

1. This algorithm takes  $O(m)$  to process the whole sequence. That is because the algorithm runs on the inputs which are the edges(m).

2. T

union (A, B)

union (A, C)

find (C)

Output: set 0

find (D)

Output: set 1

union (G, H)

union (F, G)

find (H)

Output: set 3

union (C, F)

find (H)

Output: set 0

3. This wouldn't work in this case because id2 needs to be stored outside of the for-loop. Or, the value of ID[i] will be compared to the new value of id2 instead of the original value of id2

4. R

5. 5

Finding the MST by "Eyeballing" the weighted graph:

0 → 1 → 3 → 2 → 4 → 6

Finding another spanning tree that's not minimal:

0 → 1 → 3 → 2 → 6

6. Because the MST is the most efficient path between two vertices has to use the least weighted edge to reach the end vertex. As a result, we get the most efficient path from two nodes with the least weight possible.

7.

8. For a sparse graph, you have less edges than the vertices, and for a dense graph you have much more edges. When forming an adjacency-matrix, the time complexity is  $O(v^2)$  and for an adjacency-list it's  $O(E)$ .

- Dense:  $O(E \log E) \rightarrow O(E \log v^*) \rightarrow O(2E \log E) \rightarrow O(E \log E)$

- Sparse:  $O(E \log v) \rightarrow O(E \log E^*) \rightarrow O(2E \log v) \rightarrow O(E \log E)$

9.

10. Algorithm: buildMatrixUsingPred( int[] predecessor )

int[][] retMatrix = matrix for i = 0 to matrix.length

for j = 0 to matrix[i].length

    If i != j AND i = predecessor[j]

    Return end-if

```
    else
      ReturnMatrix[i][j] = -1
    end-else end-for
  end-for
  return retMatrix
```

11.

Sorted linked list.

Worst-case of extractMin  $O(1)$

Worst-case of decreaseKey  $O(n)$

Unsorted array.

Worst-case of extractMin  $O(n)$

Worst-case of decreaseKey is  $O(1)$

12.

13. We can use Dijkstra's Algorithm which can use either while loops or recursion. It has to iterate through each node and find a path for every vertex.

Running time estimate would be  $O(V + E \log V)$ .