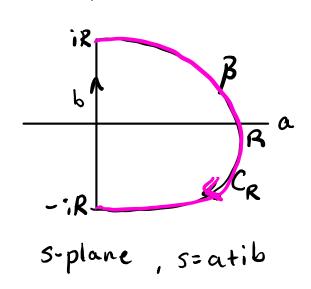
We want to find $s \in G$ which solves f(s) = 0, where f(s) is given by

Too Ambitious.

Instead, settle for finding conditions on R. T st. Re(s)(0) for all zeros of f(s)

Stability condition.



For stability we want no zeros of f(s) inside B (as R->00)

By the argument principle, this holds if W(T; 0) = 0where $T = f(\beta)$

First ask what does f(CR) look like?

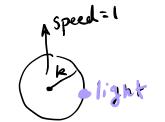
on Gr

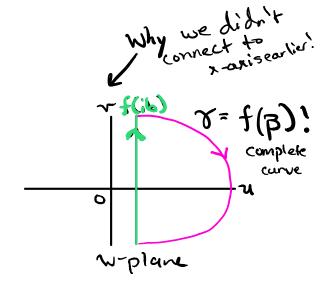
We're thinking of arbitrarily large R. Oscillates Reid + Ke-TRCOSD (= ; TR sin(0) like crazy w) negligible -> 0 as R-> 0 amplitude " So the image of the semicircle is another big semicircle. a part of 7=f(3)the part of 5-plane w-plane doesn't f(s) = Reid, Rs>1 for reasons below Need to map imaginary axis as Well. * Look at f(ib) as b runs from -R to R * f(ib)= ib+ ke-ibT = k cos(Tb) + i (b-ksin(Tb)) w plane is utiv! What does the curve (u(b), v(b)) look like? "Think of b (the parameter in the parametric equations for a curve) as a kind of time.

$$U(b) = k\cos(\tau b)$$

$$V(b) = -k\sin(\tau b) + b$$
Circular motion + vertical
translation
frequency τ
radius k
upward "peed"
of 1

f(ib) = path traced by moving lighthulb.

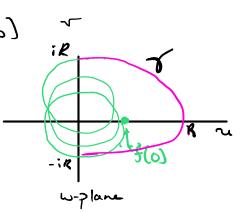




W(T;0) = 0 here, so no Zeros of sin right half plane → control system Stable (as expected, since no delay)

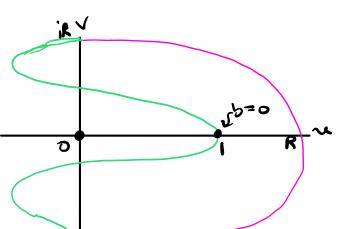
If
$$T$$
 large,
 $u(b) = k\cos(Tb)$, $-R \leq b \leq R$; $R \rightarrow \infty$
 $v(b) = -k\sin(Tb) + b$

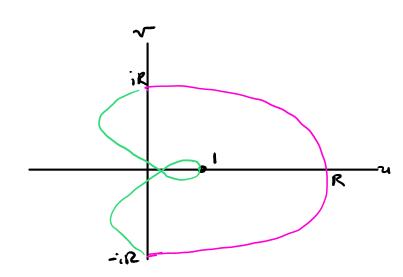
when b=0, f(ib)=k=u(b)+iv(b)as b in creases the center of our circle changes. i.c we encircle the origin many times — \Rightarrow wickidly unstable



For small T > U, (U.1)

(k=1)

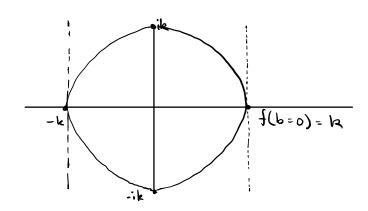




Slightly larger (T=1.3)

What's the critical point?

The critical case is when the lowest point due to circular motion is the same as the vertical distance troubled by translation.



 $C_{c} = \frac{\pi}{2k}$