

If we can find an rel s.E. the circle on the z-plane maps to the given physical circle in the w-plane.

We want diameter = distance from z to edge

$$\frac{1}{1-r} - \frac{1}{1+r} - \frac{1}{2}$$

$$\Rightarrow r^{2} - 6r + 1 = 0$$

$$r = \frac{6 \pm \sqrt{32}}{2} = \frac{3 \pm 2 - \sqrt{2}}{2}$$

only want rel, so

We can simplify further by shifting circle to the origin.

Let t = 2 - 1, $t \in \mathbb{I}$ t-plane |t| = 1 $|t| = r_0$ $|t| = r_0$

$$\phi = c_1 \log(c_2 R), \quad R = 1 \pm 1$$

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$$\log(c_2) = 0$$

$$c_2 = 1$$

$$1 = c_1 \log(1 \cdot r_0)$$

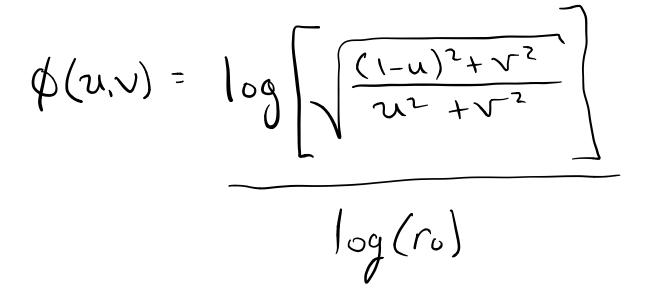
$$c_1 = \frac{1}{\log(r_0)}$$

$$\phi = \frac{\log(R)}{\log(r_0)} = \frac{\log(1t1)}{\log(r_0)}$$

$$= \frac{\log(12-11)}{\log(r_0)} = \frac{\ln(1\frac{1}{w}-11)}{\log(r_0)}$$

$$w = u + i$$

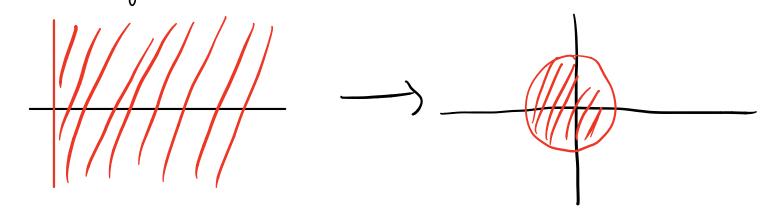
$$\left|\frac{1}{u+iv}-1\right| = \left|\frac{(1-u)-iv}{u+iv}\right| = \sqrt{\frac{(1-u)^2+v^2}{u^2+v^2}}$$



Mobius Transforms

O: Find a conformal map from the right half-plane into the unit dis k.

So the imaginary axis maps to a unique circle.



Solution: convert to a 1/2 problem.

we can translate the first one and second one X++

$$\frac{1}{x+\frac{1}{2}} + 1 \rightarrow \frac{1-2x}{1+2x}$$

$$f(z) = \frac{az+b}{cz+d}, \quad ad-bc \neq 0$$