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Question 1: List Equality

a. $[X, Y, | Z]$ **and** $[p, q, r, s, t, | [u, v, y]]$

$[p, q, r, s, t, | [u, v, y]]$
 $= [p, q, r, s, t, u, v, y]$
 $= [p, q | [r, s, t, u, v, y]]$

$[p, q | [r, s, t, u, v, y]]$
 $[X, Y, | Z]$

$X = p$

$Y = q$

$Z = [r, s, t, u, v, y]$

If $X = p$, $Y = q$, and $Z = [r, s, t, u, v, y]$, then the lists $[X, Y, | Z]$ and $[p, q, r, s, t, | [u, v, y]]$ are equal.

b. $[a, [Y | [b, c]], d]$ **and** $[a, [b, [b, c]] | Z]$

$[a, [Y | [b, c]], d]$
 $= [a, [Y, b, c], d]$

$[a, [Y, b, c], d]$
 $[a, [b, [b, c]] | Z]$

These two lists are not equal because the first list ($[a, [Y, b, c], d]$) expects 3 values within $[Y, b, c]$ whereas, the second list ($[a, [b, [b, c]] | Z]$) expects two values within $[b, [b, c]]$.

c. $[yyz | [yow | [yyc | [yvr | [yul | [YEG]]]]]]$ **and** $[A1, A2 | A3]$

$[yyz | [yow | [yyc | [yvr | [yul | [YEG]]]]]]$
 $= [yyz, yow | [yyc | [yvr | [yul | [YEG]]]]$
 $= [yyz, yow, yyc | [yvr | [yul | [YEG]]]$
 $= [yyz, yow, yyc, yvr | [yul | [YEG]]]$
 $= [yyz, yow, yyc, yvr, yul | [YEG]]$
 $= [yyz, yow, yyc, yvr, yul, YEG]$
 $= [yyz, yow | [yyc, yvr, yul, YEG]]$

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$[yyz, yow \mid [yyc, yvr, yul, YEG]]$
 $[A1, A2 \mid A3]$

$A1 = yyz$

$A2 = yow$

$A3 = [yyc, yvr, yul, YEG]$

If $A1 = yyz$, $A2 = yow$, and $A3 = [yyc, yvr, yul, YEG]$, then the lists $[yyz \mid [yow \mid [yyc \mid [yvr \mid [yul \mid [YEG]]]]]$ and $[A1, A2 \mid A3]$ are equal.

d. $[apple, Z, bee \mid [Z, car, door]]$ **and** $[X \mid [bee, Y \mid [Q \mid R]]]$

$[apple, Z, bee \mid [Z, car, door]]$
 $= [apple, Z, bee, Z, car, door]$

$[X \mid [bee, Y \mid [Q \mid R]]]$
 $= [X, bee, Y, Q \mid R]$

$[apple, Z, bee, Z, car, door]$
 $[X, bee, Y, Q \mid R]$

$X = apple$

$Z = bee$

$Y = bee$

$Q = Z = bee$

$R = [car, door]$

If $X = apple$, $Z = Y = Q = bee$, and $R = [car, door]$, then the lists $[apple, Z, bee \mid [Z, car, door]]$ and $[X \mid [bee, Y \mid [Q \mid R]]]$ are equal.

e. $[Z \mid [Z \mid [[Z \mid [[Z]]]]]]$ **and** $[b \mid Y]$

$[Z \mid [Z \mid [[Z \mid [[Z]]]]]]$
 $= [Z, Z \mid [[Z \mid [[Z]]]]]$
 $= [Z, Z, [Z \mid [[Z]]]]$
 $= [Z, Z, [Z, [Z]]]$
 $= [Z \mid [Z, [Z, [Z]]]]$

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$[Z \mid [Z, [Z, [Z]]]]$

$[b \mid Y]$

$Z = b$

$Y = [Z, [Z, [Z]]]$

If $Z = b$ and $Y = [Z, [Z, [Z]]]$, then $[Z \mid [Z \mid [[Z \mid [[Z]]]]]$ and $[b \mid Y]$ are equal.

f. $[U \mid [W \mid [U]]]$ **and** [the, quick, brown, fox, W]

$[U \mid [W \mid [U]]]$

$= [U, W \mid [U]]$

$= [U, W, U]$

$[U, W, U]$

[the, quick, brown, fox, W]

$U = \text{the}$

$W = \text{quick}$

$U = \text{brown}$

These two lists are not equal because U cannot be equal to two different values.

g. $[\text{first} \mid [U \mid [[R] \mid U]]]$ **and** $[Q, [], [Q] \mid U]$

$[\text{first} \mid [U \mid [[R] \mid U]]]$

$= [\text{first} \mid [U \mid [[R] \mid U]]]$

$= [\text{first}, U \mid [[R] \mid U]]$

$= [\text{first}, U, [R] \mid U]$

$= [\text{first}, U, [R] \mid U]$

$[\text{first}, U, [R] \mid U]$

$[Q, [], [Q] \mid U]$

$Q = \text{first}$

$U = []$

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$[R] = [Q] = \text{first}$

If $Q = R = \text{first}$ and $U = []$, then the lists $[\text{first} \mid [U \mid [[R] \mid U]]]$ and $[Q, [], [Q] \mid U]$ are equal.

h. $[\text{Did} \mid [[\text{An}, X] \mid [\text{ever}, \text{Win}, \text{An}, X]]]$ **and** $[\text{Only}, [\text{One}, \text{oscar}] \mid [\text{Did}, X, \text{hammerstein}, \text{TheSecond}]]$

$[\text{Did} \mid [[\text{An}, X] \mid [\text{ever}, \text{Win}, \text{An}, X]]]$
 $= [\text{Did}, [\text{An}, X] \mid [\text{ever}, \text{Win}, \text{An}, X]]$
 $= [\text{Did}, [\text{An}, X], \text{ever}, \text{Win}, \text{An}, X]$

$[\text{Only}, [\text{One}, \text{oscar}] \mid [\text{Did}, X, \text{hammerstein}, \text{TheSecond}]]$
 $= [\text{Only}, [\text{One}, \text{oscar}], \text{Did}, X, \text{hammerstein}, \text{TheSecond}]$

$[\text{Did}, [\text{An}, X], \text{ever}, \text{Win}, \text{An}, X]$
 $[\text{Only}, [\text{One}, \text{oscar}], \text{Did}, X, \text{hammerstein}, \text{TheSecond}]$

$\text{Did} = \text{Only} = \text{ever}$

$\text{An} = \text{One} = \text{hammerstein}$

$X = \text{Win} = \text{TheSecond} = \text{oscar}$

If $\text{Did} = \text{Only} = \text{ever}$, $\text{An} = \text{One} = \text{hammerstein}$, and $X = \text{Win} = \text{TheSecond} = \text{oscar}$, then the lists $[\text{Did} \mid [[\text{An}, X] \mid [\text{ever}, \text{Win}, \text{An}, X]]]$ and $[\text{Only}, [\text{One}, \text{oscar}] \mid [\text{Did}, X, \text{hammerstein}, \text{TheSecond}]]$ are equal.