Small Review

ECE 2200:

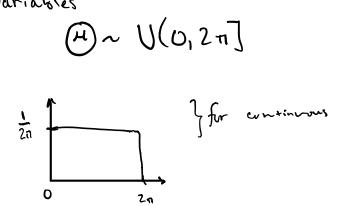
$$\frac{\chi(t)}{\chi(t)} = \frac{\chi(t)}{\chi(t)} \chi(t) + h(t)$$

$$\chi = \chi(\omega) H(\omega)$$

ECE 3100

Random variables

pdf



Combined ??? :!!  $X(t) = a \cos(\omega_c t + \omega)$ Phose shift is randomly distributed

## Review of Basic Probability

## Probability Space

Example of Random Experiments

R (1) flip a fair coin twice

R 2 throw a die

R 3 take ECE4110 runtil you pass

R 4 throw a dort to unit disk

Possible OUTCOMES

RI: HT, HH, TH, TT

RZ: 1,2,3,4,5,6

RS: Pass, fail

Ru: {z2+y2<1: -1<x21, -1<y1}

Events: a subset of outcomes

Probability Space

Space probability measure (12, F, Pr)

Sample space collection of events I want to assign probabilities to level of resolution we observe our random experiment at

All events CIL

F example: For RZ, even orad?

F = { 0, so, {1,353, {2,4,63}}

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Axions

(i) 2 E F

(ii) If AEF, ACEF

(iii) If A; E7 U A: E7

e countable inter also Hare! AnB = (ACUBC) [

only require a countable union to belong to f

F → [0,1]

(i) 0 = Pr(A) = 1

(ii) Pr(2)=1

if one event occurs the other events do not

(iii) If A, Az..., is a sequence of mutually exclusive events then  $Pr(VAi) = \sum_{i} Pr(Ai)$ 

Properties that Follow

(i) Pr(Ac) = 1- Pr(A)

Proof: Pr(AUAC) = Pr(A) + Pr(AC)

Pr(A) = 1= Pr(A) + Pr(A)

Pr(A4) = 1 - Pr(A)

(iii) If A = B then P-(A) = Pr(B)

Proof: B= AU (A'nB)

Pr(B) = Pr(A) + Pr(A'NB) > Pr(A)

(iv) Pr(AUB) = Pr(A)-Pr(B)-Pr(AnB)

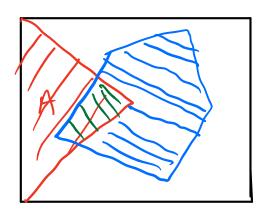
Union Bound  $Pr(YAi) < \sum_{i=1}^{n} Pr(Ai)$ 

## Conditional Probability

If A and B are two events, Pr(B) +0, then

$$P_{c}(A|B) = \frac{P_{c}(A\cap B)}{P_{c}(B)}$$

"B becomes the new universe, B=12"



Paradox of Two Children

I have two children.

- (i) one of them is a buy
- (ii) one of them is a boy who was born on Wednesday

Pr(both are boys)?

(i) 
$$Pr(BB \mid (B,B),(B,G)) = \frac{Pr(BB)}{Pr(BB,BG)} = \frac{Pr(BB)}{Pr(BB) + Pr(BG)} = \frac{\frac{1}{4} + \frac{2}{4}}{\frac{1}{4} + \frac{2}{4}} = \frac{1}{3}$$

(ii) B\* = boy bon Wedresday, B= boy born NOT on Wednesday

$$P_{r}(B^{*}B^{*}\cup B^{*}B) = \frac{P_{r}(B^{*}B^{*}) + P_{r}(B^{*}B)}{P_{r}(B^{*}B^{*}) + P_{r}(B^{*}B) + P_{r}(B^{*}B)}$$

$$= \frac{1}{14} \cdot \frac{1}{14} \cdot 2 \frac{1}{14} \cdot \frac{6}{14}$$

$$= \frac{1}{14} \cdot \frac{1}{14^{2}} + 2 \frac{1}{14^{2}} + 2 \frac{1}{14} \cdot \frac{1}{2}$$

$$= \frac{13}{13}$$