ModelSelection

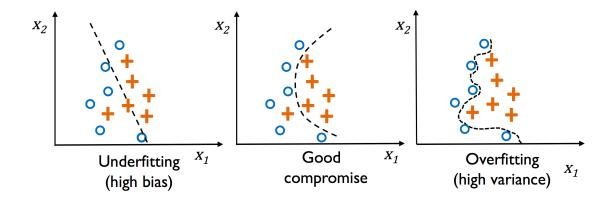
January 1, 2025

1 Model Comparison and Selection

- since no single classifier will work best for all the problems, we need to experiment with a handful
- need to effectively compare the models and select the best one for the problem

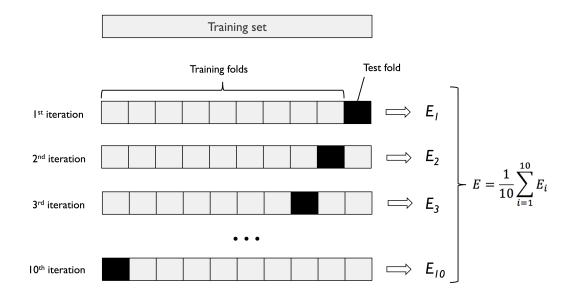
1.1 Over and under fitting models

- over or under fitting can occur if training data is not properly sampled or features are not properly selected
- models can suffer from underfitting (high bias) if the model is too simple
 - bias measures how far off the predictions are from the correct values in general if we rebuild the model multiple times on different datasets
- models can suffer from overfitting the training data (high variance) if the model is too complex for the underlying training data
 - variance measures the consistency (or variability) of the model prediction for classifying
 a particular example if we retrain the model multiple times, e.g., on different subsets of
 the training dataset
- the following figure demonstrates under and over fitting the models based



1.2 K-fold cross-validation

• k-fold cross-validation help obtain reliable can us esof the timates model's performance on unseen data



- stratified k-fold cross-validation can yield better bias and variance estimates, especially in cases of unequal class proportions
- https://scikit-learn.org/stable/modules/generated/sklearn.model_selection.StratifiedKFold.html

1.2.1 Breast Cancer Wisconsin dataset

- details: https://archive.ics.uci.edu/ml/datasets/Breast+Cancer+Wisconsin+(Diagnostic)
- let's use the binary classification dataset for detecting breast cancer

```
[1]: import pandas as pd
     import numpy as np
[2]: url = 'https://archive.ics.uci.edu/ml/machine-learning-databases/
      ⇔breast-cancer-wisconsin/wdbc.data'
     df = pd.read csv(url, header=None)
[3]: df
     # Note col 0 is ID of the sample and col 1 is the corresponding diagnoses (M = \Box
      \rightarrow malignant, B = benign)
                 0 1
                            2
                                   3
                                            4
                                                    5
                                                              6
                                                                        7
                                                                                  8
```

```
567
       927241
                   20.60
                          29.33
                                  140.10
                                           1265.0
                                                    0.11780 0.27700 0.35140
                Μ
568
                                            181.0
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                    7.76
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                                   47.92
                                                    0.05263
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                                                                       0.00000
           9
                      22
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                                                                   27
                                                                            28
     0.14710
                  25.380
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0
                                  184.60
                                           2019.0
                                                    0.16220
                                                              0.66560
                                                                       0.7119
1
     0.07017
                  24.990
                           23.41
                                   158.80
                                           1956.0
                                                    0.12380
                                                              0.18660
                                                                       0.2416
2
                           25.53
                                   152.50
     0.12790
                  23.570
                                           1709.0
                                                    0.14440
                                                              0.42450
                                                                       0.4504
3
     0.10520
                  14.910
                           26.50
                                   98.87
                                            567.7
                                                    0.20980
                                                              0.86630
                                                                        0.6869
4
     0.10430
                  22.540
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                   •••
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                                           2027.0
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                                                                        0.4107
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     0.09791
                  23.690
                           38.25
                                   155.00
                                                    0.11660
                                                              0.19220
                                           1731.0
                                                                       0.3215
566
     0.05302
                  18.980
                           34.12
                                   126.70
                                           1124.0
                                                    0.11390
                                                              0.30940
                                                                       0.3403
567
     0.15200
                  25.740
                           39.42
                                   184.60
                                           1821.0
                                                    0.16500
                                                              0.86810
                                                                        0.9387
                                                    0.08996
568
     0.00000
                   9.456
                           30.37
                                   59.16
                                            268.6
                                                              0.06444
                                                                       0.0000
         29
                  30
                            31
0
     0.2654
              0.4601
                      0.11890
1
     0.1860
              0.2750
                      0.08902
2
     0.2430
              0.3613
                      0.08758
3
     0.2575
              0.6638
                      0.17300
4
     0.1625
              0.2364
                      0.07678
     0.2216
564
              0.2060
                      0.07115
     0.1628
              0.2572
565
                      0.06637
566
     0.1418
              0.2218
                      0.07820
567
     0.2650
              0.4087
                      0.12400
     0.0000
568
              0.2871
                      0.07039
```

[569 rows x 32 columns]

[4]: df.describe()

```
[4]:
                       0
                                    2
                                                 3
                                                                            5
                                                                                \
            5.690000e+02
                           569.000000
                                                     569.000000
     count
                                        569.000000
                                                                   569.000000
            3.037183e+07
                             14.127292
                                         19.289649
                                                      91.969033
                                                                   654.889104
     mean
            1.250206e+08
                              3.524049
                                          4.301036
                                                      24.298981
                                                                   351.914129
     std
            8.670000e+03
                              6.981000
                                                      43.790000
     min
                                          9.710000
                                                                   143.500000
     25%
            8.692180e+05
                             11.700000
                                         16.170000
                                                      75.170000
                                                                   420.300000
     50%
            9.060240e+05
                             13.370000
                                         18.840000
                                                      86.240000
                                                                   551.100000
     75%
            8.813129e+06
                             15.780000
                                         21.800000
                                                     104.100000
                                                                   782.700000
            9.113205e+08
                             28.110000
                                         39.280000
                                                     188.500000
     max
                                                                  2501.000000
                     6
                                  7
                                               8
                                                            9
                                                                         10
     count
            569.000000
                         569.000000
                                      569.000000
                                                   569.000000
                                                                569.000000
              0.096360
                           0.104341
                                        0.088799
                                                     0.048919
                                                                  0.181162
     mean
                                                                  0.027414
     std
              0.014064
                           0.052813
                                        0.079720
                                                     0.038803
```

```
0.052630
                       0.019380
                                   0.00000
                                                 0.000000
                                                              0.106000
min
25%
                                   0.029560
                                                 0.020310
                                                              0.161900
         0.086370
                       0.064920
50%
         0.095870
                       0.092630
                                   0.061540
                                                 0.033500
                                                              0.179200
75%
         0.105300
                       0.130400
                                   0.130700
                                                 0.074000
                                                              0.195700
                       0.345400
         0.163400
                                   0.426800
                                                 0.201200
                                                              0.304000
max
                22
                             23
                                                        25
                                                                     26
                                                                         \
                                          24
count
       569.000000
                    569.000000
                                 569.000000
                                                569.000000
                                                            569.000000
         16.269190
                      25.677223
                                 107.261213
                                               880.583128
                                                               0.132369
mean
std
         4.833242
                       6.146258
                                   33.602542
                                                569.356993
                                                               0.022832
min
         7.930000
                      12.020000
                                   50.410000
                                                185.200000
                                                               0.071170
                      21.080000
                                   84.110000
                                                515.300000
25%
        13.010000
                                                               0.116600
50%
        14.970000
                      25.410000
                                   97.660000
                                                686.500000
                                                               0.131300
75%
        18.790000
                      29.720000
                                 125.400000
                                               1084.000000
                                                               0.146000
        36.040000
                      49.540000
                                 251.200000
                                               4254.000000
                                                               0.222600
max
                27
                             28
                                          29
                                                       30
                                                                    31
count
       569.000000
                    569.000000
                                 569.000000
                                              569.000000
                                                           569.000000
         0.254265
                       0.272188
                                   0.114606
                                                 0.290076
                                                              0.083946
mean
std
         0.157336
                       0.208624
                                   0.065732
                                                 0.061867
                                                              0.018061
min
         0.027290
                       0.00000
                                   0.00000
                                                 0.156500
                                                              0.055040
25%
         0.147200
                       0.114500
                                   0.064930
                                                 0.250400
                                                              0.071460
50%
                       0.226700
                                   0.099930
         0.211900
                                                 0.282200
                                                              0.080040
75%
         0.339100
                       0.382900
                                   0.161400
                                                 0.317900
                                                              0.092080
max
          1.058000
                       1.252000
                                   0.291000
                                                 0.663800
                                                              0.207500
```

[8 rows x 31 columns]

```
[5]: # Let's create X and y numpy ndarrays
X = df.loc[:, 2:].values
y = df.loc[:, 1].values
```

[6]: y

```
'B',
 'M', 'B', 'M',
 [7]: # let's encode the labels with LabelEncoder
from sklearn.preprocessing import LabelEncoder
[8]: le = LabelEncoder()
y = le.fit_transform(y)
[9]: y[:10]
[9]: array([1, 1, 1, 1, 1, 1, 1, 1, 1])
[10]: y.shape
[10]: (569,)
[11]: X.shape
```

```
[11]: (569, 30)
[12]: le.classes_
      # 0 is Benign (Not-Cancer) and 1 is Malignant (Cancer)
[12]: array(['B', 'M'], dtype=object)
[13]: # let's Scale the data using StandardScaler
      from sklearn.preprocessing import StandardScaler
[14]: sc = StandardScaler()
      sc.fit(X) # fit the whole data to calculate mean and standard deviation
      X_sc = sc.transform(X) # transform training set
[15]: # let's do the StratifiedKFold cross validation
      from sklearn.model_selection import StratifiedKFold
      # use logistic regression classifier
      from sklearn.linear_model import LogisticRegression
      #https://scikit-learn.org/stable/modules/generated/sklearn.linear_model.
       \hookrightarrow Logistic Regression. html
[16]: kfold = StratifiedKFold(n_splits=10)
[17]: scores = []
      for k, (train, test) in enumerate(kfold.split(X_sc, y)): # iterator
          lr_model = LogisticRegression(random_state=1, solver='lbfgs')
          #print(train.shape, test.shape)
          lr_model.fit(X_sc[train], y[train])
          score = lr_model.score(X_sc[test], y[test])
          scores.append(score)
          print(f'Fold:{k+1:2d}, Class dist.:{np.bincount(y[train])}, Acc: {score:.
       93f}')
     Fold: 1, Class dist.: [322 190], Acc: 0.982
     Fold: 2, Class dist.: [322 190], Acc: 0.982
     Fold: 3, Class dist.:[321 191], Acc: 0.982
     Fold: 4, Class dist.: [321 191], Acc: 0.965
     Fold: 5, Class dist.:[321 191], Acc: 0.982
     Fold: 6, Class dist.: [321 191], Acc: 0.982
     Fold: 7, Class dist.:[321 191], Acc: 0.947
     Fold: 8, Class dist.: [321 191], Acc: 1.000
     Fold: 9, Class dist.:[321 191], Acc: 1.000
     Fold:10, Class dist.: [322 191], Acc: 0.982
[18]: print(f'CV accuracy : {np.mean(scores):.3f}, +/- {np.std(scores):.3f}')
     CV accuracy: 0.981, +/- 0.015
```

```
[19]: # better: use scikit learn's cross_val_score
      from sklearn.model_selection import cross_val_score
[20]: | lr_model = LogisticRegression(random_state=1, solver='lbfgs')
      scores = cross_val_score(estimator=lr_model, X=X_sc, y=y, cv=10, n_jobs=-1)
      # n_{jobs} = -1 means use all available processors to do computation in parallel
[21]: | print(f'CV accuracy scores: {scores}')
     CV accuracy scores: [0.98245614 0.98245614 0.98245614 0.96491228 0.98245614
     0.98245614
      0.94736842 1.
                            1.
                                       0.98214286]
[22]: print(f'CV accuracy: {np.mean(scores):.3f}, +/- {np.std(scores):.3f}')
     CV accuracy: 0.981, +/- 0.015
[23]: # let's compare a handful of Classifiers
      from sklearn.neural_network import MLPClassifier
      from sklearn.neighbors import KNeighborsClassifier
      from sklearn.svm import SVC
      from sklearn.gaussian process import GaussianProcessClassifier
      from sklearn.gaussian_process.kernels import RBF
      from sklearn.tree import DecisionTreeClassifier
      from sklearn.ensemble import RandomForestClassifier, AdaBoostClassifier
      from sklearn.naive bayes import GaussianNB
      from sklearn.discriminant_analysis import QuadraticDiscriminantAnalysis
[24]: names = ["KNN", "Linear SVM", "RBF SVM", "Gaussian Process",
               "Decision Tree", "Random Forest", "Neural Net", "AdaBoost",
               "Naive Bayes", "QDA", 'Logistic Reg']
      scores = [] # store (name, mean, std_dev) for each classifier
      classifiers = [
          KNeighborsClassifier(3),
          SVC(kernel="linear", C=0.025),
          SVC(gamma=2, C=1),
          GaussianProcessClassifier(1.0 * RBF(1.0)),
          DecisionTreeClassifier(max depth=5),
          RandomForestClassifier(max_depth=5, n_estimators=10, max_features=1),
          MLPClassifier(alpha=1, max_iter=1000),
          AdaBoostClassifier(),
          GaussianNB(),
          QuadraticDiscriminantAnalysis(),
          LogisticRegression(random_state=1, solver='lbfgs')
      ]
      # iterate over classifiers
      for name, clf in zip(names, classifiers):
```

```
cvs = cross_val_score(estimator=clf, X=X_sc, y=y, cv=10, n_jobs=-1)
    scores.append((name, np.mean(cvs), np.std(cvs)))
/usr/local/lib/python3.12/site-
packages/sklearn/ensemble/_weight_boosting.py:519: FutureWarning: The SAMME.R
algorithm (the default) is deprecated and will be removed in 1.6. Use the SAMME
algorithm to circumvent this warning.
  warnings.warn(
/usr/local/lib/python3.12/site-
packages/sklearn/ensemble/_weight_boosting.py:519: FutureWarning: The SAMME.R
algorithm (the default) is deprecated and will be removed in 1.6. Use the SAMME
algorithm to circumvent this warning.
  warnings.warn(
/usr/local/lib/python3.12/site-
packages/sklearn/ensemble/_weight_boosting.py:519: FutureWarning: The SAMME.R
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/usr/local/lib/python3.12/site-
packages/sklearn/ensemble/_weight_boosting.py:519: FutureWarning: The SAMME.R
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 warnings.warn(
/usr/local/lib/python3.12/site-
packages/sklearn/ensemble/_weight_boosting.py:519: FutureWarning: The SAMME.R
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/usr/local/lib/python3.12/site-
packages/sklearn/ensemble/_weight_boosting.py:519: FutureWarning: The SAMME.R
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algorithm to circumvent this warning.
 warnings.warn(
/usr/local/lib/python3.12/site-
packages/sklearn/ensemble/_weight_boosting.py:519: FutureWarning: The SAMME.R
algorithm (the default) is deprecated and will be removed in 1.6. Use the SAMME
algorithm to circumvent this warning.
  warnings.warn(
/usr/local/lib/python3.12/site-
packages/sklearn/ensemble/_weight_boosting.py:519: FutureWarning: The SAMME.R
algorithm (the default) is deprecated and will be removed in 1.6. Use the SAMME
algorithm to circumvent this warning.
  warnings.warn(
/usr/local/lib/python3.12/site-
packages/sklearn/ensemble/_weight_boosting.py:519: FutureWarning: The SAMME.R
algorithm (the default) is deprecated and will be removed in 1.6. Use the SAMME
algorithm to circumvent this warning.
```

```
warnings.warn(
     /usr/local/lib/python3.12/site-
     packages/sklearn/ensemble/_weight_boosting.py:519: FutureWarning: The SAMME.R
     algorithm (the default) is deprecated and will be removed in 1.6. Use the SAMME
     algorithm to circumvent this warning.
       warnings.warn(
[25]: scores
[25]: [('KNN', 0.9647869674185465, 0.02239183921884522),
       ('Linear SVM', 0.9736215538847116, 0.021152440486425998),
       ('RBF SVM', 0.6274122807017544, 0.006965956216784447),
       ('Gaussian Process', 0.9789473684210526, 0.017189401703741607),
       ('Decision Tree', 0.9175438596491228, 0.04004460424741518),
       ('Random Forest', 0.9403195488721805, 0.03343225060091806),
       ('Neural Net', 0.975407268170426, 0.02104239610504222),
       ('AdaBoost', 0.963095238095238, 0.027680410820357663),
       ('Naive Bayes', 0.9315162907268169, 0.0327113878182645),
       ('QDA', 0.9560776942355889, 0.02110040899790857),
       ('Logistic Reg', 0.9806704260651629, 0.01456955548732776)]
[26]: # let's sort the scores in descending order of accuracy
      scores.sort(key=lambda t: t[1], reverse=True)
[27]: scores
[27]: [('Logistic Reg', 0.9806704260651629, 0.01456955548732776),
       ('Gaussian Process', 0.9789473684210526, 0.017189401703741607),
       ('Neural Net', 0.975407268170426, 0.02104239610504222),
       ('Linear SVM', 0.9736215538847116, 0.021152440486425998),
       ('KNN', 0.9647869674185465, 0.02239183921884522),
       ('AdaBoost', 0.963095238095238, 0.027680410820357663),
       ('QDA', 0.9560776942355889, 0.02110040899790857),
       ('Random Forest', 0.9403195488721805, 0.03343225060091806),
       ('Naive Bayes', 0.9315162907268169, 0.0327113878182645),
       ('Decision Tree', 0.9175438596491228, 0.04004460424741518),
       ('RBF SVM', 0.6274122807017544, 0.006965956216784447)]
```

1.3 ROC curve

- Receiver Operating Characteristic (ROC) graphs are used to select models for classification based on the performance with respect to the FPR and TPR
- the diagonal of the ROC curve can be interpreted as random guessing
 - classification models that fall below the diagonal are considered as worse than random guessing
- a perfect classifier would fall into the top-left corner of the graph with a \mathbf{TPR} of $\mathbf{1}$ and and an \mathbf{FPR} of $\mathbf{0}$

• based on ROC curve, we can compute ROC area under the curve (ROC AUC) to characterize the performance of a classification model

1.3.1 Logistic Regression - ROC curve for cross validation

 \hookrightarrow classifier

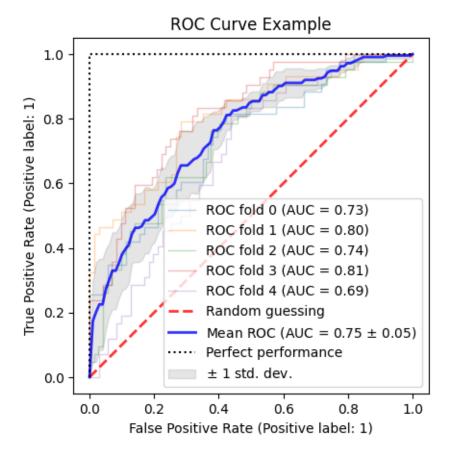
X_train = X_sc[:, [4, 14]]

• https://scikit-learn.org/stable/auto_examples/model_selection/plot_roc_crossval.html

```
[30]: from sklearn.metrics import RocCurveDisplay, auc import matplotlib.pyplot as plt import numpy as np from sklearn.model_selection import StratifiedKFold

[31]: # To generate more representitive ROC graph, # we'll use just 2 features 4 and 14 making it more challenging for the _____
```

```
[35]: cv = StratifiedKFold(n_splits=5) # just to 5 fold
      classifier = LogisticRegression(random_state=1, solver='lbfgs')
      tprs = []
      aucs = []
      mean_fpr = np.linspace(0, 1, 100)
      fig, ax = plt.subplots()
      # create and add ROC for each fold
      for i, (train, test) in enumerate(cv.split(X train, y)): # iterator
          classifier.fit(X_train[train], y[train])
          viz = RocCurveDisplay.from_estimator(classifier, X_train[test], y[test],
                               name=f'ROC fold {i}',
                               alpha=0.3, lw=1, ax=ax)
          interp_tpr = np.interp(mean_fpr, viz.fpr, viz.tpr)
          interp_tpr[0] = 0.0
          tprs.append(interp_tpr)
          aucs.append(viz.roc_auc)
      # add curve for random guessing
      ax.plot([0, 1], [0, 1], linestyle='--', lw=2, color='r',
              label='Random guessing', alpha=.8)
      mean_tpr = np.mean(tprs, axis=0)
      mean tpr[-1] = 1.0
      mean_auc = auc(mean_fpr, mean_tpr)
      std_auc = np.std(aucs)
      # add curve for mean scores
      ax.plot(mean_fpr, mean_tpr, color='b',
              label=r'Mean ROC (AUC = %0.2f $\pm$ %0.2f)' % (mean_auc, std_auc),
              lw=2, alpha=.8)
```



1.4 ROC Curve to compare models

```
[37]: import pandas as pd
      import numpy as np
      from sklearn.metrics import roc_curve, auc, roc_auc_score
      import matplotlib.pyplot as plt
      import numpy as np
      from sklearn.model_selection import StratifiedKFold
      from sklearn.preprocessing import StandardScaler
      from itertools import cycle
      from sklearn.model_selection import train_test_split
[38]: # let's compare a handful of Classifiers
      from sklearn.neural network import MLPClassifier
      from sklearn.neighbors import KNeighborsClassifier
      from sklearn.svm import SVC
      from sklearn.gaussian_process import GaussianProcessClassifier
      from sklearn.gaussian_process.kernels import RBF
      from sklearn.tree import DecisionTreeClassifier
      from sklearn.ensemble import RandomForestClassifier, AdaBoostClassifier
      from sklearn.naive_bayes import GaussianNB
      from sklearn.discriminant_analysis import QuadraticDiscriminantAnalysis
[39]: url = 'https://archive.ics.uci.edu/ml/machine-learning-databases/
       ⇔breast-cancer-wisconsin/wdbc.data'
      df = pd.read csv(url, header=None)
[40]: X = df.loc[:, 2:].values
      y = df.loc[:, 1].values
[41]: le = LabelEncoder()
      y = le.fit_transform(y)
[42]: sc = StandardScaler()
      sc.fit(X) # fit the whole data to calculate mean and standard deviation
      X_sc = sc.transform(X) # transform training set
[43]: names = ["KNN", "Linear SVM", "RBF SVM", "Gaussian Process",
               "Decision Tree", "Random Forest", "Neural Net", "AdaBoost",
               "Naive Bayes", "QDA", 'Logistic Reg']
      classifiers = [
          KNeighborsClassifier(2),
          SVC(kernel="linear", C=0.025),
          SVC(gamma=2, C=1),
          GaussianProcessClassifier(),
          DecisionTreeClassifier(),
          RandomForestClassifier(),
```

```
MLPClassifier(),
          AdaBoostClassifier(),
          GaussianNB(),
          QuadraticDiscriminantAnalysis(),
          LogisticRegression(random_state=1, solver='lbfgs')
      ]
      mean fpr = np.linspace(0, 1, 100)
      #cv = StratifiedKFold(n_splits=5) # just to 5 fold
[45]: # let's plot the ROC Curves for all the classifiers
      fig, ax = plt.subplots(figsize=(10, 6))
      lw=2
      X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=.2,
                                                      random_state=0)
      for name, classifier in zip(names, classifiers):
          classifier.fit(X_train, y_train)
          RocCurveDisplay.from_estimator(classifier, X_test, y_test,
                               name=f'{name}',
                               alpha=0.3, lw=1, ax=ax)
      ax.set(xlim=[-0.05, 1.05], ylim=[-0.05, 1.05], title="ROC Curve Example")
      ax.legend(loc="lower right")
      plt.title("ROC Curves of Classifiers")
      plt.xlabel('False Positive Rate')
      plt.ylabel('True Positive Rate')
     plt.legend(loc="lower right")
     plt.show()
     /usr/local/lib/python3.12/site-
     packages/sklearn/ensemble/_weight_boosting.py:519: FutureWarning: The SAMME.R
     algorithm (the default) is deprecated and will be removed in 1.6. Use the SAMME
     algorithm to circumvent this warning.
       warnings.warn(
     /usr/local/lib/python3.12/site-packages/sklearn/linear_model/_logistic.py:469:
     ConvergenceWarning: lbfgs failed to converge (status=1):
     STOP: TOTAL NO. of ITERATIONS REACHED LIMIT.
     Increase the number of iterations (max_iter) or scale the data as shown in:
         https://scikit-learn.org/stable/modules/preprocessing.html
     Please also refer to the documentation for alternative solver options:
         https://scikit-learn.org/stable/modules/linear_model.html#logistic-
       n_iter_i = _check_optimize_result(
```

