

Module 10

10.1 615 miles

10.2 $\frac{(n-1)!}{2}$ because you chose any first city and account for the reverse

10.3 123, 1-2-3, 12-3, 13-2, 23-1

10.4

10.5

a. Alg1 0, 01, 012, 0123. Alg2 0, 02, 021, 0213

b. Algorithm 1: $O(n-1)$

c. Algorithm 2: $\frac{(n-1)!}{2}$

10.6 #1 is a polynomial, 2 is a polynomial, 4 is not, 5 and 6 both are.

10.7 #1 is because it meets all the conditions, 2 is not because there aren't different states and no cost. 3 is not because they're infinite state space. And 4 is a combinatorial optimization

10.8

A1 If we create one tour to 0. We flip a coin to determine if a given tour has less cost than our best tour or not. Heads means yes. tails is no.

$\text{minTour} = s_0 \xrightarrow{s_1} \text{minTour} = s_0 \xrightarrow{\text{tails}} \text{minTour} = s_0$
 $s = s_0 \qquad s = s_1 \qquad s = s_2$

$\xrightarrow{\text{Heads}} \text{minTour} = s_2 \xrightarrow{s_3} \text{minTour} = s_2$
 $s = s_2 \qquad s = s_3$

A2 There, we would still use the coin to randomize a tour but we also roll a die to decide which two points

$\text{minTour} = S_0 \xrightarrow[(1,2)]{S_1} \text{minTour} = S_0 \xrightarrow[\text{heads}]{S_1} \text{minTour} = S_1$
 $S = S_0 \quad S = S_1 \quad S = S_1$

$\xrightarrow[(3,4)]{S_2} \text{minTour} = S_1 \xrightarrow[\text{tails}]{S_2} \text{minTour} = S_1$
 $S = S_2 \quad S = S_2$

10.9 Alg 1: $O(n-1)$
 Alg 2: $\frac{O(n-1)!}{2}$

10.10 nextState (state s)

$t = s$

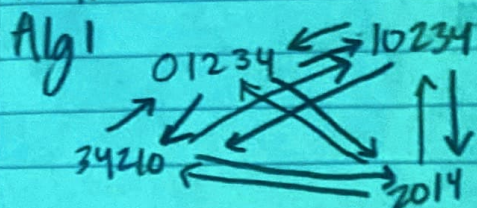
pick a random point in t

pick a number smaller than the first

Swap the numbers

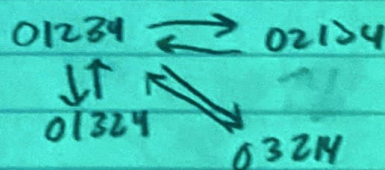
return t

10.11



There are $(n-1)!$ States

Alg 2



There are $\frac{(n-1)!}{2}$ states

10.12 Alg 1: nextState(s)

b = generate random arrangement
return b

Alg 2: nextState(s)

b = s

Pick any random items in b

Swap

If one doesn't fit put in new bin
return b

10.14

$$\begin{array}{c} 5^2 \\ \swarrow \quad \searrow \\ 4^2 + 6^2 = 52 \end{array} + \begin{array}{c} 5^2 \\ \swarrow \quad \searrow \\ 3^2 + 7^2 = 58 \end{array} = 50$$

10.15 as $T \rightarrow \infty$ $r \rightarrow 1$
as $T \rightarrow 0$ $r \rightarrow \infty$