Aproximacion de pade

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0.1. Problema

Aproximación del seno

```
program pade
implicit none
!declaracion de variables
real(kind=8), external :: seno_p
real(kind=8) :: seno_z, x, y, error, dx
real, parameter :: Pi= 3.1415926
integer :: i, n
!salida de datos
open (11, file = 'seno.dat')
 n = 1000
 x = -2.0 * Pi
 dx = 4.0 * Pi/n
 do i = 1, n
   x = x + dx
     seno_z=Sin(x)
     y = seno_p(x)
      print*, x, seno_z, y !resultados
      write(11,*) x, seno_z, y
  end do
print*, ''
close (11)
end program pade
!=========
function seno_p(x)
```

Gráfica

end function seno_p

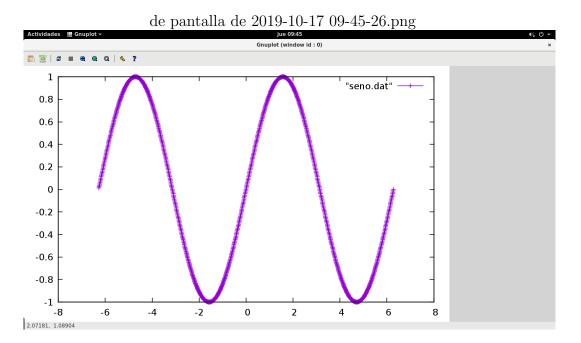


Figura 1:

Error relativo

```
program pade
implicit none
real(kind=8), external :: seno_p
real(kind=8) :: seno_z, x, y, error_p, dx
real, parameter :: Pi = 3.1415926
integer :: i, n
open (11, file = 'errorseno.dat')
 n = 1000
 x = -2.0 * Pi
 dx= 4.0 * Pi/n
   do i = 1, n
      x = x + dx
       y = seno_p(x)
        seno_z=Sin(x)
         error_p = (seno_z - y) / seno_z
          print*, x, error_p
           write(11,*) x, error_p
   end do
   close (11)
end program pade
!=========
function seno_p(x)
!==========
implicit none
real (kind=8), intent(in):: x
```

```
real (kind=8) :: seno_p, seno_w, seno_v
seno_w = x - (x**3) * (2363.0/18183.0) + (x**5) * (12671.0/4363920.0)
seno_v = 1 + (x**2) * (445.0/12122.0) + (x**4) * (601.0/872784.0) + (x**6)*(121.0/seno_p = seno_w/seno_v
end function seno_p
```

Gráfica del error relativo

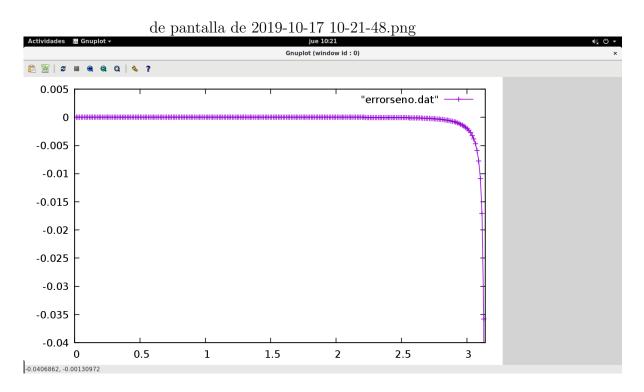


Figura 2:

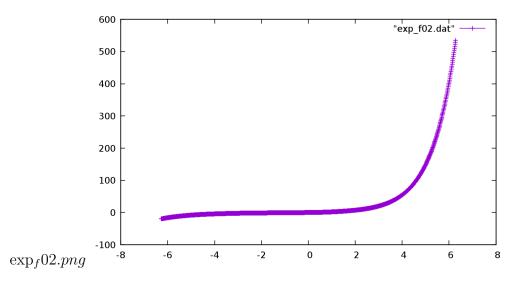
0.2. Problema

Funcion exponencial "F02"

```
program pade
implicit none
!declaracion de variables
real(kind=8), external :: exp_f02
real(kind=8) :: x, y, error, exp_a, dx
real, parameter :: Pi= 3.1415926
integer :: i, n
!salida de datos
open (11, file = 'exp_f02.dat')
 n = 1000
 x = -2.0 * Pi
 dx = 4.0 * Pi/n
 do i = 1, n
      x = x + dx
      y = exp_f02(x)
        exp_a = exp(x)
         error = exp_a - (y/exp_a)
         print*, x, error !resultados
           write(11,*) x, error
  end do
print*, ''
close (11)
end program pade
! =========
```

end function exp_f02

Gráfica de función exponencial F02



Funcion exponencial "F11"

```
program pade
implicit none
!declaracion de variables
real(kind=8), external :: exp_f11
real(kind=8) :: x, y, error, exp_a, dx
real, parameter :: Pi= 3.1415926
integer :: i, n
!salida de datos
open (11, file = 'exp_f11.dat')
 n = 1000
 x = -2.0 * Pi
 dx = 4.0 * Pi/n
 do i = 1, n
     x = x + dx
      y = exp_f11(x)
        exp_a = exp(x)
         error = exp_a - (y/exp_a)
         print*, x, error !resultados
           write(11,*) x, error
  end do
print*, ''
close (11)
end program pade
!=========
function exp_f11(x)
```

```
!=========
```

implicit none

$$w = 1.00 + x * (1.00/2.00)$$

$$v = 1.00 - x * (1.00/2.00)$$

$$exp_f11 = w/v$$

end function exp_f11

Gráfica de función exponencial F11

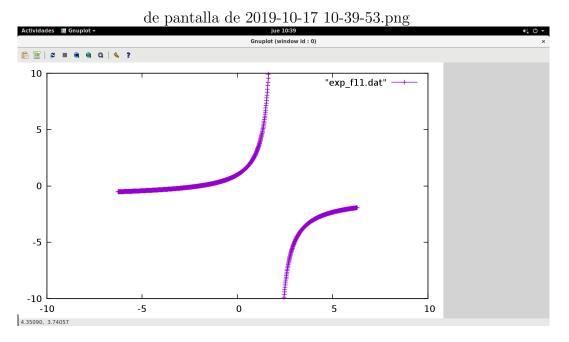


Figura 4:

Funcion exponencial "F20"

```
program pade
implicit none

!declaracion de variables
real(kind=8), external :: exp_f20
real(kind=8) :: x, y, error, exp_a, dx
real, parameter :: Pi = 3.1415926
integer :: i, n

!salida de datos
open (11, file = 'exp_f20.dat')
```

```
n = 1000
  x = -2.0 * Pi
  dx= 4.0 * Pi/n
  do i = 1, n
      x = x + dx
       y = \exp_f 20(x)
        exp_a = exp(x)
          error = exp_a - (y/exp_a)
          print*, x, error, y!resultados
           write(11,*) x, error, y
  end do
print*, ''
close (11)
end program pade
!=========
function exp_f20(x)
!==========
implicit none
real (kind=8), intent(in):: x
real (kind=8) :: exp_f20, w, v
v = 1.00
W = 1.00 + x + (x**2.00) * (1.00/2.00)
exp_f20 = w/v
end function exp_f20
```

Función exponencial F20

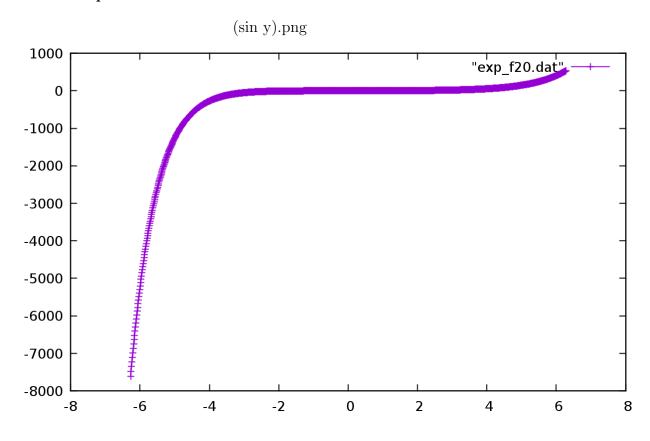


Figura 5: