

A Scoping Review of Robotic Tails for Land-based Mobile Robot Locomotion

Damian Crosby^{1,*}, Joaquin Carrasco², William Heath² and Andrew Weightman¹

¹*Department of Mechanical, Aerospace and Civil Engineering, School of Engineering, Faculty of Science and Engineering, The University of Manchester, Manchester, United Kingdom*

²*Department of Electrical and Electronic Engineering, School of Engineering, Faculty of Science and Engineering, The University of Manchester, Manchester, United Kingdom*

Correspondence*:

Damian Crosby

damian.crosby@manchester.ac.uk

2 ABSTRACT

3 The aim of this review was to systematically identify and review literature relating to the design,
4 development and implementation of robotic tails that improve land-based mobile robot locomotion,
5 including static and dynamic balance and jumping, to inform the design of future systems. A
6 systematic literature review was conducted to identify papers relating to land-based robots utilising
7 tails to improve performance in IEEE Xplore, Web of Science and Scopus between January 1980
8 and December 2018. 68 papers were identified, of which 47 papers included a physical robot
9 or prototype, and 33 distinct physical robotic systems were determined. In order of prevalence,
10 robotic tails have been utilised for aerial reorientation, locomotion stability, induced turning,
11 turning stability and velocity change stability. The most common tail structure for individual robots
12 was rigid (79%) with the majority of tails identified composed of a single tail segment (70%) and
13 actuation predominately by revolute electric motors (91%). Control systems were predominately
14 closed outer-loop type. The literature illustrates robotic tails can improve performance but existing
15 work has been limited to low degree of freedom systems. The authors propose that increased
16 robot performance should be contrasted with the additional energy consumption and storage
17 requirements needed to facilitate this.

18 **Keywords:** keyword, keyword, keyword, keyword, keyword, keyword, keyword, keyword

1 INTRODUCTION

19 The motivation for mobile robotics has predominately been driven by the need for systems which can
20 explore hazardous and extreme environments which are too dangerous for people. For example nuclear
21 decommissioning, where radiation is potentially fatal, or planetary exploration, where it is not possible

to send and retrieve astronauts. Mobile robots have been successfully developed and utilised to explore nuclear sites such as Sellafield and Fukushima as well as the Martian surface, however obstacles and challenging terrain limit activities and can lead to the loss of robots which are often non recoverable. Mobile robots have evolved from wheeled machines to legged systems, which can run, jump or hop. These abilities enable mobile robotic systems to better adapt and navigate adverse terrain; In other words mobile robotic systems are becoming increasingly agile. As mobile robots move more towards increased agility, dynamic abilities and biomimetics, this has influenced the direction of research into investigating strategies for improving dynamic performance and stability by exploring the use of robotic tails to improve performance and robustness. Saab & Rone ? recently published a state-of-the-art review of robotic tails in which the authors considered the design, modelling, analysis and implementation of robotic tails for mobile robots. The authors highlighted that robotic tails can be utilised for enhancing stability, manoeuvrability and propulsion of mobile robots, accomplished by enabling inertial adjustment. The review summarises challenges for future development with respect to mechanical design, modelling and control.

In this paper we present the results of a systematic review of literature relating to robotic tails for land-based mobile robot locomotion. This research complements the work of Saab & Rone ? identifying an additional 41 papers and 16 robotic systems. Furthermore, we provide details of tail structure and classification, control, actuation, mass, length, and tail functionality. In this paper we define “tail” as anything that is referred to in the literature as such that meets the inclusion criteria and the topic of the review. This includes tails that are static or unactuated, as they can still influence robot locomotion.

2 LITERATURE SEARCH

A computerised literature search was undertaken of the electronic databases: **IEEE Xplore**, **Web of Science** and **Scopus** between January 1980 and December 2018, searching for **Tail** or **Appendage** in the document title. Papers were excluded if they concerned water walking, swimming or flying robots, as the use of tails in fluid dynamics was not in the scope of the review. The language was limited to English. To identify relevant studies the titles and abstracts of the literature within the databases were scanned with the search terms:

(Tail* **OR** Appendage) **is contained in** *Document Title* **AND** Robot* **NOT** (Fish **OR** Swim) **NOT** (Surgery **OR** Medic* **OR** Tumour) **NOT** (Helicopter **OR** Unmanned Aerial Vehicle **OR** UAV) **NOT** Underwater **NOT** (Chemical **OR** Chemistry) **NOT** Tailor* **is contained in** *Document Title*

The Chemical **OR** Chemistry search terms were included to exclude “tail” in the molecular sense (i.e. the and tail of a polar molecule). The Tailor* negative search term was included to exclude false positives caused by Tail*. An additional search was also conducted using Tail **AND** Tails **AND** Tailed **AND** Tailor* to verify that no relevant records contained both Tail* and Tailor* stems in separate words in the *Document Title*.

To ensure the author identified all relevant literature, that may have been missed by the database search, the authors screened the reference list of the identified papers and cross referenced with the database results.

2.1 Selection and Exclusion Criteria

The following selection and exclusion criteria were utilised to identify literature to meet the aim of the review:

1. Concerning the use of robotic tails with mobile land-based robots to aid locomotion including static and dynamic stability while rolling (i.e. wheeled), walking, hopping/jumping and in free fall.
2. Excluding robotic tails for aquatic locomotion (including water walking), or to aid aerial robotic flight.

2.2 Study Selection Process

The first author (DC) conducted the initial database searches screening all the titles and abstracts. Duplicate records were removed using MATLAB code, which compared the identified paper titles from each database search result, followed by manual inspection of the results by the first author (DC). The full-text of the selected studies were then independently screened against the selection and exclusion criteria by two authors (DC and AW). Any disagreements were resolved through another author acting as a reviewer (WH).

2.3 Data Extraction and Presentation

After literature that met the inclusion criteria had been identified it was analysed and synthesised to identify approaches and corresponding technical details. The following information was extracted and tabulated:

- The **Paper Structure**, which is one of three categories:
 - **Abstract Model:** Papers that discussed tailed robots as an abstract mathematical concept, based on free body models that were based on first principles.
 - **Simulation:** Papers that discussed a detailed virtual model of a tailed robot similar to a physical prototype.
 - **Experimental:** Papers that used a physical prototype or existing robot to generate experimental data.
- The **Locomotion** of the robot or abstract mechanical model, which contains one or more of the following keywords:
 - **Walking:** Leg-based locomotion (bipedal, quadrupedal etc.) on a solid surface with no aerial phase (e.g. Human).
 - **Hopping:** Leg-based locomotion with an aerial phase (e.g. Kangaroo).
 - **Wheeled:** Wheel-based locomotion (e.g. Car).
 - **Tracked:** Track-based locomotion (e.g. Tank).
- The **Control System Architecture** which categorises the control systems into 4 different types based on a simplified control schema. The types are defined as (and illustrated in Figure ??):
 1. A fully “blind” *open-loop* system with no feedback control whatsoever, the system is controlled by a fixed pattern or model that runs in a sequence and takes no inputs.
 2. An *inner-loop* system where position data from the tail actuators are used as inputs to the control system to control the tail position.
 3. An *outer-loop* system where sensor data from the robot (IMU, accelerometer, gyroscope etc.) are used as inputs to the control system to control the tail position.
 4. A *multi-loop* system where both sensor data from the robot *and* position data from the tail actuators are used as inputs to the control system to control the tail position.
- The **Tail Structure**, categorised into three types and described in Figure 3.
 - **Rigid:** Tail is constructed from one or more *rigid* bodies connected by joints. The joints move in order to move the tail, the bodies do not deform.

- 102 • **Flexible:** Tail is constructed from one or more *flexible* bodies connected together rigidly. The bodies
103 deform continuously in order to move the tail.
- 104 • **Pseudo-Flexible:** Tail is constructed from a large number of rigid bodies connected by joints,
105 so many that they approximate a flexible body (this is also referred to in some publications as
106 “serpentine”, for example in ??? and ?).
- 107 • The **Number of Segments** in the tail, which corresponds to the number of bodies connected together
108 with joints in the tail, not including the rest of the robot. Segments can be *Active* or *Passive*, depending
109 on if they are directly controlled by an actuator.
- 110 • The **Tail Dimension Class**, which categorises the tails based on the movement space M of the tip of
111 the tail (or end effector). If a volume V is conceptualised, centred around the base of the tail such
112 that $M \subseteq V$, then M can be found on four distinct operations of V . The classes are defined as (and
113 illustrated in Figure 4):
 - 114 • **Class 1:** M is on a curve on the surface of V .
 - 115 • **Class 2:** M is on a section of V .
 - 116 • **Class 3:** M is on the surface of V .
 - 117 • **Class 4:** M is a volume within (or equal to) V .
- 118 • The **Tail Dimension Class**, which categorises the tails based on the movement space of the tip of the
119 tail (or end effector). The classes are defined as (and illustrated in Figure 4):
 - 120 1. A single revolute joint moves the tip along a circular arc on a plane.
 - 121 2. Multiple parallel revolute joints move the tip within a trimmed portion of a plane.
 - 122 3. Two perpendicular revolute joints move the tip within a trimmed portion of a spherical surface.
 - 123 4. Multiple perpendicular or parallel revolute joints move the tip within a volume.
- 124 • The **Tail Degrees of Freedom** which is typically the number of active segments multiplied by the
125 dimensions each one can be actuated in.
- 126 • The **Actuator** that is used to move the active segments.
- 127 • The **Tail Mass**, in kilograms.
- 128 • The **Body Mass**, in kilograms.
- 129 • The **Tail Length**, in metres.

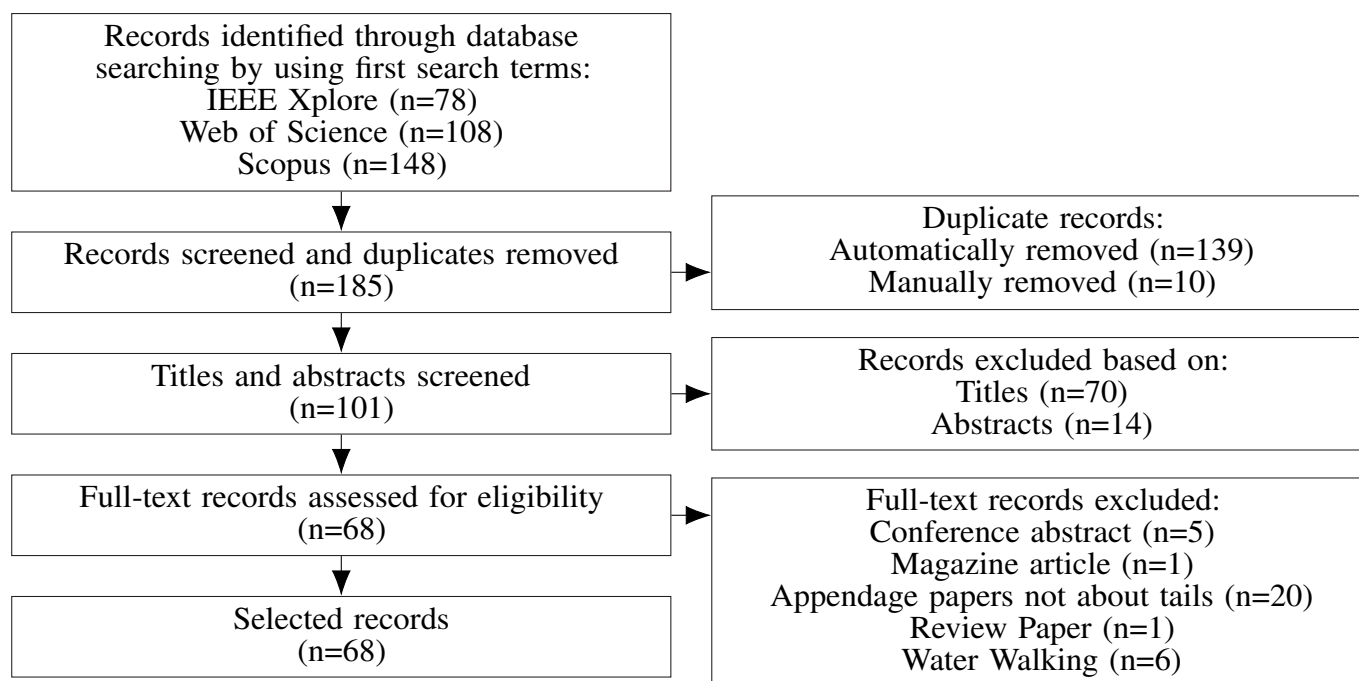


Figure 1. Flowchart of the study selection process.

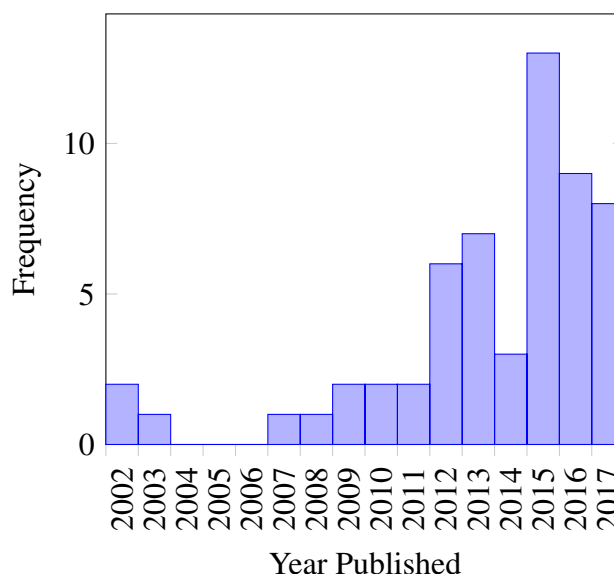


Figure 2. Histogram of the years the 68 selected records were published.

3 RESULTS

Figure 1 illustrates the flowchart of the study selection process and the papers identified. In total **185** studies were identified after duplicates were removed, this reduced to **101** papers after the titles and abstracts had been screened. Out of the **101** papers **33** were excluded because:

- The paper was a short abstract for a conference (**5**).
- The paper was a magazine article (**1**).
- The paper included the **Appendage** keyword in the *Document Title* but was not about tails (**20**).

- 136 • The paper was the review paper ? (1).
- 137 • The paper concerned robots walking on water, like a pond skater (6).

138 This process led to the remaining 68 studies being analysed with data extracted, as detailed in Table ??.

139 33 unique physical robots have been identified from the records (that were physically experimented on in

140 an **Experimental** paper), as detailed in Table ?. Since there were some robots which had multiple records

141 associated with them, some of the records had some duplicate data, which was merged together for each

142 individual physical robot. The data is displayed in Table ?. Papers which did not have a physical robot

143 have this data displayed separately in Table ?. Figure 2 is a histogram of robotic tail papers published as a

144 function of year, the first paper was published in 2002 and approximately 71% (42 papers) of the papers

145 have been published in the last five years since 2013.

146 3.1 Paper Structure

147 Out of the 68 studies identified, 44 were **Experimental** papers, 16 were **Abstract Model** papers, and 8

148 were **Simulation** papers. **Experimental** papers typically develop a control system which is first verified

149 on a simulated model (either an **Abstract Model** or a more complex **Simulation**) then build a prototype or

150 use an existing robot to experimentally verify the control system.

151 3.2 Physical Robots

152 As explained previously, all **Experimental** papers included a physical robot or prototype. In total, 33

153 unique physical robots were found (*images can be found in the supplementary material, all images have*

154 *been sourced from selected papers unless specified*). Out of these, 9 were used in multiple papers. 23

155 named robots were identified from the literature, the rest of the robots had no name and had only a single

156 paper associated with them apart from ? and ?. Table ?? lists the physical robots by name, with the papers

157 they were referenced in and the year the first paper mentioning the robot was published. Table ?? lists the

158 physical robots by their properties. Table ?? lists all the papers that do not have physical robots connected

159 with them.

160 3.3 Research Objectives of Robots Identified in the Literature

161 Table ?? shows diagrams of non-unique research objectives that involved the tail operating in free space

162 (i.e. not in contact with the ground or other objects). All of them involved counteracting or reducing

163 torques.

164 3.3.1 Legged, Wheeled and Tracked

165 Of the 43 **Experimental** papers that included walking, wheeled, tracked or hopping robots, 11 had

166 the objective of correcting any torques induced on the robot so it lands with the correct orientation

167 (?????????), 8 had the objective of correcting torques induced by the unstable motion of the robot to

168 prevent it falling over (?????????), 4 had the objective of minimising roll torques to prevent the robot

169 falling over during a turn (????), and 3 had the objective of initiating a yaw torque on the robot, enabling it

170 to have a smaller turning circle (???). 7 papers dealt with “tail-dragging” robots (????????), that had the

171 tail acting as an appendage for additional stability, locomotion or object manipulation. ? also considered

172 use of a tail (along with rejecting angular momentum) to rebalance the robot following a disturbance, in

173 their example, a “wrecking ball” impacting the torso of the robot. ? used the tail to allow their hopping

174 robot to jump higher. The remaining 2 papers (??) did not state a specific objective.

175 3.3.2 No Locomotion

176 For the 11 papers that dealt with robots with no locomotion, the objectives were more varied. 5 had the

177 objective of testing mechanisms for later inclusion on a legged robot (?????). ? and ? had the objective

178 of re-orienting a robot when dropped, ? had a tail that was designed to vary its stiffness using a novel

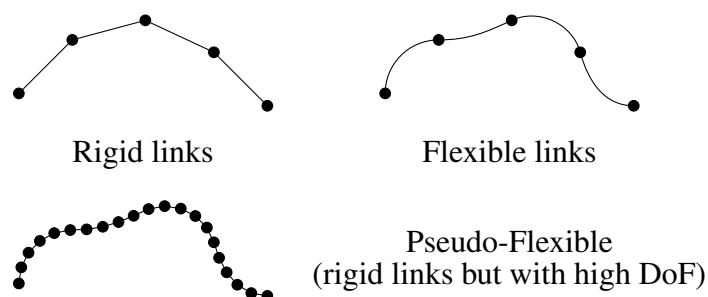


Figure 3. Tail structure classification. Black dots indicate individual joints which may be active or passive.

mechanism, in order for it to be used as both a “hard” appendage when used as a ground support, and a “soft” appendage for other functions. ? used the tail as a self-righting mechanism, and ? considered a novel actuation system for a robot appendage based on a scorpion tail. The desire for mobile robotic systems which can explore hazardous and extreme environments has led to the development of systems which have greater functionality, adaptability, autonomy and dynamic ability. The enablers for the development of the next generation of mobile robotic systems include:

1. Increased simulation capabilities such that designs can be optimised before prototyping,
2. Advances in embedded computing power improving sensing and intelligent control systems. The capability of mobile robots, which can walk, run, hop and jump has created a need for the investigation and development of systems which can improve dynamic performance and robustness of outcome.

Many research groups have developed robotic tail models and physical systems for the purpose of improving the dynamic performance of mobile robots. Mobile robots utilising tail actuators have demonstrated improvements in performance, and they predominately have a limited number of degrees of freedom (????). There are several distinct areas for future research.

3.4 Robot Physical Properties

3.4.1 Walking Robots

Of the 12 walking robots, 3 were Bipedal (?????), 3 were Quadrupedal (???), 5 were Hexapedal (?????), and 1 was Octopedal (?). (?) was Bipedal, but used the tail as a “third leg”, technically making it Tripedal.

3.5 Tail Physical Properties

3.5.1 Tail Structure

Table ?? illustrates that a rigid tail, made up of rigid bodies connected by joints, is the commonest physical tail structure with 31 robots, followed by a flexible structure, made up of flexible bodies that act as joints, with 4 robots, and pseudo-flexible, made up of a large number of mostly passive rigid joints that closely approximate a flexible body, with 3 robots (Figure 3 gives an illustration of this difference). Most of the non rigid robots were static experiments with no locomotion, apart from (??), though several (???) were testing static systems with an eventual aim of mounting on a legged robot.

3.5.2 Tail Segmentation

Table ?? illustrates that 22 robots had one tail segment, and 9 robots had more than one tail segment. Out of the 9 robots with more than one tail segment: 5 had 2-segments, 1 had 3-segments, 1 had 4-segments and 2 had 6-segments. ?? was a piece of unactuated flexible rope, which could be considered to have a nearly infinite number of segments. A common justification for an increased number of segments was the

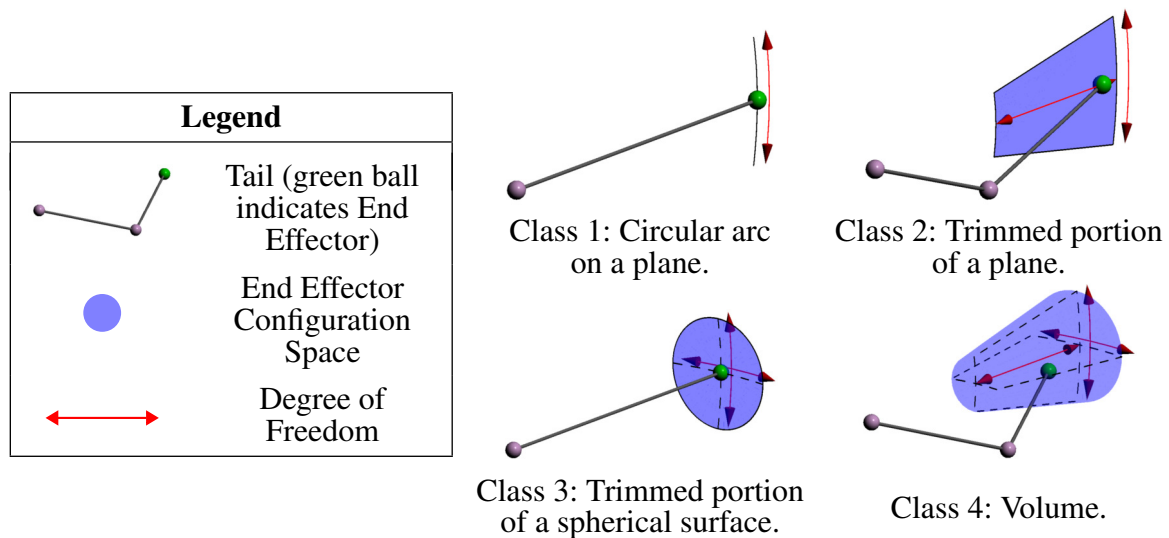


Figure 4. Tail Dimension Class visual illustration.

210 increased reaction torque available for a given length, as found in ?. This came at the cost of requiring
 211 additional actuators, except in ? which used a passive system, though the gains were marginal in that case
 212 (a 7% increase in jump height).

213 3.5.3 Tail Dimension Class

214 Tables ?? and ?? illustrate that 17 robots had a tail dimension class of **1**, where the range of motion for
 215 the tail end effector is restricted to a circular arc on a plane, typically a simple “pendulum” design of a
 216 mass on the end (or along) a rod of negligible mass with a rotary joint that allowed the robot to adjust
 217 its moment of inertia in one axis when performing a manoeuvre. 9 robots had a similar design but with
 218 an extra degree of freedom to turn the the single revolute joint into two perpendicular revolute joints,
 219 giving the tail a dimension class of **3**, where the end effector range is restricted to the trimmed surface
 220 of a sphere, typically for the purpose of allowing the robot to induce torques in two axes instead of one
 221 (such as aerial reorientation in both pitch and roll axes). Inducing torques in all three axes did not appear
 222 to be considered, as in stability applications maintaining yaw angle was not required. More complicated
 223 multi-segment designs were also found in 9 robots, which all had a tail dimension class of **2**, where the
 224 end effector is restricted to a planar cross-section of a volume, or **4**, where the end effector is free to
 225 move within a volume, typically for increased reaction torques as mentioned previously (Figure 4 gives an
 226 illustration of the different classes). Finally, 3 robots had a static tail. Of the 12 physical robots which have
 227 been developed for walking, 9 had a tail dimension class of **1**, and 3 robots had a class of **3**. For the other
 228 types of locomotion, hopping, wheeled, wheeled and hopping, and tracked there were too few papers and
 229 different class categories to determine correlations.

230 3.5.4 Tail Degrees of Freedom

231 As can be seen from Table ??, 17 robots had 1 degree of freedom, 11 robots had 2 degrees of freedom, 1
 232 robot had 3 DoF, 2 robots had 4 DoF, 1 robot had 6 DoF and 1 robot had 7 DoF. 1 robot had a static tail
 233 (??) and 1 robot (??) had an unactuated rope which had infinite degrees of freedom. Higher degrees of
 234 freedom than 2 exclusively corresponded to multi-segment designs with the corresponding performance
 235 improvements, whereas 2 degrees of freedom was a mix of additional torque axis (dimension class 3) and
 236 multi-segment designs (dimension class 2).

3.6 Tail Actuation

As can be seen from Table ??, 26 robots, or 91% used a **Revolute Motor** to actuate the tail. 4 robots used revolute motors to move cables via pulleys. For the other 9%, 1 robot had a static tail (??), 1 robot had an unactuated completely passive tail (??), and 1 robot also used stored energy via a spring instead of stored electrical energy (?).

3.7 Control Systems

3.7.1 Controller/Model

As can be seen in Figure ??, each system can be described as having a Controller/Model, where the commands for controlling the tail actuators (whether real or virtual) are generated. These can be described as “fixed” or “variable”. Fixed systems (type 1 and type 2) do not accept external input from the robot, running a periodic sequence or pattern, or following remote commands sent by a user. This is a simple control system to implement, and in some highly deterministic stability applications or experiments it is sufficient for satisfactory performance. Variable systems (type 3 and type 4) use sensor data from the robot to influence the output of the Controller/Model, typically when using the tail to correct or induce force, in a quasi feedback loop (Figure ?? shows a block diagram of each controller/model). As can be seen in Table ??, 7 papers described a type 1 (open-loop) system, 15 papers described a type 2 (inner-loop) system (typically due to the use of servo motors, which turn any system they are implemented in into at least inner-loop), 18 papers described a type 3 (outer-loop) system, and 13 papers described a type 4 (multi-loop) system. 5 papers were either static or uncontrolled systems, and 10 papers did not consider, or did not have enough information to determine, a control system.

There didn’t appear to be any noticeable correlations between the control system and other properties of the robots, as it depended on the experimental setup, and whether the system was designed to apply to determined torques induced by robot actions (such as a walking or hopping motion) or undetermined torques from the environment (such as driving off a ledge or navigating uneven terrain).

3.7.2 Feedback Control Systems

For position feedback of the tail joints (type 2 and type 4), P (?), PD (?????), PI (?), PID (????) and State Feedback (?) control systems were used.

For variable Controller/Model systems (type 3 and type 4), P (??), PD (????????????), PI (??) PID (?) and State Feedback (?) control systems relating sensor data to tail joint position. ? used a simple Bang/Bang control system due to the variable friction present on the model.

Regarding performance of different control systems, ? outlined a simulation comparing a P and PD control law, and found a marginal but noticeable increase in performance in the PD control law (a 6% increase in “crossed distance” and a 9% reduction in mechanical energy), and ? compared PD and sliding mode control, again finding an increase in performance (a 75% reduction in overshoot for the tail controller) for sliding mode control.

3.8 Locomotion/Tail Dimension Class

Table ?? shows the relationship between the robot locomotion and the tail dimension class. Class 1 was the most prevalent in all of the mobile robots, followed by class 3, whereas static experiments typically used more complex tails. Tail dimension class was generally associated with the axes the tail was designed to induce torques on, with class 1 only able to induce torque on a single axis, and class 2 being a multi segment version of class 1. Class 3 and 4 could induce torques on 2 or more axes, allowing for enhanced functionality, such as being able to control both the pitch and roll angle of the robot in aerial reorientation.

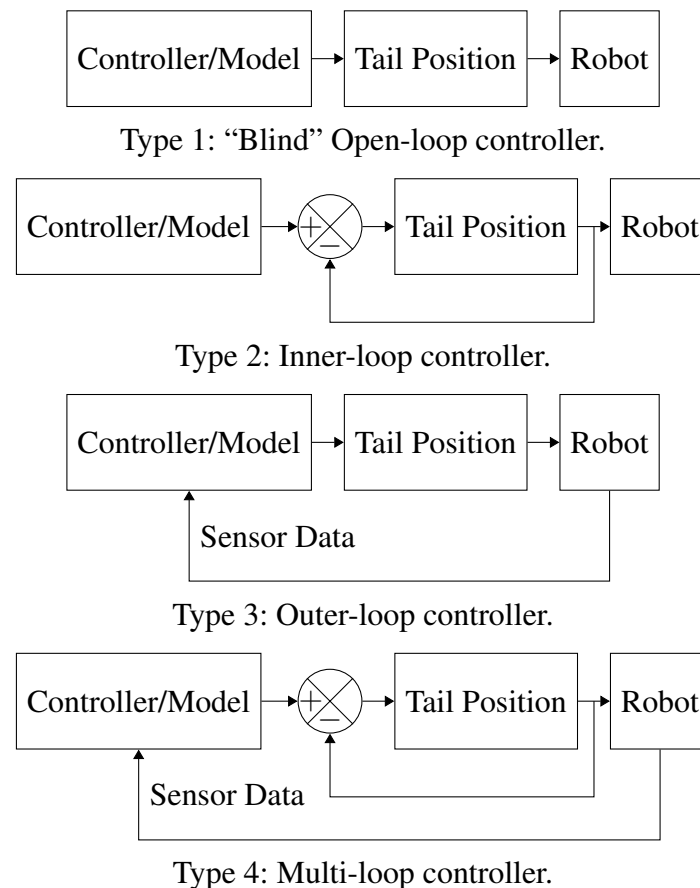


Figure 5. Control system classification for robotic tails.

4 DISCUSSION

279 4.1 Potential Future Research

280 4.1.1 Dynamically Changing Plant

281 All the studies appear to consider robots (when without their tails) that had a static mass, centre of mass
 282 and tensor of inertia. Future work could consider robots with these properties changing dynamically. It
 283 is likely that mobile robotic systems will pick up and manoeuvre payloads, carry unstable payloads such
 284 as a container filled with fluid, or will have an appendage such as a manipulator arm that is independent
 285 of locomotion. As such there will be a motivation for robotic tails to be utilised to compensate for this
 286 dynamic behaviour.

287 4.1.2 Energy Consumption and Storage

288 The use of energy in control systems is a well understood topic that has been the subject of many
 289 publications, such as ?, hence the control of the tail may be associated with the consumption of energy.
 290 However, the literature reviewed does not indicate there has been significant consideration regarding the
 291 energy consumption of the robotic tails. There are some calculations presented regarding peak power output
 292 in order to determine actuator specifications (?), but nothing considering actual energy consumption. There
 293 is likely to be a trade-off between energy consumption and the improved robot agility that a robotic tail
 294 enables. Furthermore, there are few details in the literature regarding the energy storage needs to enable the
 295 increased actuation of a robotic tail, clearly additional storage needs will add mass and therefore impact
 296 the dynamic behaviour of the mobile robotic system. The authors would encourage the community to

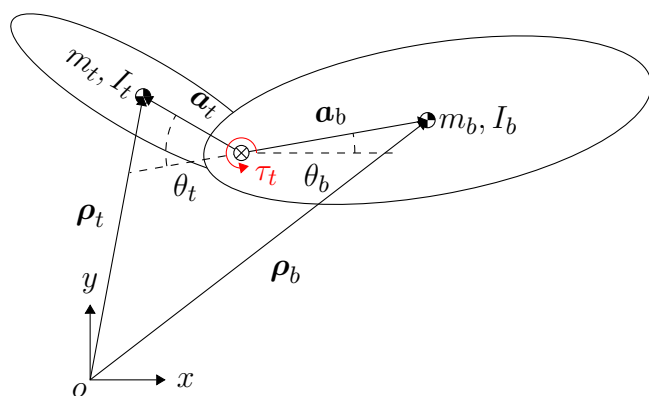


Figure 6. A planar rigid body diagram of a generic robot with a 1 DoF tail.

provide more details regarding their systems to enable comparisons between different actuator, sensor and controller configurations.

4.2 Actuator Technologies

The choice of actuator for mobile robotics systems is crucial for achieving the potential increased agility desired. DC brushed and brushless electric motors offer good speed and torque characteristics but will add significant mass and for large numbers of degrees of freedom increase control complexity. Stepper motors decrease control complexity in comparison to DC brushed/brushless motors but will add significant mass and have limited capability for high-speed operation. Relative to electric motor solutions artificial muscles are much lighter whilst having suitable force characteristics, their main limitations include hysteretic behaviour and bandwidth. The search for low mass, high force/torque, high bandwidth actuators will no doubt continue.

5 CONCLUSION

The desire for mobile robotic systems which can explore hazardous and extreme environments has led to the development of systems which have greater functionality, adaptability, autonomy and dynamic ability. The capability of mobile robots which can walk, run, hop and jump, has created a need for the investigation and development of systems which can improve dynamic performance and robustness of outcome. Many research groups have developed robotic tail models and physical systems for the purpose of improving the dynamic performance of mobile robots. Mobile robots utilising tail actuators have demonstrated improvements in performance, predominately these have a limited number of degrees of freedom. Barriers that may inhibit the development of robotic tail systems for mobile robots include the additional storage/drain on system energy supply, high performance low mass actuation for multiple degrees of freedom and complexity of control. There is clearly the potential for further research in this field, which could see improved dynamic performance, and robustness for mobile robotic systems. Robotic tails offer great potential to improve the dynamic performance of mobile robotic platforms. Research in this area has grown over the last 10 years with modelling/simulation and experimental approaches adopted, demonstrating robotic tails can improve performance. The authors hope that this scoping review will provide a useful reference for those research groups working in this area and those who wish to contribute in the future.

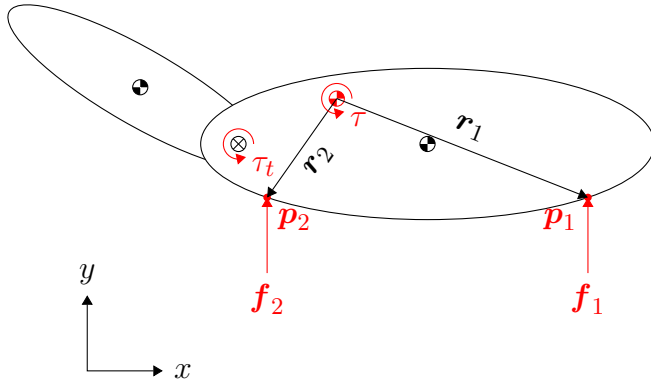


Figure 7. A planar rigid body diagram of a generic robot with a 1 DoF tail.

6 RIGID BODY MODELS

In order to understand the diverse range of functions a robot tail can perform, a rigid body model can be used in order to simplify and abstract the dynamics of each application. In essence, any robot with a tail can be described as two bodies, the main robot body with mass m_b and inertia I_b , and the tail with mass m_t and inertia I_t , joined by a pivot which can generate a torque τ_t in one or more axes. For a robot with a multi-segment tail, any configuration of the joints in the tail can be abstracted into a single pseudo-body and a base pivot torque with suitable dynamics calculations. The other coefficients of the system are a_b and a_t , which denote the vectors from each body's COM to the pivot. The kinematic state of the system can then be described with θ_b and θ_t , denoting the absolute rotation of the robot body and the relative rotation of the tail body to the robot body, and ρ_1 and ρ_2 , denoting the vectors from the origin to each body. However, only one of ρ_b and ρ_t needs to be known, since each can be calculated from the other coefficients and kinematic state variables.

6.1 Aerial Reorientation

Many robots use jumping as a means of locomotion, or to reach otherwise inaccessible areas. Other robots are designed to drive off ledges. The “jump” can be described as impulse forces f_n on one or more points p_n on the main robot body (such as the foot of a leg), where r_n describe the vectors from the robot COM, calculated by $\frac{m_1\rho_1+m_2\rho_2}{m_1+m_2}$ to the points. As long as $\sum f_i \times (m_b + m_t)g > (m_b + m_t)g$, where g is the gravity vector, then the robot will be lifted into the air. However, if $\sum f_i \times r_i \neq 0$, then a torque τ will be induced around the COM of the robot, which will then change θ_b as $\dot{\theta}_b = \frac{\tau_b}{I_b}$. This could result in the robot landing with an orientation that prevents locomotion or causes damage to the robot. This is certain to occur to some extent in a practical application, as even if all the contact points are evenly spaced from the COM ($\sum r_i = 0$), all the elements of f_n are never going to be exactly equal due to differences in actuation. Therefore, by inducing a torque τ_t on the tail

Table 1. Comparison of Robot Locomotion to Tail Dimension Class.

Locomotion	Tail Dimension Class					Total
	1	2	3	4	0 (Static)	
Walking	9	0	3	0	0	12
Hopping	1	2	1	0	0	4
Wheeled	2	1	2	1	1	7
Wheeled, Hopping	1	0	0	0	0	1
Tracked	1	0	0	0	0	1
None	1	1	2	4	0	8
Total	15	4	8	5	1	33

Table 2. Table of all the physical robots, the year it was first seen in a selected paper and the selected papers it was found in.

References	Robot Name	First Published
?	3DoF No Catch	2017
?	Cheetah-Cub	2016
?	DMST	2018
?	Dcat	2016
??	Dima	2013
?	Dima II	2015
?	Helios VIII	2009
??	IMPASS	2009
?	LoadRoACH	2018
?	MIT Cheetah	2012
???	MSU Tailbot	2013
?	MuddyBot	2016
?	OctoRoACH	2012
?????	Penn Jerboa	2015
?	R3-RT	2018
?	RoMiRAMT	2015
??	TAYLROACH	2012
??	Tailbot	2011
???	Titrus III	2002
?	USRT	2018
?	VelociRoACH	2017
??	XRL/RHex	2012
?	Zappa	2008
?	-	2018
?	-	2013
?	-	2013
?	-	2010
?	-	2014
?	-	2013
?	-	2016
?	-	2016
??	-	2017
?	-	2018

Table 3. Table of the physical robots. “Tail DoF” refers to the total number of DoF, including passive joints. Robots with passive DoF are denoted with a superscript. Number of decimal places reflects the precision found in the references.

Reference	Locomotion	Tail Structure	Number of Segments	Tail Dimension Class	Tail DoF	Actuator	Tail Mass (kg)	Body Mass (kg)	Tail Length (m)
?	None	Rigid	2	4	3	Revolute Motor	0.33	0.99	N/A
?	Walking	Rigid	1	1	1	Revolute Motor	0.053	1.197	0.128, 0.168
?	None	Pseudo-Flexible	2	3	2	Revolute Motor ³	3.5	9.525	0.3
?	Walking	Rigid	1	1	1	Revolute Motor	0.25	5.312	0.3
??	Wheeled	Rigid	1	3	2	Revolute Motor	0.4	5	0.5
?	Wheeled	Rigid	1	3	2	Revolute Motor	0.4	5	0.5
?	Tracked	Rigid	1	1	1	Revolute Motor	N/A	N/A	0.5
??	Wheeled	Rigid	1	0	0 ¹	Static Tail	N/A	N/A	0.889
?	Walking	Rigid	1	1	1	Revolute Motor	N/A	N/A	0.09
?	Walking	Rigid	1	3	2	Revolute Motor	0.74	35	0.54
???	Wheeled, Hopping	Rigid	1	1	1	Revolute Motor	0.017	0.0252	0.127
?	Walking	Rigid	1	3	2	Revolute Motor	N/A	N/A	0.02
?	Walking	Rigid	1	1	1	Revolute Motor	0.017	0.035	0.1
????	Hopping	Rigid	1	3	2	Revolute Motor	0.15	2.269	0.21
?	None	Pseudo-Flexible	2	2	2	Revolute Motor	N/A	8.8	N/A
?	Wheeled	Rigid	2	2	2	Revolute Motor	N/A	N/A	N/A
??	Walking	Rigid	1	1	1	Revolute Motor	0.004	0.045	0.115
??	Wheeled	Rigid	1	1	1	Revolute Motor	0.017	0.16	0.127
???	Walking	Rigid	1	3	2	Revolute Motor	0.1	0.1	N/A
?	None	Rigid	6	4	6	Revolute Motor ³	0.51	6.507	0.48
?	Walking	Rigid	1	1	1	Revolute Motor	0.008	0.0767	0.09
??	Walking	Rigid	1	1	1	Revolute Motor	0.6	8.1	0.59
?	Walking	Rigid	1	1	1	Revolute Motor	0.7	0.05	0.15
?	Hopping	Flexible	4	2	4	Revolute Motor ³	0.047	N/A	0.21
?	Walking	Rigid	1	1	1	Revolute Motor	0.005	0.0395	0.12
?	None	Rigid	1	3	2	Revolute Motor	0.07	0.105	0.73
?	None	Rigid	1	1	1	Spring	0.048	0.204	N/A
?	Hopping	Rigid	1	1	1	Revolute Motor	0.371	0.423	0.177
?	Wheeled	Rigid	1	1	1	Revolute Motor	0.089	0.862	0.27
?	Hopping	Pseudo-Flexible	6	2	6 ²	Revolute Motor	0.1	1.045	0.235
?	None	Flexible	2	4	4	Revolute Motor ³	N/A	N/A	0.41
??	Wheeled	Flexible	∞	4	∞	Unactuated	0.035	0.7	0.7
?	None	Flexible	3	4	7	Revolute Motor	N/A	N/A	N/A

¹(Static) ²(1 Active, 5 Passive) ³(Cable Driven)

Table 4. Table of all the papers that did not use physical robots. “Tail DoF” refers to the total number of DoF, including passive joints. Papers with passive DoF are denoted with a superscript. Number of decimal places reflects the precision found in the references.

Reference	Locomotion	Tail Structure	Number of Segments	Tail Dimension Class	Tail DoF	Actuator	Tail Mass (kg)	Body Mass (kg)	Tail Length (m)
?	Walking	Rigid	1	1	1	N/A	0.7	N/A	0.15
?	Hopping	Rigid	1	1	1	N/A	N/A	N/A	N/A
?	Wheeled	Pseudo-Flexible	10	1	10 ¹	Revolute Motor	0.307	N/A	0.2
?	N/A	Rigid	N/A	N/A	Multiple	N/A	N/A	N/A	N/A
?	Walking	Flexible	10	2	12 ²	N/A	1327.96 (mg)	N/A	0.2659
?	Wheeled	Rigid	1	1	1	N/A	N/A	N/A	N/A
?	Walking	Rigid	1	3	2	N/A	1.4347	26.9078	0.6
?	Walking	N/A	1	1	1	N/A	N/A	N/A	N/A
?	N/A	Rigid	1	1	1	N/A	0.5-4	N/A	0.2-0.5
?	Walking, Hopping	Rigid	1	3	2	N/A	N/A	N/A	0.1
?	Walking	Rigid	1	1	1	N/A	1	N/A	0.8
?	None	Flexible	1/2	3/4	2/4	Linear Screw Motor ³	2.25	N/A	0.5
?	None	Pseudo-Flexible	2	3	4	Cable Driven	0.33585	N/A	0.44
?	Walking	Rigid	6	2	1-6	N/A	2.4	N/A	0.5
?	None	Rigid	6	4	6	N/A	0.449	N/A	0.48
?	Walking	Pseudo-Flexible	12	4	3	Revolute Motor	3.96	N/A	0.5118
?	Walking	Pseudo-Flexible	2	3	2	Revolute Motor ³	1	N/A	0.12
?	Walking	Rigid	1	1	1	N/A	0.3	15	1.0
?	Walking	Rigid	1	3	2	N/A	0.026, 0.00753	N/A	0.106, 0.116
?	Wheeled	Rigid	1	1	1	N/A	N/A	N/A	N/A
?	Hopping	Rigid	1	1	1	N/A	1.5	28.5	0.4

¹(1 Active, 9 Stiffness Adjustment) ²(10 Active, 2 Passive) ³(Cable Driven)

Table 5. Comparison of control system classification with paper structure. In addition to the classifications specified in figure ??, 0 indicates a tail with no control system.

Paper Category	Control System Classification					
	N/A	0	1	2	3	4
Abstract Model	???	?	?	-	?????	???
Modelling & Simulation	????	-	?	-	??	-
Experimental	?	???	????	????????????	????????	????????

Table 6. Non-unique tail functions operating in free space.

Function	Diagram	Description	Papers
Aerial Reorientation	<p>The diagram illustrates two scenarios for aerial reorientation. The top scenario shows a robot jumping (upward blue arrow) and landing (downward blue arrow) with its tail extended, illustrating reorientation around the Roll Axis. The bottom scenario shows a robot jumping and landing with its tail extended, illustrating reorientation around the Pitch Axis.</p>	<p>The robot either jumps or moves off an edge. Whilst airborne, the tail is used to correct any torques induced on the robot so it lands with the correct orientation. This can be in the pitch or roll axis.</p>	<p>???????????? (Total: 14)</p>
Locomotion Stability	<p>The diagram shows a robot on a rough surface, tilted to the right. A red arrow indicates the direction of the tail's movement to correct the tilt. The text 'Roll Axis' is written below the diagram.</p>	<p>The robot walks or drives over a rough surface. The tail is used to correct torques induced by the unstable motion of the robot to prevent it falling over.</p>	<p>???????????? (Total: 13)</p>
Induced Turning	<p>The diagram shows a robot moving forward (indicated by a blue arrow). A red arrow indicates the direction of the tail's movement to initiate a yaw torque. The text 'Yaw Axis' is written below the diagram.</p>	<p>The tail is used to initiate a yaw torque on the robot, enabling it to have a smaller turning circle.</p>	<p>???? (Total: 4)</p>
Turning Stability	<p>The diagram shows a robot making a turn (indicated by a blue arrow). A red arrow indicates the direction of the tail's movement to minimise roll torques. The text 'Roll Axis' is written below the diagram.</p>	<p>When a fast moving robot makes a turn, the tail is used to minimise roll torques to prevent it falling over.</p>	<p>???? (Total: 4)</p>
Velocity Change Stability	<p>The diagram shows a robot undergoing acceleration or deceleration (indicated by blue arrows). A red arrow indicates the direction of the tail's movement to minimise pitch torques. The text 'Pitch Axis' is written below the diagram.</p>	<p>When a fast moving robot undergoes acceleration (or deceleration) the tail is used to minimise pitch torques to prevent it falling over.</p>	<p>?? (Total: 2)</p>