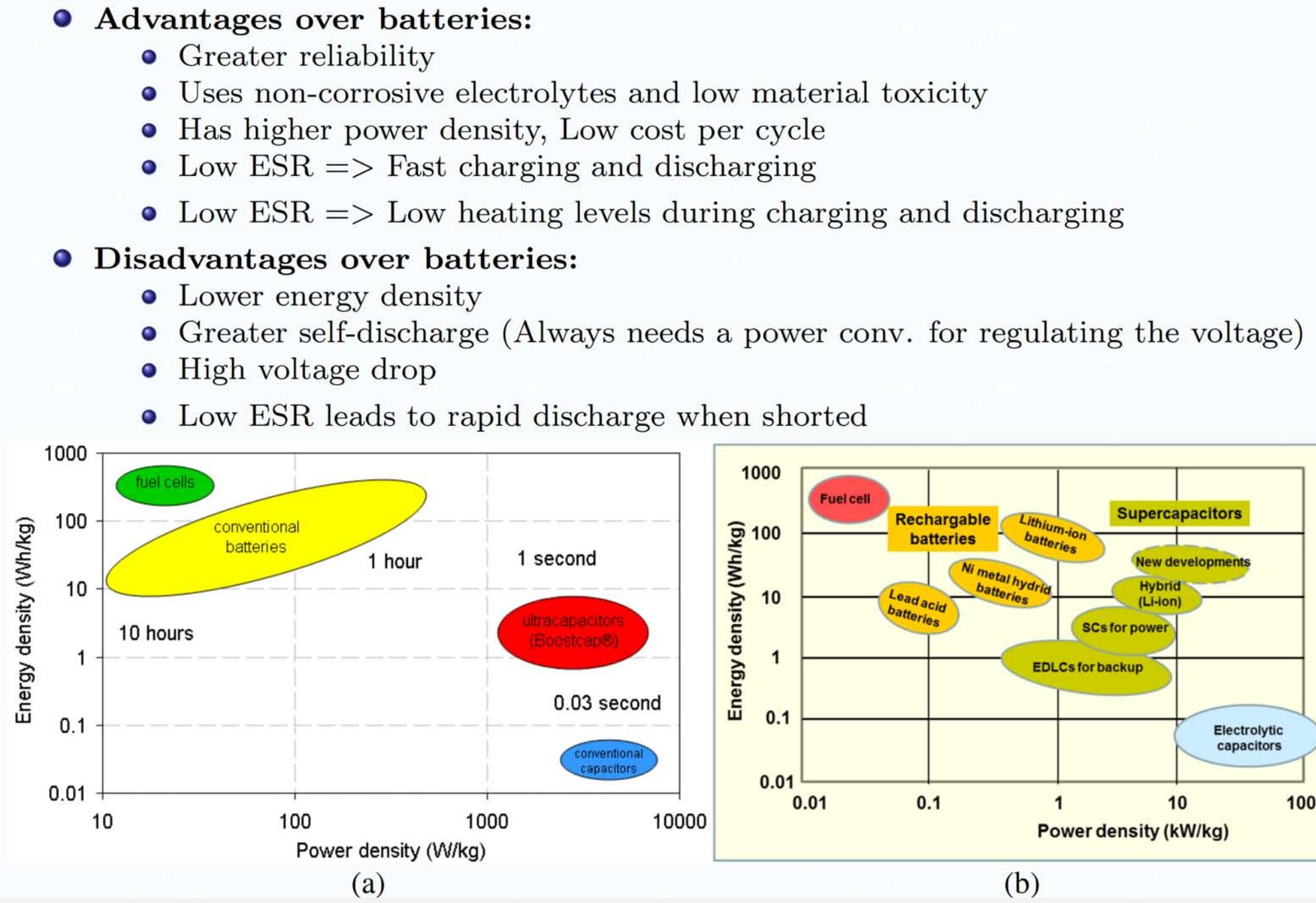
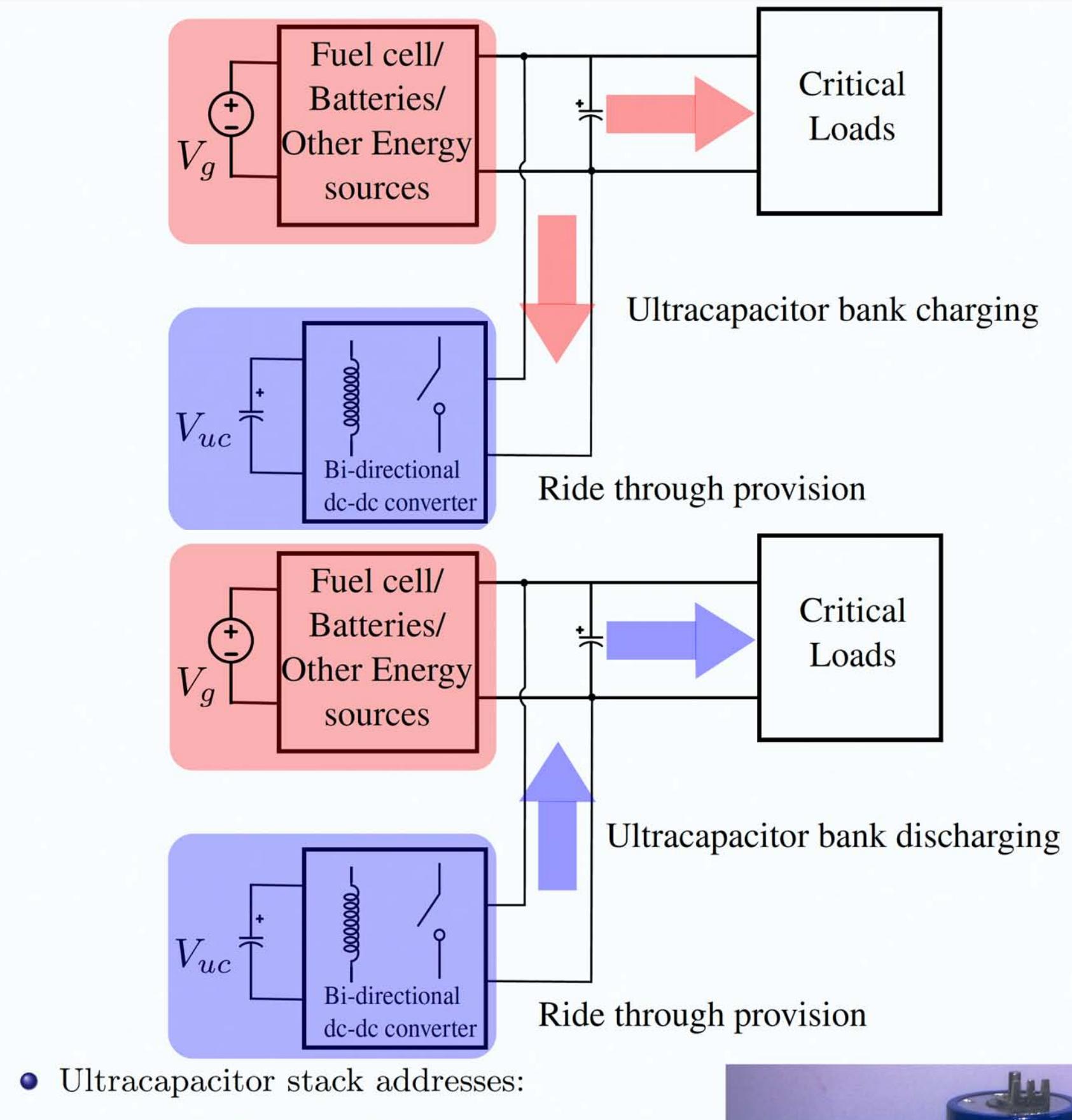


## Comparison of energy storage elements



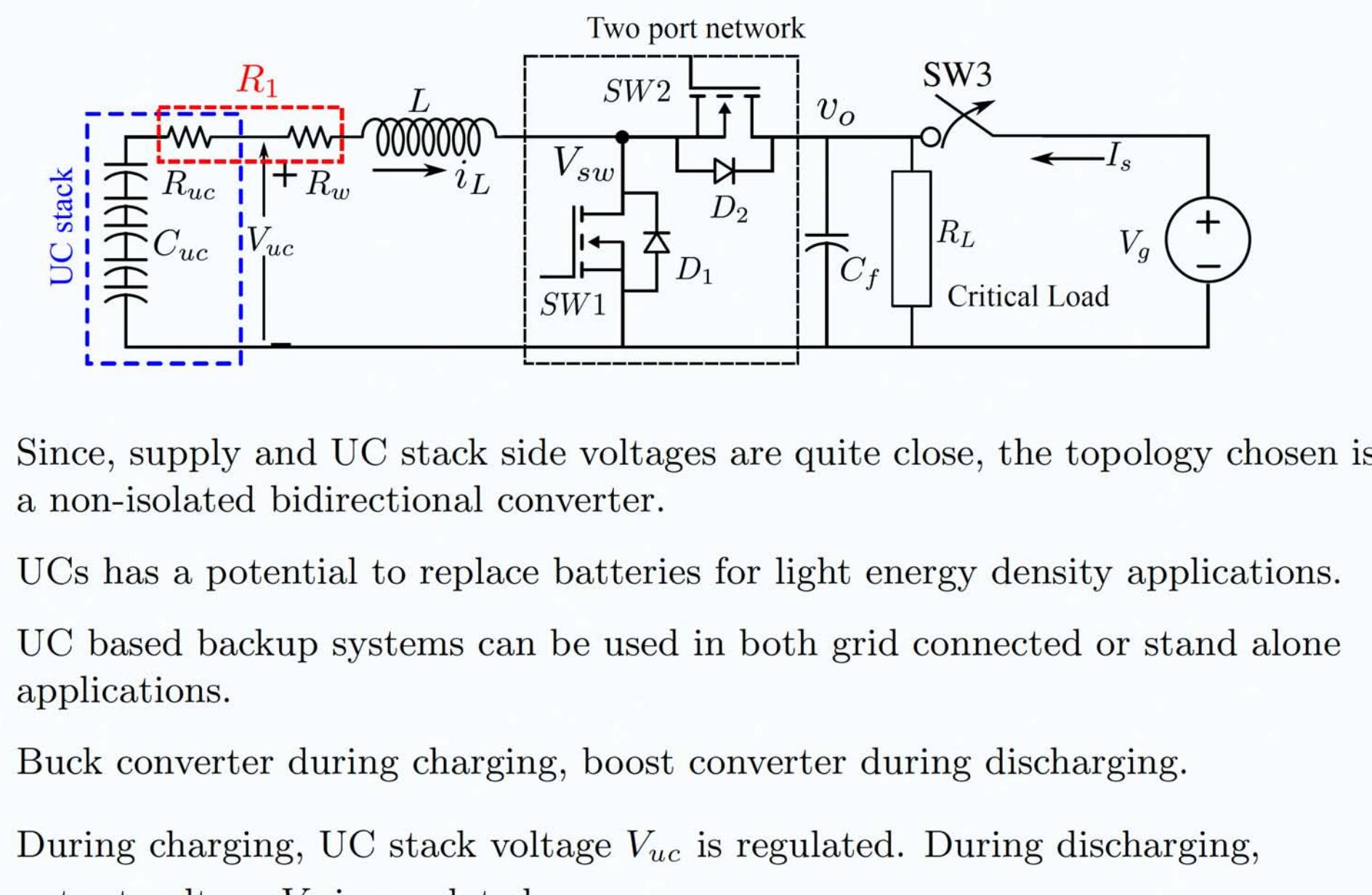
## Ultracapacitor based backup systems



- Ultracapacitor stack addresses:
  - Short duration black-outs
  - Peak power demands
  - Load leveling the battery packs in EV/HEV.
- Ultracapacitors used widely in power quality improvement, traction, EV/HEV etc;



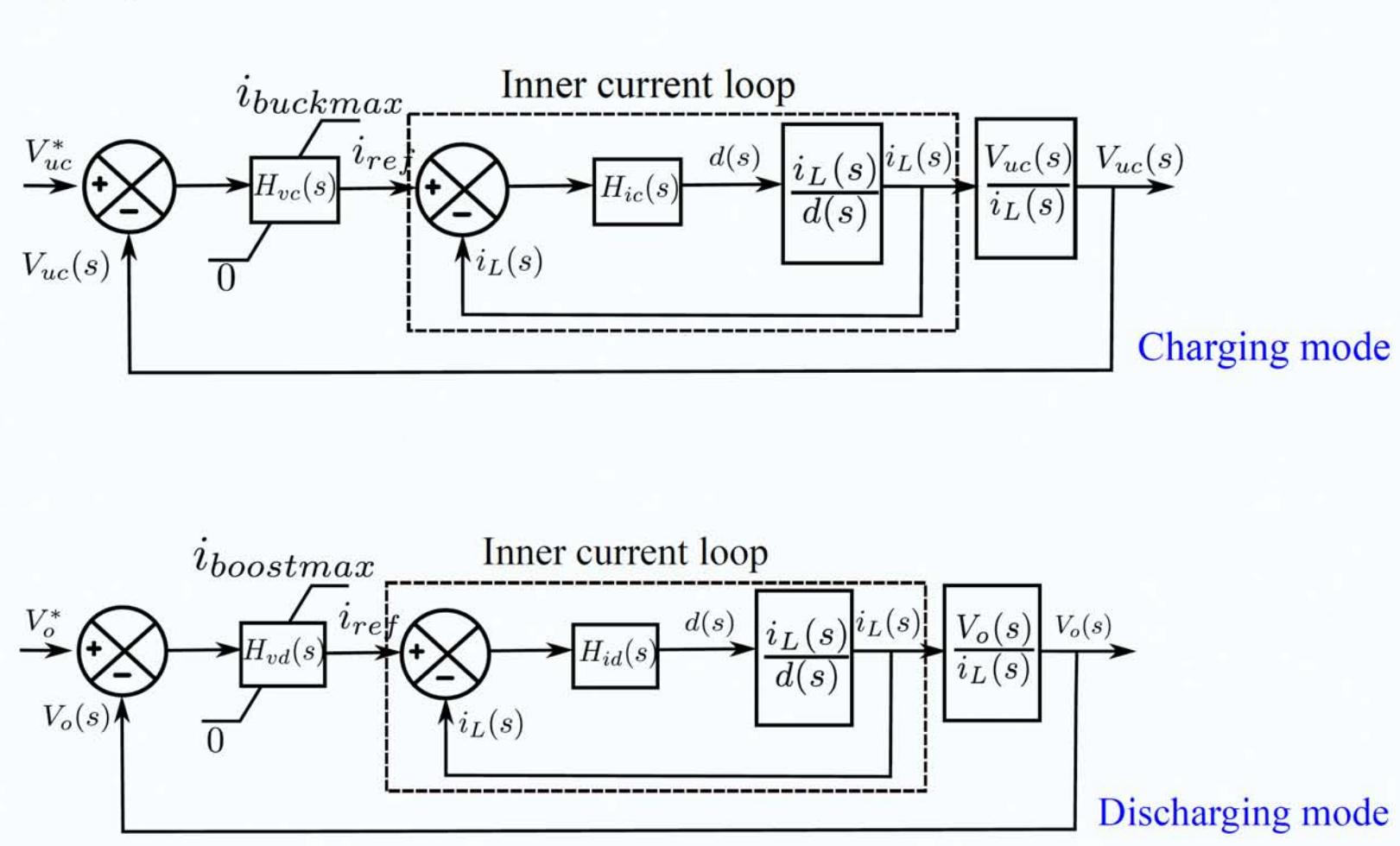
## Power Supply for momentary power mains failures



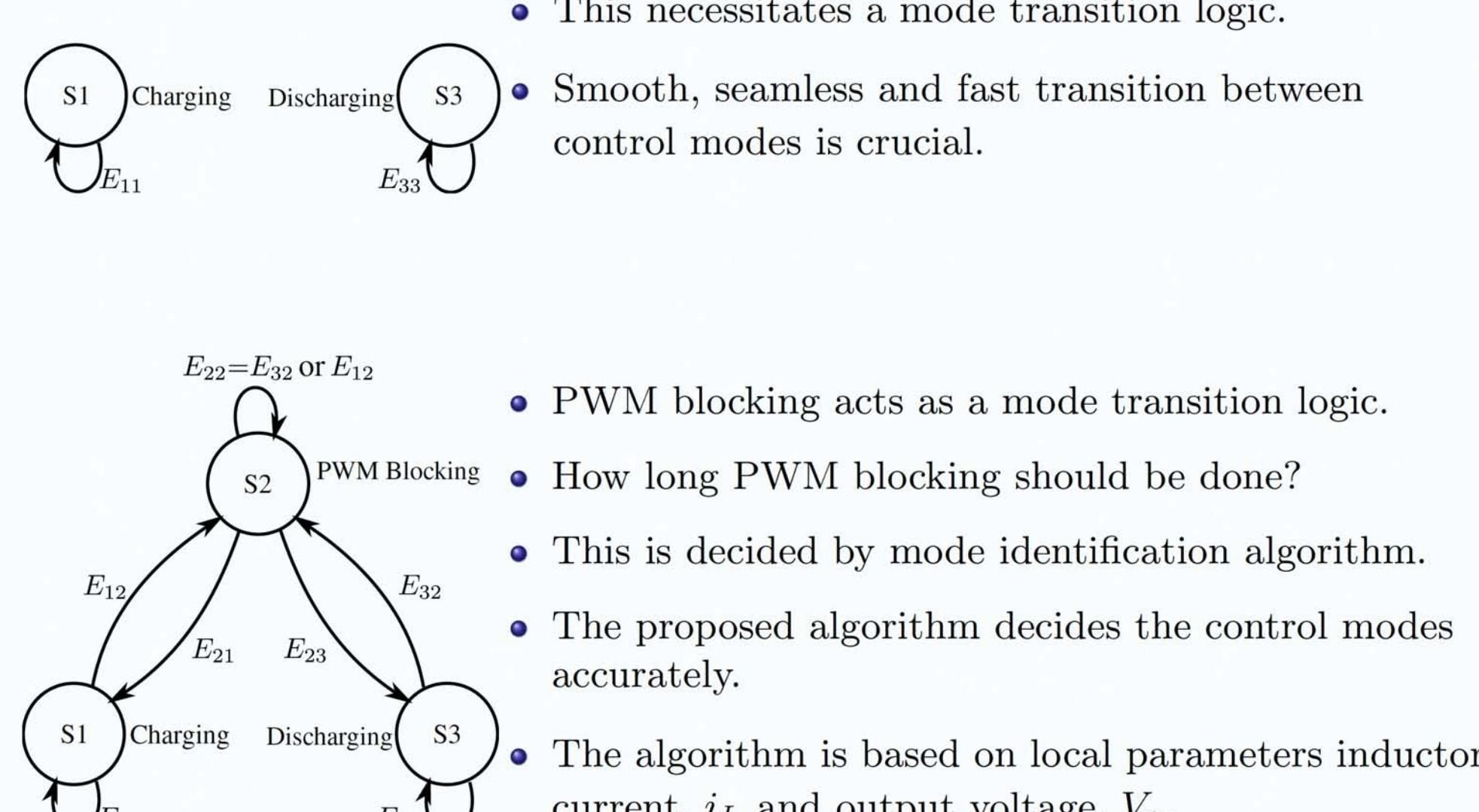
- Since, supply and UC stack side voltages are quite close, the topology chosen is a non-isolated bidirectional converter.
- UCs has a potential to replace batteries for light energy density applications.
- UC based backup systems can be used in both grid connected or stand alone applications.
- Buck converter during charging, boost converter during discharging.
- During charging, UC stack voltage  $V_{uc}$  is regulated. During discharging, output voltage  $V_o$  is regulated.

## PWM blocking for seamless mode transition

- UC based converters have two operating modes - a) charging mode, b) discharging mode.



- Both operating modes have different control structures.
- However, the two states share the same physical elements of converter.
- This necessitates a mode transition logic.
- Smooth, seamless and fast transition between control modes is crucial.



## Mode identification algorithm

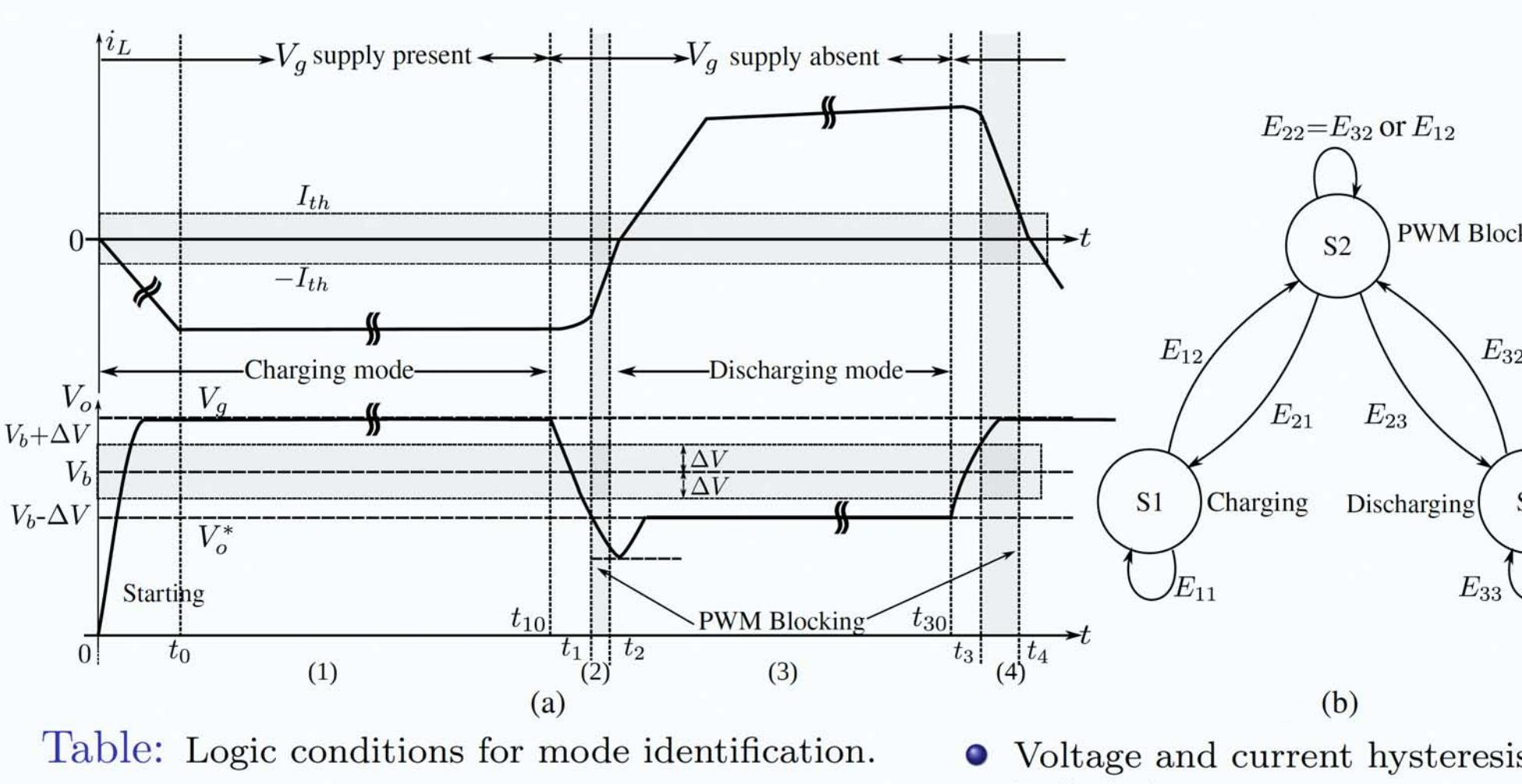
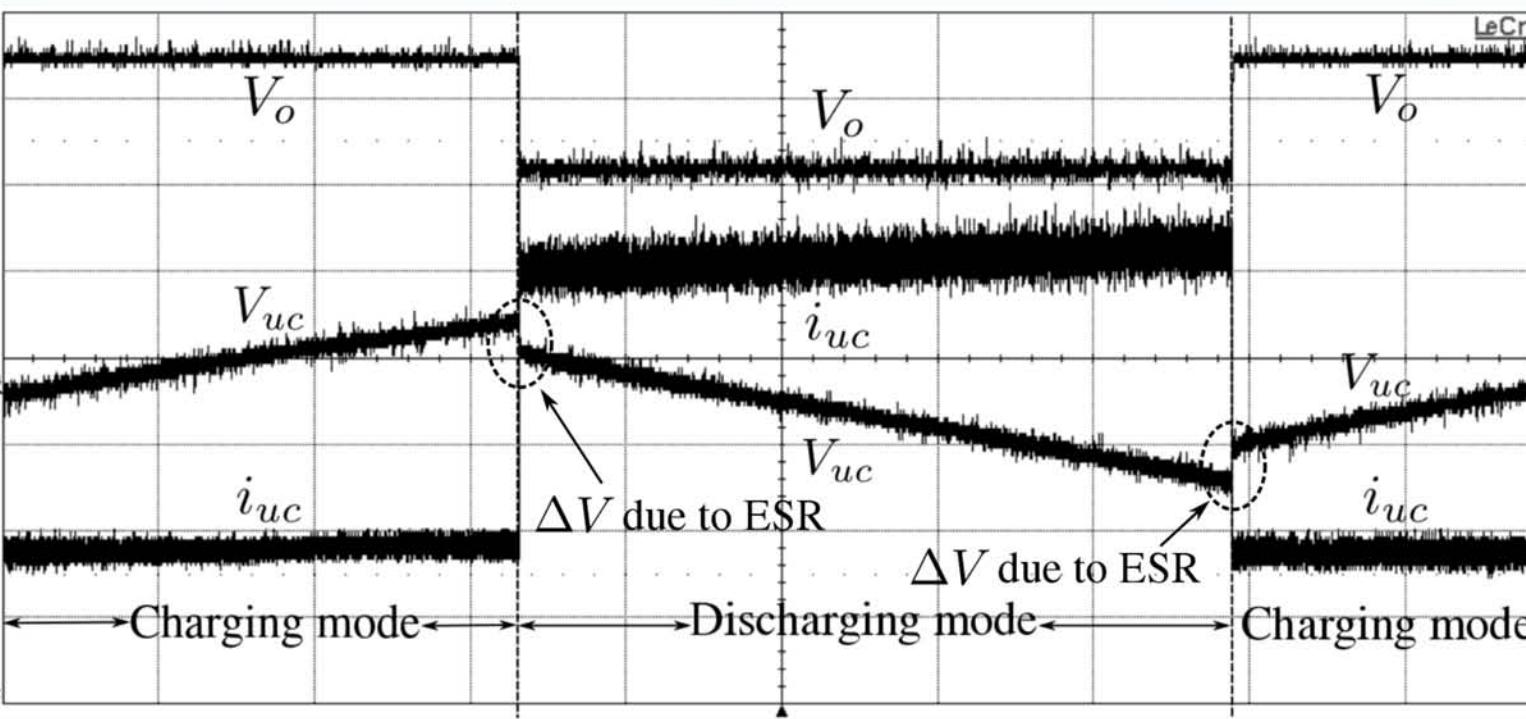


Table: Logic conditions for mode identification.

Time durations	$i_L$	$V_o$	State
$0 < t < t_1$	$i_L > I_{TH}$	$V_o > V_b + \Delta V$	Charging mode (S1)
$t_1 < t < t_2$	$i_L < I_{TH}$	$V_o > V_b - \Delta V$	Charging-Discharging tr. (S2)
$t_2 < t < t_3$	$i_L > -I_{TH}$	$V_o < V_b - \Delta V$	Discharging mode (S3)
$t_3 < t < t_4$	$i_L > I_{TH}$	$V_o > V_b + \Delta V$	Discharging-Charging tr. (S2)

- Voltage and current hysteresis included.
- This reduces error mode identification.
- Fastest mode transition using PWM blocking.

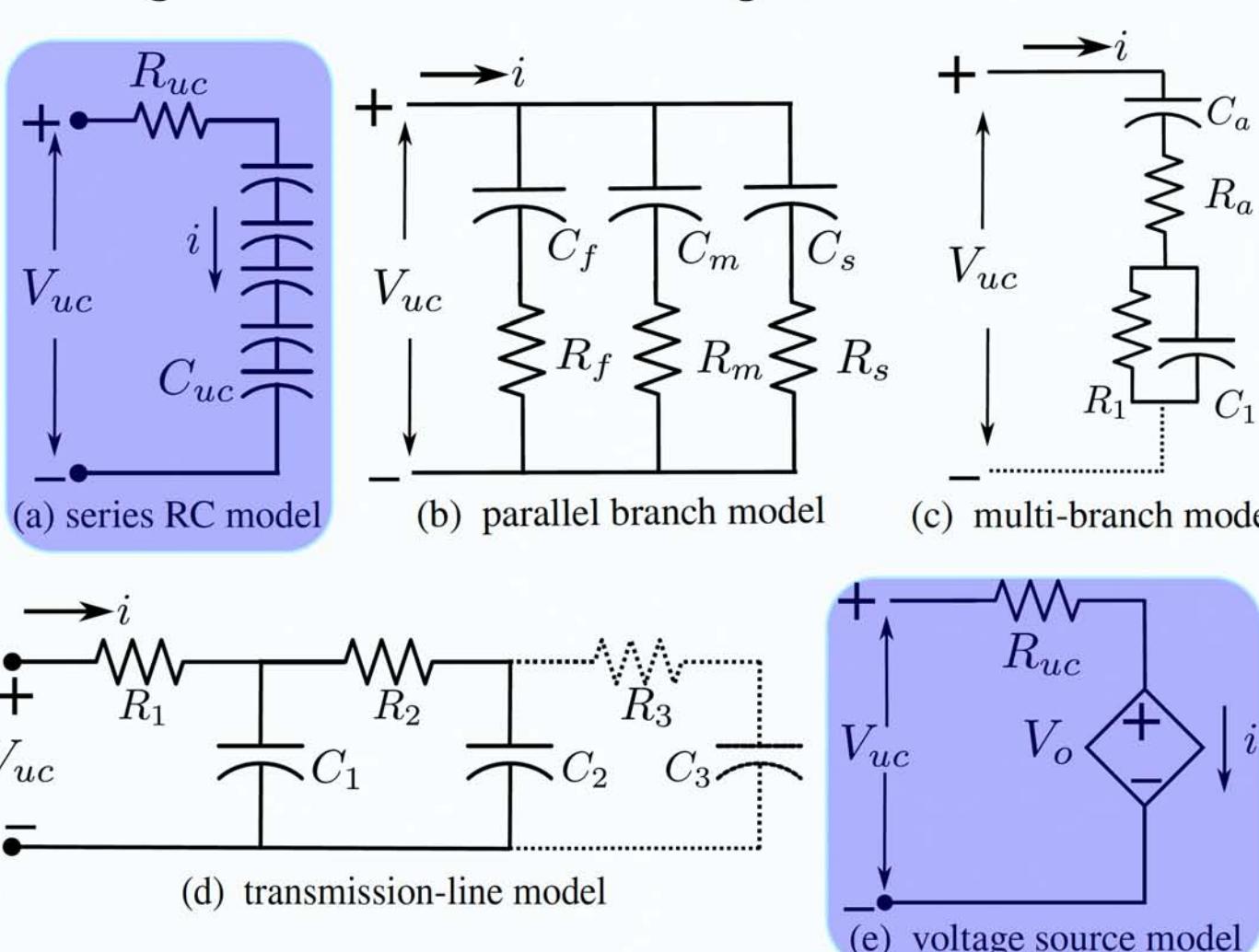
## Experimental results for PWM blocking



- Smooth and seamless transition between control modes is achieved.
- Accurate mode identification is performed using mode identification algorithm.
- The proposed control allows decoupled controls for both operating modes.
- During PWM blocking, no control on dynamics of inductor current  $i_L$ .
  - An alternate virtual resistance based control allows complete control over time duration, inductor current  $i_L$  dynamics during mode transition.
  - Prevents undue stress on switches and inductor unlike PWM blocking control in case of error mode identification.

## Simplified modelling of ultracapacitors

- UCs are usually modelled as series/parallel RC networks.
- Modelling of UC as a large capacitance in series with ESR is quite popular.
- Here, modelling of UC as a variable voltage source is studied.



## Motivation for modelling of ultracapacitors

Ultracapacitors as variable voltage sources

Table: Experimental set-up for UC based bidirectional dc-dc converter.

Hardware details	
Filter inductor, $L$	300 $\mu H$
Filter capacitor, $C_f$	2000 $\mu F$
UC stack <sup>†</sup> capacitance $C_{uc}$ , ESR $R_{uc}$	12.5 $F$ , 0.2 $\Omega$
Maximum Power, Supply Voltage $V_g$ , $f_{sw}$	200W, 26V, 100kHz

<sup>†</sup> UC stack has 12 Maxwell BCAP0150 ultracapacitors in series.

$$\frac{i_L(s)}{d(s)} = \frac{sV_g C_{uc}}{LC_{uc}s^2 + R_1 C_{uc}s + 1} = \frac{\frac{V_g}{L}s}{s^2 + \frac{R_1}{L}s + \frac{1}{LC}} = \frac{\frac{V_g}{L}s}{(s + \lambda_1)(s + \lambda_2)}$$

$$\lambda_1 = -\frac{R_1}{2L} - \frac{1}{2L}\sqrt{\frac{C_{uc}R_1^2 - 4L}{C_{uc}}} \approx -666.268, \lambda_2 = -\frac{R_1}{2L} + \frac{1}{2L}\sqrt{\frac{C_{uc}R_1^2 - 4L}{C_{uc}}} \approx -0.4$$

Here, the approximation  $C_{uc}R_1^2 \gg L$  would be valid, allowing  $\lambda_2 = 0$ , and  $\lambda_1 = -\frac{R_1}{L}$ .

Also, the two eigen values are well separated. The quadratic systems with well separated eigen values are discussed in <sup>2</sup>.

$$Q = \sqrt{\frac{L}{C_{uc}R_1^2}}, F = 0.5 + 0.5\sqrt{1 - 4Q^2}, \lambda_1 = -\frac{FR_1}{L}, \lambda_2 = \frac{-1}{R_1 C_{uc}F}$$
 (1)

if  $Q \approx 0 \Rightarrow F \approx 1$ , then decoupling of eigen values,  $\lambda_2 = \frac{-1}{R_1 C_{uc}}$ , and  $\lambda_1 = -\frac{R_1}{L}$ .

$$\lambda_1 = -\frac{R_1}{L}, \lambda_2 = \frac{-1}{R_1 C_{uc}}$$

## Scope of this work

- Qualitative and quantitative comparison of the proposed variable voltage source model with series RC model.
- For this comparison, comparison metrics
  - $F$  and  $Q$  parameters
  - the z-domain current loop plant transfer function,  $\frac{i_L(z)}{d(z)}$  are used.
- Validation of comparison metrics over wide range of design voltage, power levels and sampling frequencies.
- Limiting operating voltage and power levels for different UC stack and converter designs for the proposed voltage source model.
- The corresponding controller design and experimental verification.
- The comparison metrics are dependent on circuit parameters.
- $P_o \in (100W, 100kW)$ ,  $V_g \in (30V, 1000V)$

## Comparison using z-domain bode plots

### Why analysis in z-domain??

- The transfer functions of a buck converter feeding a UC stack,  $\frac{i_L(z)}{d(z)}$  for both the models are derived in z-domain.
- Usually, the control is implemented in digital platform.
- The non-idealities and other delays such as sampling and PWM delays can also be readily incorporated in the z-domain models.
- z-domain transfer functions obtained from continuous time state space models.

### Why use exact discretization?

- The comparison of  $\frac{i_L(z)}{d(z)}$  for both the models is performed for wide range of design and operating conditions.
- Discretization methods such as Forward and Backward Euler, Tustin's method is not accurate for wide range of sampling frequencies,  $f_s$ <sup>2</sup>.

<sup>2</sup>F.L. Lewis, Applied Optimal Control Estimation: Digital Design & Implementation, ser. Prentice Hall and Texas Instruments digital signal processing series. Prentice-Hall, 1992.

## Small signal analysis for plant model

- Model 2:**  $\frac{\hat{i}_L(z)}{\hat{d}(z)} = \frac{V_g T_s}{L} \frac{2e^{\lambda_2 T_s(1-d)} - e^{\lambda_1 T_s(1-d)}}{(z - e^{\lambda_2 T_s})(z - e^{\lambda_1 T_s})} \times \frac{(2e^{\lambda_1 T_s + \lambda_2 T_s(1-d)} - e^{\lambda_1 T_s(1-d)} + \lambda_2 T_s)}{2e^{\lambda_2 T_s(1-d)} - e^{\lambda_1 T_s(1-d)}}$
- Approximating  $\lambda_2 = 0$
- Model 3:**  $\frac{\hat{i}_L(z)}{\hat{d}(z)} = \frac{V_g T_s}{L} \frac{2 - e^{\lambda_1 T_s(1-d)}}{(z - 1)(z - e^{\lambda_1 T_s})} (z - [\frac{2e^{\lambda_1 T_s} - e^{\lambda_1 T_s(1-d)}}{2 - e^{\lambda_1 T_s(1-d)}}])$
- Model 1:**  $\frac{\hat{i}_L(z)}{\hat{d}(z)} = \frac{V_g T_s}{L} \left[ \frac{1}{z - e^{\lambda_1 T_s}} \right] e^{\lambda_1 T_s(1-d)}$
- if  $\lambda_1 T_s \approx 0$
- $\frac{\hat{i}_L(z)}{\hat{d}(z)} = \frac{V_g T_s}{L} \left[ \frac{1}{z - 1} \right]$  This deviation not found in s-domain TFs, is analyzed in z-domain.
- The effect of variation of duty ratio,  $d$  on the three models is found to be minimal.

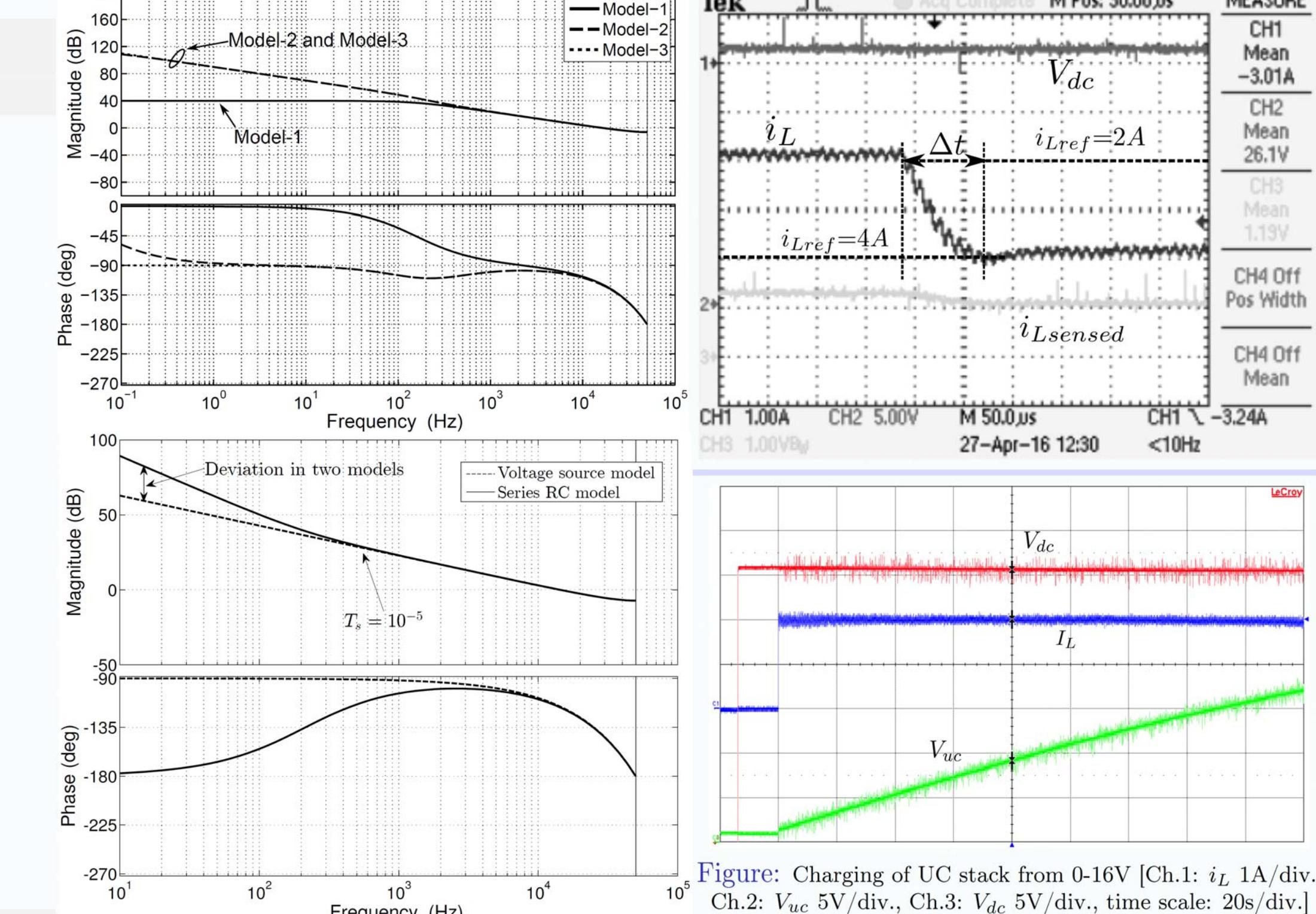


Figure: Charging of UC stack from 0-16V [Ch1:  $i_L$  1A/div., Ch2:  $V_{uc}$  5V/div., Ch3:  $V_{dc}$  5V/div., time scale: 20s/div.]

## Adaptive control for discharging mode of operation

- The control structure should accommodate for variation in:
  - plant characteristics
  - RHP zero especially due to UC stack deep discharging.

### Advantages of adaptive control

- The controller gains are estimated on-line.
- The proposed control ensures best performance criteria possible.
- Adaptive control incorporates the variation of RHP zero and varies the bandwidth accordingly<sup>4</sup>.

## Conclusions and Contributions

- Mode identification algorithm based on PWM blocking has been proposed which ensures:
  - Fastest mode transition.
  - Smooth, seamless mode transition.
  - Accurate identification of control modes.
- Alternately, virtual resistance control is proposed which allows control on current dynamics during mode transition as well.
- Simplified voltage source model for UCs similar to batteries have been proposed and verified which simplifies the controller design.
- The possibility of using this simplified model have been studied for wide range of design applications.
- For this, a generalized passives design is carried out where the variation of passives for various design applications is carried out.
- An adaptive control has been proposed which allows online variation of controller gains to accommodate system characteristics and RHZ variation.

## Key Publications

- K. Saichand and V. John, "PWM block method for control of an ultracapacitor-based bidirectional DC/DC backup system," *IEEE Transactions on Industry Applications*, vol. 52, no. 5, pp. 4126-4134, Sept 2016.
- K. Saichand, A. Kumrawat, and V. John, "High performance AC-DC control power supply for low voltage ride through inverters," *Sadhana*, vol. 41, no. 2, pp. 147-159, 2016.
- K. Saichand and V. John, "Simplified modeling of ultracapacitors for bidirectional DC-DC converter applications," accepted for publication in *Applied Power Electronics Conference*. Tampa, Florida: APEC-2017, March 2017, pp. 1-6.
- K. Saichand and V. John, "Adaptive control strategy for ultracapacitor based bidirectional DC-DC converters," accepted for publication in *Applied Power Electronics Conference*. Tampa, Florida: APEC-2017, March 2017, pp. 1-6.
- K. Saichand and V. John, "A generalized design procedure for passives in a ultracapacitor based bidirectional DC-DC system for backup power applications," accepted for publication in *Thirteenth Annual IEEE INDICON*, 2016. IISc Bangalore: IEEE Bangalore Section, December 2016, pp. 1-6.
- K. Saichand and V. John, "PWM block method for control of ultracapacitor based bidirectional DC/DC backup system," in *2014 IEEE International Conference on Power Electronics, Drives and Energy Systems (PEDES)*, IISc Bangalore, December 2014, pp. 1-6.

# Modelling and Control of Ultracapacitor based Bidirectional DC-DC converter systems

K. Saichand

Advisor: Prof. Vinod John

Power electronics group,  
Department of electrical engineering,  
Indian Institute of Science (IISc), Bangalore - 560012.

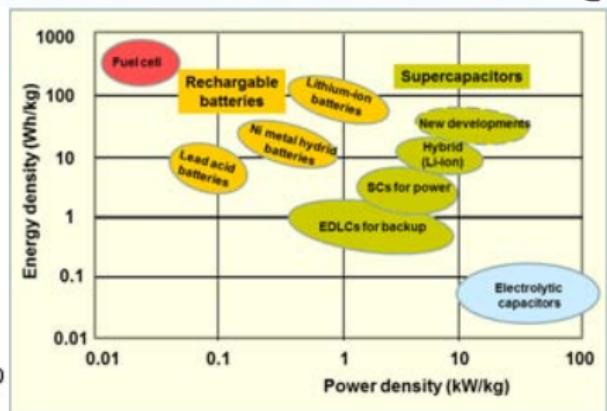
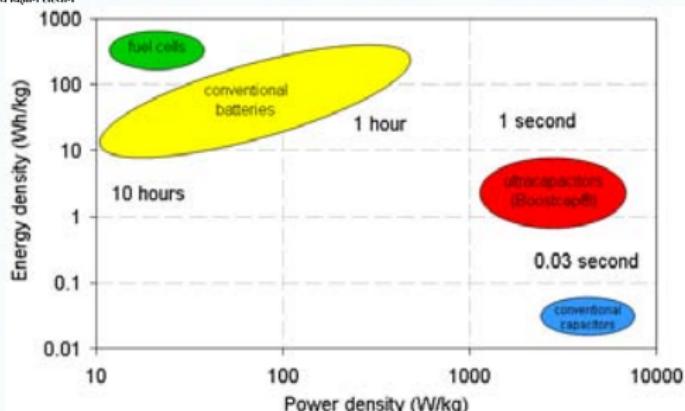
Electrical Divisional Symposium



April 7-8, 2017



# Comparison of energy storage elements

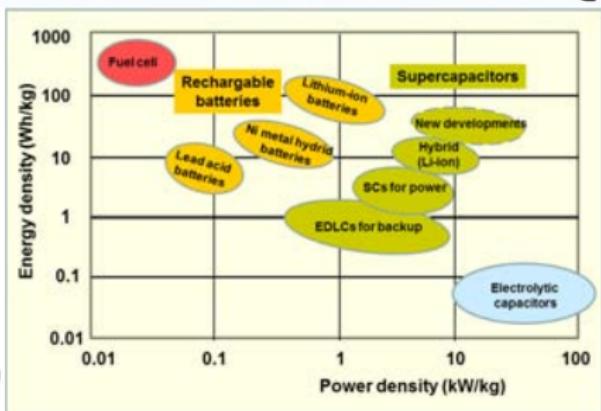
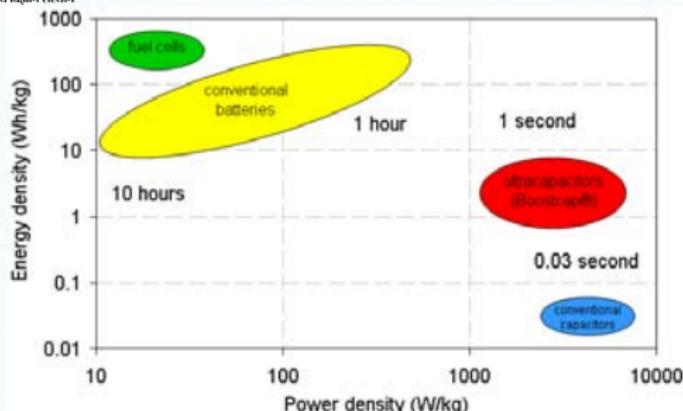


(a)  
Source: [https://upload.wikimedia.org/wikipedia/commons/6/6b/Supercapacitors\\_chart.svg](https://upload.wikimedia.org/wikipedia/commons/6/6b/Supercapacitors_chart.svg)

(b)



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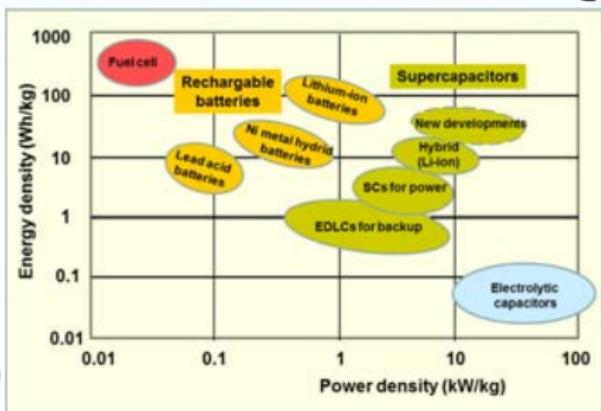
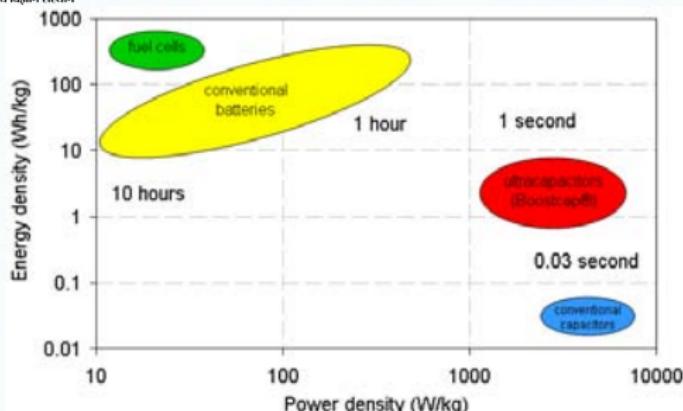
(b)

- **Advantages over batteries:**

- Greater reliability
- Uses non-corrosive electrolytes and low material toxicity
- Has higher power density, Low cost per cycle
- Low ESR => Fast charging and discharging
- Low ESR => Low heating levels during charging and discharging



# Comparison of energy storage elements



Source: [https://upload.wikimedia.org/wikipedia/commons/6/6b/Supercapacitors\\_chart.svg](https://upload.wikimedia.org/wikipedia/commons/6/6b/Supercapacitors_chart.svg)

## • Advantages over batteries:

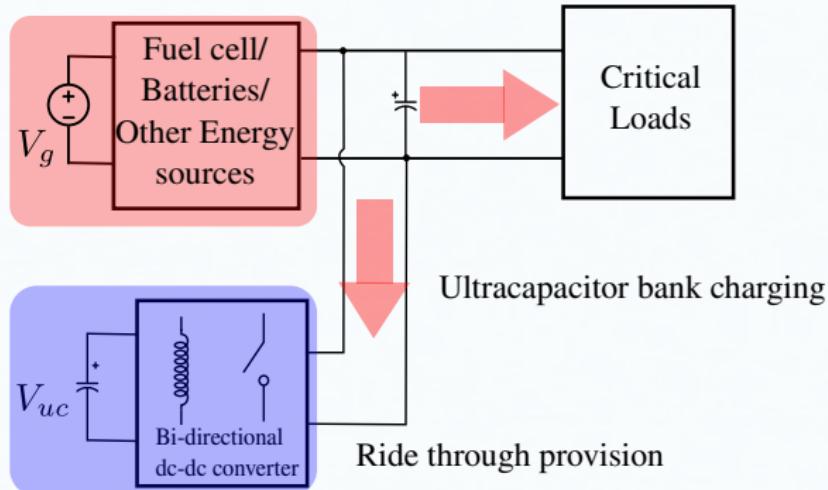
- Greater reliability
- Uses non-corrosive electrolytes and low material toxicity
- Has higher power density, Low cost per cycle
- Low ESR => Fast charging and discharging
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## • Disadvantages over batteries:

- Lower energy density
- Greater self-discharge (Always needs a power conv. for regulating the voltage)
- High voltage drop
- Low ESR leads to rapid discharge when shorted



# Ultracapacitor based backup systems

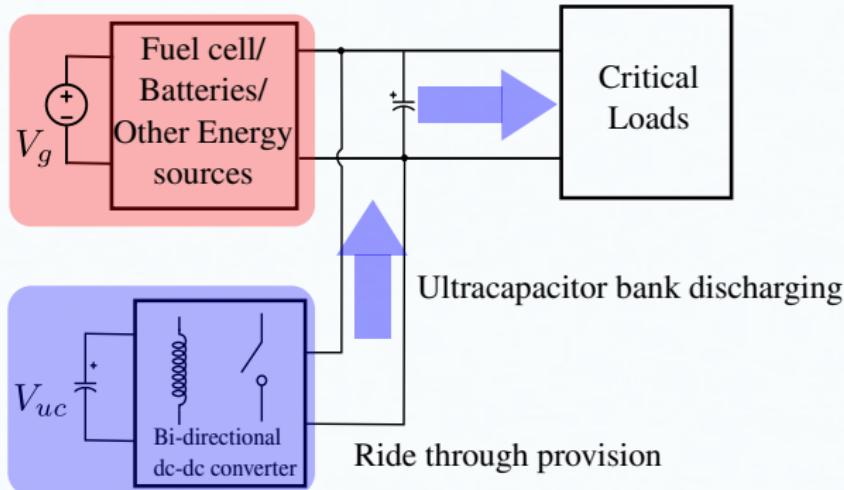


- Ultracapacitor stack addresses:
  - Short duration black-outs
  - Peak power demands
  - Load leveling the battery packs in EV/HEV.
- Ultracapacitors used widely in power quality improvement, traction, EV/HEV etc;





# Ultracapacitor based backup systems

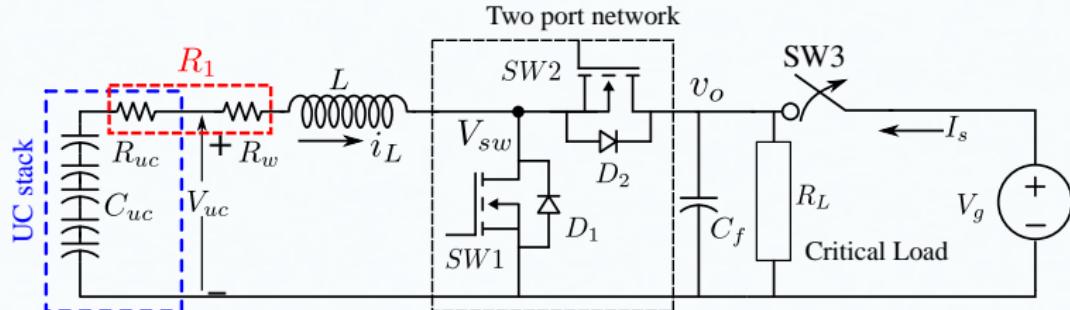


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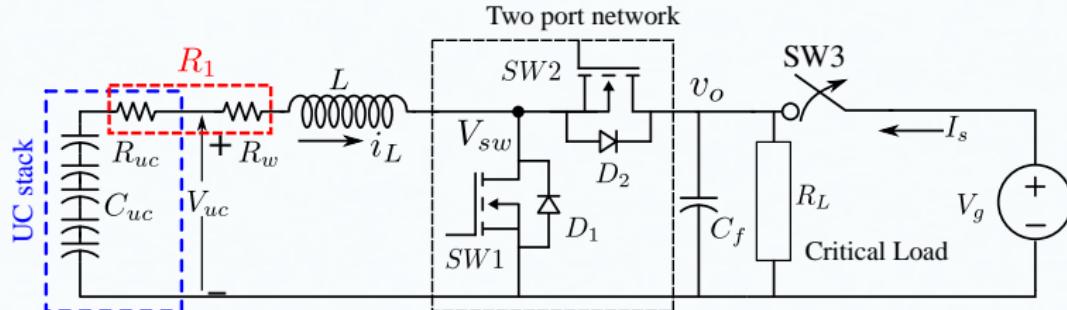
# Power Supply for momentary power mains failures



- UCs has a potential to replace batteries for light energy density applications.
- UC based backup systems can be used in both grid connected or stand alone applications.
- A non-isolated bidirectional converter is chosen since supply and UC stack side voltages are quite close.



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- A non-isolated bidirectional converter is chosen since supply and UC stack side voltages are quite close.
- System operates as buck converter during charging, boost converter during discharging.
- During charging, UC stack voltage  $V_{uc}$  is regulated. During discharging, output voltage  $V_o$  is regulated.



## List of contributions



- 1 PWM Blocking control for seamless mode transition
- 2 Virtual resistance control for seamless mode transition
- 3 Reduced order modelling of ultracapacitors
- 4 Generalized passives design for UC based backup system
- 5 Adaptive control during discharging mode of operation with enhanced performance



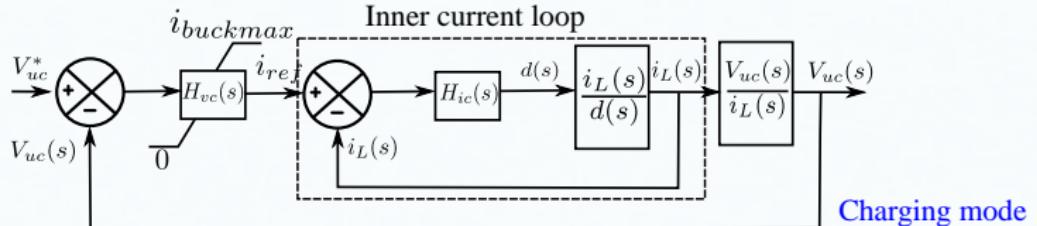
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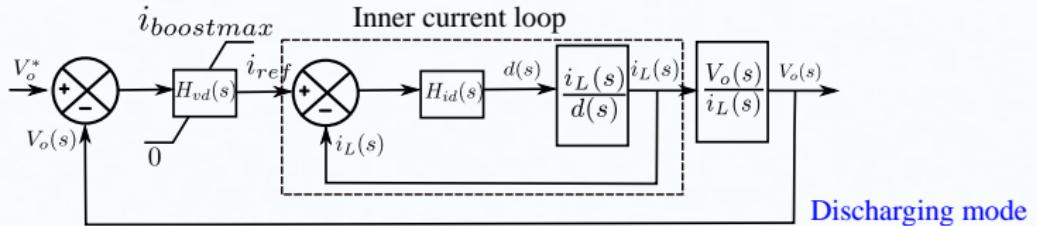
# PWM blocking for seamless mode transition

- UC based converters have two operating modes - a) charging mode, b) discharging mode.



# PWM blocking for seamless mode transition

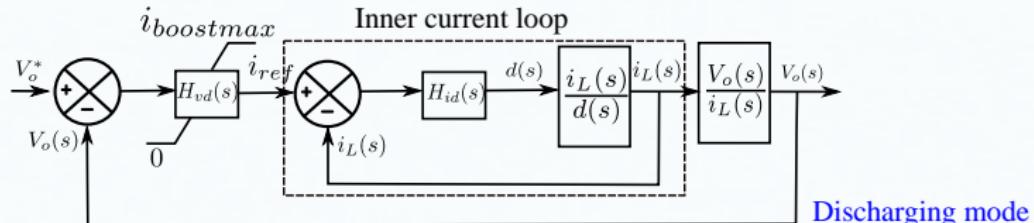
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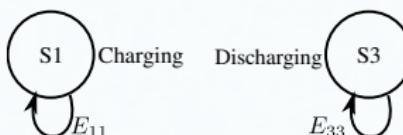
Discharging mode

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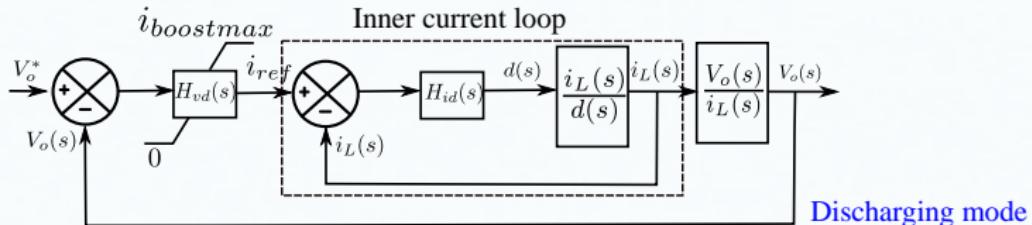


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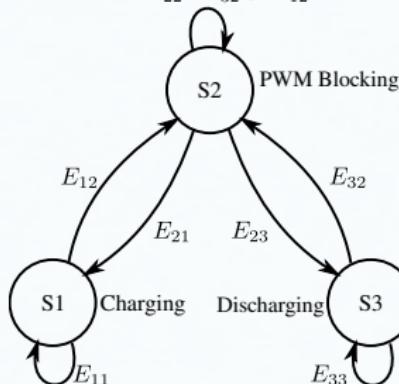


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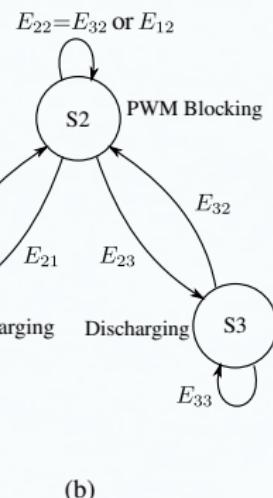
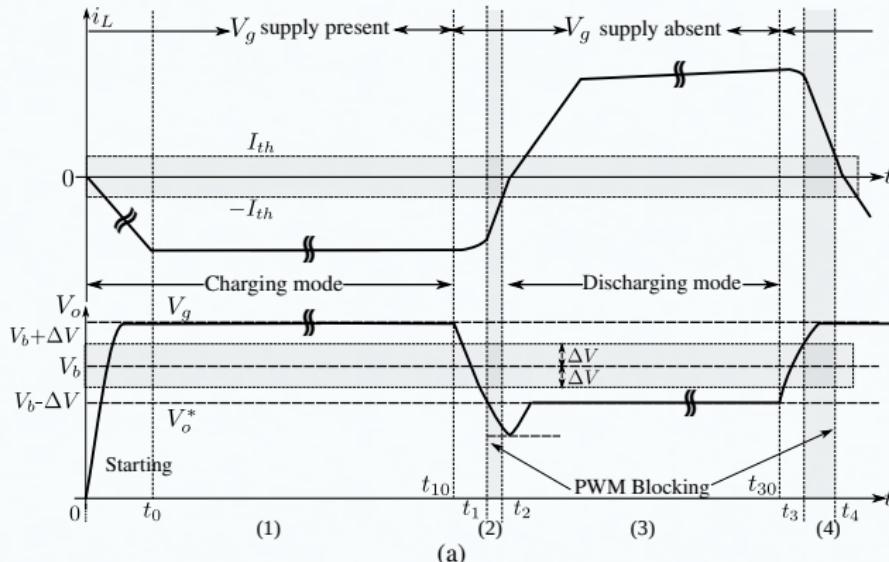
$$E_{22} = E_{32} \text{ or } E_{12}$$



- PWM blocking acts as a mode transition logic.
- How long PWM blocking should be done?
- This is decided by mode identification algorithm.
- The proposed algorithm decides the control modes accurately.
- The algorithm is based on local parameters inductor current,  $i_L$  and output voltage,  $V_o$ .

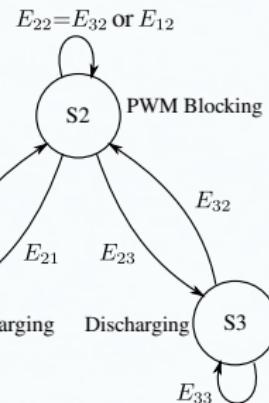
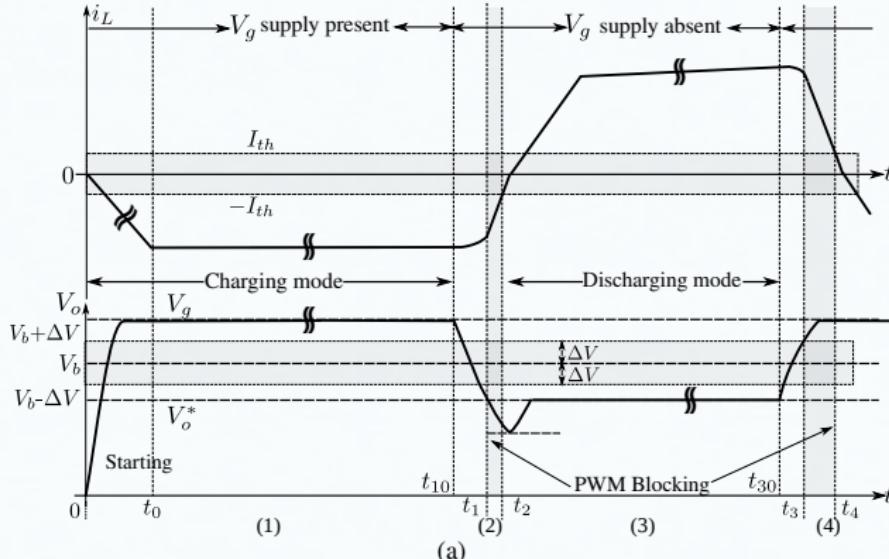


# Mode identification algorithm





# Mode identification algorithm

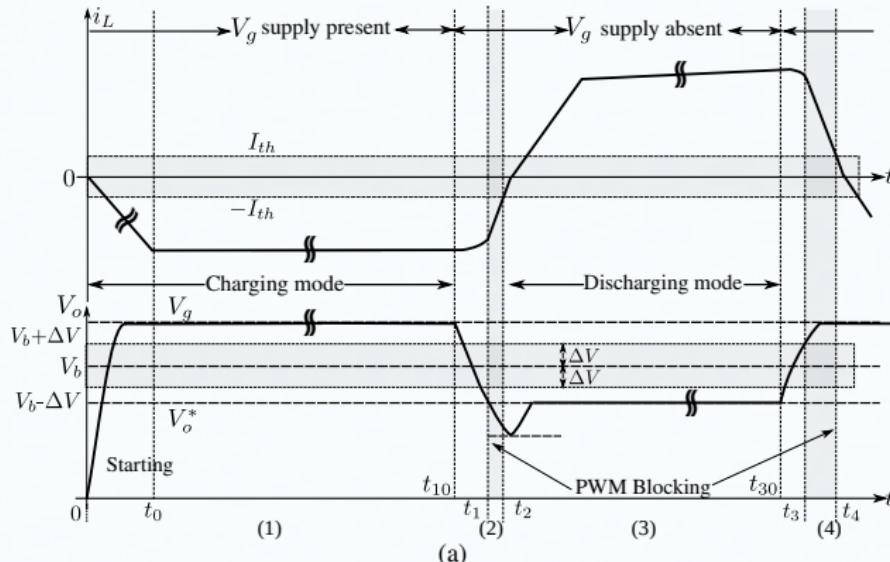


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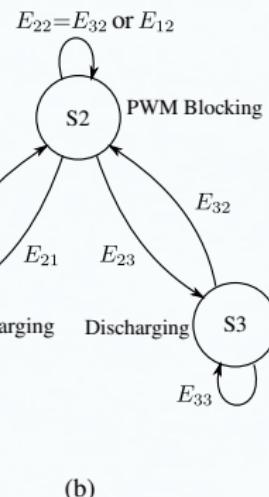


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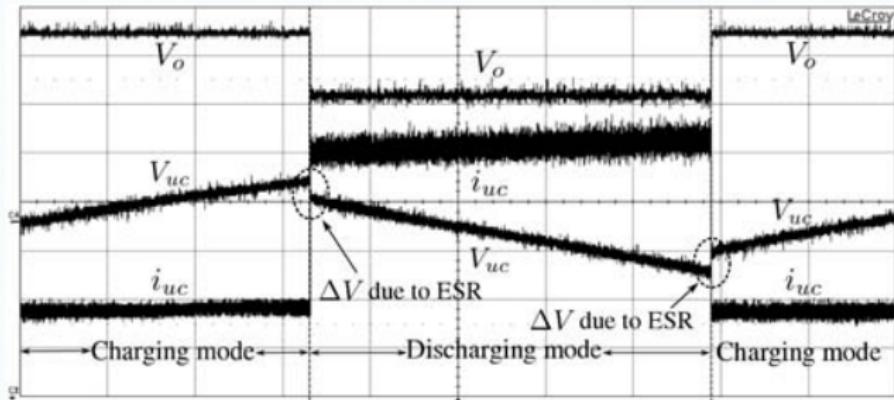
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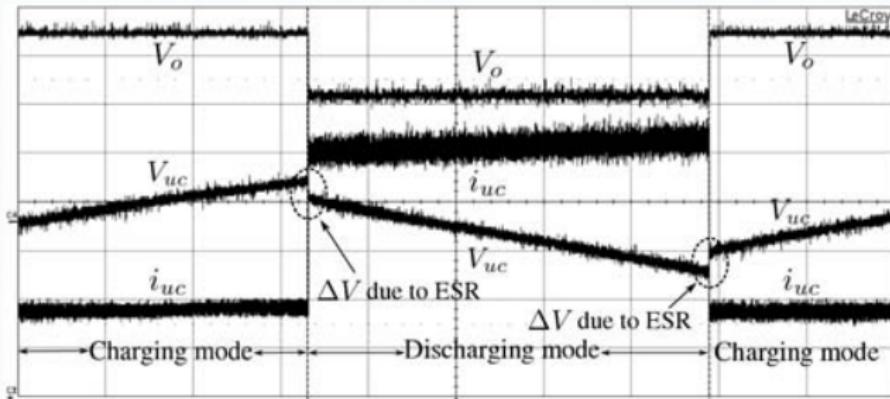
- Voltage and current hysteresis included.
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- Fastest mode transition using PWM blocking.

# Experimental results for PWM blocking



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  - A **virtual resistance based control** allows complete control over time duration, inductor current  $i_L$  dynamics during mode transition<sup>1</sup>.

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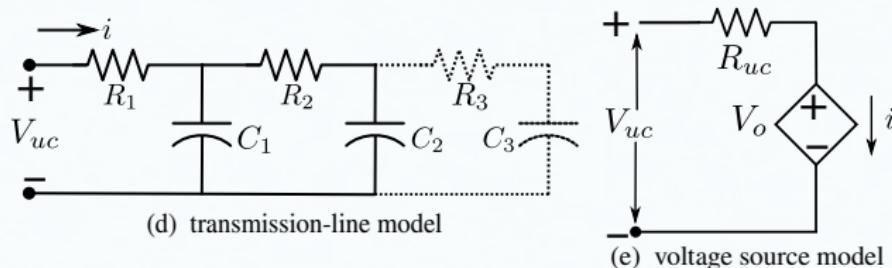
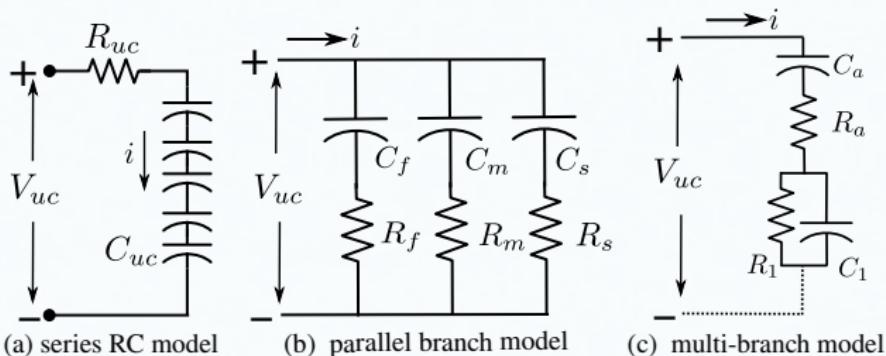


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# Reduced order modelling of ultracapacitors

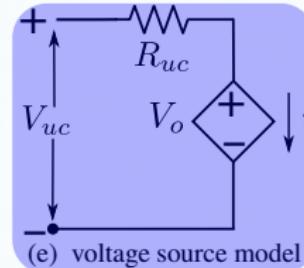
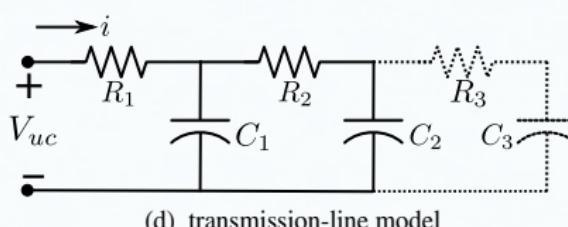
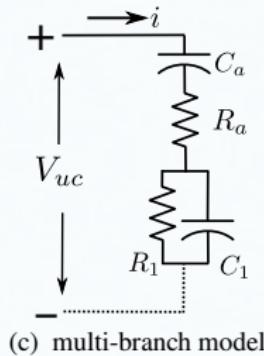
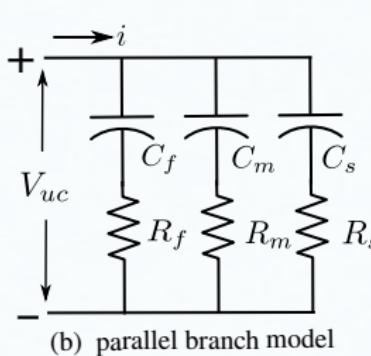
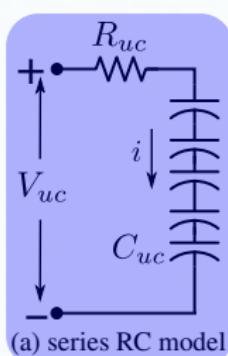


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- Modelling of UC as a large capacitance in series with ESR is quite popular.
- Here, modelling of UC as a variable voltage source is studied.



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# Motivation for modelling of ultracapacitors

## Ultracapacitors as variable voltage sources

Table: Experimental set-up for UC based bidirectional dc-dc converter.

Hardware details	
Filter inductor, $L$	$300\mu H$
Filter capacitor, $C_f$	$2000\mu F$
UC stack <sup>†</sup> capacitance $C_{uc}$ , ESR $R_{uc}$	$12.5F, 0.2\Omega$
Maximum Power, Supply Voltage $V_g$ , $f_{sw}$	$200W, 26V, 100kHz$

<sup>†</sup> UC stack has 12 **Maxwell BCAP0150** ultracapacitors in series.

$$\frac{\hat{i}_L(s)}{\hat{d}(s)} = \frac{sV_gC_{uc}}{LC_{uc}s^2 + R_1C_{uc}s + 1} = \frac{\frac{V_g}{L}s}{s^2 + \frac{R_1}{L}s + \frac{1}{LC}} = \frac{\frac{V_g}{L}s}{(s + \lambda_1)(s + \lambda_2)}$$



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$$\lambda_1 = -\frac{R_1}{2L} - \frac{1}{2L}\sqrt{\frac{C_{uc}R_1^2 - 4L}{C_{uc}}} \approx -666.268, \quad \lambda_2 = -\frac{R_1}{2L} + \frac{1}{2L}\sqrt{\frac{C_{uc}R_1^2 - 4L}{C_{uc}}} \approx -0.4$$



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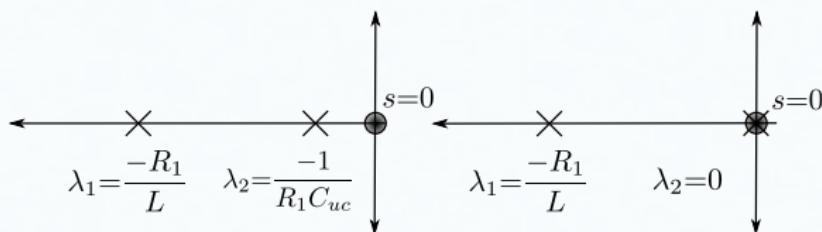
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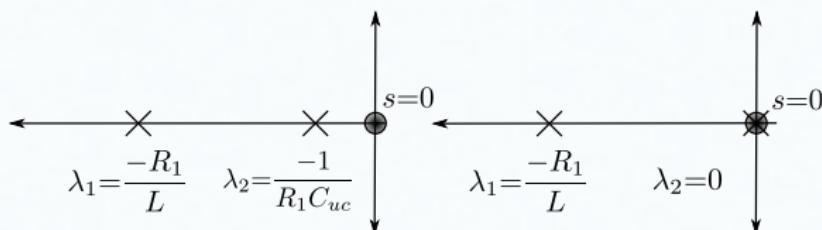
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# Comparison using $z$ -domain bode plots

## Why analysis in $z$ -domain??

- The transfer functions of a buck converter feeding a UC stack,  $\frac{\hat{i}_L(z)}{d(z)}$  for both the models are derived in  $z$ -domain.
- Usually, the control is implemented in digital platform.
- The non-idealities and other delays such as sampling and PWM delays can also be readily incorporated in the  $z$ -domain models.
- $z$ -domain transfer functions obtained from continuous time state space models.

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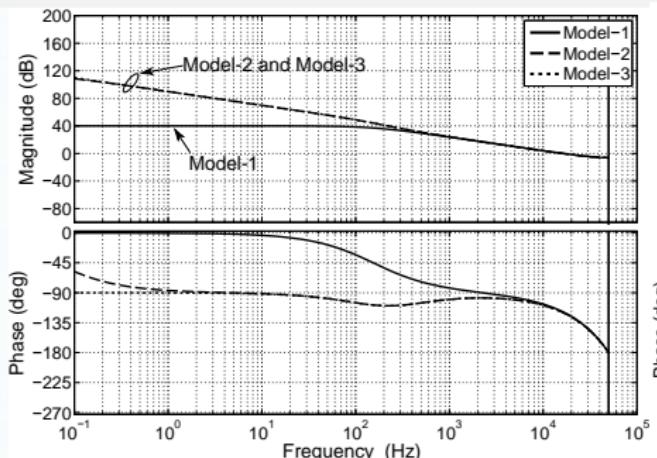
## Why use exact discretization?

- The comparison of  $\frac{\hat{i_L}(z)}{\hat{d}(z)}$  for both the models is performed for wide range of design and operating conditions.
- Discretization methods such as Forward and Backward Euler, Tustin's method are not accurate for wide range of sampling frequencies,  $f_s$ <sup>3</sup>.
- The comparison metrics are dependent on circuit parameters.
- $P_o \in (100W, 100kW)$ ,  $V_g \in (30V, 1000V)$

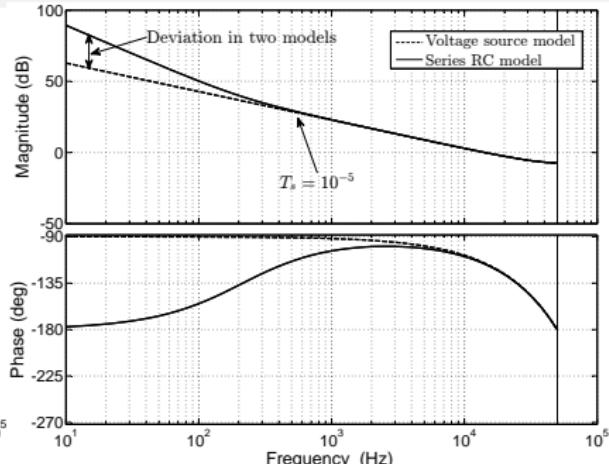
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# Comparison of $\frac{i_L(z)}{d(z)}$ for the two UC models



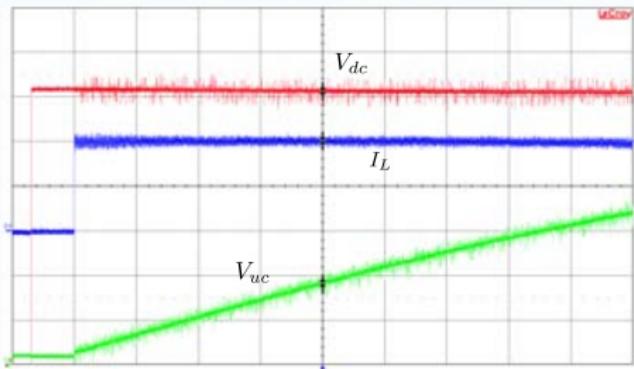
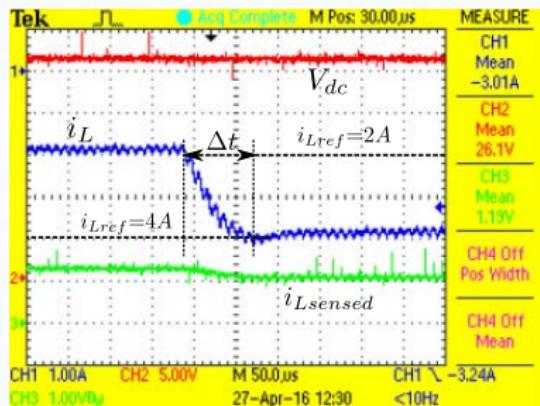
**Figure:** Bode plots comparing the three models for  $P_o=200W$ ,  $V_g=30V$ .



**Figure:** Bode plots for current loop plant transfer functions with PI control for Model 1 and Model 3.

- Model 2 and Model 3 match closely which shows that  $\lambda_2 \approx 0$  is a valid approximation.
- For a given design application, Model 1 and Model 3 diverge especially at low frequency regions.
- The deviation between the two models reduces due to high gain of PI controller at low frequencies.
- The high frequency characteristics determines the stability and bandwidth.
- Phase margin of  $70^\circ$  and bandwidth of  $10kHz$  is achieved.

# Comparison of $\frac{i_L(z)}{d(z)}$ for the two UC models



- Charging mode inner current loop bandwidth,  $f_b = \frac{4}{2\pi\Delta t}$
- Settling time,  $\Delta t$  of  $70\mu s$  is observed based on which bandwidth of  $9kHz$  is achieved.
- This verifies the dynamic performance of the designed inner loop current control.
- UC stack is charged in CC mode. The charging profile shows the stability of the designed current control.
- The charging duration can be verified by  $C_{uc} \frac{\Delta V_{uc}}{\Delta t_c} = i_L$ .
- The UC stack voltage,  $V_{uc}$  and charging current,  $i_L$  is chosen to be low, so that charging duration,  $\Delta t_c$  would be sufficiently high.



## List of works



- 1 PWM Blocking control for seamless mode transition
- 2 Virtual resistance control for seamless mode transition
- 3 Reduced order modelling of ultracapacitors
- 4 Generalized passives design for UC based backup system
- 5 Adaptive control during discharging mode of operation with enhanced performance



# Necessity and contributions

## Generalized passives design

- Why particularly necessary in UC based storage systems??
  - Batteries treated as fixed voltage sources.
  - UC stack undergo greater depth of discharge.
  - Converter design should accommodate wide range of operating conditions.

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<sup>4</sup>K. Saichand and V. John, "A generalized design procedure for passives in a ultracapacitor based bidirectional DC-DC system for backup power applications," in Thirteenth Annual IEEE INDICON, 2016. IEEE Bangalore Section, 2016.



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- The converter and passives' design should also accommodate for both the charging and discharging operating modes.
- Generalized design of passives is necessary:
  - To validate any proposed ultracapacitor model,
  - For performance studies on a UC based dc/dc systems for wide range of design applications.<sup>4</sup>.
- Crucial in modeling of ultracapacitors and in design of adaptive control.

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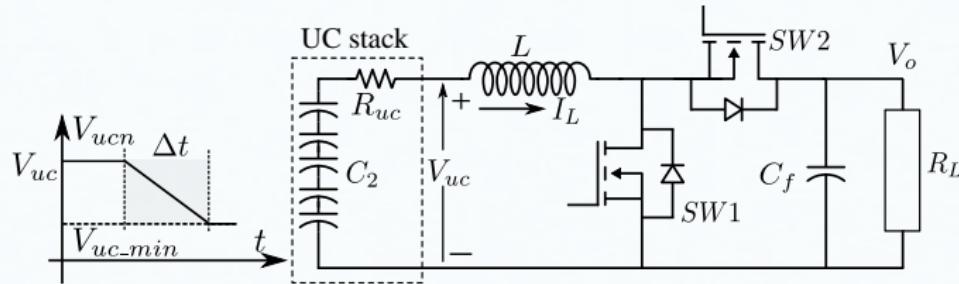
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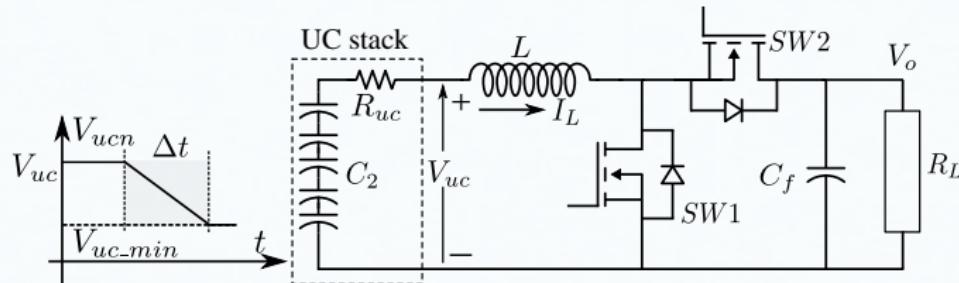
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<sup>5</sup> K. Saichand and V. John, "Adaptive control strategy for ultracapacitor based bidirectional DC-DC converters," accepted for publication in Applied Power Electronics Conference. Tampa, Florida: APEC-2017, March 2017, pp. 1-6.



- The control structure should accommodate for variation in:
  - plant characteristics
  - RHP zero especially due to UC stack deep discharging.

## Advantages of adaptive control

- The controller gains are estimated on-line.
- The proposed control ensures best performance criteria possible.
- Adaptive control incorporates the variation of RHP zero and varies the bandwidth accordingly<sup>5</sup>.

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## Conclusions and Contributions

- Mode identification algorithm based on PWM blocking has been proposed which ensures:
  - Fastest mode transition.
  - Smooth, seamless mode transition.
  - Accurate identification of control modes.
- Alternately, virtual resistance control is proposed which allows control on current dynamics during mode transition as well.
- Simplified voltage source model for UCs similar to batteries have been proposed and verified which simplifies the controller design.
- The possibility of using this simplified model have been studied for wide range of design applications.
- For this, a generalized passives design is carried out where the variation of passives for various design applications is carried out.
- An adaptive control has been proposed which allows online variation of controller gains to accommodate system characteristics and RHP zero variation.



# List of Key Publications

- [1] K. Saichand and V. John, "PWM block method for control of an ultracapacitor-based bidirectional DC/DC backup system," *IEEE Transactions on Industry Applications*, vol. 52, no. 5, pp. 4126–4134, Sept 2016.
- [2] K. Saichand, A. Kumrawat, and V. John, "High performance AC-DC control power supply for low voltage ride through inverters," *Sadhana*, vol. 41, no. 2, pp. 147–159, 2016.
- [3] K. Saichand and V. John, "Simplified modeling of ultracapacitors for bidirectional DC-DC converter applications," accepted for publication in *Applied Power Electronics Conference*. Tampa, Florida: APEC-2017, March 2017, pp. 1–6.
- [4] K. Saichand and V. John, "Adaptive control strategy for ultracapacitor based bidirectional DC-DC converters," accepted for publication in *Applied Power Electronics Conference*. Tampa, Florida: APEC-2017, March 2017, pp. 1–6.
- [5] K. Saichand and V. John, "A generalized design procedure for passives in a ultracapacitor based bidirectional DC-DC system for backup power applications," accepted for publication in *Thirteenth Annual IEEE INDICON, 2016*. IISc Bangalore: IEEE Bangalore Section, December 2016, pp. 1–6.
- [6] K. Saichand and V. John, "PWM block method for control of ultracapacitor based bidirectional dc/dc backup system," in *2014 IEEE International Conference on Power Electronics, Drives and Energy Systems (PEDES)*, IISc bangalore, December 2014, pp. 1–6.
- [7] A. Kumrawat, K. Saichand, and V. John, "Design of AC-DC control power supply with wide input voltage variation," in *2013 IEEE Innovative Smart Grid Technologies-Asia (ISGT Asia)*, Nov 2013, pp. 1–6.
- [8] K. Saichand, A. Kumrawat, and V. John, "Design of start-up power circuit for control power supplies with wide input voltage variation," in *National power electronics conference*. IIT Kanpur: NPEC, December 2013, pp. 1–6.
- [9] K. Saichand and V. John, "Virtual resistance based control for ultracapacitor based bidirectional DC/DC backup system," in *National power electronics conference*. IIT Bombay: NPEC, December 2015, pp. 1–6.



# Thank You....

