Case Study 3 – Regression Diagnostics

```
library(tidyverse)
-- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
v dplyr 1.1.2 v readr 2.1.4
v forcats 1.0.0 v stringr 1.5.0
v ggplot2 3.4.3 v tibble 3.2.1
v lubridate 1.9.2
                   v tidyr
                                1.3.0
          1.0.2
v purrr
-- Conflicts ----- tidyverse_conflicts() --
x dplyr::filter() masks stats::filter()
x dplyr::lag()
              masks stats::lag()
i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become
  library(DescTools)
  library(plotly)
Attaching package: 'plotly'
The following object is masked from 'package:ggplot2':
   last_plot
The following object is masked from 'package:stats':
   filter
The following object is masked from 'package:graphics':
   layout
```

Prediction Error

$$s_{\hat{y}_p} = \sqrt{s^2 \left[\frac{1}{n} + \frac{(x_p - \bar{X})^2}{SS_X} \mathbf{1} \right]}$$

Car stopping distance

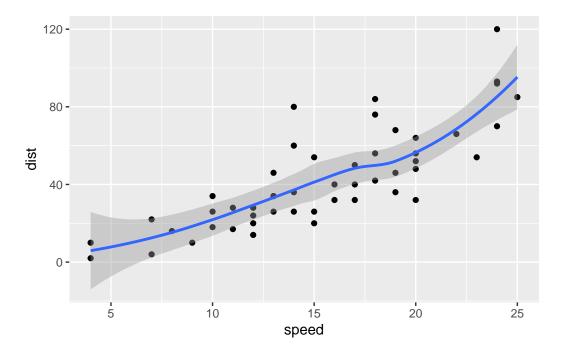
Three models

```
cars.lm <- lm(dist~speed,data=cars)
cars.sqm <- lm(sqrt(dist)~speed,data=cars)
cars.llm <- lm(log(dist)~speed,data=cars)</pre>
```

Linear

```
ggplot(cars,aes(x=speed,y=dist)) + geom_point() + geom_smooth()
```

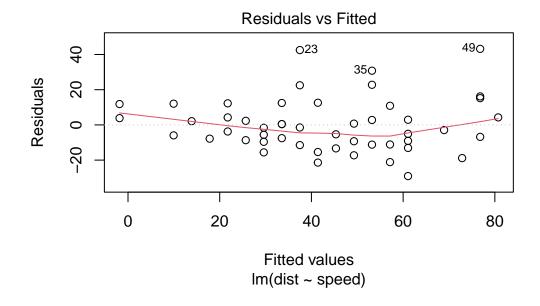
`geom_smooth()` using method = 'loess' and formula = 'y ~ x'

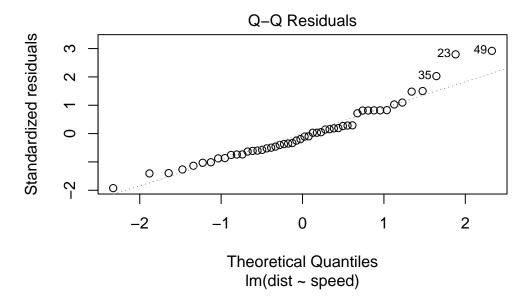


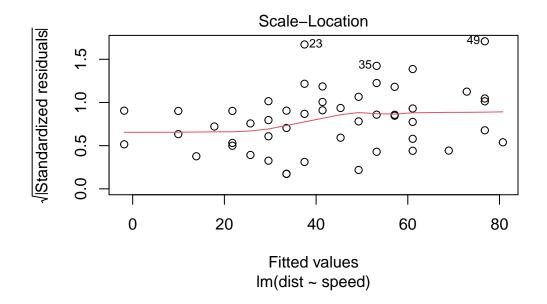
If you have loaded the plotly package, you can get an interactive version of the last scatterplot with ggplotly() [I've turned it off here to generate pdf output, only works for html output.]

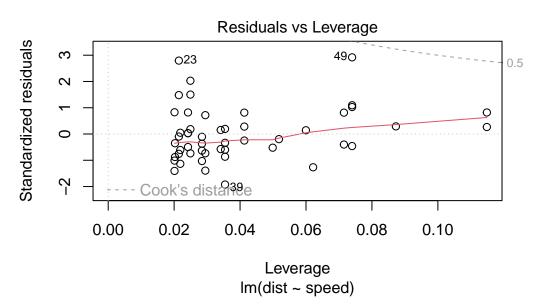
ggplotly()

plot(cars.lm)





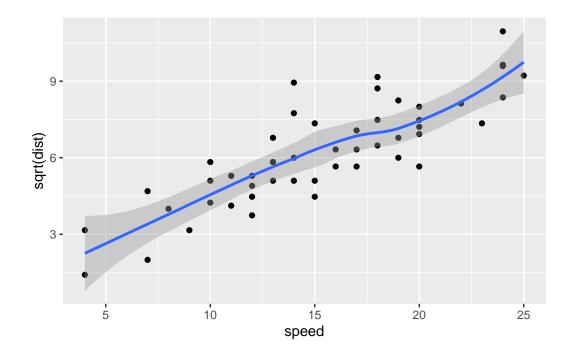




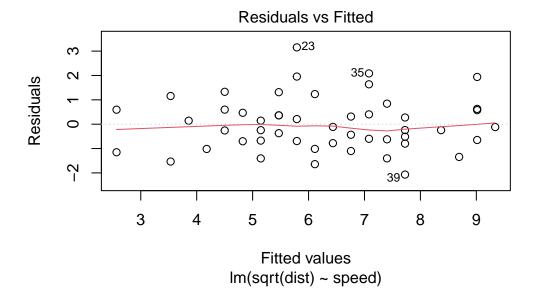
Square Root

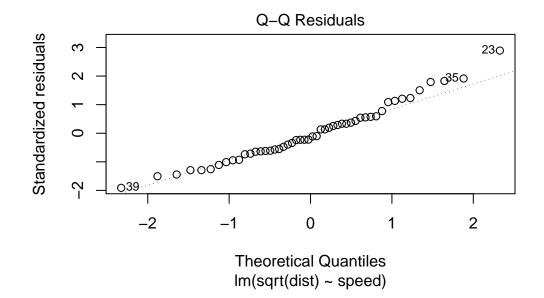
```
ggplot(cars,aes(x=speed,y=sqrt(dist))) + geom_point() + geom_smooth()

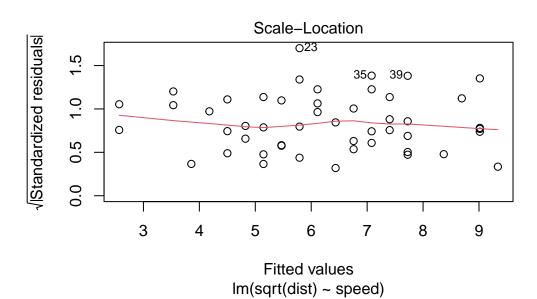
'geom_smooth()' using method = 'loess' and formula = 'y ~ x'
```

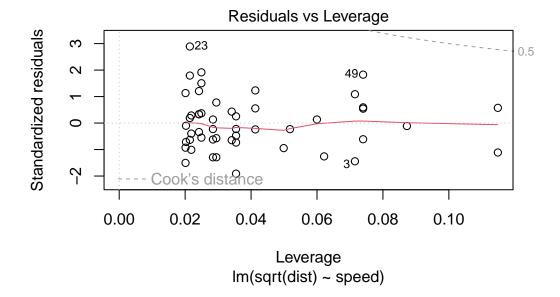


plot(cars.sqm)





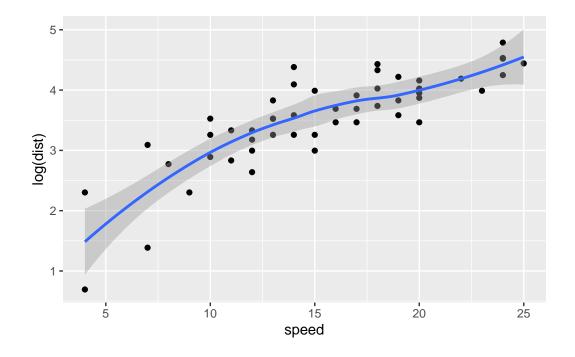


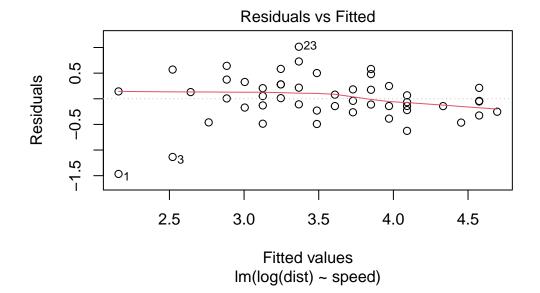


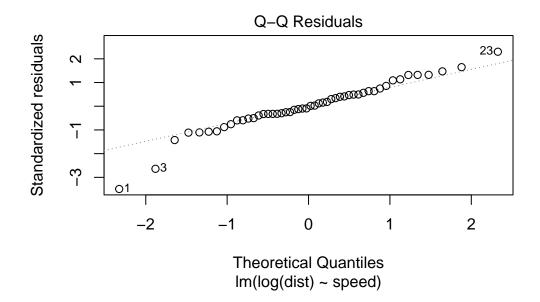
Log

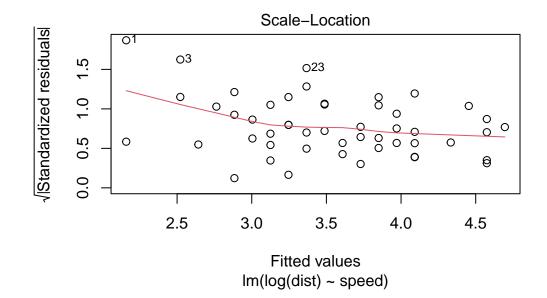
```
ggplot(cars,aes(x=speed,y=log(dist))) + geom_point() + geom_smooth()
```

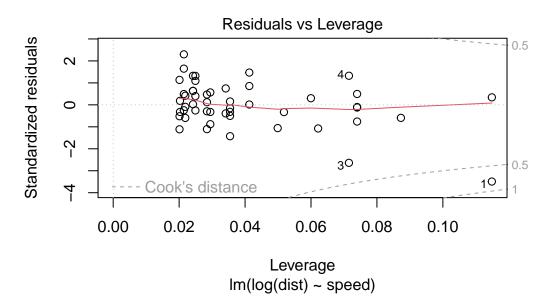
 $geom_smooth()$ using method = 'loess' and formula = 'y ~ x'











ACED Data

```
ACEDextract <- read_csv("ACED_extract1.csv",na="-999")
```

Rows: 290 Columns: 29
-- Column specification ------

```
Delimiter: ","
chr (7): SubjID, Session, Cond_code, Sequencing, Feedback, Gender, Level_Code
dbl (22): Correct, Incorrect, Reamaining, ElapsedTime, Race, pre_scaled, pos...
i Use `spec()` to retrieve the full column specification for this data.
i Specify the column types or set `show_col_types = FALSE` to quiet this message.
  ACEDextract$Session <- factor(ACEDextract$Session)</pre>
  ACEDextract$Cond_code <- factor(ACEDextract$Cond_code)</pre>
  ACEDextract$Sequencing <- factor(ACEDextract$Sequencing)</pre>
  ACEDextract$Feedback <- factor(ACEDextract$Feedback)</pre>
  ACEDextract$Gender <- factor(ACEDextract$Gender)
  ACEDextract$Race <- factor(ACEDextract$Race, 1:8)
  ACEDextract$Level_Code <- factor(ACEDextract$Level_Code)</pre>
  ACEDextract %>%
    mutate(gain=post_scaled-pre_scaled) ->
    ACEDextract
dfbetas
```

```
lm_PostxEAP <- lm(EAP.sgp~post_scaled,data=ACEDextract,na.action=na.exclude)</pre>
 dfb <- dfbeta(lm_PostxEAP)</pre>
 dfbs <- dfbetas(lm_PostxEAP)</pre>
 data.frame(dfbeta=dfb,dfbeta_scaled=dfbs) ->dfbb
 summary(dfbb)
dfbeta..Intercept.
                    dfbeta.post_scaled
                                         dfbeta_scaled..Intercept.
Min.
      :-2.202e-02
                    Min.
                          :-6.715e-04
                                         Min. :-1.263e-01
1st Qu.:-3.563e-03
                    1st Qu.:-5.982e-05
                                         1st Qu.:-2.039e-02
Median : 0.000e+00
                    Median : 0.000e+00
                                         Median : 0.000e+00
Mean : 3.980e-06
                    Mean :-2.790e-08
                                         Mean : 3.613e-05
3rd Qu.: 2.987e-03
                    3rd Qu.: 4.484e-05
                                         3rd Qu.: 1.707e-02
      : 3.594e-02
                    Max.
                           : 4.571e-04
                                         Max. : 2.088e-01
dfbeta_scaled.post_scaled
Min.
     :-0.2183489
1st Qu.:-0.0193745
Median: 0.0000000
Mean :-0.0000108
```

3rd Qu.: 0.0144733 Max. : 0.1482344

dfbb

	dfbetaIntercept.	dfbeta.post_scaled	dfbeta_scaledIntercept.
1	-0.0107997611	2.158032e-04	-0.0617189357
2	0.0049771633	-7.922792e-05	0.0284315957
3	-0.0131832484	2.836516e-04	-0.0755063814
4	-0.0041814717	3.963175e-05	-0.0239235676
5	-0.0045446370	5.483782e-05	-0.0259824724
6	-0.0020347195	4.528577e-05	-0.0116225720
7	0.0005818237	-4.136881e-06	0.0033233050
8	-0.0036894991	3.496886e-05	-0.0211008426
9	0.0084326716	-1.017528e-04	0.0483270417
10	-0.0035088364	4.509210e-05	-0.0200497965
11	-0.0035626546	2.533118e-05	-0.0203894917
12	0.0026831469	-1.907770e-05	0.0153425320
13	-0.0210228362	4.333390e-04	-0.1205368506
14	0.0109992656	-2.503349e-04	0.0630481121
15	-0.0031047015	2.942618e-05	-0.0177494005
16	-0.0047049813	6.554322e-05	-0.0268861764
17	-0.0048882674	6.281919e-05	-0.0279435780
18	0.0035090370	-1.215397e-04	0.0201329662
19	-0.0052515314	1.561332e-04	-0.0301456538
20	0.0099500184	-1.200618e-04	0.0570989433
21	0.0330494595	-6.714667e-04	0.1901782172
22	-0.0031409358	2.233267e-05	-0.0179678471
23	0.0002502676	1.604358e-06	0.0014294920
24	-0.0043090174	6.169595e-05	-0.0246196589
25	-0.0032354589	2.300475e-05	-0.0185103482
26	0.0056951899	-9.065767e-05	0.0325347387
27	0.0016382707	-2.565966e-05	0.0093572847
28	-0.0044531782	6.203545e-05	-0.0254459544
29	-0.0010174010	-6.522120e-06	-0.0058157422
30	-0.0136523908	3.038547e-04	-0.0783202143
31	-0.0026945387	3.251363e-05	-0.0153953469
32	0.0004942835	-5.995958e-05	0.0028329581
33	0.0052388134	-1.557551e-04	0.0300719129
34	-0.0048906986	5.901357e-05	-0.0279653053
35	0.0195328334	-4.347329e-04	0.1125765583
36	0.0008205447	3.777578e-05	0.0047039117

37	0.0116563281	-2.825172e-04	0.0670408900
38	-0.0011905019	1.436518e-05	-0.0068000913
39	0.0005050618	-6.126705e-05	0.0028951781
40	-0.0046856118	6.527339e-05	-0.0267753821
41	-0.0001584561	3.526681e-06	-0.0009050335
42	-0.0158922845	3.175631e-04	-0.0908826422
43	-0.0041814717	3.963175e-05	-0.0239235676
44	-0.0008578372	6.099392e-06	-0.0049001695
45	0.0004600663	-9.483243e-06	0.0026277054
46	-0.0029883964	4.455174e-05	-0.0170704159
47	-0.0176143407	3.630805e-04	-0.1008776691
48	0.0086962759	-6.183224e-05	0.0502769088
49	-0.0191291979	3.862813e-04	-0.1095006214
50	-0.0035626546	2.533118e-05	-0.0203894917
51	-0.0061977728	1.842659e-04	-0.0356482401
52	-0.0108685922	2.759329e-04	-0.0626082513
53	-0.0031059364	6.595622e-05	-0.0177420734
54	-0.0012296407	3.121824e-05	-0.0070239382
55	-0.0037831891	8.033804e-05	-0.0216121076
56	-0.0084822408	1.673828e-04	-0.0484598466
57	-0.0002686645	3.259064e-05	-0.0015360679
58	-0.0217198569	4.515883e-04	-0.1246406069
59	0.0043187599	-9.171117e-05	0.0246730867
60	0.0035234173	-1.220378e-04	0.0202162267
61	-0.0043090174	6.169595e-05	-0.0246196589
62	-0.0011453689	3.967123e-05	-0.0065449947
63	0.0052429082	-1.166889e-04	0.0299645876
64	-0.0142444449	2.783512e-04	-0.0814060023
65	0.0023432284	-5.215211e-05	0.0133852385
66	-0.0187178321	3.802906e-04	-0.1071631139
67	0.0045648717	-1.357182e-04	0.0261716841
68	-0.0002107169	1.498239e-06	-0.0012035328
69	0.0115729281	-2.575731e-04	0.0663085099
70	-0.0054498556	1.887623e-04	-0.0314709070
71	-0.0127214231	3.083322e-04	-0.0732649284
72	0.0061806584	-8.610029e-05	0.0353315365
73	0.0142257292	-1.348306e-04	0.0829027581
74	-0.0004831812	-2.224443e-05	-0.0027632454
75	-0.0169500658	3.772495e-04	-0.0974714823
76	-0.0202777480	4.362974e-04	-0.1165839499
77	-0.0031964327	4.576611e-05	-0.0182600781
78	0.0002548939	1.173466e-05	0.0014563605
79	-0.0135061422	3.273516e-04	-0.0778671954
, ,	0.0100001122	0.2,00100 01	0.0110011001

81	80	-0.0132451498	3.014495e-04	-0.0760445031
83	81	-0.0146944827	3.120452e-04	-0.0841733272
84	82	0.0083281924	-1.731556e-04	0.0475998941
85 0.0289256082 -6.142507e-04 0.1671014356 86 -0.0217198569 4.515883e-04 -0.1246406069 87 -0.0001208482 1.465961e-05 -0.0006903756 88 0.0038312054 -7.965649e-05 0.0218853911 89 -0.0034535894 2.455570e-05 -0.0197628872 90 -0.0108474718 2.414270e-04 -0.0621280377 91 -0.0008698271 1.211722e-05 -0.0049681622 92 0.0013044868 -1.236385e-05 0.0074519029 93 0.0095161066 -1.475975e-04 0.0543936135 94 0.0005066016 -6.145384e-05 0.0029040691 95 0.0137062484 -3.119438e-04 0.0787209302 96 -0.0023286566 2.992560e-05 -0.0133028649 97 0.0035377975 -1.225359e-04 0.0202994966 98 0.0005058317 -6.136044e-05 0.0028996235 99 -0.00707064644 -3.252382e-05 -0.0040460545 100 -0.0383833084 5.495640e-05	83	-0.0007982605	1.695149e-05	-0.0045593595
86 -0.0217198569 4.515883e-04 -0.1246406069 87 -0.0001208482 1.465961e-05 -0.0006903756 88 0.0038312054 -7.965649e-05 0.0218853911 89 -0.0034535894 2.455570e-05 -0.0197628872 90 -0.0108474718 2.414270e-04 -0.0621280377 91 -0.0008698271 1.211722e-05 -0.0049681622 92 0.0013044868 -1.236385e-05 0.0074519029 93 0.0095161066 -1.475975e-04 0.0543936135 94 0.0005066016 -6.145384e-05 0.0029040691 95 0.0137062484 -3.119438e-04 0.0787209302 96 -0.0032286566 2.992560e-05 -0.0133028649 97 0.0035377975 -1.225359e-04 0.0202994966 98 0.0005058317 -6.136044e-05 0.00284702013 101 -0.0049802294 6.400100e-05 -0.0224702013 101 -0.0038383084 5.495640e-05 -0.021928706 102 -0.0036059566 3.417705e-0	84	-0.0048267116	1.671790e-04	-0.0278060008
87 -0.0001208482 1.465961e-05 -0.0006903756 88 0.0038312054 -7.965649e-05 0.0218853911 89 -0.0034535894 2.455570e-05 -0.0197628872 90 -0.108474718 2.414270e-04 -0.0621280377 91 -0.0008698271 1.211722e-05 -0.0049681622 92 0.0013044868 -1.236385e-05 0.0074519029 93 0.0095161066 -1.475975e-04 0.0543936135 94 0.005066016 -6.145384e-05 0.0029040691 95 0.0137062484 -3.119438e-04 0.078720930 96 -0.0023286566 2.992560e-05 -0.0133028649 97 0.0035377975 -1.225359e-04 0.0202994966 98 0.0005058317 -6.136044e-05 0.0028996235 99 -0.00707064644 -3.252382e-05 -0.004460545 100 -0.0048802294 6.400100e-05 -0.0284702013 101 -0.0038383084 5.495640e-05 -0.021928706 102 -0.0036059566 3.417705e-05 </td <td>85</td> <td>0.0289256082</td> <td>-6.142507e-04</td> <td>0.1671014356</td>	85	0.0289256082	-6.142507e-04	0.1671014356
88 0.0038312054 -7.965649e-05 0.0218853911 89 -0.0034535894 2.455570e-05 -0.0197628872 90 -0.0108474718 2.414270e-04 -0.0621280377 91 -0.0008698271 1.211722e-05 -0.0049681629 92 0.0013044868 -1.236385e-05 0.0074519029 93 0.0095161066 -1.475975e-04 0.0543936135 94 0.0005066016 -6.145384e-05 0.0029040691 95 0.0137062484 -3.119438e-04 0.0787209302 96 -0.0023286566 2.992560e-05 -0.0133028649 97 0.0035377975 -1.225359e-04 0.022994966 98 0.0005058317 -6.136044e-05 0.0028996235 99 -0.0007064644 -3.252382e-05 -0.0040460545 100 -0.0048802294 6.400100e-05 -0.0224702013 101 -0.0038383084 5.495640e-05 -0.0212287066 102 -0.0036059566 3.417705e-05 -0.0206218213 103 -0.013231821 9.408086e-06 -0.00775595490 104 -0.0030138576 4.	86	-0.0217198569	4.515883e-04	-0.1246406069
89 -0.0034535894 2.455570e-05 -0.0197628872 90 -0.0108474718 2.414270e-04 -0.0621280377 91 -0.0008698271 1.211722e-05 -0.0049681622 92 0.0013044868 -1.236385e-05 0.0074519029 93 0.0095161066 -1.475975e-04 0.0543936135 94 0.005066016 -6.145384e-05 0.0029040691 95 0.0137062484 -3.119438e-04 0.0787209302 96 -0.0023286566 2.992560e-05 -0.0133028649 97 0.0035377975 -1.225359e-04 0.0022994966 98 0.0005058317 -6.136044e-05 0.0028996239 99 -0.007064644 -3.252382e-05 -0.0040460545 100 -0.0048802294 6.400100e-05 -0.0242702013 101 -0.00333383084 5.495640e-05 -0.0212287066 102 -0.0036059566 3.417705e-05 -0.0212287066 103 -0.013231821 9.408086e-06 -0.0075595490 104 -0.0033338764 4.493132e	87	-0.0001208482	1.465961e-05	-0.0006903756
90 -0.0108474718 2.414270e-04 -0.0621280377 91 -0.0008698271 1.211722e-05 -0.0049681622 92 0.0013044868 -1.236385e-05 0.0074519029 93 0.0095161066 -1.475975e-04 0.0543936135 94 0.0005066016 -6.145384e-05 0.0029040691 95 0.0137062484 -3.119438e-04 0.0787209302 96 -0.0023286566 2.992560e-05 -0.0133028649 97 0.0035377975 -1.225359e-04 0.0202994966 98 0.0005058317 -6.136044e-05 0.002896235 99 -0.0007064644 -3.252382e-05 -0.004460545 100 -0.049802294 6.400100e-05 -0.0284702013 101 -0.0338383084 5.495640e-05 -0.0219287066 102 -0.0036059566 3.417705e-05 -0.0226218213 103 -0.013231821 9.408086e-06 -0.0075595490 104 -0.0033138576 4.493132e-05 -0.0172158905 105 -0.0002828210 2.680561e-	88	0.0038312054	-7.965649e-05	0.0218853911
91 -0.0008698271 1.211722e-05 -0.0049681622 92 0.0013044868 -1.236385e-05 0.0074519029 93 0.0095161066 -1.475975e-04 0.0543936135 94 0.0005066016 -6.145384e-05 0.0029040691 95 0.0137062484 -3.119438e-04 0.0787209302 96 -0.0023286566 2.992560e-05 -0.0133028649 97 0.0035377975 -1.225359e-04 0.0202994966 98 0.0005058317 -6.136044e-05 0.0028996235 99 -0.0007064644 -3.252382e-05 -0.0040460545 100 -0.0049802294 6.400100e-05 -0.0284702013 101 -0.0038383084 5.495640e-05 -0.0219287066 102 -0.0036059566 3.417705e-05 -0.0206218213 103 -0.013231821 9.408086e-06 -0.0075595490 104 -0.0033138576 4.493132e-05 -0.0172158905 105 -0.0002828210 2.680561e-06 -0.007459458 107 -0.0046430352 5.96677	89	-0.0034535894	2.455570e-05	-0.0197628872
92 0.0013044868 -1.236385e-05 0.0074519029 93 0.0095161066 -1.475975e-04 0.0543936135 94 0.0005066016 -6.145384e-05 0.0029040691 95 0.0137062484 -3.119438e-04 0.0787209302 96 -0.0023286566 2.992560e-05 -0.0133028649 97 0.0035377975 -1.225359e-04 0.0202994966 98 0.0005058317 -6.136044e-05 0.0028996235 99 -0.0007064644 -3.252382e-05 -0.0040460545 100 -0.0049802294 6.400100e-05 -0.0284702013 101 -0.0038383084 5.495640e-05 -0.0219287066 102 -0.0036059566 3.417705e-05 -0.0219287066 103 -0.013231821 9.408086e-06 -0.0075595490 104 -0.003138576 4.493132e-05 -0.0172158905 105 -0.0002828210 2.680561e-06 -0.0016153644 106 0.017507884 -2.610118e-04 0.1003945454 107 -0.0046430352 5.966771	90	-0.0108474718	2.414270e-04	-0.0621280377
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111 -0.0042876215 6.138961e-05 -0.0244973303 112 0.0052057024 -8.153510e-05 0.0297387507 113 0.0000000000 0.000000e+00 0.000000000 114 0.0000000000 0.000000e+00 0.000000000 115 0.0049393724 -7.862635e-05 0.0282156559 116 -0.0048906986 5.901357e-05 -0.0279653053 117 -0.0020861862 3.158151e-05 -0.0119159758 118 0.0079344685 -1.182890e-04 0.0453554092 119 -0.0021136873 3.199783e-05 -0.0120730735 120 -0.0047049813 6.554322e-05 -0.0268861764 121 -0.0042662256 6.108326e-05 -0.0243750029	109	-0.0010109001	-6.480446e-06	-0.0057785209
112 0.0052057024 -8.153510e-05 0.0297387507 113 0.000000000 0.000000e+00 0.000000000 114 0.000000000 0.000000e+00 0.000000000 115 0.0049393724 -7.862635e-05 0.0282156559 116 -0.0048906986 5.901357e-05 -0.0279653053 117 -0.0020861862 3.158151e-05 -0.0119159758 118 0.0079344685 -1.182890e-04 0.0453554092 119 -0.0021136873 3.199783e-05 -0.0120730735 120 -0.0047049813 6.554322e-05 -0.0268861764 121 -0.0042662256 6.108326e-05 -0.0243750029	110	0.0035377975	-1.225359e-04	0.0202994966
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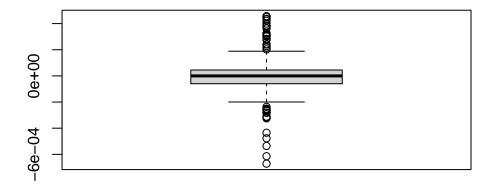
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167	-0.0106377502
168	-0.0010965307
169	-0.0625608597
170	-0.0241746841
171	-0.0043652167
172	-0.0032751181
173	-0.0003340559
174	-0.0909799861
175	-0.0580412823

176	-0.0644172290
177	0.0087155824
178	-0.0253814644
179	-0.0253814644
180	-0.1016670946
181	-0.0081120440
182	0.0190691242
183	0.0103282770
184	-0.0011335585
185	0.0198210819
186	-0.0016081068
187	-0.0358730274
188	0.0211655282
189	-0.0253814644
190	0.0145039442
191	-0.1016670946
192	0.0199200594
193	-0.0255757136
194	0.0199744800
195	0.0187050447
196	-0.0453977184
197	0.0188610730
198	-0.0428249943
199	-0.1048878532
200	-0.0081120440
201	0.0207294373
202	-0.0312827208
203	-0.0111212033
204	0.0058487487
205	0.0662622783
206	0.0090795615
207	-0.0114002919
208	-0.0588742762
209	-0.0600289095
210	0.0171535513
211	-0.0391349619
212	0.0127564874
213	0.0143813856
214	-0.0021405540
215	0.1370243174
216	0.0206755987
217	0.1482344003
218	-0.0348231817

219	0.0211655282
220	-0.0501060398
221	-0.1035457772
222	-0.0348733238
223	-0.0011335585
224	-0.0473776418
225	0.0221365267
226	-0.0869988311
227	0.0471442570
228	0.0199200594
229	0.0190691242
230	-0.0192374244
231	0.000000000
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274	0.0000000000
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283	0.0000000000
284	0.0000000000
285	0.0000000000
286	0.0000000000
287	0.0000000000
288	0.0000000000
289	0.0000000000
290	0.0000000000

boxplot(dfb[,"post_scaled"])



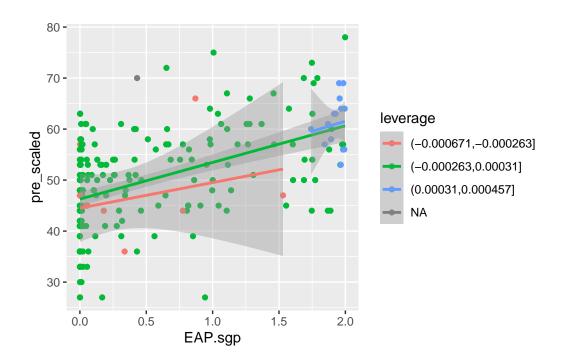
```
leverage <- cut(dfb[,"post_scaled"],quantile(dfb[,"post_scaled"],probs=c(0,.05,.95,1),na.r
summary(leverage)</pre>
```

```
ggplot(ACEDextract,aes(y=pre_scaled,x=EAP.sgp,color=leverage)) + scale_color_discrete() +
```

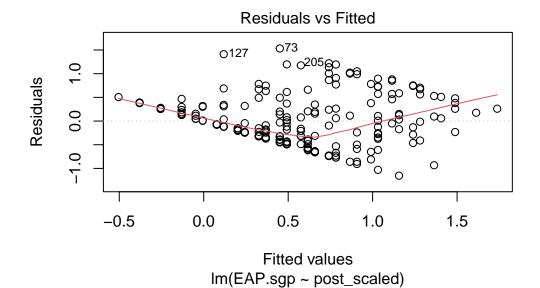
`geom_smooth()` using formula = 'y ~ x'

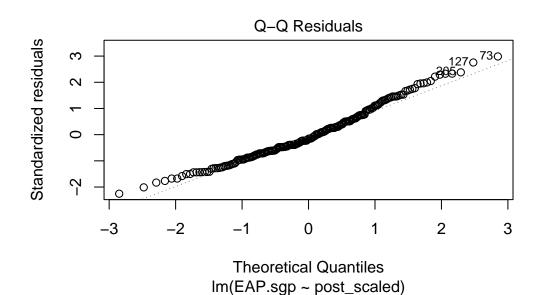
Warning: Removed 62 rows containing non-finite values (`stat_smooth()`).

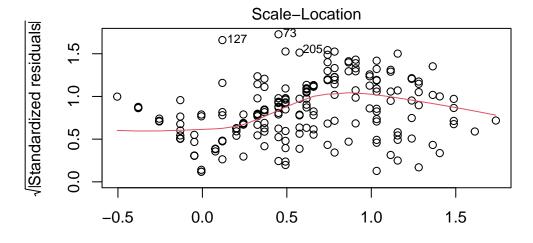
Warning: Removed 62 rows containing missing values (`geom_point()`).



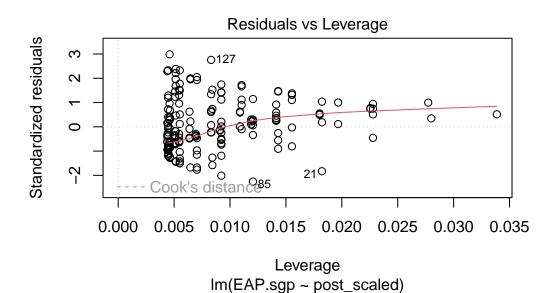
plot(lm_PostxEAP)







Fitted values Im(EAP.sgp ~ post_scaled)



27

Five Assumptions

0. Representative Sample

Missing Data

1. Independent Observations

Time Series

Clusters

2. Linear form

Transformations

3. Homoscedasticiy – Equal variances

Weighted regression

Transforming Y

4. Normality of Residuals

5. Subgroup differences

Color plots by group

Do the groups mix?

Are the slopes similar?

Analysis of Covariance (look ahead)

Outliers and influential points.

Sensisitivity Analysis

Assignment

For the regression post_scaled ~ EAP.sgp; answer the following questions?

0. Are there problems with the sample? Non-representative group? Missing data?

Sample is a single middle school in a wealthy NJ district, so low generalizability to all middle schools.

Most missing data is because control students did not get internal ACED measure (EAP.sgp)

1. Is the distribution the same for everybody in the group? Are there clusters? Serial (time) dependencies?

Grouped by classrooms. (Might want to color by class.)

- 2. Is the relationship mostly linear? Will transforming X or Y make it more linear?
- 3. Is the variance roughly the same for all values of \hat{Y} ? Will transforming Y help?
- 4. Are the residuals roughly normal? Are there any outliers? Will transforming Y help?
- 5. Are there any differences by subgroup?

In the ACED data set, pay attention to Level_Code and Condition_code.