cycle, diode D<sub>1</sub> & D<sub>2</sub> conducts,

i.e. they are in forward bias and D<sub>3</sub> & D<sub>4</sub> are in reverse bias (OFF).

→ For negative half cycle, D<sub>3</sub> & D<sub>4</sub> conducts, i.e. they are in forward bias and D<sub>1</sub> & D<sub>2</sub> are in reverse bias (OFF).

05/09/24

### \* Filter Circuit

→ Generally a capacitive filter circuit is used.  
→ The capacitor removes the large ripples & produces an output having small variations.

### \* Voltage Regulator

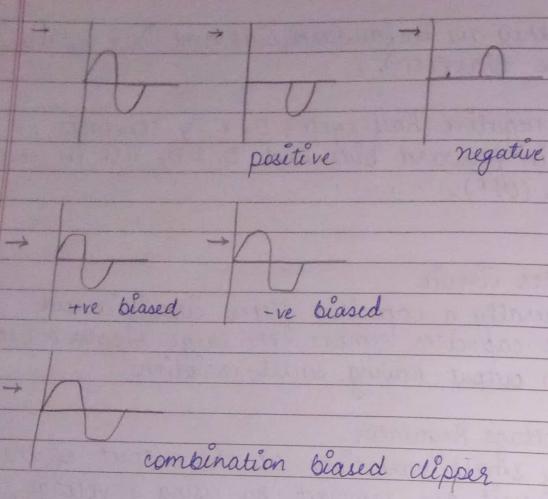
→ The small variations at the output of the filter circuit are removed by using a voltage regulator circuit or IC. (Integrated circuit)  
→ The output of the voltage regulator is constant.

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### # Applications of Diode

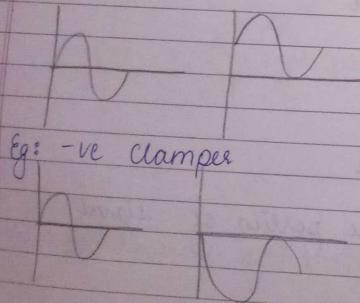
- Rectifier (already done)
- Clipper
- Clamper
- Voltage Multiplier

- Clipper: cut some portion of signal  
(soare signal ko ek side either +ve or -ve)



• **Clampers:** The positive & negative peaks of the signal can be placed at any desired value.

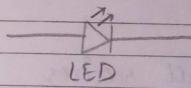
Eg: +ve clampers



• **Voltage multiplier:** It converts electrical power from a lower voltage to a higher voltage. Eg: voltage doubler ( $\times 2$ ), voltage tripler ( $\times 3$ ) etc.

### # Light Emitting Diode :- (LED)

(1) When  $e^-$  recombines with a hole, energy is released. In silicon and germanium this energy is in the form of heat. However, for some compound semi-conductors like gallium and arsenic, the energy released is in the form of light (photon). This happens by the phenomenon known as electroluminescence.



(2) It is used only in forward bias and the p-n junction is heavily doped.

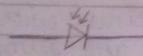
(3) Based on the semi-conductor material used and the amount of doping, an LED will emit a specific colored light. Eg: aluminium Gallium Arsenide (AlGaAs)-Infrared

- GaAsP = Red, orange, yellow
- AlGaP = Green
- InGaN = Blue, Blue-green near UV

### → Applications

- (1) Electronic Display
- (2) Remote Controls
- (3) Lightings

### # Photo Diode



\*Assignment Ques

Ques What is a Photo diode? Draw it's symbol and explain it's working principle.

### Applications:-

- (1) Infrared remote control receiver
- (2) Flame Detector
- (3) Photo detector

## Unit-4 Digital Electronics

10/04/24

### # Bipolar Junction Transistor (BJT)

- Invented by Dr. William Shockley and Dr. John Bardeen at Bell Labs:
- It is a semi-conductor device formed by sandwiching either p-type or n-type material between a pair of opposite type.
- The output voltage current and power are controlled by input current. Therefore BJT's are also known as current controlling device.
- The term Bipolar reflects the fact that both e<sup>-</sup>s and holes participate as charge carriers.

### # Types

BJT are of two types :

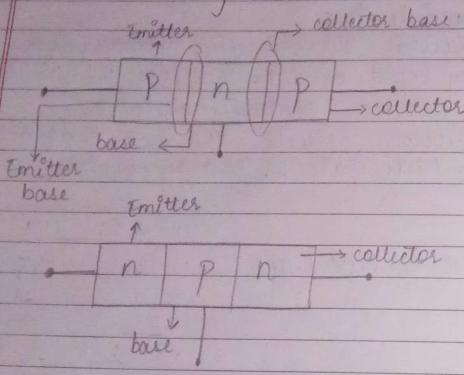
- 1. NPN
- 2. PNP

### # Construction :

- BJT is a three terminal device. The terminals are: emitter, base, collector.
- Emitter : → heavily doped  
→ emitter is charge carriers into base
- Base : lightly doped
- Collector : → intermediate doping (btw emitter and base)  
→ collector region is physically larger as compared to emitter and base.

→ collects charge carriers.

- BJT has two junctions:
- Emitter base junction
- Collector base junction



⇒ Symbol : npn      pnp

⇒ BJT Configurations :

- BJT can be configured in 3 different ways.

I Common base E — C — B

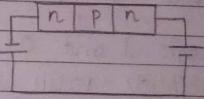
2 Common Emitter E — C — B

3 Common collector B — C — E

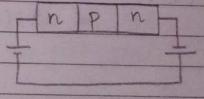
# Biasing a transistor / Transistor action / Region of operation

Class      Emitter Base Junction      Collector Base Junction      R.O      n-p-n circuit diagram

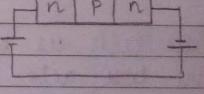
I      F.B      R.B      Active



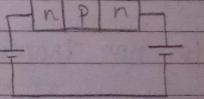
II      F.B      R.B      Saturation



III      R.B      F.B      Cut-off



IV      R.B      F.B      Inverted



### # Notes

- When a BJT is used in active region, we are dealing with analog electronics.
- When a BJT is used in saturation or cut-off region then we are dealing with digital electronics.

### ④ Logic

- There are 2 logic levels
  - Logic High (1)
  - Logic Low (0)

- Logic 1 and 0 does not necessarily mean the absolute value 1 and 0.  
ex:  $\geq 220V = 1$   
 $< 220V = 0$

### ④ Transistor BJT as a switch:

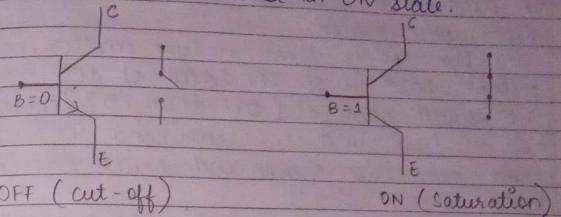
- Base tells us whether the switch is on or no.  
The base acts as a controlling element of the switch.

For npn transistor, if  
 $B=0$  (cut off) OFF  
 $B=1$  (saturation) ON

- Base = logic 0, the transistor is in cutoff region

and switch is said to be in OFF state.

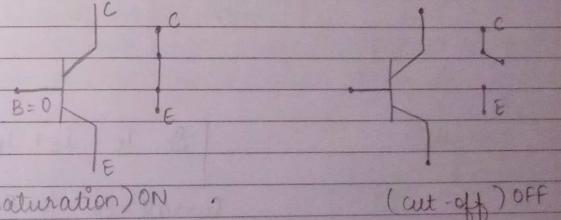
- Base = logic 1, the transistor is in saturation region and switch is said to be in ON state.



For pnp transistor, if  
 $B=0$  (saturation) ON  
 $B=1$  (cut off) OFF

- Base = logic 0, the transistor is in saturation region and switch is said to be in ON state.

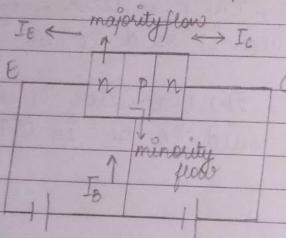
- Base = logic 1, the transistor is in cut off region and switch is said to be in OFF state.



### ④ Working Principle (npn transistor)

- A BJT is essentially used as an amplifier

- E-B junction in F.B and C-B junction is R.B.  
The F.B of E-B junction causes the emitter current to flow in the collector region through the lightly doped base region.
- The flow of  $e^-$  from n-type emitter into the p-type base is in the ratio of 100:5 i.e. 20:1 i.e. small no. of  $e^-$  (less than 5%) combine with hole in base and the remaining 95% tend to cross over base region and reach the collector region.
- When active mode/region, the current proportionally ↑ from the collector pin to the emitter pin.
- Conventional current in opposite to flow of  $e^-$ .



$$\text{So, } I_E = I_C + I_B$$

Current Eq<sup>n</sup> for BJT

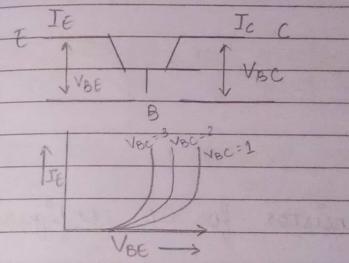
Input / Output (I/O) Characteristics of BJT / Transfer characteristics of BJT.

For Input characteristics :-

It is obtained with respect to input current and input voltage for a given value of output voltage.

# I/O of npn transistor in CB configuration :-

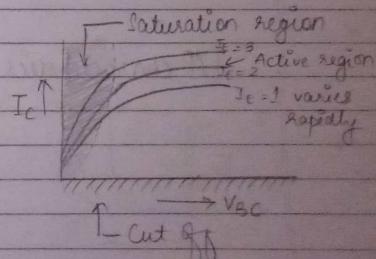
→ Circuit arrangement



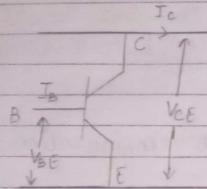
Input parameter	
I/P	$I = I_E$
I/P	$V = V_{BE}$
O/P	$I = I_C$
O/P	$V = V_{BC}$

For Output characteristics:

It is obtained with respect to output current and output voltage for a given value of input current.



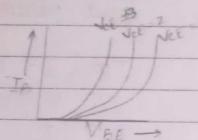
# I/O for npn transistor for CE configuration



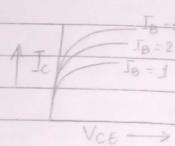
Parameter

$$\begin{array}{ll} \text{I/P} & I = I_B \\ \text{I/P} & V = V_{BE} \\ \text{O/P} & I = I_C \\ \text{O/P} & V = V_{CE} \end{array}$$

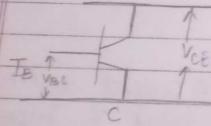
I/P characteristics



O/P characteristics



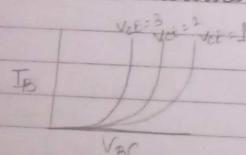
# I/O for npn transistor for CC configuration



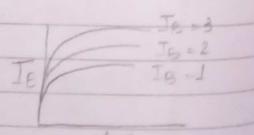
Parameters

$$\begin{array}{ll} \text{I/P} & I = I_B \\ \text{I/P} & V = V_{BC} \\ \text{O/P} & I = I_E \\ \text{O/P} & V = V_{CE} \end{array}$$

I/P characteristics



O/P characteristics



Current gain:

It is defined as the ratio of output current to input current.

$$CG = \frac{\text{O/P } I}{\text{I/P } I}$$

→ For common base configurations : the CG is denoted by ' $\alpha$ ' and is given by  $\alpha = \frac{I_c}{I_e}$

→ For common ~~emitter~~ emitter configuration, the CG is denoted by ' $\beta$ ' and is given by  $\beta = \frac{I_c}{I_b}$

→ For common collector configuration, the CG is denoted by ' $\gamma$ ' and is given by  $\gamma = \frac{I_e}{I_b}$

⇒ Relationship between ' $\alpha$ ' and ' $\beta$ ' :-

The current eq^n of BJT is given by →

$$I_e = I_c + I_b \quad \text{①}$$

divide the eq^n ① by  $I_c$

$$\frac{I_e}{I_c} = 1 + \frac{I_b}{I_c}$$

$$\frac{1}{\alpha} = 1 + \frac{1}{\beta}$$

$$\therefore \alpha = \frac{\beta}{1 + \beta} \quad \text{and} \quad \beta = \frac{\alpha}{1 - \alpha}$$

⇒ Relationship between ' $\beta$ ' and ' $\gamma$ '

The current eq<sup>n</sup> of BJT is given by →  
 $I_E = I_C + I_B$  ②  
 divide the eq<sup>n</sup> ② by  $I_B$

$$\frac{I_E}{I_B} = \frac{I_C}{I_B} + 1$$

$$\frac{I_E}{I_B} = \frac{I_C}{I_B} + 1$$

$$\therefore \gamma = \beta + 1 \quad \text{and} \quad \beta = \gamma - 1$$

Relationship between ' $\alpha$ ' and ' $\gamma$ ' :-

The current eq<sup>n</sup>  $I_E = I_C + I_B$  — ③

Divide the eq<sup>n</sup> ③ by  $I_E$

$$\frac{I_E}{I_E} = \frac{I_C}{I_E} + \frac{I_B}{I_E}$$

$$1 = \alpha + \frac{1}{\gamma}$$

$$\alpha = -1 + \frac{1}{\gamma} \quad \text{and} \quad \gamma = \frac{1}{1-\alpha}$$

Ques 1 The values for a ' $\gamma$ ' of transistor is 0.95.  
 Find the value of ' $\beta$ ' also find value of ' $\alpha$ ' if  
 $\beta$  changes to 100.

$$\alpha = 0.95$$

$$\beta = ?$$

$$\beta = \frac{\alpha}{1-\alpha}$$

$$= \frac{0.95}{1-0.95}$$

$$= \frac{0.95 \times 100}{0.05 \times 100}$$

$$= \frac{95}{5}$$

$$\Rightarrow \beta = 19$$

$$\beta = 100$$

$$\alpha = ?$$

$$\alpha = \frac{\beta}{\beta+1}$$

$$= \frac{100}{100+1}$$

$$= \frac{100}{101}$$

$$\alpha = 0.99$$

Ques 2 For npn transistor the emitter current is  $I_E$  mA and the common emitter current gain is 100. Determine the collector and base current and also determine the value of ' $\gamma$ '.

$$I_E = 10 \text{ mA}, \beta = 100, I_C = ?, I_B = ?, \gamma = ?, \alpha = ?$$

$$\alpha = \frac{\beta}{\beta+1} = \frac{100}{100+1} = \frac{100}{101} = 0.99$$

$$\beta = \gamma - 1 = 100 = \gamma = 1$$

$$100 + 1 = \gamma$$

$$\gamma = 101$$

$$\alpha = \frac{I_c}{10 \times 10^{-3}} = 0.99 = \frac{I_c}{10 \times 10^{-3}}$$

$$0.0099 = I_c$$

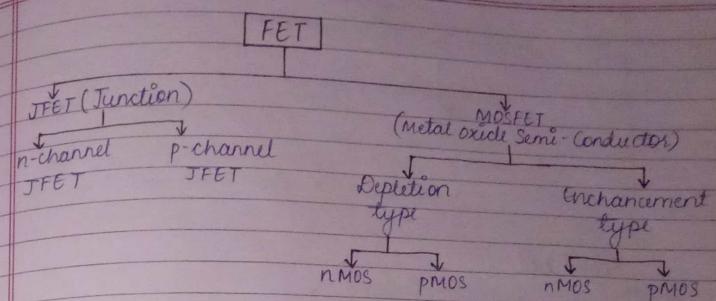
$$\begin{aligned} I_E &= I_C + I_B \\ 10 \times 10^{-3} &= 0.0099 + I_B \\ 10 \times 10^{-3} - 0.0099 &= I_B \\ \Rightarrow I_B &= 0.0001 \end{aligned}$$

$\Rightarrow$  Difference between FET and BJT

Bipolar Junction Transistor

Field Effect Transistor

- It is a Bipolar device (both majority and minority charge carrier).
- BJT is a current control device.
- Low input resistance
- +ve temp. coefficient.
- less noisy
- Occupies more space
- It is a uni-polar device (only majority charge carrier).
- FET is a voltage control device.
- Very high input resistance
- -ve temp. coefficient
- Comparatively more noisy.
- Occupies less space and is scalable.



### Junction FET (JFET)

Construction : It is a 3 terminal device

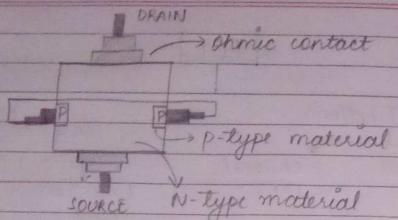
- ↳ Gate
- ↳ Drain
- ↳ Source

- n-channel
- Two p-type materials are induced in an n-type substrate.

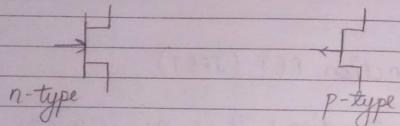
$\rightarrow$  Both p-type regions/materials are connected together to form the GATE terminal.

$\rightarrow$  Top side forms the DRAIN terminal and bottom side forms the source terminal.

$\rightarrow$  The contacts used are OHMIC contacts.

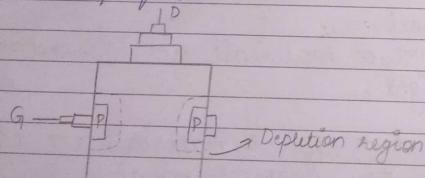


Symbol :

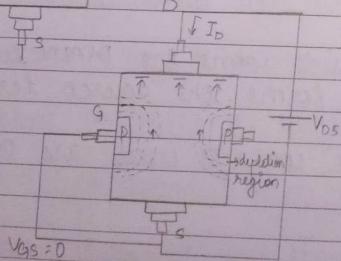


→ Working Principle (n-channel):

① At no bias / Equilibrium



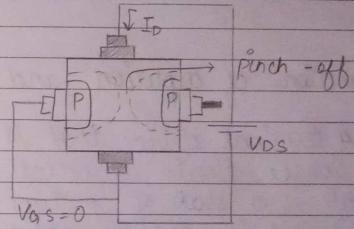
②  $V_{GS} = 0$   
 $V_{DS} > 0$



• As  $V_{DS}$  is applied,  $e^-$  are drawn towards drain terminal and a ' $I \rightarrow I_D$ ' (Drain current) flows through the device.

• Since it is reverse biased depletion region ↑, the width of the depletion region in upper region will be more compared to lower region.

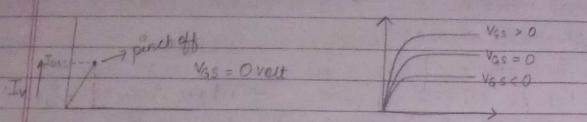
• As we go on ↑  $V_{DS}$ , 2 depletion regions would touch, and condition referred to as pinch-off will result.



• The  $V_{DS}$  at this point is known as pinch-off voltage ( $V_p$ )

• The  $I \rightarrow I_D$  doesn't drop off at pinch off rather maintains a saturation level defined as Maximum Drain current ( $I_{DSS}$ ), when at  $V_{DS} > V_p$ .

→ VI characteristics / Transfer characteristics



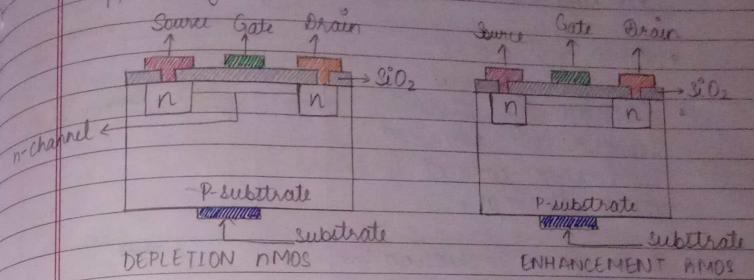
### # MOSFET / IGFET (Insulated Gate)

Semi-conductor (Silicon)  
oxide  
metal

→ Construction of depletion and enhancement

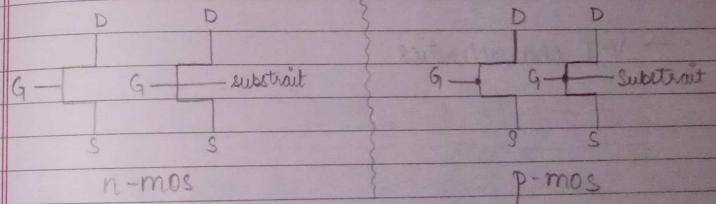
- \* It is 4 terminal device that is :  
Gate, Source, Drain, Substrate
- \* Substrate is a slab of p-type material (for n-mos) and is the foundation on which the device is constructed.
- \* Silicon-dioxide ( $\text{SiO}_2$ ) is a type of insulator (di-electric) which sets up opposing electric field within the dielectric when exposed to electric field.
- \* In depletion type MOSFET an n-channel is present between the drain and source.
- \* In enhancement type MOSFET the channel is formed.
- \* Source and drain terminals are connected through metallic contact with diffused

depleted regions.

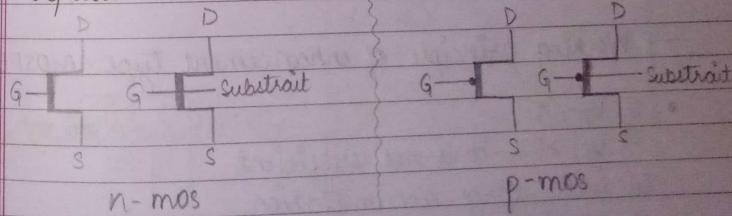


Symbols :

→ Enhancement :-

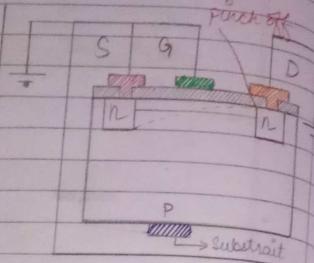


→ Depletion :-



### Working principle of depletion type (n mos)

- $V_{GS} = 0$  and  $V_{DS} > 0$
- Electrons will attract towards +ve terminal and then current  $I_D$  starts flowing.
- As we go on increasing  $V_{DS}$ , the voltage can pinch off the channel and therefore drain current saturates and maintains its value

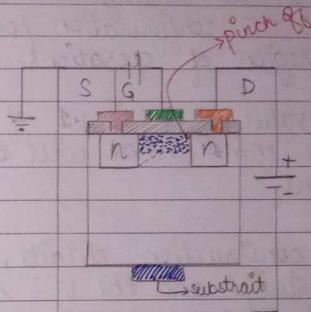


$$V_{GS} = 0$$

$$V_{DS} > 0$$

no power between Drain and source. Therefore  $I_D = 0$  and MOSFET is not conducting.

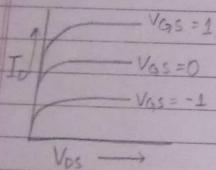
- $V_{GS} > 0$ , will pressure holes into p-substrate and electrons will be attracted towards the gate and will accumulate in the region of  $S\&G$ .
- The  $V_{GS}$  voltage where channel gets induced (form) is known as threshold voltage. ( $V_{TH}$  /  $V_T$ )



- $V_{GS} > V_{TH}$  and  $V_{DS} > 0$  and kept constant conducting and a current  $I_D$  starts to flow.

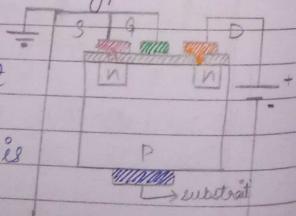
- $I_D$  eventually reaches saturation by pinch-off process as that of depletion mos.

### V-I characteristics

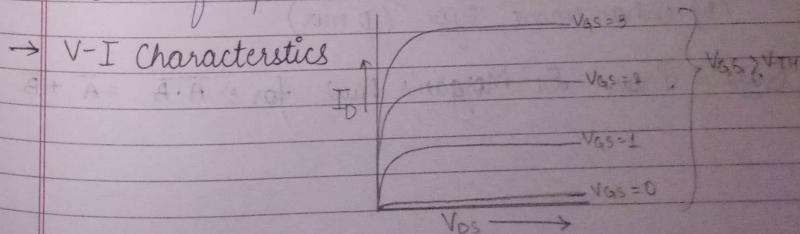


### Working principle of enhancement type MOSFET

- If  $V_{GS} = 0$ ,  $V_{DS} > 0$ , it is not sufficient to have large accumulation of carriers and hence there is



### V-I Characteristics



### Assignment Questions

- Ques1: Draw the circuit diagram for the p-n-p junction for active, saturation, cut-off and inverted junction.
- Ques2: Explain the working principle of pnp transistor in active region.
- Ques3: Draw the circuit arrangement of pnp transistor in CB, CE, CC configuration for all the different region of operations.

Ques4: The inverse value of ' $\gamma$ ' is 1.1 if the anmeter current is 20mA. What will be the value of base current.

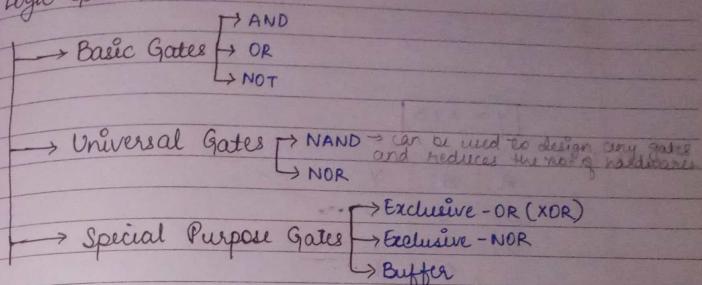
Ques5: Give the construction details, discuss the working principle and the V-I characteristics of p-channel JFET.

Ques6: Give the constructional details, symbol and discuss the working principle and V-I characteristics of  
 a) depletion type (pmos)  
 b) enhancement type (pmos)

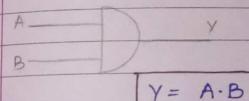
Ques7: Prove De Morgan's Law for  $\overline{A \cdot B} = \overline{A} + \overline{B}$

14th May 2024

### # Logic Gates



⇒ AND Gate

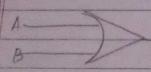


Truth Table

A	B	$Y = A \cdot B$
0	0	0
0	1	0
1	0	0
1	1	1

\* 1 I.C. has 4 AND Gates and 1 AND Gate has 3 pins, therefore total pins =  $4 \times 3 = 12$  pins.  
 + 2 more pins are required for power supply.  
 Hence in total 14 pins are required in 1 I.C.

⇒ OR Gate

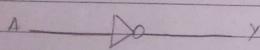


$$[Y = A + B]$$

Truth Table

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

⇒ NOT Gate

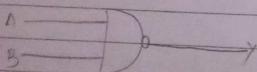


$$[Y = \bar{A}]$$

Truth Table

A	Y
0	1
1	0

⇒ NAND Gate (Not AND)

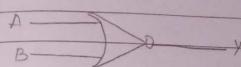


$$[Y = \bar{A} \cdot \bar{B}]$$

Truth Table

A	B	Y	$\bar{Y}$
0	0	1	0
0	1	0	1
1	0	0	1
1	1	0	1

⇒ NOR Gate (Not OR)



$$[Y = \bar{A} + \bar{B}]$$

Truth Table

A	B	Y	$\bar{Y}$
0	0	1	0
0	1	0	1
1	0	0	1
1	1	0	1

⇒ XOR Gate (Exclusive OR)



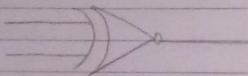
$$\begin{aligned}[Y &= A \oplus B \\ &= A\bar{B} + \bar{A}B]\end{aligned}$$

### Truth Table

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	0

agar inputs same honge toh output 0, and if differ honge toh output will be 1.

⇒ XNOR Gate (Exclusive NOR)



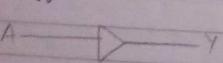
$$\boxed{Y = A \oplus B \\ = AB + \bar{A}\bar{B}}$$

### Truth Table

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1

agar inputs same honge toh output = 1, and if different then output = 0.

Buffer



$$\boxed{Y = A}$$

jab input let's say 5V hai and op 4.8V and we want it 5V toh  
we use buffer in that case.

### # Boolean Algebra

#### # De Morgan's Law

It states that, break the bar and change the sign

ex:

$$\begin{aligned} ① \quad A + B &= \bar{A} \cdot \bar{B} \\ ② \quad A \cdot B &= \bar{A} + \bar{B} \end{aligned}$$

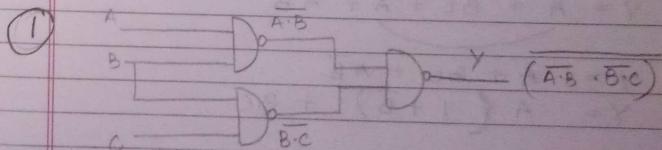
→ Prove De Morgan's Law

$$① \quad A + B = \bar{A} \cdot \bar{B}$$

A	B	A + B	LHS		RHS	
			$\bar{A} + \bar{B}$	$\bar{A} \cdot \bar{B}$	$\bar{A}$	$\bar{B}$
0	0	0	1	1	1	1
0	1	1	0	1	0	0
1	0	1	0	0	1	0
1	1	1	0	0	0	0

⇒ Hence LHS = RHS

Ques Reduce the following using Boolean Algebra / De Morgan's Law

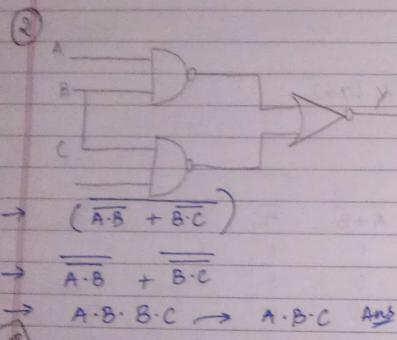


$$\left( \overline{A \cdot B} + \overline{B \cdot C} \right)$$

$$\rightarrow \overline{A \cdot B} + \overline{B \cdot C}$$

$$\rightarrow A \cdot B + B \cdot C$$

$$\rightarrow B \cdot (A+C) \text{ Ans}$$



$$\rightarrow (\overline{A \cdot B} + \overline{B \cdot C})$$

$$\rightarrow \overline{A \cdot B} + \overline{B \cdot C}$$

$$\rightarrow A \cdot B \cdot B \cdot C \rightarrow A \cdot B \cdot C \text{ Ans}$$

Ques Simplify and solve the following Boolean equation

$$Y = A + A \cdot B \cdot C + \overline{A} \cdot B \cdot C + A \cdot D + \overline{A} \cdot \overline{D} + A \cdot \overline{B}$$

$$Y = A + BC(A + \overline{A}) + A(D + \overline{D}) + A\overline{B}$$

$$Y = A + BC(1) + A(1) + A\overline{B}$$

$$Y = A + BC + A + A\overline{B}$$

$$Y = A + BC + A\overline{B}$$

$$Y = A(1 + \overline{B}) + BC$$

$$Y = A(1) + BC$$

$$Y = A + BC \text{ Ans}$$

Ans  
Ques 8

Minimize the following

$$① Y = \overline{AB} + ABC + \overline{ABC} + \overline{AB} + \overline{AD} + \overline{BC}$$

②

