

## **Assignment-11 [15 marks]**

### **Octave**

Q. (Intro to ML)

In this question, we will revisit the problem we have solved in Assignment-3. We will code a 1-D linear regression problem. We will provide pseudo-code here, the students are required to transform it into a Matlab/Octave code.

**Important Note:** Please don't use external library. Octave default data structures and methods should suffice.

The data files are train.csv and test.csv.

File structure:

The structure of both files are similar. Train.csv has  $n_{\text{train}} = 10^4$  rows and test.csv has  $n_{\text{test}} = 10^3$  rows, each row corresponding to one data point. Each row has two values separated by comma. The first value is feature and second value is label of the data point. The first row of both files may/may not contain headers.

Example-

If one row of train.txt is :

4,7

Then feature,  $x = 4$  and label,  $y = 7$ .

Pseudo-code

Step-1:[1.5 marks]

- Read files train.csv
- Create vector -  $X_{\text{train}}$  (dim -  $n_{\text{train}} \times 1$ ) and vector -  $y_{\text{train}}$  (dim -  $n_{\text{train}} \times 1$ )
- Add a column to  $X_{\text{train}}$  so that its dimension becomes  $n_{\text{train}} \times 2$ . First column of  $X_{\text{train}}$  should be all 1 and 2nd column is the same as before adding extra column.

Example -

```
X_train = [  
           2  
           3  
           4  
           ]
```

```
New X_train = [  
               1  2  
               1  3
```

```

1 4
]

```

**Step-2:[0.5 marks]**

Generate a 2-D vector  $\mathbf{w}$  (dim: 2 x 1) initialised randomly with floating point numbers.

**Step-3:[1.5 marks]**

Plot  $y$  vs  $x$  using matplotlib where  $x$  is the feature and  $y$  is the label read from the file train.csv. (A scatter plot)

Consider  $\mathbf{x}' = [1 \ x]$  (prepending 1 to  $x$  to generate 2-dimensional  $x$ -vector)

On the same figure plot the line  $\mathbf{w}^T \mathbf{x}'$  vs  $x$ . (A straight line not necessarily passing through the scatter plot)

Your figure should have a dot corresponding to each datapoint  $(x,y)$  and a straight line on the plot corresponding to  $\mathbf{w}^T \mathbf{x}'$ .

**Step-4:[2.5 marks]**

Set  $\mathbf{w}_{\text{direct}} = (\mathbf{X}_{\text{train}}^T \mathbf{X}_{\text{train}})^{-1} \mathbf{X}_{\text{train}}^T \mathbf{y}_{\text{train}}$  (if  $M$  is a matrix  $M^{-1}$  is inverse of  $M$ )

$\mathbf{X}_{\text{train}}$  is the  $n_{\text{train}} \times 2$  matrix defined earlier and  $\mathbf{y}_{\text{train}}$  is the corresponding label vector.

Plot  $y$  vs  $x$  using matplotlib where  $x$  is the feature and  $y$  is the label read from the file train.csv. (A scatter plot)

Consider  $\mathbf{x}' = [1 \ x]$  (prepending 1 to  $x$  to generate 2-dimensional  $x$ -vector)

On the same figure plot the line  $\mathbf{w}_{\text{direct}}^T \mathbf{x}'$  vs  $x$ . (A straight line that should ideally pass through the scatter plot)

Your figure should have a dot corresponding to each datapoint  $(x,y)$  and a straight line on the plot corresponding to  $\mathbf{w}_{\text{direct}}^T \mathbf{x}'$ .

**Step-5: [4.5 marks]**

$\mathbf{w}$  - 2-dim vector initialised earlier (step-2)

Loop: for  $\text{nepoch} = 1$  to  $N$  ( $N$  is the number of pass through the data(~2) , play with it to

find best fit)

Loop : for  $j = 1$  to  $n_{\text{train}}$

$(x,y) \leftarrow j\text{th row of train.csv}$

$\mathbf{x}' \leftarrow [1, \ x]^T$

$\mathbf{w} \leftarrow \mathbf{w} - \eta * (\mathbf{w}^T \mathbf{x}' - y) * \mathbf{x}'$  ( $\eta = 0.00000001$  students can change this value)

If  $j \% 100 == 0$

Then plot  $y$  vs  $x$  as earlier and use current value of  $w$  to plot  $w^T x'$  vs  $x$

**Step-6: [0.5 marks]**

Finally redraw the plot as earlier with latest value of  $w$  from the training. (like in step 3 and 4)

**Note:-** Don't use test.csv for training. That is test.csv should not be used before this point. Marks will be deducted otherwise.

**Step-7:[4 marks]**

- Read files test.csv
- Create vector -  $X_{\text{test}}$  (dim -  $n_{\text{test}} \times 1$ ) and vector -  $y_{\text{test}}$  (dim -  $n_{\text{test}} \times 1$ )
- Add a column to  $X_{\text{test}}$  so that its dimension becomes  $n_{\text{test}} \times 2$ . First column of  $X_{\text{test}}$  should be all 1 and 2nd column is the same as before adding extra column.
- Let  $y_{\text{pred1}} = X_{\text{test}} * w$  ( $w$  is the final value after doing step 5)
- Calculate root mean squared error between  $y_{\text{pred1}}$  and  $y_{\text{test}}$ .
- Let  $y_{\text{pred2}} = X_{\text{test}} * w_{\text{direct}}$
- Calculate root mean squared error between  $y_{\text{pred2}}$  and  $y_{\text{test}}$ .

**Derivation of Updates (optional reading)**

In the loop of step 5 we did the following

$$w \leftarrow w - \eta * (w^T x' - y) * x'$$

The objective of the above step is to reduce the least squared error.

Let error =  $0.5(w^T x' - y)^2$

So, derivative w.r.t.  $w$  gives:  $(w^T x' - y) x'$

We need to descend down the gradient to reach the minima, so we subtract  $\eta$  times the above derivative from  $w$  to gradually reach minima. We set  $\eta$  to small value because otherwise,  $w$  may overshoot the minima.  $W_{\text{direct}}$  can also be computed on the same line by setting derivative to zero (Google it!).

