

## All Trigno Formulas

- $\sin(A+B) = \sin A \cdot \cos B + \cos A \cdot \sin B$
- $\sin(A-B) = \sin A \cdot \cos B - \cos A \cdot \sin B$
- $\cos(A+B) = \cos A \cdot \cos B - \sin A \cdot \sin B$
- $\cos(A-B) = \cos A \cdot \cos B + \sin A \cdot \sin B$
- $\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$
- $\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \cdot \tan B}$
- $\cot(A+B) = \frac{\cot B \cdot \cot A - 1}{\cot B + \cot A}$
- $\cot(A-B) = \frac{\cot B \cdot \cot A + 1}{\cot B - \cot A}$
- $\sin C + \sin D = 2 \sin\left(\frac{C+D}{2}\right) \cdot \cos\left(\frac{C-D}{2}\right)$
- $\sin C - \sin D = 2 \cos\left(\frac{C+D}{2}\right) \cdot \sin\left(\frac{C-D}{2}\right)$
- $\cos C + \cos D = 2 \cos\left(\frac{C+D}{2}\right) \cdot \cos\left(\frac{C-D}{2}\right)$
- $\cos C - \cos D = -2 \sin\left(\frac{C+D}{2}\right) \cdot \sin\left(\frac{C-D}{2}\right)$   
 $= 2 \sin\left(\frac{C+D}{2}\right) \cdot \sin\left(\frac{D-C}{2}\right)$



$$\sin 2x = 2 \sin x \cdot \cos x = \frac{2 \tan x}{1 + \tan^2 x}$$

$$\begin{aligned} \cos 2x &= \cos^2 x - \sin^2 x = 2 \cos^2 x - 1 \\ &= 1 - 2 \sin^2 x = \frac{1 - \tan^2 x}{1 + \tan^2 x} \end{aligned}$$

$$\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}$$

$$\sin 3x = 3 \sin x - 4 \sin^3 x$$

$$\cos 3x = 4 \cos^3 x - 3 \cos x$$

$$\tan 3x = \frac{3 \tan x - \tan^3 x}{1 - 3 \tan^2 x}$$

- odd  $F(x) \Rightarrow F(-x) = -F(x)$

- Even  $F(x) \Rightarrow F(-x) = +F(x)$

$$\cos(-x) = \cos x$$

$$\sin(-x) = -\sin x$$

$$\tan(-x) = -\tan x$$

$$\sec(-x) = \sec x$$

$$\csc(-x) = -\csc x$$

$$\cot(-x) = -\cot x$$



$$- 2 \sin A \cdot \cos B = \sin(A+B) + \sin(A-B)$$

$$\bullet 2 \cos A \cdot \sin B = \sin(A+B) - \sin(A-B)$$

$$\bullet 2 \cos A \cdot \cos B = \cos(A+B) + \cos(A-B)$$

$$\bullet -2 \sin A \cdot \sin B = \cos(A+B) - \cos(A-B)$$

$$\bullet \sin(A+B) \cdot \sin(A-B) = \sin^2 A - \sin^2 B$$

$$\bullet \cos(A+B) \cdot \cos(A-B) = \cos^2 A - \sin^2 B$$

$\sin^2 \theta + \cos^2 \theta = 1$	$1 + \cos 2x = 2 \cos^2 x$
$\sec^2 \theta - \tan^2 \theta = 1$	$1 - \cos 2x = 2 \sin^2 x$
$\operatorname{cosec}^2 \theta - \cot^2 \theta = 1$	$\tan x = \frac{1 - \cos 2x}{\sin x}$

### \* General Solution of Trigonometry

$$\bullet \sin x = 0 \Rightarrow x = n\pi$$

$$\sin x = \sin y \rightarrow x = nx + (-1)^n \cdot y$$

$$\bullet \cos x = 0 \rightarrow x = (2n+1) \frac{\pi}{2}$$

$$\cos x = \cos y \rightarrow x = 2nx \pm y$$

$$\bullet \tan x = 0 \rightarrow x = n\pi$$

$$\tan x = \tan y \rightarrow x = nx + y$$