

STAT4355HW5

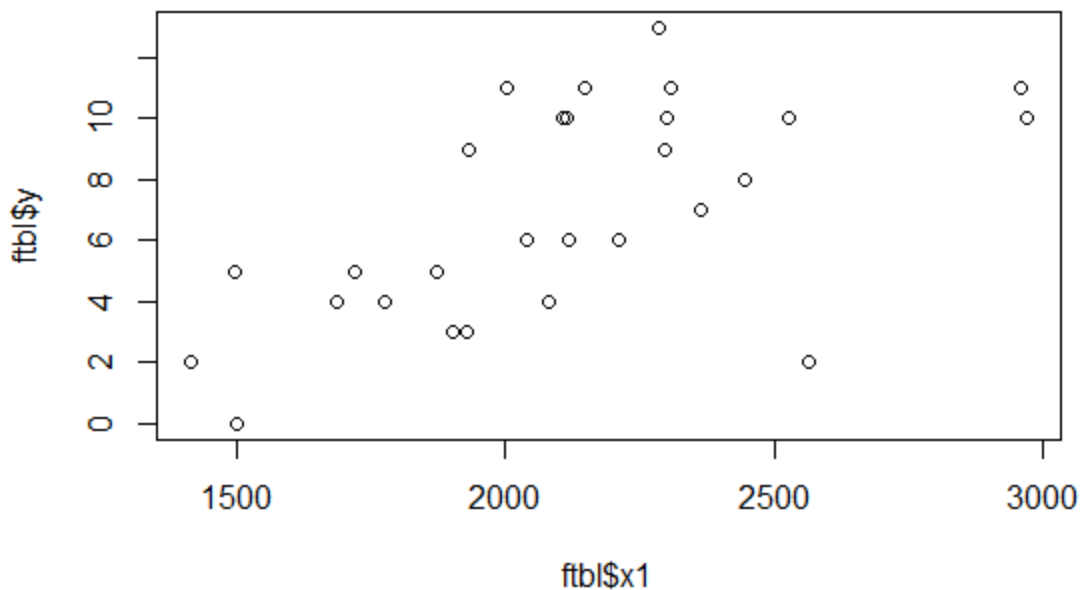
[Code ▾](#)

This is an R script with the purpose of running multiple linear regression on football data

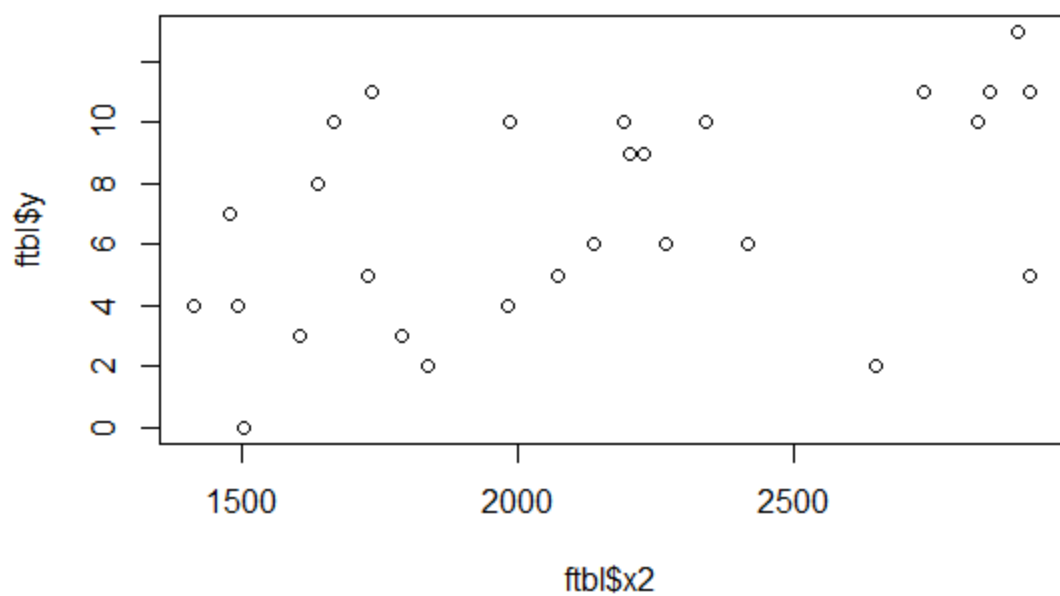
(a)

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```
#load the data
ftbl <- read.csv(file = 'football.csv')
#9 scatterplots for number of games won (y) against other vars
plot(ftbl$x1, ftbl$y)
```

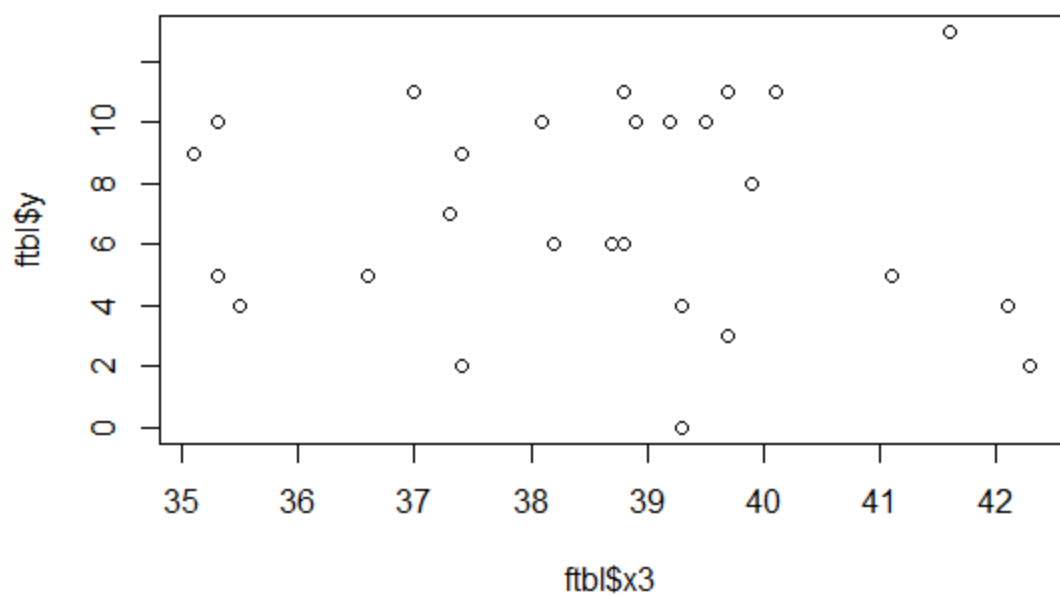
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```
plot(ftbl$x2, ftbl$y)
```



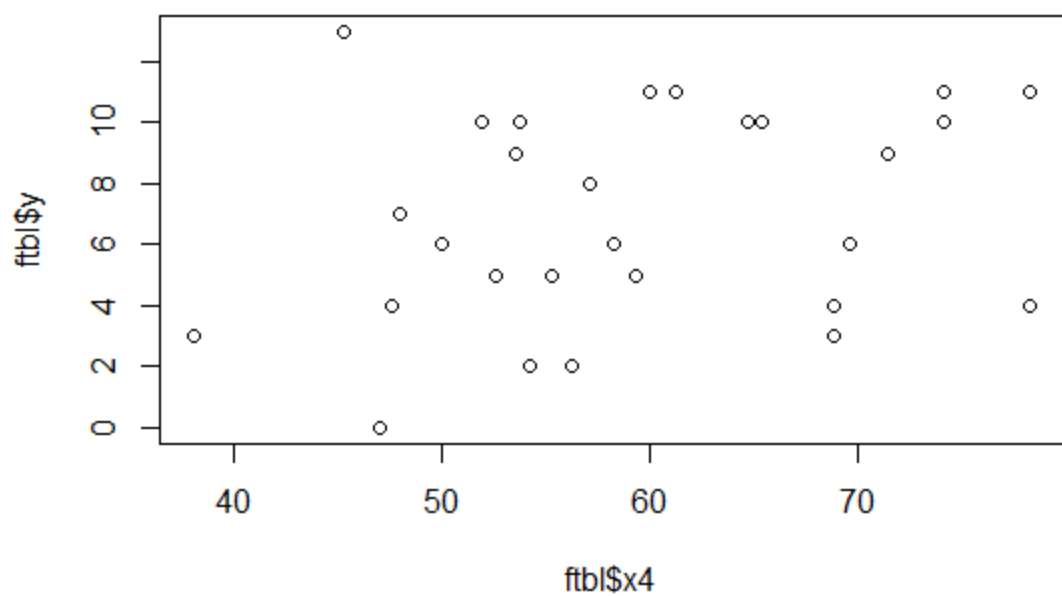
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```
plot(ftbl$x3, ftbl$y)
```



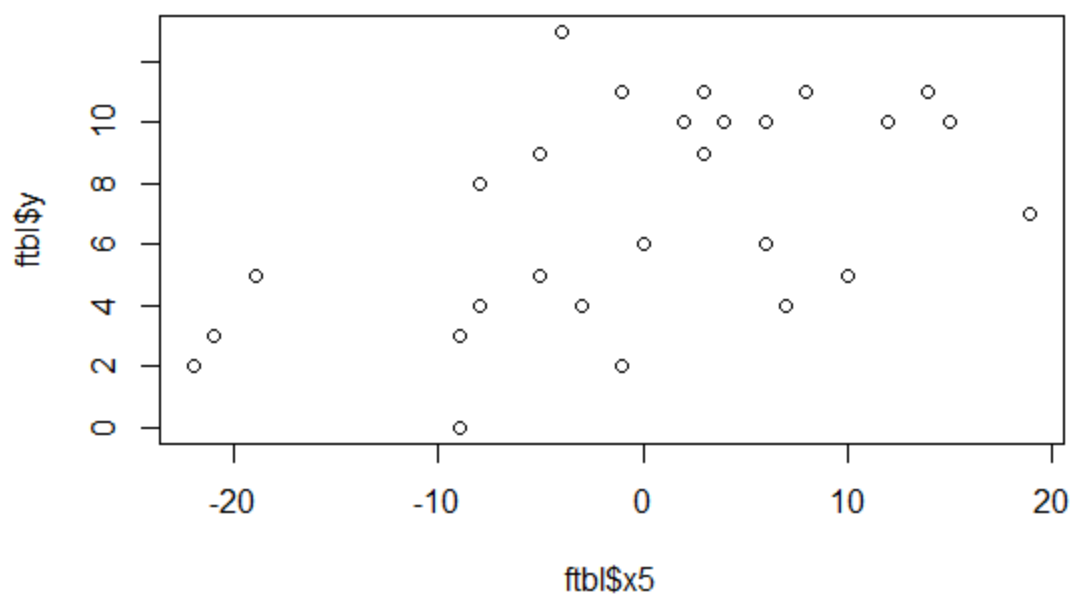
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```
plot(ftbl$x4, ftbl$y)
```



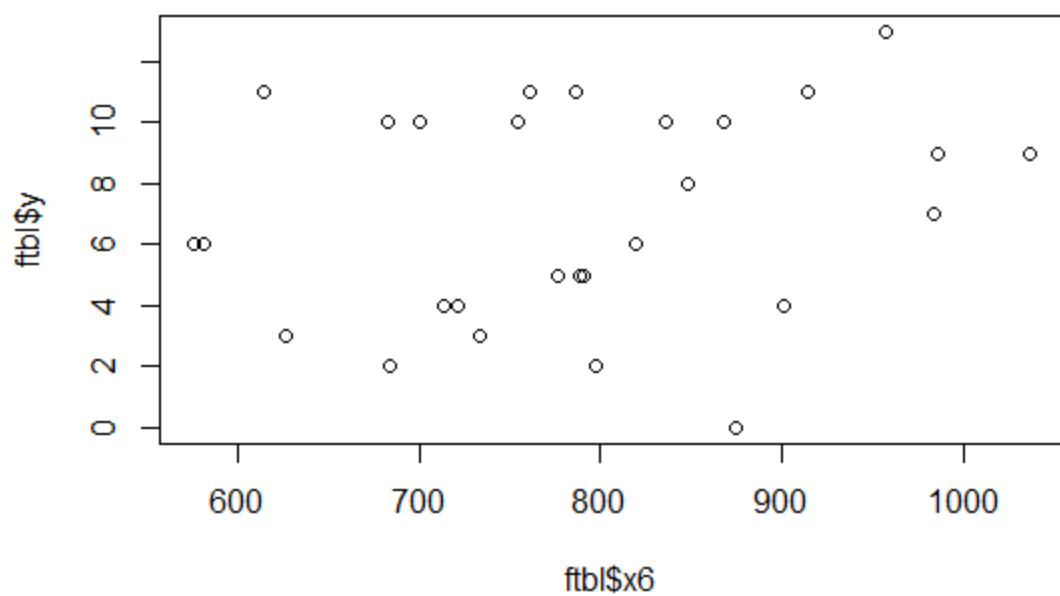
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```
plot(ftbl$x5, ftbl$y)
```



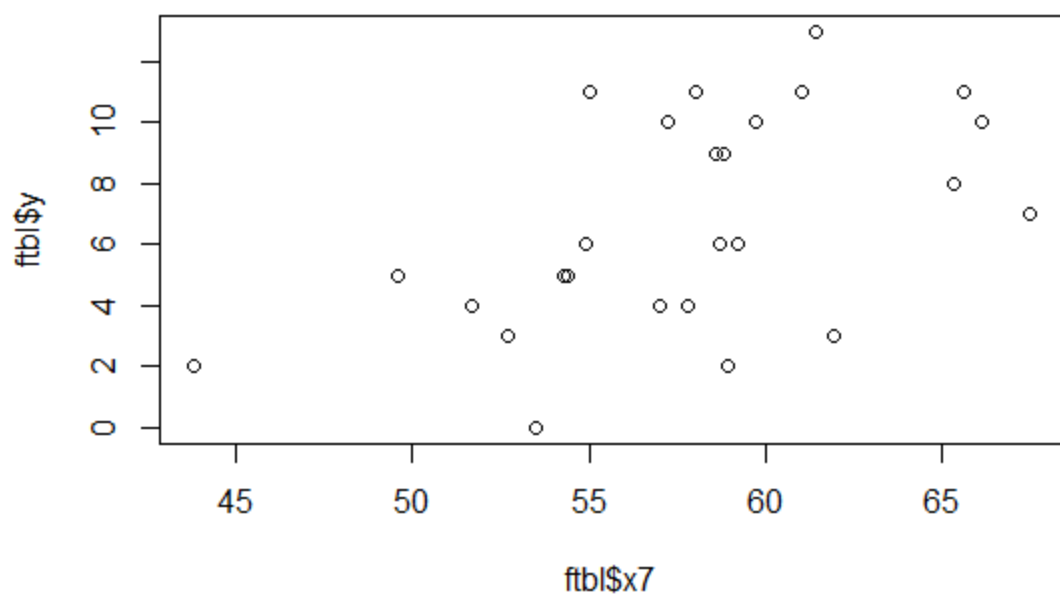
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```
plot(ftbl$x6, ftbl$y)
```



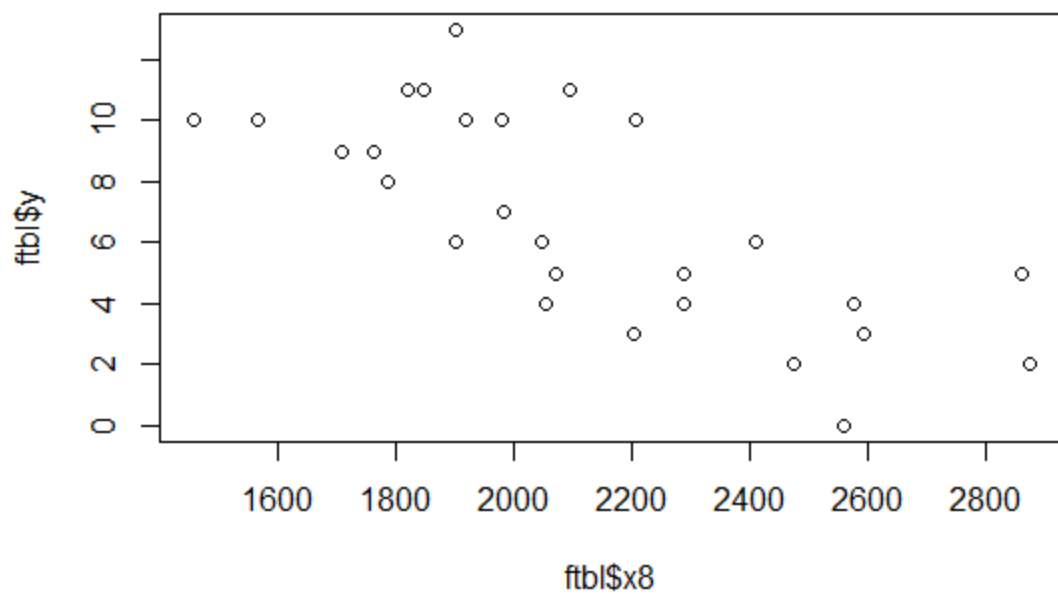
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```
plot(ftbl$x7, ftbl$y)
```



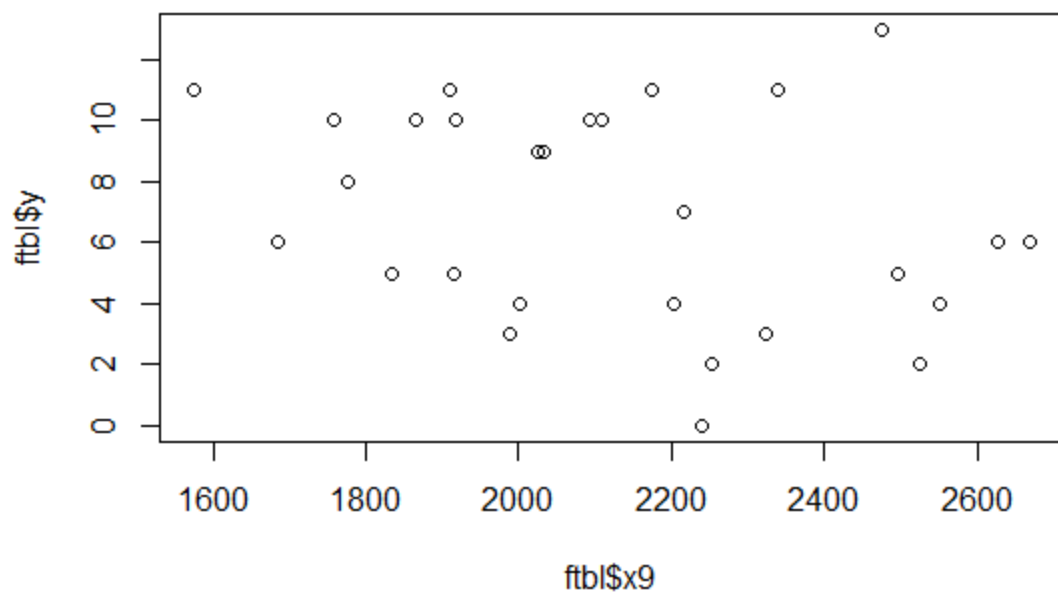
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```
plot(ftbl$x8, ftbl$y)
```



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```
plot(ftbl$x9, ftbl$y)
```



(b)

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```
#build model with most associated vars
lm1 <- lm(y~x1+x2+x5+x7+x8, data = ftbl)
#model summary
summary(lm1)
```

```
Call:
lm(formula = y ~ x1 + x2 + x5 + x7 + x8, data = ftbl)

Residuals:
    Min       1Q   Median       3Q      Max
-2.7152 -0.6710 -0.2079  1.2287  3.7252

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -0.0516532   9.0751149  -0.006  0.995510
x1           0.0008480   0.0017008   0.499  0.623008
x2           0.0034689   0.0007673   4.521  0.000169 ***
x5           0.0103765   0.0440046   0.236  0.815766
x7           0.1336928   0.1375471   0.972  0.341628
x8          -0.0047048   0.0013412  -3.508  0.001986 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.768 on 22 degrees of freedom
Multiple R-squared:  0.7896,    Adjusted R-squared:  0.7418
F-statistic: 16.51 on 5 and 22 DF,  p-value: 8.363e-07
```

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sigma(lm1)^2

[1] 3.126997

Fitted linear model:

$y\text{-hat} = -0.0516532 + 0.0008480x_1 + 0.0034689x_2 + 0.0103765x_5 + 0.1336928x_7 + -0.0047048x_8$

- i. $(\sigma)^2 = 3.126997$
- ii. $R^2 = 0.7896$
- iii. adjusted $R^2 = 0.7418$

(c)

β^1 : For a one unit increase in rushing yardage, number of games won is associated with a 0.0008480 increase on average.

β^2 : For a one unit increase in passing yardage, number of games won is associated with a 0.0034689 increase on average.

β^5 : For a one unit increase in turnover differential, number of games won is associated with a 0.0103765 increase on average.

β^7 : For a one unit increase in percentage of rushing plays, number of games won is associated with a 0.1336928 increase on average.

β^8 : For a one unit increase in opponents' rushing yardage, number of games won is associated with a 0.0047048 decrease on average.

$(\sigma)^2$: The model on average has a squared error of 3.126997.

(d)

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```
#anova from pg.46
fit <- lm(y~x1+x2, data=ftbl)
anova(fit)
```

Analysis of Variance Table

Response: y

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
x1	1	115.068	115.068	22.378	7.492e-05 ***
x2	1	83.343	83.343	16.208	0.0004635 ***
Residuals	25	128.553	5.142		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

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#Source of Variation	SS	DF	MS	F0
#Regression	198.41	2	99.205	19.2926
#Residual	128.553	25	5.14212	
#Total	326.963	27		

ANOVA Table commented in code above^

(e)

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```
#anova from pg.47
fit0<-lm(y~1, data=ftbl)
anova(fit0, fit)
```

Analysis of Variance Table

Model 1: y ~ 1

Model 2: y ~ x1 + x2

	Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
1	27	326.96				
2	25	128.55	2	198.41	19.293	8.556e-06 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

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#Source of Variation	SS	DF	MS	F0
#Regression	198.41	2	99.205	19.293
#Residual	128.55	25	5.142	
#Total	326.96	27		

ANOVA Table commented in code above^

(f)

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```
# test for significance of regression at significance level of 0.05
qf(0.05, 2, 25, lower.tail=FALSE)
```

```
[1] 3.38519
```

The two ANOVA tables are the same.

(g)

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```
#Test the value of passing yardage given all the other 4 predictors at significance level of 0.05
reduced <- lm(y~x1+x5+x7+x8, data = ftbl)
anova(reduced, lm1)
```

Analysis of Variance Table

Model 1: $y \sim x1 + x5 + x7 + x8$

Model 2: $y \sim x1 + x2 + x5 + x7 + x8$

	Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
1	23	132.703				
2	22	68.794	1	63.909	20.438	0.000169 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

i.

H0: $\beta^2 = 0$

H1: $\beta^2 \neq 0$

ii. F-distribution

iii. $F = 20.438$

p-value = 0.000169

p-value is very small, much less than .05 and F is quite large; we do reject the null hypothesis and conclude that x2, passing yardage, is a significant contributor.

(h)

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```
#investigate the contribution of the 3 predictors
reduced1 <- lm(y~x2+x8, data = ftbl)
anova(reduced1, lm1)
```

Analysis of Variance Table

Model 1: $y \sim x2 + x8$

Model 2: $y \sim x1 + x2 + x5 + x7 + x8$

	Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
1	25	83.938				
2	22	68.794	3	15.144	1.6144	0.2147

i.

$H_0: \beta^1 = 0, \beta^5 = 0, \beta^7 = 0$

$H_1: \beta^1 \neq 0, \beta^5 \neq 0, \beta^7 \neq 0$

ii. F-distribution

iii.

$F = 1.6144$

$p\text{-value} = 0.2147$

$p\text{-value}$ is not less than .05 and F is quite small; we do not reject the null hypothesis and conclude that x_1 , x_5 , and x_7 are not significant contributors.

(i)

I prefer the reduced model with predictors x_2 and x_8 as it has a higher RSS and is more significant.

(j)

R code is within this notebook pdf