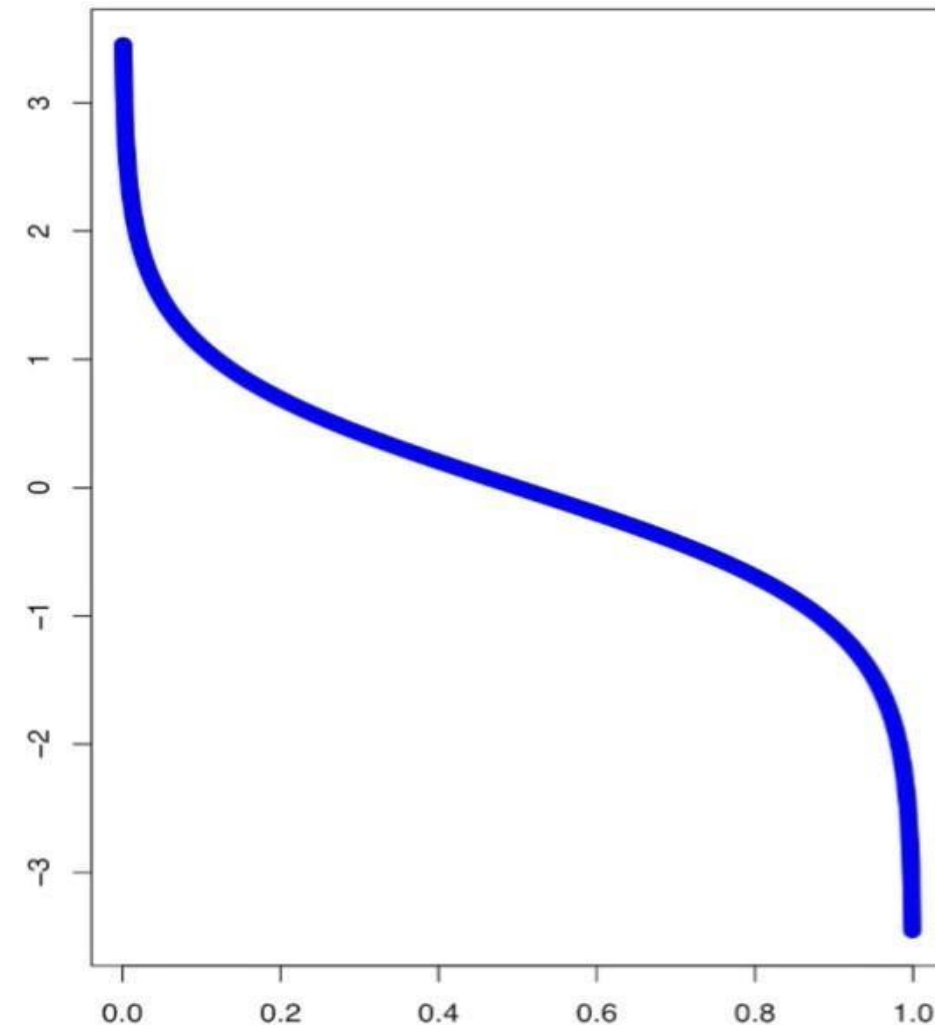


# Summary - AdaBoost

1. Assign equal sample weights for each sample, that is, sample weight =  $1 / \text{number of samples}$
2. Bootstrap the samples as per the weights assigned and build a weak learner on that sample
3. Once the weak learner is built, AdaBoost chooses the alpha, which measures the importance of it based on the error made by that weak learner
$$\alpha_t = \frac{1}{2} \log\left(\frac{1-\epsilon_t}{\epsilon_t}\right)$$
4. Calculate the new sample weights for the next weak learner
  - a. New sample weight for incorrect samples = sample weight \*  $\exp(\alpha)$  /  $z_t$
  - b. New sample weight for correct samples = sample weight \*  $\exp(-\alpha)$  /  $z_t$
5. Create a bootstrapped dataset with the odds of each sample being chosen based on their new sample weights
6. Repeat the process n number of times
7. The final prediction is a weighted majority vote/average of all the weak learners

# Summary - AdaBoost

- As evident from the graph, importance of each weak learner decreases with the increase in error made by that learner, that is when error is zero, importance of that weak learner is the highest.
- If the total error is greater than 0.5 then negative importance flips the class prediction.



**Importance VS Error of each learner**

# Gradient Boosting for Classification

- It relies on the intuition that the next model, when combined with previous models, minimizes the overall prediction error
- In Gradient Boosting, instead of predicting the actual labels of the data at each iteration, it tries to predict the residual errors made by the previous predictor.

Steps involved in the gradient boosting algorithm for classification are

1. Initialize the model with initial prediction for all observations
2. Calculate the residual for each observation.
3. Build a tree and calculate the output value for each leaf node
4. Update all predictions using previous probabilities and new output value
5. Repeat steps 2-4 until maximum number of estimators reached

# Let's understand this with an example

Let's consider an example dataset, where X is assumed to be the age of people and Y is whether they like a particular movie or not.

X	Y
10	0
20	1
30	1
40	1
50	0
60	1

- Let's find log odds for Y = 1

- $\log(4/2) = 0.69$

- Let's find out the probability using the below formula :

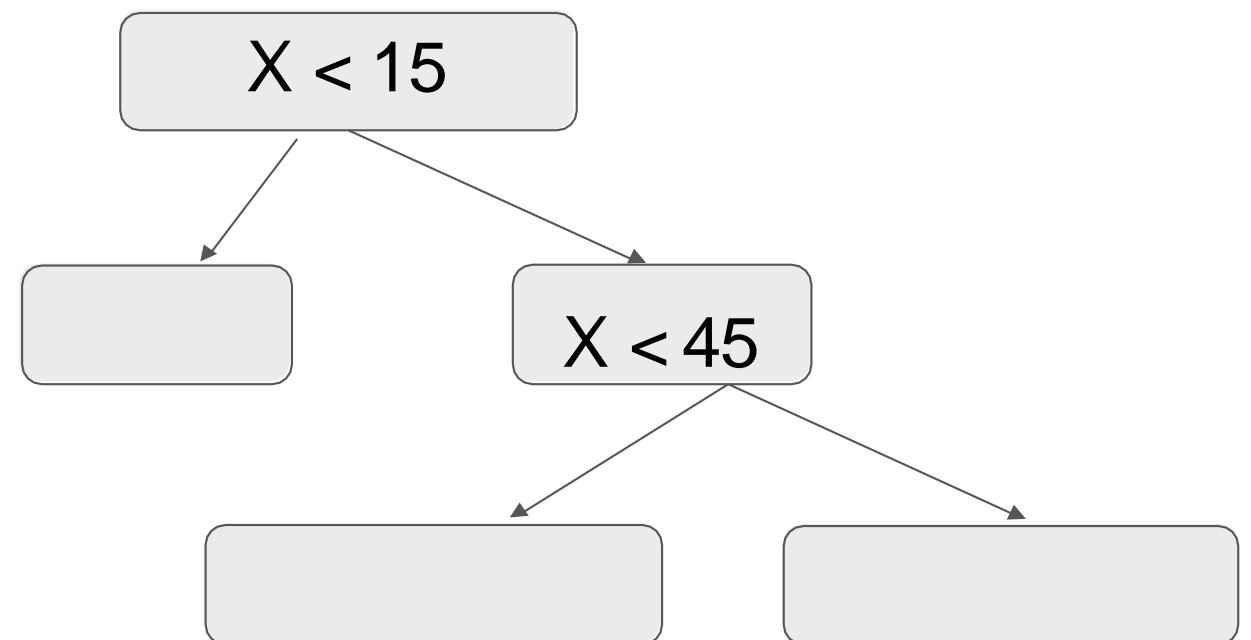
$$P = \frac{e^{\log(odds)}}{1 + e^{\log(odds)}}$$

- $P(Y = 1) = (e^{(0.69)}) / (1 + e^{(0.69)}) = 0.67$

# Let's calculate residuals for our predictions

We will build a tree with `max_depth = 2` to predict residuals.

X	Y	Residual (observed- predicted probability)
10	0	-0.67
20	1	0.33
30	1	0.33
40	1	0.33
50	0	-0.67
60	1	0.33

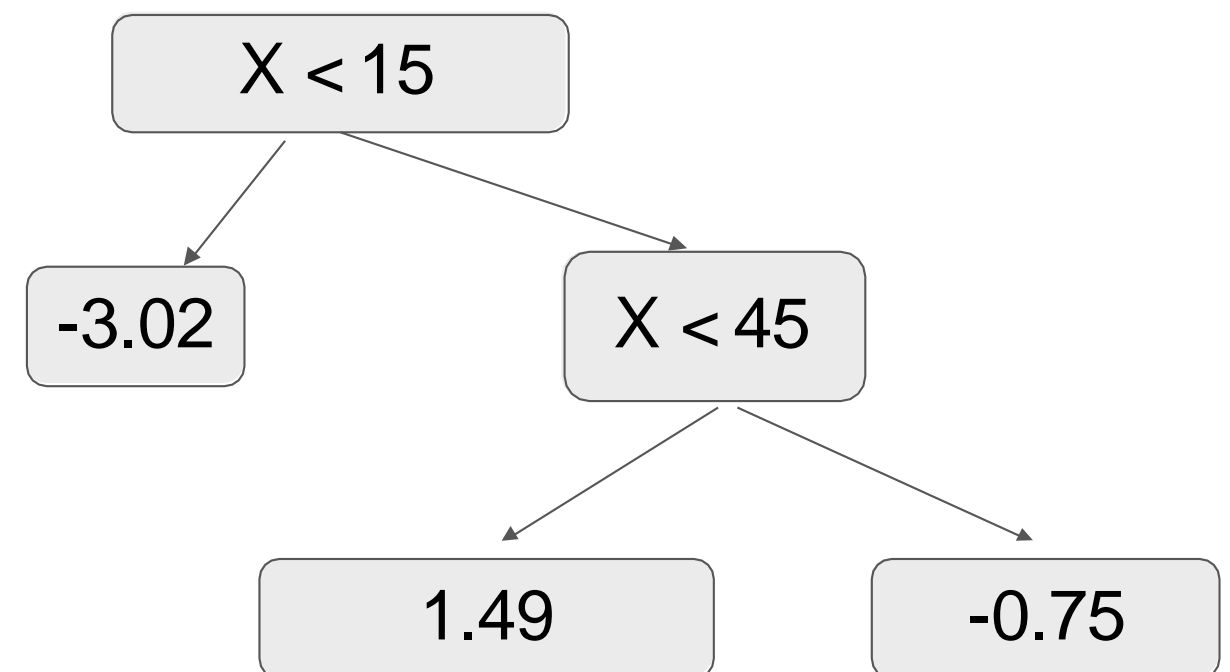


# Transformation formula

We can calculate the output value of each leaf using the following formula:

$$\frac{\sum Residual}{\sum [PreviousProb * (1 - PreviousProb)]}$$

X	Y	Residual
10	0	-0.67
20	1	0.33
30	1	0.33
40	1	0.33
50	0	-0.67
60	1	0.33



# Update Predictions

We'll update our predictions using below formula with a learning rate of 0.8

$$OldTree + LearningRate * NewTree$$

X	Y	Residual	Y1 = Previous(log odds) + (LR * New values)	Output1 = New predictions (e^Y1) / (1 + e^Y1)
10	0	-0.67	-1.72	0.15
20	1	0.33	1.88	0.87
30	1	0.33	1.88	0.87
40	1	0.33	1.88	0.87
50	0	-0.67	0.09	0.52
60	1	0.33	0.09	0.52

# Calculate the Residuals again

We'll calculate the residuals again and repeat the same steps until we get good prediction probabilities

X	Y	Residual	$Y1 = \text{Previous (log odds)} + (\text{LR} * \text{New values})$	Output1 = predicted probability $(e^{Y1}) / (1 + e^{Y1})$	Residuals
10	0	-0.67	-1.72	0.15	-0.15
20	1	0.33	1.88	0.87	0.13
30	1	0.33	1.88	0.87	0.13
40	1	0.33	1.88	0.87	0.13
50	0	-0.67	0.09	0.52	-0.52
60	1	0.33	0.09	0.52	0.48

Probabilities are closer to actual labels

Residuals are getting smaller



# Loss function

- Loss function is same as is generally use in case of classification models **with some variations**
- The loss function used in gradient boosting is log-likelihood. Our goal is to maximize the log likelihood function (or minimize negative log likelihood).

$$\log(\text{likelihood of the observed data given the prediction}) = [y_i * \log(p) + (1 - y_i) * \log(1 - p)]$$

Where,  $y_i$  is the observed value (0 or 1) and  $p$  is the predicted probability.

- Writing this in terms of log(odds) and differentiating, we get:

$$\frac{d}{d\log(\text{odds})} (y_i \log(\text{odds}) + \log(1 + e^{\log(\text{odds})})) = -y_i + \frac{e^{\log(\text{odds})}}{1 + e^{\log(\text{odds})}}$$

# Steps for XGBoost

1. In XGBoost, initial prediction for all observations is taken as mean of the target values for regression and 0.5 for binary classification problems.
2. Calculate the residual for each observation.
3. Build a tree and calculate the output value for each leaf node

## How a tree is built in XGBoost?

- a. At each level, XGBoost calculates a **similarity score(ss)** for the node and the possible two leaves.

SS for Regression

$$\frac{(\sum Residuals)^2}{Number\ of\ Samples + \lambda}$$

SS for Classification

$$\frac{(\sum Residuals)^2}{[Probability * (1 - Probability)] + \lambda}$$

- b. The formula for similarity score is derived directly from the loss function and helps to find the optimal point which minimizes the loss function.

- c. Where  $\lambda$  is a regularization parameter in loss function of XGBoost



# Steps for XGBoost

d. Gain is calculated for each possible split, where gain is calculated as -

**Left leave ss + Right leave ss - Root node ss**

e. The split which maximizes the gain is considered as best split and is chosen to grow a tree.

f. After building a tree, output value is calculated for each of the leaves.

 <p>Output Value - Regression</p>	$\frac{\sum Residuals}{Number\ of\ Samples + \lambda}$
 <p>Output Value - Classification</p>	$\frac{\sum Residuals}{[Probability * (1 - Probability)] + \lambda}$

4. Update all predictions using previous probabilities and new output value - same as Gradient Boosting.

5. Repeat steps 1-5 until maximum number of estimators reached.

# Hyperparameter Tuning - Importance and Caution !

1. Needed to handle overfitting
2. Can help improve performance
3. But excessive use can bias the whole model not useful for 'new' data
4. Need to be careful and appropriate study of data should be done

# Hyperparameters in XGBoost

- **Learning\_rate / eta:** Gradient boosted decision trees are quick to learn and overfit training data. One effective way to slow down learning in the model is to use a learning rate, also called shrinkage.
- **gamma:** A node is split only when the resulting split gives a positive reduction in the loss function. Gamma specifies the minimum loss reduction required to make a split. Higher the gamma value, lesser the chances of overfitting.
- **scale\_pos\_weight:** Control the balance of positive and negative weights. It can have any positive value as input. It helps in imbalanced classification problems.

# Hyperparameters in XGBoost

A key one is to select a subset of columns while building an individual tree, level in a tree or node split in a level in a tree

- **colsample\_bytree:** This denotes the the ratio of columns to be used when constructing each tree. It takes input as float values between (0,1] i.e. between greater than 0% of features and less than or equal to 100% of features.
- **colsample\_bylevel:** This denotes the ratio of columns for each new level of a tree. If colsample\_bytree is used, then columns are subsampled from the set of columns chosen for the current tree.
- **colsample\_bynode:** This denotes the ratio of columns to be used for each node i.e. for each split. If colsample\_bylevel is used, then columns are subsampled from the set of columns chosen for the current level.

Note: Three parameters defined above works cumulatively, for example, if we have total 32 columns and if {'colsample\_bytree':0.5, 'colsample\_bylevel':0.5, 'colsample\_bynode':0.5}, then we leave only 4 columns to choose from at each split.