

PRACTICAL EXERCISES: 30 PERIODS**Searching and Sorting Algorithms**

1. Implement Linear Search. Determine the time required to search for an element. Repeat the experiment for different values of n , the number of elements in the list to be searched and plot a graph of the time taken versus n .
2. Implement recursive Binary Search. Determine the time required to search an element. Repeat the experiment for different values of n , the number of elements in the list to be searched and plot a graph of the time taken versus n .
3. Given a text `txt [0...n-1]` and a pattern `pat [0...m-1]`, write a function `search (char pat [], char txt [])` that prints all occurrences of `pat []` in `txt []`. You may assume that $n > m$.
4. Sort a given set of elements using the Insertion sort and Heap sort methods and determine the time required to sort the elements. Repeat the experiment for different values of n , the number of elements in the list to be sorted and plot a graph of the time taken versus n .

Graph Algorithms

5. Develop a program to implement graph traversal using Breadth First Search
6. Develop a program to implement graph traversal using Depth First Search
7. From a given vertex in a weighted connected graph, develop a program to find the shortest paths to other vertices using Dijkstra's algorithm.
8. Find the minimum cost spanning tree of a given undirected graph using Prim's algorithm.
9. Implement Floyd's algorithm for the All-Pairs- Shortest-Paths problem.
10. Compute the transitive closure of a given directed graph using Warshall's algorithm.

Algorithm Design Techniques

11. Develop a program to find out the maximum and minimum numbers in a given list of n numbers using the divide and conquer technique.
12. Implement Merge sort and Quick sort methods to sort an array of elements and determine the time required to sort. Repeat the experiment for different values of n ,

the number of elements in the list to be sorted and plot a graph of the time taken versus n.

State Space Search Algorithms:

- 13. Implement N Queens problem using Backtracking. Approximation Algorithms
Randomized Algorithms
- 14. Implement any scheme to find the optimal solution for the Traveling Salesperson problem and then solve the same problem instance using any approximation algorithm and determine the error in the approximation.
- 15. Implement randomized algorithms for finding the kth smallest number.

The programs can be implemented in C/C++/JAVA/ Python.

Searching and Sorting Algorithms

1. Implement Linear Search. Determine the time required to search for an element. Repeat the experiment for different values of n , the number of elements in the list to be searched and plot a graph of the time taken versus n .

AIM:

To write a program for linear search algorithm.

ALGORITHM:

STEP1: Start

STEP2: Get the list elements from the user

STEP3: Set the target element.

STEP4: Select the first elements as the current element.

STEP5: Compare to current element with the target element

STEP6: If there is a next element, then set current element to next element and go to step2

STEP7: Target element not found, go to step9

STEP8: Target element found, return location & print the execution time

STEP9: Stop

PROGRAM:

```
# include<stdio.h>
# include<time.h>
int main()
{
    int arr[20], size, key, i, index;
    clock_t start, end;
    clrscr();
    start = clock();
    printf("Number of elements in the list: ");
    scanf("%d", &size);
    printf("Enter elements of the list: ");
    // loop for the input of elements from 0 to number of elements-1
    for (i = 0; i < size; i++)
        scanf("%d", &arr[i]);
    printf("Enter the element to search ie. key element: ");
    scanf("%d", &key);
    // loop for traversing the array from 0 to the number of elements-1
    for (index = 0; index < size; index++)
        if (arr[index] == key) // comparing each element with the key element
            break; // cursor out of the loop when a key element found

    if (index < size) // condition to check whether previous loop partially traversed or not
        printf("Key element found at index %d /n", index); // printing the index if key found
    else
        printf("Key element not found /n");
```

```
end = clock();
double execution_time = (((double)(end - start))/CLOCKS_PER_SEC);
printf("Time taken is %f",execution_time);
getch();
return 0;
}
```

OUTPUT:

```
Number of elements in list:5
Enter the element of the list
23
45
67
89
10
Enter the element to search ie: key element:10
Key element found at index 4
Time taken is 11.428571
```

RESULT:

Thus the program was executed successfully.

2. Implement recursive Binary Search. Determine the time required to search an element. Repeat the experiment for different values of n , the number of elements in the list to be searched and plot a graph of the time taken versus n .

AIM:

To write a program for binary search algorithm

ALGORITHM:

STEP1: Start .

STEP2:Get the list elements from the user.

STEP3:Set the target element.

STEP4:Find the middle element in the sorted list.

STEP5:If target & middle element are matched , then return the position & go to step9.

STEP6:If both are not matched ,then check whether the target element is smaller or larger than the middle element.

STEP7:If target is larger than middle element set $low = mid + 1$, then repeat the step4,5,6

STEP8:If target is larger than middle element set $high = mid - 1$, then repeat the step4,5,6

STEP6:Stop.

PROGRAM:

```
# include<stdio.h>
# include<time.h>
void binary_search(int [], int, int, int);
int main()
{
    int key, size, i;
    int list[25];
    clock_t start, end;
    clrscr();
    start = clock();
    printf("Enter size of a list: ");
    scanf("%d", &size);
    printf("Enter elements\n");
    for(i = 0; i < size; i++)
    {
        scanf("%d",&list[i]);
    }
    printf("Enter key to search\n");
    scanf("%d", &key);
    binary_search(list, 0, size, key);
    end = clock();
    double execution_time = (((double)(end - start))/CLOCKS_PER_SEC);
    printf("Time taken is %f",execution_time);
    getch();
    return 0;
}
void binary_search(int list[], int lo, int hi, int key)
{
```

```

int mid;
if (lo > hi)
{
    printf("Key not found\n");
    return;
}
mid = (lo + hi) / 2;
if (list[mid] == key)
{
    printf("Key found\n");
}
else if (list[mid] > key)
{
    binary_search(list, lo, mid - 1, key);
}
else if (list[mid] < key)
{
    binary_search(list, mid + 1, hi, key);
}
}

```

OUTPUT:

```

Enter size of a List:5
Enter elements
16
37
48
62
87
Enter key to search
62
Key found
The key element position is 4
Time taken is 25.000000_

```

RESULT:

Thus the program for executed successfully.

3. Given a text txt [0...n-1] and a pattern pat [0...m-1], write a function search (char pat [], char txt []) that prints all occurrences of pat [] in txt []. You may assume that n > m.

AIM:

To write a program for text and pattern search.

ALGORITHM:

STEP1: Start .

STEP2:Get the text from the user.

STEP3:Get the Pattern from the user

STEP4: Calculate the len of the text and the pattern given

STEP5: use for loop to find the pattern matching with the text.

STEP6: If any matching found print the result

PROGRAM:

```
#include <stdio.h>
#include <string.h>
void search(char* pat, char* txt)
{
    int M = strlen(pat);
    int N = strlen(txt);
    int i
    for ( i = 0; i <= N - M; i++)
    {
        int j;
        for (j = 0; j < M; j++)
            if (txt[i + j] != pat[j])
                break;
        if (j == M) // if pat[0...M-1] = txt[i, i+1, ...i+M-1]
            printf("Pattern found at index %d \n", i);
    }
}
int main()
{
    char txt[] = "AABAACAADAABAAABAA";
    char pat[] = "AABA";
    search(pat, txt);
    return 0;
}
```

OUTPUT:

```
pattern found at index 0  
pattern found at index 9  
pattern found at index 13
```

RESULT:

Thus the program was executed successfully.

4. Sort a given set of elements using the Insertion sort and Heap sort methods and determine the time required to sort the elements. Repeat the experiment for different values of n , the number of elements in the list to be sorted and plot a graph of the time taken versus n .

4(A) INSERTION SORT:

AIM:

To write program for insertion sort algorithm

ALGORITHM:

STEP1: Start

STEP2: Read number of array elements n

STEP3: Read array elements A_i

STEP4: Sort the elements using insertion sort

In pass p , move the element in position p left until its correct place is found among the first $p + 1$ elements.

Element at position p is saved in temp, and all larger elements (prior to position p) are moved one spot to the right. Then temp is placed in the correct spot.

STEP5: Stop

PROGRAM:

// INSERTION SORT

```
#include <stdio.h>
#include<time.h>
int main(void)
{
    clock_t start, end;
    start = clock();
    int n, i, j, temp;
    int arr[64];
    printf("Enter number of elements\n");
    scanf("%d", &n);
    printf("Enter %d integers\n", n);
    for (i = 0; i < n; i++)
    {
        scanf("%d", &arr[i]);
    }
    for (i = 1; i < n; i++)
    {
        j = i;
        while (j > 0 && arr[j - 1] > arr[j])
        {
            temp = arr[j];
```

```

        arr[j] = arr[j - 1];
        arr[j - 1] = temp;
        j--;
    }
}
printf("Sorted list in ascending order:\n");
for (i = 0; i < n; i++)
{
    printf("%d\n", arr[i]);
}
end = clock();
double execution_time = (((double)(end - start))/CLOCKS_PER_SEC);
printf("Time taken is  %f",execution_time);
}

```

OUTPUT:

```

Enter the number of elements 6
Enter 6 integers
67
89
10
34
120
12
Sorted list in ascending order :
10
12
34
67
89
120
Time taken is 45.329670_

```

RESULT:

Thus the program was executed successfully.

4(B) HEAP SORT:

AIM:

To write program for heap sort algorithm

ALGORITHM:

STEP1:Start.

STEP2:Construct a binary tree with given list of elements.

STEP3:Delete the root element from Min Heap using heapify method.

STEP4:Put the delete element into the Sorted list.

STEP5:Repeat the same until Min heap becomes empty.

STEP6:Display the sorted List.

STEP7:Stop.

PROGRAM:

//HEAP SORT

```
#include<stdio.h>
```

```
#include<conio.h>
```

```
int temp;
```

```
void heapify (int arr[], int size, int i)
```

```
{
```

```
int largest = i;
```

```
int left = 2*i + 1;
```

```
int right = 2*i + 2;
```

```
if (left < size && arr[left] >arr[largest])
```

```
largest = left;
```

```
if (right < size && arr[right] > arr[largest])
```

```
largest = right;
```

```
if (largest != i)
```

```

{
temp = arr[i];
arr[i]= arr[largest];
arr[largest] = temp;
heapify(arr, size, largest);
}

}
void heapSort(int arr[], int size)
{
int i;
for (i = size / 2 - 1; i >= 0; i--)
heapify(arr, size, i);
for (i=size-1; i>=0; i--)
{
temp = arr[0];
arr[0]= arr[i];
arr[i] = temp;
heapify(arr, i, 0);
}
}
void main()
{
int arr[] = { 1, 10, 2, 3, 4, 1, 2, 100,23, 2};
int i;
int size = sizeof(arr)/sizeof(arr[0]);
clock_t start, end;
clrscr();

```

```
start = clock();

heapSort(arr, size);

printf("Sorted Elements:");

for (i=0; i<size; ++i)

printf(" %d",arr[i]);

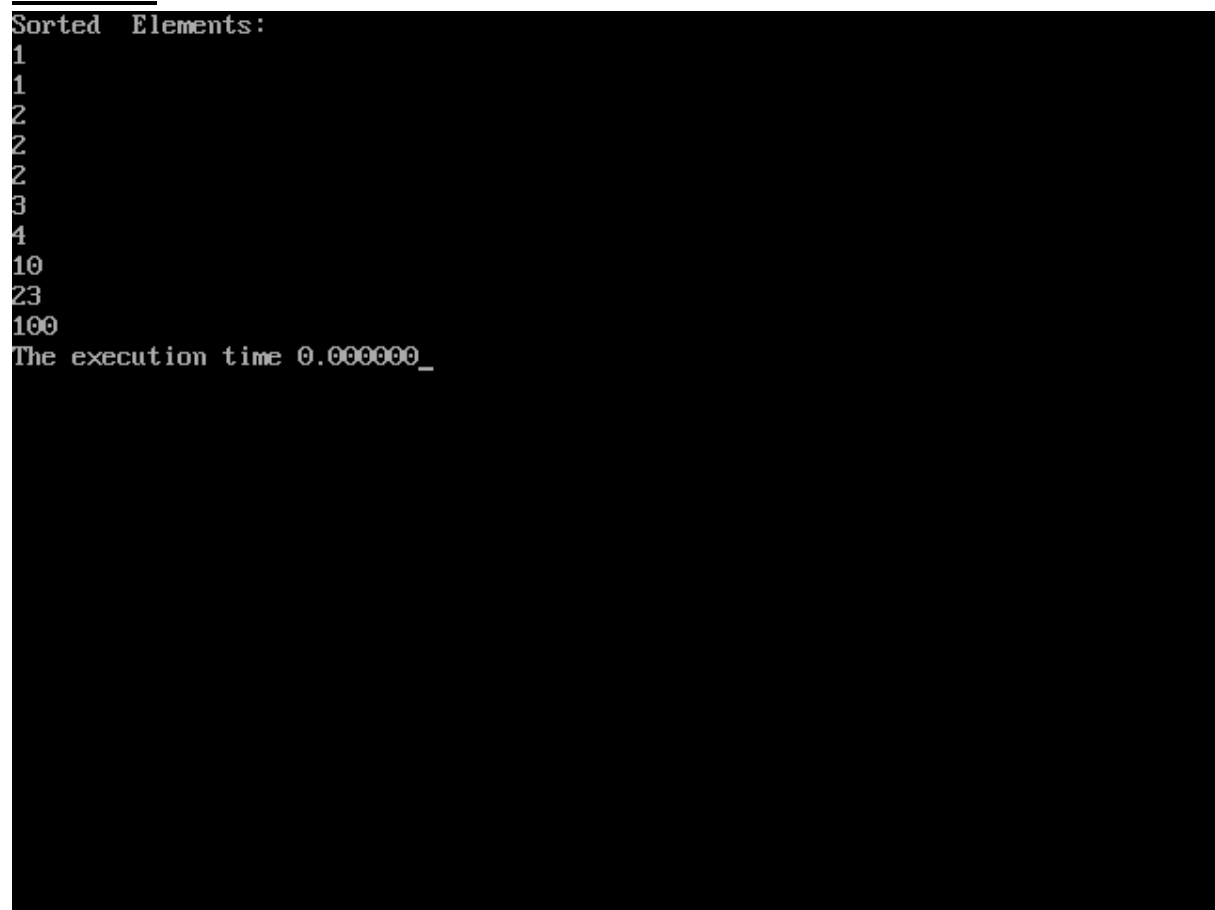
end = clock();

double execution_time = (((double)(end - start))/CLOCKS_PER_SEC);

printf("Time taken is  %f",execution_time);
getch();

}
```

OUTPUT:



```
Sorted Elements:
1
1
2
2
2
3
4
10
23
100
The execution time 0.000000_
```

RESULT:

Thus the program was executed successfully.

Graph Algorithms

5. Develop a program to implement graph traversal using Breadth First Search

AIM:

To write a program for graph traversal using Breadth First Search (BFS) algorithm.

ALGORITHM:

STEP1:Start.

STEP2:Choose any one node to start traversing.

STEP3:Visit its adjacent unvisited node.

STEP4:Insert the visited node into the queue.

STEP5:If there is no adjacent node,remove the first node from the queue .

STEP6:Repeat the steps3,4,5 until the queue is empty.

STEP7:Stop.

PROGRAM:

```
#include<stdio.h>
#include<conio.h>
int a[20][20],q[20],visited[20],n,i,j,f=-1,r=0;
void bfs(int v)
{
    q[++r]=v;
    visited[v]=1;
    while(f<=r)
    {
        for(i=1;i<=n;i++)
            if(a[v][i] && !visited[i])
            {
                visited[i]=1;
                q[++r]=i;
            }
        f++;
        v=q[f];
    }
}
void main()
{
    int v;
    clrscr();
    printf("\n Enter the number of vertices:");
    scanf("%d",&n);
    for(i=1;i<=n;i++){
        q[i]=0;
        visited[i]=0;
    }
    printf("\n Enter graph data in matrix form:\n");
    for(i=1;i<=n;i++)
```

```

for(j=1;j<=n;j++)
scanf("%d",&a[i][j]);
printf("\n Enter the starting vertex:");
scanf("%d",&v);
bfs(v);

printf("\n The node which are reachable are:\n");

for(i=1;i<=n;i++)
if(visited[i])
printf("%d\t",q[i]);
else
printf("\n Bfs is not possible");
}

```

OUTPUT:

```

Enter number of vertices:5

Enter graph data in matrix form:
0 1 1 0 0
1 0 1 1 1
1 1 0 1 0
0 1 1 0 1
0 1 0 1 0

Enter the starting vertex:1

The node which are reachable are :
1      2      3      4      5

```

RESULT:

Thus the program was executed successfully.

6. Develop a program to implement graph traversal using Depth First Search

AIM:

To write a program for graph traversal using Depth First Search (DFS) algorithm.

ALGORITHM:

STEP1:Start.

STEP2: Start by declaring the structure for creating the node with vertex and edges

STEP2A:Declare function to read the graph and insert values for the graph

STEP2B:Traversal starts from a vertex by visiting each adjacent vertex by traversing

STEP3A:Graph can have cycles so make sure the nodes are not revisited

STEP3B:If a node is visited, mark it and store in an array and then move on to the next

STEP4:Based on the adjacency matrix, values are searched in the graph and printed

STEP7: Stop.

PROGRAM:

```
#include<stdio.h>
#include<conio.h>
int a[20][20],reach[20],n;
void dfs(int v){
int i; reach[v]=1;
for(i=1;i<=n;i++){
if(a[v][i] && !reach[i]) {
printf("\n %d->%d",v,i);
dfs(i);
}
}
}
void main(){
int i,j,count=0;
printf("\n Enter number of vertices:");
scanf("%d",&n);
for(i=1;i<=n;i++){
reach[i]=0;
for(j=1;j<=n;j++){
a[i][j]=0;
}
}
printf("\n Enter the adjacency matrix:\n");
for(i=1;i<=n;i++){
for(j=1;j<=n;j++){
scanf("%d",&a[i][j]);
}
}
dfs(1);
printf("\n");
for(i=1;i<=n;i++){
if(reach[i])
count++;
}
}
```



```
if(count==n)
printf("\n Graph is connected");
else
printf("\n Graph is not connected");
}
```

OUTPUT:

```
Enter number of vertices:5

Enter the adjacency matrices:
0 1 1 0 0
1 0 1 1 1
1 1 0 1 0
0 1 1 0 1
0 1 0 1 0

1->2
2->3
3->4
4->5

graph is connected
```

RESULT:

Thus the program was executed successfully.

7. From a given vertex in a weighted connected graph, develop a program to find the shortest paths to other vertices using Dijkstra's algorithm.

AIM:

To develop a program to find the shortest paths to other vertices using Dijkstra's algorithm for a given vertex in a weighted connected graph.

ALGORITHM:

STEP1: Start

STEP2: Obtain no. of vertices and adjacency matrix for the given graph

STEP3: Create cost matrix from adjacency matrix. $C[i][j]$ is the cost of going from vertex i to vertex j . If there is no edge between vertices i and j then $C[i][j]$ is infinity

STEP4: Initialize visited[] to zero

STEP5: Read source vertex and mark it as visited

STEP6: Create the distance matrix, by storing the cost of vertices from vertex no. 0 to $n-1$ from the source vertex
 $distance[i] = cost[0][i];$

STEP7: Choose a vertex w , such that $distance[w]$ is minimum and $visited[w]$ is 0. Mark $visited[w]$ as 1.

STEP8: Recalculate the shortest distance of remaining vertices from the source.

STEP9: Only, the vertices not marked as 1 in array visited[] should be considered for recalculation of distance. i.e. for each vertex v
if($visited[v] == 0$)
 $distance[v] = \min(distance[v], distance[w] + cost[w][v])$

STEP10: Stop.

PROGRAM:

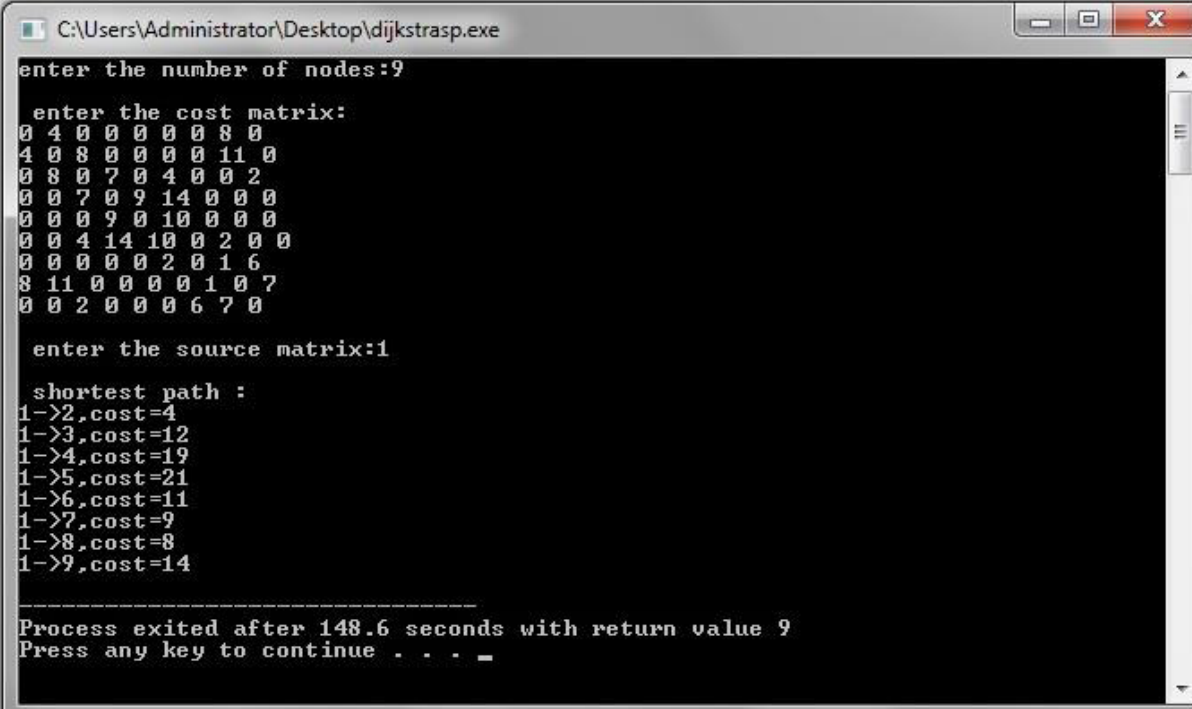
```
#include<stdio.h>
#define infinity 999
void dij(int n, int v, int cost[20][20], int dist[])
{
    int i, u, count, w, flag[20], min;
    for(i=1; i<=n; i++)
        flag[i]=0, dist[i]=cost[v][i];
    count=2;
    while(count<=n){
        min=99;
        for(w=1; w<=n; w++)
            if(dist[w]<min && !flag[w]) {
                min=dist[w];
                u=w;
            }
        flag[u]=1;
        count++;
        for(w=1; w<=n; w++)
            if((dist[u]+cost[u][w]<dist[w]) && !flag[w])
                dist[w]=dist[u]+cost[u][w];
    }
```

```

}
}
int main(){
int n,v,i,j,cost[20][20],dist[20];
printf("enter the number of nodes:");
scanf("%d",&n);
printf("\n enter the cost matrix:\n");
for(i=1;i<=n;i++)
for(j=1;j<=n;j++){
scanf("%d",&cost[i][j]);
if(cost[i][j] == 0)
cost[i][j]=infinity;
}
printf("\n enter the source matrix:");
scanf("%d",&v);
dij(n,v,cost,dist);
printf("\n shortest path : \n");
for(i=1;i<=n;i++)
if(i!=v)
printf("%d->%d,cost=%d\n",v,i,dist[i]);
}

```

OUTPUT:



```

C:\Users\Administrator\Desktop\dijkstrasp.exe
enter the number of nodes:9

enter the cost matrix:
0 4 0 0 0 0 0 8 0
4 0 8 0 0 0 0 11 0
0 8 0 7 0 4 0 0 2
0 0 7 0 9 14 0 0 0
0 0 0 9 0 10 0 0 0
0 0 4 14 10 0 2 0 0
0 0 0 0 0 2 0 1 6
8 11 0 0 0 0 1 0 7
0 0 2 0 0 0 6 7 0

enter the source matrix:1

shortest path :
1->2,cost=4
1->3,cost=12
1->4,cost=19
1->5,cost=21
1->6,cost=11
1->7,cost=9
1->8,cost=8
1->9,cost=14

-----
Process exited after 148.6 seconds with return value 9
Press any key to continue . . . _

```

RESULT:

Thus the program was executed successfully.

8. Find the minimum cost spanning tree of a given undirected graph using prim's algorithm.

AIM:

To write a program to find the minimum cost spanning tree of a given undirected graph using prim's algorithm.

ALGORITHM:

STEP1: Start

STEP2: Select a starting vertex

STEP3: Select an edge connecting the tree vertex and fringe vertex that has minimum weight.

STEP4: Repeat Steps 4 and 5 until there are fringe vertices

STEP5: Add the selected edge and the vertex to the minimum spanning tree T

STEP6: [END OF LOOP]

STEP7: EXIT

PROGRAM:

```
#include<stdio.h>
#include<conio.h>
int a, b, u,v, n, i, j, ne=1;
int visited[10]={0}, min, mincost=0, cost[10][10];
void main()
{
printf("\n Enter the number of nodes:");
scanf("%d",&n);
printf("\n Enter the adjacency matrix:\n");
for(i=1;i<=n;i++)
for(j=1;j<=n;j++)
{
scanf("%d",&cost[i][j]);
if(cost[i][j]==0)
cost[i][j]=999;
}
visited[1]=1;
printf("\n");
while(ne<n)
{
for(i=1,min=999;i<=n;i++)
for(j=1;j<=n;j++)
if(cost[i][j]<min)
if(visited[i]!=0)
{
min=cost[i][j];
a=u=i;
b=v=j;
}
if(visited[u]==0 || visited[v]==0)
{
```

```
printf("\n Edge %d:(%d %d) cost:%d", ne++,a, b, min);
mincost+=min;
visited[b]=1;
}
cost[a][b]=cost[b][a]=999;
}
printf("\n Minimum cost=%d",mincost);
}
```

OUTPUT:

```
Enter the number of nodes:5

Enter the adjacency matrix:
999  3  2  6  999
3  999  4  999  2
2  4  999  4  999
6  999  4  999 999
999  2 999  999 999

Edge 1:(1 3)cost=2
Edge 2:(2 5)cost=2
Edge 3:(1 2)cost=3
Edge 4:(3 4)cost=4
Minimum cost=11
```

RESULT:

Thus the program was executed successfully.

9. Implement Floyd's algorithm for the All-Pairs- Shortest-Paths problem.

AIM:

To write a program to find the all pair shortest paths problem using Floyd's algorithm

ALGORITHM:

STEP1: Start.

STEP2: Initialize the solution matrix same as the input graph matrix as a first step.

STEP3: Then we update the solution matrix by considering all vertices as an intermediate vertex.

STEP4: The idea is to one by one pick all vertices and update all shortest paths which include the picked vertex as an intermediate vertex in the shortest path.

STEP5: When we pick vertex number k as an intermediate vertex, we already have considered vertices

STEP6: {0, 1, 2, .. k-1} as intermediate vertices.

STEP7: For every pair (i, j) of source and destination vertices respectively, there are two possible cases.

STEP8: k is not an intermediate vertex in shortest path from i to j. Keep the value of dist[i][j] as it is.

STEP9: k is an intermediate vertex in shortest path from i to j. Update the value of dist[i][j] as dist[i][k] + dist[k][j].

STEP10: Stop.

PROGRAM:

```
#include<stdio.h>
int min(int,int);
void floyds(int p[10][10],int n){
    int i,j,k;
    for(k=1;k<=n;k++){
        for(i=1;i<=n;i++){
            for(j=1;j<=n;j++){
                if(i==j)
                    p[i][j]=0;
                else
                    p[i][j]=min(p[i][j],p[i][k]+p[k][j]);
            }
        }
    }
    int min(int a,int b){
        if(a<b)
            return(a);
        else
            return(b);
    }
    main(){
        int p[10][10],w,n,e,u,v,i,j;
        printf("\n Enter the number of vertices:");
        scanf("%d",&n);
        printf("\n Enter the number of edges:\n");
        scanf("%d",&e);
        for(i=1;i<=n;i++){
```

```

for(j=1;j<=n;j++)
p[i][j]=999;
}
for(i=1;i<=e;i++){
printf("\n Enter the end vertices of edge%d with its weight \n",i);
scanf("%d%d%d",&u,&v,&w);
p[u][v]=w;
}
printf("\n Matrix of input data:\n");
for(i=1;i<=n;i++) {
for(j=1;j<=n;j++)
printf("%d \t",p[i][j]);
printf("\n");
}
floyds(p,n);
printf("\n Transitive closure:\n");
for(i=1;i<=n;i++){
for(j=1;j<=n;j++)
printf("%d \t",p[i][j]);
printf("\n");
}
printf("\n The shortest paths are:\n");
for(i=1;i<=n;i++)
for(j=1;j<=n;j++){

if(i!=j)
printf("\n <%d,%d>=%d",i,j,p[i][j]);
}
}

```

OUTPUT:

```

D:\suresh\DAALAB PROGRAMS\allpairs.exe
Enter the number of vertices:5
Enter the number of edges:
9
Enter the end vertices of edge1 with its weight
1 2 6
Enter the end vertices of edge2 with its weight
1 3 8
Enter the end vertices of edge3 with its weight
1 5 -4
Enter the end vertices of edge4 with its weight
2 4 1
Enter the end vertices of edge5 with its weight
2 5 7
Enter the end vertices of edge6 with its weight
3 2 4
Enter the end vertices of edge7 with its weight
4 1 2
Enter the end vertices of edge8 with its weight
4 3 -5
Enter the end vertices of edge9 with its weight
5 4 3

```

```
Matrix of input data:
999      6      8      999      -4
999      999     999      1      7
999      4      999     999     999
2        999     -5     999     999
999      999     999      3      999

Transitive closure:
0        -2      -6      -1      -4
3        0       -4      1      -1
7        4       0       5       3
2        -1      -5      0      -2
5        2       -2      3       0

The shortest paths are:
<1,2>=-2
<1,3>=-6
<1,4>=-1
<1,5>=-4
<2,1>=3
<2,3>=-4
<2,4>=1
<2,5>=-1
<3,1>=7
<3,2>=4
<3,4>=5
<3,5>=3
<4,1>=2
<4,2>=-1
<4,3>=-5
<4,5>=-2
<5,1>=5
<5,2>=2
<5,3>=-2
<5,4>=3

-----
Process exited after 91.57 seconds with return value 5
Press any key to continue . . .
```

RESULT:

Thus the program was executed successfully.

10. Compute the transitive closure of a given directed graph using Warshall's algorithm.

AIM:

To write a program to compute the transitive closure of a given directed graph using Warshall's algorithm.

ALGORITHM:

Transitive closure

1. Given a directed graph, find out if a vertex j is reachable from another vertex i for all vertex pairs (i, j) in the given graph.
2. Here reachable mean that there is a path from vertex i to j.
3. The reach-ability matrix is called transitive closure of a graph.

PROGRAM:

//Transitive closure of a graph using Warshall's algorithm

```
#include <stdio.h>
intn,a[10][10],p[10][10];
void path(){
    inti,j,k;
    for(i=0;i<n;i++)
    for(j=0;j<n;j++)
    p[i][j]=a[i][j];
    for(k=0;k<n;k++)
    for(i=0;i<n;i++)

    for(j=0;j<n;j++)
    if(p[i][k]==1&& p[k][j]==1)
    p[i][j]=1;
}
void main(){
    inti,j;
    printf("Enter the number of nodes:");
    scanf("%d",&n);
    printf("\nEnter the adjacency matrix:\n");
    for(i=0;i<n;i++)
    for(j=0;j<n;j++)
    scanf("%d",&a[i][j]);
    path();
    printf("\nThe path matrix is shown below\n");
    for(i=0;i<n;i++){
    for(j=0;j<n;j++)
    printf("%d ",p[i][j]);
    printf("\n");
    }
}
```

OUTPUT:

```
Enter number of nodes:6

Enter the adjacency matrix:
0 0 0 0 0 0
0 0 0 0 0 0
0 0 0 1 0 0
1 0 0 0 0 0
1 1 0 0 0 0
1 0 1 0 0 0

The path matrix is shown below
0 0 0 0 0 0
0 0 0 0 0 0
1 0 0 1 0 0
1 0 0 0 0 0
1 1 0 0 0 0
1 0 1 1 0 0
```

RESULT:

Thus the program was executed successfully.

Algorithm Design Techniques

11. Develop a program to find out the maximum and minimum numbers in a given list of n numbers using the divide and conquer technique.

AIM:

To write a program to find the maximum and minimum number in a given list of n numbers using the divide and conquer technique.

ALGORITHM:

STEP1: Start.

STEP2: The main() function calls the minimum() by passing array,array size,1 as arguments.

STEP3: Then the function minimum()

- a) Checks the condition $i < n$, If it is true
- b) Then it compares $a[\text{min}] > a[i]$ if it is also true
- c) Then min initialised to i and calls the function by itself by increasing i value until the condition $a[\text{min}] > a[i]$ becomes false.
- d) This function returns the min to the main function main() prints the $a[\text{min}]$ value of the array.

STEP4: The main() function calls the maximum() function by passing array,array size,1 as arguments.

STEP5: Then the function maximum()

- a) Checks the condition $i < n$, if it is true
- b) Then it compares $a[\text{max}] < a[i]$ if it is true
- c) Then max initialise to i and calls the function itself by increasing i value until the condition $a[\text{max}] < a[i]$ becomes false.
- d) This function returns the max to the main function.
- e) main() function prints the $a[\text{max}]$ value of the array.

PROGRAM:

```
#include <stdio.h>
#include <conio.h>
int minimum(int a[],int n,int i)
{
    static int min=0;;
    if(i<n)
    {
        if(a[min]>a[i])
        {
            min=i;
            minimum(a,n,++i);
        }
    }
    return min;
}
int maximum(int a[],int n,int i)
{
    static int max=0;;
    if(i<n)
    {
        if(a[max]<a[i])
        {
```

```

    max=i;
    maximum(a,n,++i);
}
}
return max;
}
int main()
{
    int a[1000],i,n,sum;

    printf("Enter size of the array \n : ");
    scanf("%d", &n);
    printf("Enter elements in array \n: ");
    for(i=0; i<n; i++)
    {
        scanf("%d", &a[i]);
    }
    printf("minimum of array is : %d",a[(minimum(a,n,1))]);
    printf("\nmaximum of array is : %d",a[(maximum(a,n,1))]);
}

```

OUTPUT:

RESULT:

Thus the program was executed successfully.

12. Implement Merge sort and Quick sort methods to sort an array of elements and determine the time required to sort. Repeat the experiment for different values of n , the number of elements in the list to be sorted and plot a graph of the time taken versus n .

AIM:

To sort the elements in the given array using Quick sort methods

ALGORITHM:

STEP1: Define the function for performing quick sort

STEP2A: Allocate a pivot element in the list and compare the first and last elements

STEP2B: If the elements are not in order, swap them and order them in list

STEP3: This is done for all the elements stored in the list

STEP4A: Declare the number of elements and count them

STEP4B: Print the ordered/sorted list of elements

STEP5: Stop

PROGRAM:

```
include <stdio.h>
include <time.h>
voidExch(int *p, int *q){
int temp = *p;
*p = *q;
*q = temp;
}
voidQuickSort(int a[], int low, int high){
int i, j, key, k;
if(low>=high)
return;
key=low;

i=low+1;
j=high;
while(i<=j){
while ( a[i] <= a[key] )
i=i+1;
while ( a[j] > a[key] )
j=j -1;
if(i<j)
Exch(&a[i], &a[j]);
}
Exch(&a[j], &a[key]);
QuickSort(a, low, j-1);
QuickSort(a, j+1, high);
}
void main(){
int n, a[1000],k;
clock_t t1,t2; double ts; clrscr();
printf("\n Enter How many Numbers: ");
scanf("%d", &n);
printf("\nThe Random Numbers are:\n");
for(k=1; k<=n; k++){
```

```

a[k]=rand();
printf("%d\t",a[k]);
}
st=clock();
QuickSort(a, 1, n);
et=clock();
ts=(double)(et-st)/CLOCKS_PER_SEC;
printf("\nSorted Numbers are: \n ");
for(k=1; k<=n; k++)
printf("%d\t", a[k]);
printf("\nThe time taken is %e",ts);
}

```

OUTPUT:

```

Enter how many numbers:20

The Random Numbers are:
346      130      10982     1090     11656     7117     17595     6415     22948     31126
9004     14558     3571      22879     18492     1360      5412      26721     22463     25047

sorted numbers are:
130      346      1090     1360     3571      5412      6415      7117      9004      10982
11656     14558     17595     18492     22463     22879     22948     25047     26721     31126

The timetaken is  0.000000e+00_

```

RESULT:

Thus the program was executed successfully.

12.b. Merge sort

AIM:

To sort the elements in the given array using Merge sort methods

ALGORITHM:

STEP1: Define the function for performing merge sort

STEP2: Obtain the number of elements for list1 and list2

STEP3: Enter the ordered elements for list 1 and list 2

STEP4: Compare the elements of both lists and merge them

STEP5: Then perform sorting of two lists after merging them together as one list

STEP6: Print the combined or merged and ordered/sorted list of elements

STEP7: Stop

PROGRAM:

```
#include <stdio.h>
#include<time.h>
int b[50000];
void Merge(int a[], int low, int mid, int high){
    int i, j, k;
    i=low; j=mid+1; k=low;
    while ( i<=mid && j<=high ) {
        if( a[i] <= a[j] )
            b[k++] = a[i++] ;
        else
            b[k++] = a[j++] ;
    }
    while (i<=mid)
        b[k++] = a[i++] ;
    while (j<=high)
        b[k++] = a[j++] ;
    for(k=low; k<=high; k++)
        a[k] = b[k];
}
```

```
void MergeSort(int a[], int low, int high){
    int mid;
    if(low >= high)
        return;
    mid = (low+high)/2 ;
    MergeSort(a, low, mid);
    MergeSort(a, mid+1, high);
    Merge(a, low, mid, high);
}

void main(){
    int n, a[50000],k;
    clock_t t,et;
```

```

doublets;
printf("\n Enter How many Numbers:");
scanf("%d", &n);
printf("\nThe Random Numbers are:\n");
for(k=1; k<=n; k++) {
a[k]=rand();
printf("%d\t", a[k]);
}
st=clock();
MergeSort(a, 1, n);
et=clock();
ts=(double)(et-st)/CLOCKS_PER_SEC;
printf("\n Sorted Numbers are : \n ");
for(k=1; k<=n; k++)
printf("%d\t", a[k]);
printf("\nThe time taken is %e",ts);
}

```

OUTPUT:

```

Enter How many Numbers:30

The Random Numbers are:
346    130    10982   1090    11656   7117    17595   6415    22948   31126
9004    14558   3571    22879   18492   1360    5412    26721   22463   25047
27119   31441    7190    13985   31214   27509   30252   26571   14779   19816

sorted numbers are:
130    346    1090    1360    3571    5412    6415    7117    7190    9004
10982   11656   13985   14558   14779   17595   18492   19816   22463   22879
22948   25047   26571   26721   27119   27509   30252   31126   31214   31441

The time taken is 0.000000e+00_

```

RESULT:

Thus the program was executed successfully.

State Space Search Algorithms

13. Implement N Queens problem using Backtracking.

AIM:

To implement the program for N-Queen problem using Backtracking.

ALGORITHM:

- 1) Start in the leftmost column
- 2) If all queens are placed return true
- 3) Try all rows in the current column. Do following for every tried row.
 - a) If the queen can be placed safely in this row then mark this [row, column] as part of the solution and recursively check if placing queen here leads to a solution.
 - b) If placing queen in [row, column] leads to a solution then return true.
 - c) If placing queen doesn't lead to a solution then unmark this [row, column] (Backtrack) and go to step (a) to try other rows.
- 3) If all rows have been tried and nothing worked, return false to trigger Backtracking.

PROGRAM:

```
#include<stdio.h>
#include<math.h>
int a[30],count=0;
int place(int pos){
    int i;
    for(i=1;i<pos;i++){
        if((a[i]==a[pos])||((abs(a[i]-a[pos])==abs(i-pos))))
            return 0;
    }
    return 1;
}
void print_sol(int n){
    int i,j; count++;
    printf("\n\nSolution # %d:\n",count);
    for(i=1;i<=n;i++){
        for(j=1;j<=n;j++){
            if(a[i]==j)
                printf("Q\t");
            else
                printf("*\t");
        }
        printf("\n");
    }
}
void queen(int n){
    int k=1;
    a[k]=0;
    while(k!=0){
        a[k]=a[k]+1;
        while((a[k]<=n)&&!place(k))
```

```

a[k]++;
if(a[k]<=n){
if(k==n)
print_sol(n);
else{
k++;
a[k]=0;
}
}
else
k--;
}
}
void main(){
inti,n;
printf("Enter the number of Queens\n");
scanf("%d",&n);
queen(n);
printf("\nTotal solutions=%d",count);
}

```

OUTPUT:

```

Enter the number of Queens
4

solution #1:
*      Q      *      *
*      *      *      Q
Q      *      *      *
*      *      Q      *

solution #2:
*      *      Q      *
Q      *      *      *
*      *      *      Q
*      Q      *      *

total solutions=2

```

RESULT:

Thus the program was executed successfully.

Approximation Algorithms Randomized Algorithms

14. Implement any scheme to find the optimal solution for the Travelling Salesperson problem and then solve the same problem instance using any approximation algorithm and determine the error in the approximation.

AIM:

To implement the program for Travelling Salesperson problem using Backtracking.

ALGORITHM:

1. Check for the disconnection between the current city and the next city
2. Check whether the travelling sales person has visited all the cities
3. Find the next city to be visited
4. Find the solution and terminate

PROGRAM:

```
#include<stdio.h>
ints,c[100][100],ver;
float optimum=999,sum;
/* function to swap array elements */
void swap(int v[], int i, int j) {
    int t;
    t = v[i];
    v[i] = v[j];
    v[j] = t;
}
/* recursive function to generate permutations */
void brute_force(int v[], int n, int i) {
    // this function generates the permutations of the array from element i to element n-1
    int j,sum1,k;
    //if we are at the end of the array, we have one permutation
    if (i == n) {
        if(v[0]==s) {
            for (j=0; j<n; j++)
                printf ("%d ", v[j]);
            sum1=0;
            for( k=0;k<n-1;k++) {
                sum1=sum1+c[v[k]][v[k+1]];
            }
            sum1=sum1+c[v[n-1]][s];
            printf("sum = %d\n",sum1);
            if (sum1<optimum)
                optimum=sum1;
        }
    }
    else
        // recursively explore the permutations starting at index i going through index n-1*/
        for (j=i; j<n; j++) { /* try the array with i and j switched */
            swap (v, i, j);
```

```

brute_force (v, n, i+1);
/* swap them back the way they were */
swap (v, i, j);
}
}
void nearest_neighbour(int ver) {
int min, p, i, j, vis[20], from;
for(i=1; i<=ver; i++)
vis[i]=0;
vis[s]=1;
from=s;
sum=0;
for(j=1; j<ver; j++) {
min=999;
for(i=1; i<=ver; i++)
if(vis[i] !=1 && c[from][i]<min && c[from][i] !=0 ) {
min= c[from][i];
p=i;
}
vis[p]=1;
from=p;
sum=sum+min;
}
sum=sum+c[from][s];
}
void main () {
int ver, v[100], i, j;
printf("Enter n : ");
scanf("%d",&ver);
for (i=0; i<ver; i++)
v[i] = i+1;
printf("Enter cost matrix\n");
for(i=1; i<=ver; i++)
for(j=1; j<=ver; j++)
scanf("%d",&c[i][j]);
printf("\nEnter source : ");
scanf("%d",&s);
brute_force (v, ver, 0);
printf("\nOptimum solution with brute force technique is=%f\n", optimum);
nearest_neighbour(ver);
printf("\nSolution with nearest neighbour technique is=%f\n", sum);
printf("The approximation val is=%f", ((sum/optimum)-1)*100);
printf(" % ");
}

```

OUTPUT:

```
Enter n : 4
Enter cost matrix
0 10 15 20
5 0 9 10
6 13 0 12
8 8 9 0

Enter source : 1
1 2 3 4 sum = 39
1 2 4 3 sum = 35
1 3 2 4 sum = 46
1 3 4 2 sum = 40
1 4 3 2 sum = 47
1 4 2 3 sum = 43

Optimum solution with brute force technique is=35.000000
Solution with nearest neighbour technique is=39.000000
The approximation val is=11.428571
-----
Process exited after 59.19 seconds with return value 1
Press any key to continue . .
```

RESULT:

Thus the program was executed successfully.

15. Implement randomized algorithms for finding the kth smallest number.

ALGORITHM:

Given an array A[] of n elements and a positive integer K, find the Kth smallest element in the array. It is given that all array elements are distinct.

Brute force and efficient solutions

We will be discussing four possible solutions for this problem:-

1. Brute Force approach: Using sorting
2. Using Min-Heap
3. Using Max-Heap
4. Quick select: Approach similar to quick sort

Brute force approach: Using sorting

The idea is to sort the array to arrange the numbers in increasing order and then returning the Kth number from the start.

PROGRAM:

```
#include <stdio.h>
```

```
#include <stdlib.h>
```

```
// Compare function for qsort
```

```
int cmpfunc(const void* a, const void* b)
```

```
{  
    return (*(int*)a - *(int*)b);  
}
```

```
// Function to return k'th smallest element in a given array
```

```
int kthSmallest(int arr[], int n, int k)
```

```
{  
    // Sort the given array  
    qsort(arr, n, sizeof(int), cmpfunc);
```

```
    // Return k'th element in the sorted array
```

```
    return arr[k - 1];  
}
```

```
// Driver program to test above methods
```

```
int main()
```

```
{  
    int arr[] = { 12, 3, 5, 7, 19 };  
    int n = sizeof(arr) / sizeof(arr[0]), k = 2;  
    printf("K'th smallest element is %d",  
        kthSmallest(arr, n, k));  
    return 0;  
}
```

OUTPUT:

```
k'th smallest element is 5
```

RESULT:

Thus the program was executed successfully.