

### 7.1

A complete graph is an undirected graph where each distinct pair of vertices has a unique edge connecting them. This is intuitive in the sense that you are basically choosing 2 vertices from a collection of  $n$  vertices simplified to  $C(n,2)$ . Using the formula for binomial coefficients,  $C(n,2) = n(n-1)/2$ . In terms of big  $O$  it is  $O(n^2)$

### 7.2

$d$  of a  $V$  is the number of  $m$  connected to it

$D/2 = m$  because in a connected graph you have vertices getting connections from two other vertices

### 7.3

1 - 2 - 3 - 1

Pros - transversal

Cons - Each edge needs twice as much storage space.

### 7.4

The size of the adjacency matrix representation is  $O(V * V)$  and the size of the adjacency list representation is  $O(|V|+|E|)$

### 7.5

```
LinkedList<GraphE> [] adjList
```

```
int n
```

```
public adjacencyList( int n)
```

```
{
```

```
    This.n = n
```

```
    This.adjList = LinkedList<GraphE> [] new LinkedList<> [n]
```

```
    for (int i = 0; i < n; i++)
```

```
    {
```

```
        adjList[i] = new LinkedList<GraphE>
```

```
    }
```

```
}
```

### 7.6

By checking the outputs we could find out whether the graph is a connected tree. If the output of `numConnectedComponents` is 1 and the output of `exist cycle` is false then the graph is a connected tree.

### 7.8

We need to modify the code to add a counter variable to the `breadthFirstMatrix` method and we have to increment it at the end of the program after line 9

### 7.9

Because  $V^2$  is the largest term we can really discard the other elements. An adjacency list is more efficient in terms of storage because it only stores what is necessary.

7.12

Vertex 0 leads to an infinite loop because it just iterates through the same elements, we can solve this by adding a counter to check if all nodes were visited

7.13

Order the DFS

Loop through the graph

Get visited list

At  $i$  you need to check all of the vertices that it are connected to vertex at  $i$

Recursively check its connected vertices