Rn, vectors, span, linear dependence, bases, din T: Rn > Rn (linear transformations), Gaussian elimination kernel/image/null-space/rang=, eigenvalues, symmetric matrices

We will cover:

You should know:

- fields (scalars) : IR, O, finite fields
- · vector spaces
- linear transformations
- Lim, bases of vector spaces
- elgenvalues + eigenvectors ~10 determinants
- -polynomials
- inner product spaces (least squares)
 Spectral theorem
 Singular value decompositions
- Structure of linear operators (square matrices)

 Tordar canonical form

 Cayley Hamilton Theorem

Le+

$$A = \begin{bmatrix} 1 & 3 & 5 \\ -2 & -8 & 2 \end{bmatrix}$$

$$correct (A) = ?$$

$$\begin{bmatrix}
0 & 3 & 5 \\
-2 & -8 & 2
\end{bmatrix}
\xrightarrow{R_1 + 2R_1}
\begin{bmatrix}
1 & 3 & 5 \\
0 & -2 & 12
\end{bmatrix}
\xrightarrow{R_2 / 2 - 2}
\begin{bmatrix}
1 & 3 & 5 \\
0 & 0 - 6
\end{bmatrix}
\xrightarrow{R_1 - 3R_2}
\begin{bmatrix}
1 & 0 & 23 \\
0 & 1 & -6
\end{bmatrix}$$

what scalar operations did we use?

Addition (+)

Multiplication (.)

Division (1)

Subtraction (-)

also identify 0,1?

Definition (appendix C of FIS): A field is a set IF equipped with the following

- @ Two special elemens 071 in 15
- 6 operation addition (+): IFXIF -> IF (a, b) atb
- @ operation multiplication (.) IF XIF -> IF (a, b) a.b (or ab)

(IF, 0, 1, +, .) must satisfy the following properties (axioms)

- (F) Commutativity of 't', '. ' + a, b & IF [a+b=b+a], [a-b=b-a]
- (FZ) Associativity of 't', '.': Ya,b,cEIF (a+(b+c) = (a+b)+c) (a-(bc) = (ab)-c)
- (F3) Existence of identity elements of 't', 1.1: takit, Tota=a, [1.a=a]
- (FY) Existence of inverses: Y arif, Ybtorif, I cidelf 1.2 [atc=0], [b.d=1]
- (F5) Distributivity: Y a, b, c & F a · (b+c) = a · b + a · c