4. Type Rules for for-loop

for (int i=e0; e1; s1) s2

5)
$$\frac{\Gamma \mid -_{e} s1: \tau}{\Gamma \mid -_{s} s1;}$$
 (stmt-expr)

6)
$$\frac{\Gamma \mid -_e s2: \tau}{\Gamma \mid -_s s2;}$$
 (stmt-expr)

3)
$$\overline{\Gamma \mid -_{e} true :bool}$$
 (True)

4)
$$\overline{\Gamma \mid -efalse :bool}$$
 (False)

$$\frac{\Gamma,(l,i:\tau)\mid_{-sl}i=e0\quad\forall_{\tau}:(l,i:\tau)}{\Gamma\mid_{-sl}\tau\ i;\ i=e0}\quad\forall_{\tau}:(l,i:\tau)\not\models\Gamma$$

$$\frac{\Gamma_{,}(l,i:int),(-,e0:int)\mid -_{sl}\tau\ i;\ i=e0\ \tau_{i}<\tau_{e0}\ \Gamma_{,}(l,i:int)\mid -_{e}e1:bool\ \tau_{e1}< bool\ \Gamma_{,}(l,i:int)\mid -_{s}s1\ \Gamma_{,}(l,i:int)\mid -_{s}s2}{\Gamma\mid -_{s}for\ (int\ i=e0;\ e1;\ s1)\ s2}\ \ \text{(for)}$$

5. derivation

```
(return : int[]) |- sl int[] y; y = new int[2]; y[1] = 1; return y;
```

9)
$$\frac{\Gamma = (return : int[]), (l,y:int[]) \mid -_{e} y:int[] \quad int[] \leq int[] \quad (return : int[]) \in \Gamma}{\Gamma = (return : int[]), (l,y:int[]) \mid -_{s} return y;}$$
 (return)

8)
$$\frac{\Gamma = (return : int[]), (l,y:int[]) \mid -_e y : int[]}{\Gamma = (return : int[]), (l,y:int[]) \mid -_e 1 : int}}{\Gamma = (return : int[]), (l,y:int[]) \mid -_e y[1] : int}$$
(array-lookup)

$$\frac{\Gamma = (return:int[]), (l,y:int[]) \mid -_e y[1]:int[] \qquad \Gamma = (return:int[]), (l,y:int[]) \mid -_e 1:int \qquad int[] \leq int}{\Gamma = (return:int[]), (l,y:int[]) \mid -_e y[1] = 1;}$$
 (assign)

$$\frac{\Gamma = (return:int[]), (l,y:int[]) \mid -_{e}y:int[]}{\Gamma = (return:int[]), (l,y:int[]) \mid -_{e}new:int[2]:int[]} int[] < i$$

(assign)

$$\frac{\Gamma = (return : int[]), (l,y:int[]) \mid_{sl} y = new \ int[2]; \quad \forall_{\tau} : (l,y:\tau') \not\models \Gamma}{\Gamma = (return : int[]) \mid_{sl} int[] \ y; \ y = new \ int[2];} \quad \text{(var-decl)}$$

 $\frac{\Gamma = (return : int[]) \mid -_{sl} int[] \ y; \ \Gamma = (return : int[]) \mid -_{sl} y = new \ int[2]; \ \Gamma = (return : int[]) \mid -_{sl} y[1] = 1; \ \Gamma = (return : int[]) \mid -_{sl} return \ y}{\Gamma = (return : int[]) \mid -_{sl} int[] \ y; \ y = new \ int[2]; \ y[1] = 1; \ return \ y;}$

(seq)

¹⁾ $\Gamma=(return:int[]) \mid \neg_{sl} int[] y; y=new int[2]; y[1]=1; return y;$