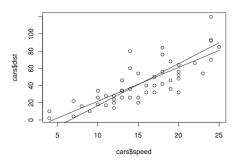
### Math 314: Statistics

Chapter 10: Regression



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# The Regression Line

- The regression line for y on x estimates the average value for y corresponding to each value of x.
- Associated with each increase of one SD in x, there is an increase of only r SDs in y, on the average.
- To see why r is the right factor, consider the cases r = 0, r = 1 and r = -1.
- The regression line is a smoothed version of the graph of averages.
- The equation for the regression line is (where r = the correlation coefficient):

$$(y - \text{mean}_y) = r \frac{\text{SD}_y}{\text{SD}_x} (x - \text{mean}_x)$$

$$(\text{mean}_x, \text{mean}_y)$$

$$r \text{SD}_y$$

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# Using R to Find a Regression Line

• Example from pages 132–133.

```
> x <- c(1, 3, 4, 5, 7)
```

$$> y <- c(5, 9, 7, 1, 13)$$

- > source("http://www.adjoint-functors.net/SDline.R")
- > SDline(x, y)

```
$meanX=4, $meanY=7, $slope=2, $correlation=0.4
```

- > linearModel <-  $lm(y \sim x)$
- > summary(linearModel)

#### Coefficients:

```
Estmate Std. Error t value Pr(>|t|)
(Intercept) 3.800 4.733 0.803 0.481
x 0.800 1.058 0.756 0.505
```

Residual standard error: 4.733 on 3 degrees of freedom

Multile R-squared: 0.16, Adjusted R-squared: -0.12

F-statistic: 0.5714 on 1 and 3 DF, p-value: 0.5046

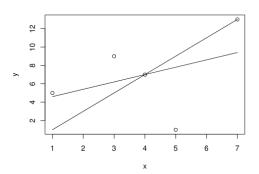
### Plot the SD and Regression Lines

• Example from pages 132–133

```
> x <- c(1, 3, 4, 5, 7)
```

$$> y <- c(5, 9, 7, 1, 13)$$

- > plot(x, y)
- > lines(x, 2\*x 1, type="l")
- > lines(x, 0.8\*x + 3.8, type="l")



### Cars Data

- Use the following to get the equation for the SD line of the cars data
- SDline(cars\$speed, cars\$dist)
- plot(cars\$speed, cars\$dist)
- Add the SD line to your plot.
- Use the following to get the regression line
- ullet linearModel <- lm(cars\$dist $\sim$ cars\$speed)
- Add the regression line to your plot.

