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```
%%Author : R.U. Hettiarachchi %%  
%%Index : 170221T %%
```

Given Design Parameters :

```
A_p_tilde = 0.05; %Max Passband Ripple  
A_a_tilde = 47; %Min stopband attenuation  
Omega_p1 = 500;  
Omega_p2 = 1050;  
Omega_a1 = 600;  
Omega_a2 = 900;  
Omega_s = 2800;  
T = 2*pi/Omega_s;
```

Calculating Realistic Specs :

```
B_t1 = Omega_a1 - Omega_p1;  
B_t2 = Omega_p2 - Omega_a2;  
  
B_t = min(B_t1,B_t2)  
Omega_c1 = Omega_p1 + B_t/2  
Omega_c2 = Omega_p2 - B_t/2
```

Calculating Kaiser Parameters %%

```
delta_p_tilde = (10^(0.05*A_p_tilde)-1)/(10^(0.05*A_p_tilde)+1)  
delta_a_tilde = 10^(-0.05*A_a_tilde)  
  
delta = min(delta_p_tilde,delta_a_tilde)  
  
A_a = -20*log10(delta) %Actual Stopband Loss  
A_p = 20*log10((1+delta)/(1-delta)) %Actual Passband Ripple  
  
% -> Find alpha  
alpha = 0;
```

```

if (A_a >21 && A_a <= 50) alpha = 0.5842*(A_a-21)^0.4 +
    0.07886*(A_a-21); else alpha = 0.1102*(A_a-8.7); end

% -> Find D
D = 0.9222;
if(A_a > 21) D = (A_a - 7.95)/14.36; end

% -> Find N
N = (Omega_s*D)/B_t+1;
N = ceil(N) + mod(ceil(N)-1,2) %smallest odd integer satisfying the
    inequality

```

Construct Kaiser Window

```

n = -(N-1)/2 : 1 : (N-1)/2;
w = my_kaiser(N,alpha);

figure;
stem(n,w);
xlabel('n');
ylabel('w[n]');
axis([- (N-1)/2 (N-1)/2 0 1 ])
title('Window Function');
grid on;
saveas(gcf,'window','eps')

```

Construct Impulse Response of the Ideal Filter

```

h = (1./(n*pi)).*(sin(Omega_c1*n*T) - sin(Omega_c2*n*T));
h((N-1)/2+1) = 1 + (2/Omega_s)*(Omega_c1 - Omega_c2) ;
n = 0 : (N-1); %shifting by (N-1)/2

```

Causal Impulse Response of the Filter

```

close all;
h_w = h.*w.';

figure;
stem(n,h_w);
xlabel('nT');
ylabel('h_w[n]');
axis([0 (N-1) -0.15 0.75 ])
title('Causal Impulse Response');
grid on;
saveas(gcf,'cir','eps')

```

Magnitude response of the digital filter & Passbands zoomed in

```

freqz(h_w);

```

```

[z,w] = freqz(h_w);
w = w./T;

figure;
plot(w,20*log10(abs(z)))
grid on;
axis([0 1400 20*log10(0) 20*log10(1.1) ])
xlabel('Frequency rad/s');
ylabel('Magnitude (dB)');
title('Magnitude response of the digital filter');
saveas(gcf,'magnitude response of filter','epsc')

figure;
plot(w,20*log10(abs(z)))
grid on;
axis([200 550 20*log10(0.98) 20*log10(1.005) ])
xlabel('Frequency rad/s');
ylabel('Magnitude (dB)');
title('Magnitude response - Lower Passband');
saveas(gcf,'upper passband','epsc')

figure;
plot(w,20*log10(abs(z)))
grid on;
axis([1000 1400 20*log10(0.98) 20*log10(1.005) ])
xlabel('Frequency rad/s');
ylabel('Magnitude (dB)');
title('Magnitude response - Upper Passband');
saveas(gcf,'lower passband','epsc')

```

Input Signal

Freq components,

```

Omega1 = Omega_c1/2;
Omega2 = Omega_c1 + (Omega_c2-Omega_c1)/2;
Omega3 = Omega_c2 + (Omega_s/2-Omega_c2)/2;

% Generate the Input signal

samples = 300; % Enough to achieve a steady-state response.
n1 = 0:1:samples;
n2 = 0:0.1:samples;

x      = cos(Omega1.*n1*T) + cos(Omega2.*n1*T) + cos(Omega3.*n1*T);
X_env  = cos(Omega1.*n2*T) + cos(Omega2.*n2*T) + cos(Omega3.*n2*T);

R = cos(Omega1.*n1*T) + cos(Omega3.*n1*T);

stem(n1(1:100),x(1:100))
xlabel('n')

```

```

ylabel('Amplitude')
title(strcat(['Input signal x[n]', ' ', '- Time Domain']));
hold on
plot(n2(1:1000),X_env(1:1000),'-.')
legend('Input signal','Input Signal Continuous Time Shape');

figure;
L = length(x);
NFFT = 2^nextpow2(L); % Next power of 2 from length of y
Y = fft(x,NFFT)/L;
f = Omega_s/(2)*linspace(0,1,NFFT/2+1);

% Plot single-sided amplitude spectrum.
plot(f,2*abs(Y(1:NFFT/2+1)))
title('Single-Sided Amplitude Spectrum of x(nT)')
xlabel('Frequency (rad/s)')
ylabel('|X(w)|')
saveas(gcf,'Xw','epsc')

figure
L=1400;
X = fft(x,L);
H_w = fft(h_w,L);
filtered = ifft(X.*H_w);
stem(filtered(1:100));
grid on;
title('Filtered Input Signal x(nT)')
saveas(gcf,'Xw','epsc')

figure
plot(filtered(42:42+85))
hold on
out = conv(h_w,x,'same'); %% 'same' is there to crop the filtered
    signal
plot(out(4:85))
title('Filtered Input Signal Using conv()')

figure;
L = length(out);
NFFT = 2^nextpow2(L); % Next power of 2 from length of y
Y = fft(out,NFFT)/L;
f = Omega_s/(2)*linspace(0,1,NFFT/2+1);

plot(f,2*abs(Y(1:NFFT/2+1))) % Plot single-sided amplitude
    spectrum.
title('Single-Sided Amplitude Spectrum of the Filtered Signal')
xlabel('Frequency (rad/s)')
ylabel('|Y(f)|')

```

Expected Signal in the Freq domain

```
figure;
L = length(R);
NFFT = 2^nextpow2(L); % Next power of 2 from length of y
Y = fft(R,NFFT)/L;
f = Omega_s/(2)*linspace(0,1,NFFT/2+1);

plot(f,2*abs(Y(1:NFFT/2+1))) % Plot single-sided amplitude
    spectrum.
title('Single-Sided Amplitude Spectrum of the Expected Filtered
    Signal')
xlabel('Frequency (rad/s)')
ylabel('|Y(f)|')
saveas(gcf,'efs','epsc')
```

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