

Mini Project #1

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Task Description: The project is a programming exercise that requires to code the K-means clustering Machine Learning algorithm. Once implemented, the coded algorithm should be able to regroup into $K(1, 2, 3, 200)$ clusters of digit images from the "Optical Character Recognition (OCR)" dataset provided by Prof. Dr. H. Jaeger. Additionally, a few examples of visualizations of the obtained results should be provided.

Summary: Attached along this report, should it be found a Jupyter Notebook which contains the Python script that implements the K-means clustering algorithm from the Dr. Herbert Jaeger's Machine Learning Lecture Notes. The algorithm is described in the following steps:

- **Given:** a training data set $(x_i)_{i=1, \dots, N} \in \mathbb{R}^n$, and a number K of clusters that one maximally wishes to obtain
- **Initialization:** randomly assign the training points to K sets S_j ($j = 1, \dots, K$).
- **Repeat:** For each set S_j , compute the mean $\bar{x}_j = \text{Sum}(x) / |S_j|$ for $x \in S_j$. This mean vector \bar{x}_j is the center of gravity of the vector cluster S_j . Create new sets S'_j by putting each data point x_i into that set S'_j where $\text{Modulus}(x_i - \bar{x}_j)$ is minimal. If some S'_j remains empty, dismiss it and reduce K to K' by subtracting the number of dismissed empty sets (this happens rarely). Put $S_j = S'_j$ (for the nonempty sets) and $K = K'$.
- **Termination:** Stop when in one iteration the sets remain unchanged.

Analysis