

Assignment 2:

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1. And, OR operators:

In the fuzzy logic, elements belong to a set with a certain probability. Meaning that its membership is a value of $0 \le x \le 1$ equivalent to truth variables with a membership value $0 \le y \le 1$. The <u>AND</u> operator denotes the minimum of two actual values, And the <u>OR</u> operator denotes the maximum of two actual values. For example :

If:
$$F(Y = 1) = 0.5$$
, $F(Y = 2) = 0.4$) then:
(OR) $Y = 1 \ \forall \ Y = 2 = \max(0.5, 0.4) = 0.5$
(AND) $Y = 1 \ \land \ Y = 2 = \min(0.5, 0.4) = 0.4$

2. Example:

values as (0.3, 0.8, 0.2, 0.7)

a. Compute the membership degree (short, medium, and long) foreach input:

Short
$$(0.3) = -0.3/0.6+1 = 0.5$$

Medium $(0.3) = 0.3/0.6 = 0.5$
Long $(0.8) = 0$

Short
$$(0.8) = 0$$

Medium $(0.8) = -0.8/0.4+2.5 = 0.5$
Long $(0.8) = 0.8/0.4 - 1.5 = 0.5$

Short
$$(0.2) = -0.2/0.6+1 = 0.66$$

Medium $(0.2) = 0.2/0.6 = 0.33$
Long $(0.2) = 0$

Short
$$(0.7) = 0$$

Medium $(0.7) = -0.7/0.4 + 2.5 = 0.75$

Long
$$(0.7) = 0.7/0.4 - 1.5 = 0.25$$

b. Calculate firing strengths of rules:

Rule1: If (x1=short long) and (x2=medium long) and (x3=medium long) and (x4=medium) Then iris **versicolor**

Fuzzy Rule 1:

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min(max(short(x1), long(x1)), max(medium(x2), long(x2)), max(medium(x3), long(x3)), medium(x4))
= min(max(0.5,0), max(0.5,0.5), max(0.5,0.5), max(0.33, 0), 0.75)
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= \min(0.5, 0.5, 0.5, 0.33, 0.75)
= 0.33
Rule 2: If (x3=short medium) and (x4=short) Then iris setosa
Fuzzy Rule 2:
min(max(short(x3), medium(x3)), short(x4))
=min( max(0.66, 0.33), 0)
=min(0.66, 0)
=()
Rule 3: If (x2=short medium) and (x3=long) and (x4=long) Then iris
virginica
min(max(short(x2), medium(x2)), long(x3), long(x4))
=min( max(0, 0.5), 0, 0.25)
=min(0.5, 0, 0.25)
=0
Rule 4: If (x1=medium) and (x2=short medium) and (x3=short) and
(x4=long) Then iris versicolor
min(medium(x1), max(short(x2), mediu(x2)), short(x3), long(x4))
=min(0.5, max(0, 0.5), 0.66, 0.25)
=\min(0.5, 0.5, 0.66, 0.25)
=0.25
Probability versicolor = max(0.33, 0.25) = 0.25
Probability setosa = 0
Probability virginica = 0
Regarding the probability we figure out the iris will be versicolor because it
is the maximum probability and the other probability it is equal zero.
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3. Accuracy:

The classifier has an accuracy of 77%.