# Theoretical and Empirical Validation of Software Product Measures<sup>1</sup>

### **Lionel Briand**

Centre de Recherche Informatique de Montréal (CRIM)

Software Engineering Group
1801 McGill College av.

Montréal, PQ, H3A 2H4

Canada
e-mail: lbriand@crim.ca

### **Khaled El Emam**

Centre de Recherche Informatique de Montréal (CRIM)

Software Engineering Group
1801 McGill College av.

Montréal, PQ, H3A 2H4

Canada
e-mail: kelemam@crim.ca

#### Sandro Morasca

Dipartimento di Elettronica e Informazione Politecnico di Milano Piazza L. Da Vinci 32, I-20133, Milano Italy e-mail: morasca@elet.polimi.it http://www.elet.polimi.it/~morasca

### **Abstract**

In this paper we present and discuss a concrete method for validating measures of software product internal attributes and provide guidelines for its application. This method integrates much of the relevant previous work, such as measurement theory, properties of measures, and the Goal/Question/Metric paradigm (GQM). We identify two types of validation: theoretical and empirical. The former addresses the question "is the measure measuring the attribute it is purporting to measure?", and the latter addresses the question "is the measure useful in the sense that it is related to other variables in expected ways?"

## 1. Introduction: When Is a Measure Valid?

Recent software engineering literature has reflected a concern for methods to validate measures of attributes of software products (e.g., see [KPF95], [S92], [FK90]). This concern is driven, at least partially, by a recognition that: (i) common practices for the validation of software engineering measures are not acceptable on scientific grounds, and (ii) valid measures are essential for effective software project management and sound empirical research. For example, in a recent paper [KPF95], the authors write: "Unless the software measurement community can agree on a valid, consistent, and comprehensive theory of measurement validation, we have no scientific basis for the discipline of software measurement, a situation potentially disasterous for both practice and research." It is therefore crucial for the software engineering community to discuss and eventually reach consensus on precise methods for validating measures.

In this paper, we will focus on the validation of measures of the *internal attributes* of software products. Internal attributes, as defined in [F91], can be measured purely in terms of the product itself, independent of how it relates to its environment. Software size, complexity, cohesion, and coupling are examples of internal attributes of software products.

Internal product attributes are interesting for software engineers as long as they are a part of software engineering theories. A theory defines relationships amongst product, process, and resource attributes. For example, a simple theory could define a negative association between code complexity and maintainability (i.e., the more complex code is less maintainable). As another example, consider Parnas' theory about design [P72], which is commonly accepted amongst researchers and practitioners. Parnas' theory states that high cohesion within modules and low coupling across modules are desirable design attributes, in that a software system designed accordingly is easier to understand, modify,

<sup>&</sup>lt;sup>1</sup> This paper appears as Technical Report number ISERN-95-03, International Software Engineering Research Network, 1995.

and maintain. When supported by convincing empirical evidence, theories help us better understand software engineering phenomena and can also be useful for prediction purposes.

If an attribute is not part of any theory, one must question whether the attribute is worth studying at all since we do not know if it is useful<sup>2</sup>. This perspective is shared by other researchers in software engineering measurement. For instance, the authors of [F91][FK90] quote Kyburg's phrase "If you have no viable theory into which X enters, you have very little motivation to generate a measure of X," and stress their support of this statement.

It is quite surprising that, in an empirical discipline such as software engineering, theories are often accepted without any empirical proof of their truthfulness. This is not at all to say that theories like Parnas' should be discarded because no empirical evidence is provided when they are proposed. However, we point out the need for thorough theoretical and empirical study before these theories become widely accepted.<sup>3</sup> Theories cannot be empirically tested unless we can measure the attributes involved in these theories. Therefore, for example, we cannot study the relationship between code complexity and maintainability unless we can really measure the attributes of complexity and maintainability with a sufficient degree of accuracy.

To this end, the two following kinds of validation are necessary in software engineering.

- a) **Theoretical validation** (e.g., see [W88]) is carried out to show that a measure is really measuring the attribute it is purporting to measure. This is, of course, the most basic form of validation, and a prerequisite to demonstrating the usefulness of a measure (which is empirical validation), since one cannot properly test theories if one is not sure that s/he is measuring the attributes in those theories.
- b) **Empirical validation** (e.g., see [S92]) is carried out to demonstrate that a measure is useful in the sense that it is related to other variables in expected ways (as defined in the theories). As mentioned earlier, it is questionable whether it is worth showing that a measure is measuring a particular attribute if that attribute is not part of a theory.

It is our position that neither kind of validation is sufficient by itself. Both must be carried out. Therefore, we will say that a measure is valid if it successfully undergoes both kinds of validation, i.e. (a) it is demonstrated that the measure actually measures what it purports to measure, and (b) there is an accumulation of convincing evidence that it is useful, i.e., empirical validation is an on-going activity, so really there are degrees of validity: the more evidence the more valid a measure is.

In this paper we present and discuss a concrete method for the theoretical and empirical validation of measures of internal software product attributes and provide guidelines for its application. In this method, we also integrate many of the relevant existing concepts for validation (e.g., measurement theory [F91][Z91], properties of measures [BMB96], and GQM [BR88]). To briefly summarize our method, below are its four main steps:

<sup>&</sup>lt;sup>2</sup>Theories may be more or less straightforward and may look more or less obvious. Some theories may no longer require to be empirically demonstrated. As a very simple example, the size of a compiled program is an interesting attribute if one wants to know whether it can be stored in a floppy disk. It is all-too-obvious that there is a one-to-one relationship between the size of the compiled program (the product's internal attribute) and the size of the floppy disk (the resource's internal attribute). This relationship has been empirically demonstrated so many times that nobody thinks of conducting further experiments on this. However, even though implicitly, this theory has been formulated and validated.

<sup>&</sup>lt;sup>3</sup>As a matter of fact, in [BMB94] we have provided such a study of Parnas' design principles. The result of the study basically confirms Parnas' ideas. However, 22 years elapsed between Parnas' proposal and this study!

- a) Define measurement and validation goals (as stipulated in G/Q/M).
- b) Define Empirical Relational Systems and Formal Relational Systems (as stipulated in measurement theory).
- c) Conduct original empirical validation of the measure.
- d) Replicate the original empirical validation.

The paper is organized as follows. In Section 2 we present how to theoretically validate a measure (step (b)). In Section 3 we discuss how to empirically validate a measure (steps (c) and (d)). Section 4 describes how the G/Q/M paradigm ties in with our method for validation (step (a)). In these sections, we attempt to reconcile the different views regarding methods for the validation of measures that have appeared in the literature, and to integrate validation more closely with some of the elements of measurement theory. We conclude in Section 5 with an overall summary of the paper.

## 2. Theoretical Validation

Measurement theory is a useful formal tool for building and validating measures. In this section, we will discuss the issues related to the definition of Empirical Relational Systems (Section 2.1) and Formal Relational Systems (Section 2.2) — two essential parts of measurement theory — in the context of validation. We subsequently discuss the relationship between our method for theoretical validation and some recent work on measurement validation (Section 2.3). Finally (Section 2.4), we provide a summary of the issues related to theoretical validation.

### 2.1 Defining Empirical Relational Systems

Theoretical validation is concerned with demonstrating that a measure is measuring the concept it is purporting to measure. The first requirement for theoretical validation is that the analyst has a good intuitive understanding of the concept that is being measured and/or that the software engineering community has a consensual intuitive understanding of the concept. This means that a measure  $\mu$  of an attribute must be consistent with the intuitive understanding of this attribute. For instance, if  $\mu$  is supposed to measure the "height" of people, and we empirically know that person P1 is taller than person P2, we require that  $\mu(P1) > \mu(P2)$ .

Theoretical validation then involves modeling this intuitive understanding of the attribute we want to measure. In the framework of measurement theory [F91, Z91], intuition and empirical knowledge are modeled by empirical relational systems, whose definition is provided below. (This definition and all definition related to the basics of measurement theory are taken from [Z91, pp. 40 - 51], based on [R79].)

A relational system A is an ordered tuple  $(A, R_1, ..., R_n, o_1, ..., o_m)$  where A is a nonempty set of objects, the  $R_i$ , i = 1, ..., n are ki-ary relations on A and the  $o_i$ , j=1,...,m are closed binary operations.

# Empirical Relational System:

$$A = (A, R_1, ..., R_n, o_1, ..., o_m).$$

A is a non-empty set of empirical objects that are to be measured (in our case program texts, flowgraphs, etc.).

- $R_i$  are ki-ary empirical relations on A with i = 1,...,n (for example, the empirical relation "equal to or more complex").
- $o_j$  are binary operations on the empirical objects A that are to be measured with j=1,...,m (for example a concatenation of control flowgraphs).

The empirical relational system describes the part of reality on which measurement is carried out (via the set of objects A) and our empirical knowledge of the objects' attributes we want to measure (via the collection of empirical relations  $R_i$ 's).

Depending on the attributes we want to measure, different empirical relations are used. For instance, if we are interested in program length, we may want to use the relation "longer than" (e.g., "program  $P_1$  is longer than program  $P_2$ "); if we are interested in program complexity, we may want to use the relation "more complex than" (e.g., "program  $P_3$  is more complex than program  $P_4$ ").

Binary operations may be seen as a special case of ternary relations between objects. For instance, suppose that  $o_1$  is the concatenation operation between two programs. We may see it as a relation Concat(Program1, Program2, Program3), where Program3 is obtained as the concatenation of Program1 and Program2, i.e., Program3 = Program1  $o_1$  Program2. It is important to notice that an empirical relational system does not contain any reference to measures or numbers. Only "qualitative" statements are made, based on our *intuition* and *knowledge of the attribute*. Therefore, the definition of empirical relational systems is inherently subjective.

Usually, the relations contained in empirical relational systems are of different kinds. We will provide here three instances. We will assume that we want to build an empirical relational system for the size of program bodies, i.e., executable sections of programs, as defined in [W88].

A first set of relations defines *partial orders*. For instance, for any triplet (Program1, Program2, Program3) as defined above, the following empirical relational system property holds:

```
(Concat(Program1, Program2, Program3) ⇒ Program3 » Program1) and (Concat(Program1, Program2, Program3) ⇒ Program3 » Program2)
```

where """ is an empirical relation meaning "has a larger or equal size than." In this example, such a property defines a partial order on the set of program bodies.

*Equivalence relations* constitute another type of usually defined relations. For instance, for any quadruple of program bodies (Program1, Program2, Program3, Program4), the following empirical relational system property holds:

```
(Concat(Program1, Program2, Program3) and

Concat(Program2, Program1, Program4)) ⇒ Program3 ~ Program4
```

where "~" is an empirical equivalence relation meaning "has the same size as."

A last example of a relation is the *identification of special objects*. For instance, one may assume that there is a particular program body, the empty program body, whose size is less than the size of any other program body. Notice

that this alone does not imply that the empty program body should have size equal to zero, since no measure has been defined yet.

One's understanding of the empirical relational system of the attribute s/he is trying to measure is crucial in deriving valid and useful measures. However, confusion in terminology and lack of consensus in the software engineering community make it more difficult to formalize empirical relational systems. "Complexity" is a good example of confusion in software engineering [BMB96]. We therefore believe it is important that software measurement researchers agree on a basic set of properties that the empirical relational systems of common internal attributes (i.e., complexity, coupling, etc.) should have. This will help software engineering researchers and practitioners (1) to use a less ambiguous terminology and (2) have guidelines to define their own empirical relational systems in order to derive useful measures.

# 2.2 Defining Formal Relational Systems

Once an empirical relational system is defined, a measure — as described in Definition 2.1 below — for the attribute of study can be defined. This is equivalent to saying that each entity in the set of entities of the empirical relational system is associated with a value. These values have to satisfy relations that preserve the relations existing between the entities in the empirical relational system—see Definition 2.2 below. Therefore, the empirical relations are mapped onto relations between the values of measures. The pair (values of a measure, relations between the values of the measure) is called a formal relational system.

### Formal Relational System:

 $\boldsymbol{B} = (B, S_1, \dots, S_n, \bullet_1, \dots \bullet_m).$ 

*B* is a non-empty set of formal objects, for example numbers or vectors.

Si are ki-ary relations on B such as "greater than" or "equal to or greater than".

 $\bullet_i$  are closed binary operations B such as addition or multiplication.

Every object a of A is mapped into a value of B, i.e., it is measured according to measure  $\mu(a)$ . Every empirical relation  $R_i$  is mapped into a formal relation  $S_i$ . For instance, the relation "more complex than" between two programs is mapped into the relation ">" between the complexity measures of two programs. The formal relations must preserve the meaning of the empirical statements. For instance, suppose that  $R_1$  is the empirical relation "more complex than," and  $S_1$  is the formal relation ">,"  $\mu$  is a complexity measure if and only if for any two programs  $P_1$ ,  $P_2$ , with program  $P_1$  more complex than program  $P_2$ , we have  $\mu(P_1) > \mu(P_2)$ .

# **Definition 2.1** (Measure $\mu$ ):

A measure  $\mu$  is a mapping  $\mu:A \to B$  which yields for every empirical object  $a \in A$  a formal object (measurement value)  $\mu(a) \in B$ . Of course, this mapping may not be arbitrary. This leads to the following definition of a scale.

# **Definition 2.2** (Scale):<sup>4</sup>

\_

<sup>&</sup>lt;sup>4</sup> Definition 2.2 was slightly changed as compared to the one in [Z91].

Let  $\mathbf{A} = (A, R_1, ..., R_n, o_1, ..., o_m)$  be an empirical relational system and  $\mathbf{B} = (B, S_1, ..., S_n, \bullet_1, ... \bullet_m)$  a formal relational system and  $\mu$  a measure. The Triple  $(\mathbf{A}, \mathbf{B}, \mu)$  is a scale if and only if for all i, j and for all  $a_1, ..., a_k$ ,  $b, c \in A$  the following holds

$$R_i(a_1,...a_k) \Leftrightarrow S_i(\mu(a_1),...,\mu(a_k))$$
 and  $\mu(b \ o_i \ c) = \mu(b) \bullet_i \ \mu(c)$ 

If B = R is the set of real numbers, the Triple  $(A, B, \mu)$  is a **real scale**.

The formal relational system describes (via the set B) the values of the measures for the studied objects' attributes. For instance, these may be integer numbers, real numbers, vectors of integer and/or real numbers, etc. A formal relational system also describes (via the collection of relations  $S_i$ 's) the relations of interest between the measures.

The relations of the empirical relational system are translated into relations of the formal relational system. This can be demonstrated by taking size as an example. First, it is necessary to introduce some notation, taken from [BMB96]. Let a system S be represented by a pair  $\langle E,R \rangle$ , where E represents the set of elements of S, and R is a binary relation on E (R  $\subseteq$  E x E) representing the relationships between S's elements. Given a system S= $\langle E,R \rangle$ , a system m= $\langle E_m,R_m \rangle$  is **said to be** a module of S iff  $E_m \subseteq E$  and  $R_m \subseteq R$ . Typical kinds of relations of the formal relational system are (following the examples given in Section 2.1) [BMB96]:

1. **Equalities.** Equivalence relations between entities may be translated into equalities between measures of those entities' attributes. For example, we show below the *module additivity* property:

$$(m_1 \subseteq S \text{ and } m_2 \subseteq S \text{ and } E = E_{m1} \cup E_{m2} \text{ and } E_{m1} \cap E_{m2} = \varnothing) \longrightarrow Size(S) = Size(m_1) + Size(m_2)$$

2. Inequalities. Partial orders on sets of entities may be translated into inequalities between measures measures of those entities' attributes. The following property states that the size of a system built by merging two modules that may overlap cannot be greater than the sum of the sizes of the modules, due to the presense of common elements:

$$(m_1 \subseteq S \text{ and } m_2 \subseteq S \text{ and } E = E_{m_1} \cup E_{m_2}) \longrightarrow Size(S) \subseteq Size(m_1) + Size(m_2)$$

3. **Assignment of special values.** For instance, the measure of the size of the empty program body may be set to the value zero. Thus:

$$(E = \emptyset) \rightarrow Size(S) = 0$$

According to the above properties only (which are not complete, please see [BMB96] for the remaining properties), several measures introduced in the literature can be classified as size measures. For code measures, for example, these include LOC, #Modules, #Procedures, #Occurrences of Operators, #Unique Operators.

The measures we define are often intended to measure some standard attribute of entities, such as size, complexity, cohesion, or coupling. We may want to check if this is true; for instance, we may want to check whether a measure we defined to measure size of program bodies is really a size measure. This can be done by using a set of properties which characterize all measures of a specified attribute. Instances of such properties can be found in the literature [W88, L91,TZ92, BMB96]. Again, such properties are defined based on one's intuition. However, as mentioned above, we believe that some kind of generalized consensus must be reached on them, so as to:

- a) Avoid communication problems among researchers and practitioners.
- b) Avoid definitions of ambiguous measures, whose meaning is uncertain.
- c) Provide the modeler with an additional means to check whether his/her empirical modeling is correct. For instance, suppose that one believes that data flow complexity of software is an internal product attribute that is relevant to some specified goal. Suppose also that s/he has an intuitive understanding of what a complexity measure should look like. After defining an empirical relational system (e.g., under the form of mathematical properties as explained in Section 2.1), a formal relational system, and a measure from the former to the latter, s/he may find out that the measure does not satisfy his/her intuitive understanding of what a complexity measure is. At this point, s/he may choose to either: revise the empirical relational system s/he defined, or accept that measure as a function that measures something other than data flow complexity.

### 2.3 Comparison with Recent Work in the Literature

In [KPF95], the term "theoretical validation" is used in a much broader sense. Theoretical validation as presented in that article includes validation of measurement instruments, validation of data collection procedures (i.e., referred to as protocols in the paper), and satisfaction of some general requirements about measures similar to the ones mentioned by Weyuker [W88]:

- An attribute is measurable if it allows different entities to be distinguished from one another.
- Each unit of an attribute contributing to a valid measure is equivalent.
- Different entities can have the same attribute value.
- Consistent with the precepts of measurement theory [BEM96, F91, R79], a valid measure should obey the representation condition (i.e., preserve the intuitive expected behavior of the measured attibute).

Even though we acknowledge the importance of all four requirements mentioned above, only the representation condition has been the focus of our discussion in this section. This is because it is very likely the most difficult requirement to satisfy in the definition of a valid measure.

In addition, [KPF95] states that "any definition of an attribute that implies a particular measurement scale is invalid. [..] any property of an attribute that is asserted to be general property but implies a specific measurement scale must also be invalid." In general, then, this criterion means that any property that implies a scale stronger than the nominal scale would be considered invalid since it would exclude nominal scale units. This also means that any property that implies an ordering of software products (such as "larger than" or "more complex than") would be, by definition, considered invalid. It is, however, important to note that when talking about complexity, size, coupling, or any internal software product attribute, most of the interesting properties, such as the additivity property for Size attributes (see previous section and [BMB96]), imply the existence of at least an interval scale. It would therefore certainly not be reasonable to accept the above restricting criterion since doing so would mean exclusion of many interesting properties of our measures.

# 2.4 Summary

To conclude this section, theoretical validation requires that:

- a) an empirical relational system be defined, e.g., through the definition of properties and based on defined relations and operations between entities,
- b) a suitable formal relational system be defined,
- the properties of the empirical relational system be preserved by the formal relational system when the measure to be validated is used to do the mapping between them.

We believe that basic properties for the definition of empirical and formal relational systems for some of the basic software engineering measurement concepts such as complexity, coupling, etc., should be the object of a consensus in the software engineering community. We proposed such a set of basic and fundamental properties in [BMB96].

# 3. Empirical Validation

Once a measure can be considered valid from a theoretical point of view, the assumptions upon which the empirical relational system is based and the measure itself must be validated empirically. In this section, we will first provide the basic framework for empirical validation (Section 3.1). Then, we will examine in more detail the issues related to the statistical techniques to use in the validation process and their relationship to measurement theory principles (Section 3.2). Based on this, we will discuss (Section 3.3) techniques for the analysis of experimental data and the building of models. Due to its very nature, empirical validation may not provide convincing evidence of empirical validity. In Section 3.4., we discuss a set of possible causes for this lack of evidence. If the results of the empirical study provide evidence that a measure is valid, then the next step is to confirm and generalize this result, which is the subject of Section 3.5. We conclude with Section 3.6 which compares our approach to empirical validation to recent work in the literature.

## 3.1 Basic Method for Empirical Validation

Empirical validation of a measure, as we define it here, is concerned with providing evidence that the measure is in fact useful. A measure is useful if it is related to a measure of some external attribute<sup>5</sup>, e.g., maintainability. Measures of internal product attributes in software engineering are artificial concepts and do not hold any meaning in themselves. For example, a complexity measure, implicitly or explicitly, is always defined in relation to some external attribute such as error-proneness, effort, etc. In itself, a measure of the internal attribute of complexity, such as cyclomatic complexity, does not have any concrete meaning and usefulness besides its intuitive relationships with external attribute measures, e.g., likelihood of defect detection.

We want to remark that, to some extent, the same is true for other measures too. For example, the measures of size of an object have always, implicitly or explicitly, been defined in relation to some goal. For instance, consider two size measures that have been defined for objects, weight and volume. These measures do not have a concrete meaning in

<sup>&</sup>lt;sup>5</sup> While we have focused on internal attributes thus far, it should also be noted that the external attribute measure should undergo the same process as that used for the theoretical validation of an internal product measure before the empricial validation. It is generally easier to find sensible measures of external attributes than it is for internal ones. As an example, developing measures for cost and time, or for reliability and defects are quite straightforward.

themselves, but only in relation to some goal (e.g., volume: "Will this object fit in the trunk of my car?"; weight: "Will my car be able to carry this object without breaking?"). These two measures now seem so natural and obvious, and seem to have a meaning in themselves. This is due to the fact that

- a) the empirical relational system on which they are based captures well our understanding about the size attribute;
- b) the size attribute is deemed to be relevant—in these two different "flavors"—to a variety of goals;
- c) the two measures have been found useful in a large variety of circumstances, i.e., with respect to solving a set of practical problems.

Therefore, relating an internal attribute measure to an external attribute measure is a crucial point for the validation of measures. This requires the following three steps:

- a) Collection of data about the external attribute measure and the internal product measures of interest, e.g., complexity measures, defect instances of C++ classes. This will allow us, based on data analysis, to determine some optimal statistical relationship(s).
- b) Identification of the measurement level of internal and external attribute measures. This will determine, to some extent, the types of data analysis to be performed.
- c) Selection and use of suitable analysis and modeling mechanisms to formalize and quantify the relationship(s).

Step (1) implies that we have to collect data that are representative of the environment of study, e.g., the physical organization of development, the application domain, the platform, the programming language. Unfortunately, there is no easy way to determine what piece of data is relevant or not in the context of a study. For further discussion, refer to [BBT94]. Step (2) and Step (3) are more complex issues than they appear and are the subjects of the next two subsections, respectively.

### 3.2 Level of Measurement and Statistical Techniques

In order to determine whether an internal product attribute is related to an external product attribute, one commonly has to select a statistical technique. Several books and papers on the topic of measurement theory are conveying the idea that scale types should be used to proscribe the use of "inappropriate" statistical techniques. For example, a table similar to the one shown in Figure 1 is given in [F91]. This table, for instance, proscribes the use of the Pearson product moment correlation for scale types that are either nominal or ordinal. Such proscriptions, of course, are not unique to software engineering. For instance, they were originally presented by the psychologist Stevens [Ste46], serve as the basis of the classic text of Siegel on nonparametric statistics [SC88], and serve as an integral part of the decision tree developed by Andrews et al. [AKD+81] to guide researchers in the selection of the most appropriate statistics. Accordingly, if a researcher's measures do not reach the interval level, it is advised that s/he use non-parametric statistics (i.e., tests which make less stringent assumptions).

Scale Type	Examples of Appropriate Statistics	Type of Appropriate Statistics  Nonparametric Statistics	
Nominal	Mode Frequency Contingency Coefficient		
Ordinal	Median Kendall's tau Spearman's rho		
Interval	Mean Pearson's correlation	Nonparametric and Parametric Statistics	
Ratio	Geometric Mean Coefficient of Variation		

Figure 1: Appropriate statistics for various scale types.

However, in order to select the most "appropriate" statistics, a researcher has to know the type of scale(s) that s/he is using. The problem is that, in sofware engineering, like in other scientific disciplines, often it is very difficult to *determine* the scale type of a measure. For example, what is the scale type of cyclomatic complexity? Can we assume that the distances on the cyclomatic complexity scale are preserved across all of the scale? This is difficult to say and the answer can only be based on intuition. Despite a few available techniques to help the researchers in particular situations (see [BEM96]), the answer to those questions is hardly ever straightforward.

Therefore, there are many cases where researchers cannot demonstrate that their scales are interval, but they are confident that they are more than only ordinal. By treating them as ordinal, researchers would be discarding a good deal of information. Therefore, as Tukey [Tuk86a] notes "The question must be 'If a scale is not an interval scale, must it be merely ordinal?'"

Is it realistic to answer questions about scale type with absolute certainty, since their answers always rely on intuition and are therefore subjective? Can we know for sure the scale types of the measures we use? Knowing the scale type of a measure with absolute certainty is out of the question in the vast majority of cases. And in those cases, should we just discard our practical questions—whose answers may have a real impact on the software process—because we are not 100% positive about the scale types of the measures we are using? To paraphrase Tukey [Tuk86b], "Science is not mathematics" and we are not looking for perfection and absolute proofs but for *evidence* that our theories match reality as closely as possible. The other alternative, i.e., reject approximate theories, would have catastrophic consequences on most sciences, and in particular, on software engineering. What is not acceptable from a strictly mathematical perspective may be acceptable evidence and even a necessary one from an engineering or an experimental perspective.

It is informative to note that much of the recent progress in the social sciences would not have been possible if the use of "approximate" measurement scales had been strictly proscribed. For example, Tukey [Tuk86a] states after summarizing Stevens' proscriptions "This view thus summarized is a dangerous one. If generally adopted it would not only lead to inefficient analysis of data, but it would also lead to failure to give any answer at all to questions whose answers are perfectly good, though slightly approximate. All this loss for essentially no gain." Similarly, in the context of multiple regression, Cohen and Cohen [CC83] state: "The issue of the level of scaling and measurement precision required of quantitative variables in [Multiple Regression/Correlation] is complex and controversial. We take the position that, in practice, almost anything goes. Formally, fixed model regression analysis demands that the

quantitative independent variables be scaled at truly equal intervals ... Meeting this demand would rule out the use of all psychological tests, sociological indices, rating scales, and interview responses ... this eliminates virtually all kinds of quantitative variables on which the behavioral sciences depend." Even Stevens himself, with respect to ordinal scales, concedes that [Ste46]: "In the strictest propriety the ordinary statistics involving means and standard deviations ought not to be used with these scales, for these statistics imply a knowledge of something more than relative rank-order of data. On the other hand, for this 'illegal' statisticizing there can be invoked a kind of pragmatic sanction: In numerous instances it leads to fruitful results."

The above, evidently more pragmatic, view is under-represented in software engineering, however. This stems from the fact that some of the most influential books in our field (the ones considered as standard references on measurement theory in software engineering such as [F91][Z91]) are only presenting one side of the debate, (i.e., the side claiming that scale types should be used to proscribe data analysis techniques).

In most cases, the questions to answer (i.e., our measurement goals) determine the scale under which data must be used, and not *vice versa*. One should use the appropriate statistical technique assuming the level of measurement required by the question. If a pattern is detected, then the scientist should start thinking about the validity of the assumption s/he made about the scale types. In addition, it is sometimes possible to use different statistics assuming different scale types and compare the results.

We usually come up with an important question first (e.g., "Is there a linear relationship between two variables?"), relevant to our measurement goals. Subsequently, we usually look around for available data or develop measurement scales that we think can help us answer our questions at a reasonable cost. Also, most of the time, our learning process is exploratory and we have a very limited understanding of the phenomena we are studying, e.g., the impact of class coupling on defect detection likelihood. Some important questions require interval or ratio scales but we are not sure if the scales we are using are actually interval or ratio. Should we not analyze the data? For instance, if someone is asking the question: "If I can reduce coupling by 10% through a better design technique, how much would I gain in terms of reduction of defect density?" The answer to this—quite common—kind of question requires a ratio scale for coupling, since the reduction is given in terms of proportions (i.e., ratios), and there is a natural zero level of coupling (when modules are not related to each other). Intuitively, we can be quite sure defect density is defined on a ratio scale too. However, with respect to coupling, the level of measurement of the scale is quite difficult to determine, regardless of the definition used.

For example, if a statistically significant linear relationship is found between coupling and defect density through linear regression then, theoretically, the researcher must start wondering if the computed level of significance is real (or close to reality) since there is some uncertainty with respect to the type of the coupling scale. External information may be examined in order to confirm or otherwise the scale assumption. For example, assuming we want to model defect density, programmers may be surveyed by asking them to score the relative "difficulty" of programs with different coupling levels. If the scores confirm that the distance is, on average, preserved along the studied part of the scale (hopefully, the relevant one for the environment under study), then the equal interval properties may be assumed with greater confidence. In addition, thorough experience and a good intuitive understanding of the phenomenon under study can help a great deal. For example, in a given environment, very often programmers know the common causes of errors and their relative impact. Scales may thus be validated with the help of experts.

Such an approach is supported by numerous studies (for a more detailed discussion, see [BEM96]) which shows that, in general, parametric statistics are robust when scales are not too far from being interval. In other words, when a scale is not an exponential distortion of an interval scale, the likelihood of error of type I (i.e., the null hypothesis is

incorrectly rejected) does not significantly increase. In addition, other studies have shown that, in most cases, non-parametric statistics were of lesser power (i.e., higher likelihood of error of type II, i.e., the null hypothesis is falsely not rejected) than parametric statistics when their underlying assumptions were not violated to an extreme extent. Moreover, dealing with variable interactions in a multivariate tends to be much easier when using parametric techniques, e.g., multivariate regression analysis with interaction terms [DG84][AW91].

### 3.3 Data Analysis and Modeling

In order to identify relationships between the external attribute measure and the internal attribute measure to be validated, a number of statistical techniques for data analysis are available. When these two measures can be considered to be nearly or exactly at the interval-level of measurement, least-square regression analysis is commonly used. However, the specific functional form of the least-square regression equation is a matter of assumption and must be derived from the prior knowledge of the modeler. It is always simpler and more convenient to deal with linear models and therefore, when possible, transformations may be applied to linearize the relationship between two measures.

For example, a very common transformation used in software engineering is the logarithmic transformation. This is applied frequently in the construction of effort estimation models using linear regression. As has been noted by Bailey and Basili [Bas80], a general form of such models is:

 $E = a L^b$  where:

E = effort

L = some measure of size (usually LOC)

a, b = constants

In this particular case, an analyst could use the following estimating equation and thus use estimation procedures for linear regression models:

ln E = ln a + b ln L

When the external attribute measure cannot be considered interval (or even close to be interval) and is, for example, considered as an ordinal or a dichotomous response variable, then classification techniques such as logistic regression [HL89] can be used effectively.

When using a particular statistical technique, e.g., linear regression, to identify and formalize the relationship between a quality focus measure Y and an internal attribute measure X in order to validate X, one needs to show that X explains a statistically significant part of the variability of Y. However, X does not need to be a good predictor of Y since the objective here is only to provide statistical evidence of the existence of a dependency between the variables. For example, nobody expects to see coupling explain nearly all the variability of defect density because many other factors (e.g., human factors) are likely to have an impact. Therefore, it would not be reasonable to require that a

coupling measure explain a very large percentage of the variability of defect density in order to be validated. Obtaining statistical significance should be the only objective to empirically validate a measure.

This leads us to another issue: multivariate analysis. A particular internal attribute measure may not be significant as an isolated explanatory variable but may have a significant impact in a multivariate context, e.g., in an interaction term such as  $X_2X_3$  in the multiple regression equation below:

$$Y = \alpha_0 + \alpha_1 X_1 + \alpha_2 X_2 X_3$$

where Y is the dependent variable,  $X_i$ 's are the explanatory variables, and  $\alpha_i$ 's are the regression coefficients.

The variable  $X_3$  appears in the interaction term but may not be significant by itself. This means, assuming that  $\alpha_2$  and  $X_2$  are positive, that a larger  $X_3$  (e.g., any product measure) will increase Y (e.g., defect density) for a given value of  $X_2$ . From a more general perspective, it would not be realistic to expect all product internal attribute measures being related to the quality focus measure to be significant explanatory variables in a univariate model.

The drawback is that multivariate analysis is more complex than univariate analysis. In a multivariate context, it often becomes very difficult to interpret regression parameters and models may show instability, e.g., due to outliers which are also more difficult to detect in a n-dimension space. In addition, interaction terms may be significant and will make the model even more difficult to interpret. This is in part to construct models that are easier to interpret and use that techniques such as classification trees [SP88] and Optimized Set Reduction [BBT93; J95] have been developed. Therefore, it is important to note that regression, although the most often used approach to multivariate software engineering model construction, is not the only alternative. Machine learning techniques, such as the ones mentioned above, should be seriously considered when performing multivariate analysis, especially in an exploratory context. For further discussion, refer to [BBT92].

## 3.4 Interpreting a Lack of Relationship

During empirical validation, if there is no empirical evidence supporting the expected relationship between the internal attribute and the external attribute (i.e., the relationship is not statistically significant), then the analyst may be faced with an interpretation difficulty. The difficulty is in deciding whether the internal attribute is invalid or if there is some other explanation. Below we present four issues that ought to be considered in such a situation.

### 3.4.1 Methodological Flaws

Two main factors, which we have termed here methodological flaws, may have contributed towards a lack of significance in the studied relationship(s). The analyst should rule these out before concluding that a measure is not valid.

The first factor is the design of the empirical study that generated the data for the validation. There may have been problems in the study itself which would explain the lack of relationship. For example, if an experimental design was employed, then the analyst should investigate the possibility that some confounding variables that have an impact on the results were not appropriately controlled. This would be a problem with the internal validity of the study. Also if, for instance, the study was conducted with university students and small programming tasks, then the analyst should

consider whether the expected relationship(s) are most likely to exist only in an industrial environment with more experienced programmers and large scale programming tasks.

The second factor concerns the characteristics of the data that were collected. For example, if maintainability data on easily maintainable programs were collected, then it is likely that there would be little variation in the maintainability variable. If the analyst is using a Pearson product moment correlation to investigate the relationship, then such a restriction in range would lead to smaller empirical relationships. Also, as another example, if there are extreme outliers in the data, depending on the method of analysis, these may have a substantial impact on the strength of the empirical relationship.

## 3.4.2 Small Sample Size

Given that our criterion for the empirical validation of a measure is statistical significance, then the sample size can have a substantial impact on an analyst's findings and conclusions. This is because of statistical power. The power of a statistical test is defined as the probability of correctly rejecting the null hypothesis. The larger the sample size, the greater the statistical power of a given test. This means that if the analyst increases his/her sample size, and assuming the magnitude of the relationship remains unchanged, then s/he has a greater probability of finding the relationship statistically significant. This also means that if no relationship is identified, one possible reason is that the statistical test was not powerful (or sensitive) enough to detect it.

If an analyst does not find a statistically significant relationship, s/he should at a minimum determine whether the statistical test used was powerful enough for the given sample size. If s/he finds that the test was not powerful enough, then s/he should consider collecting more data and hence increasing the sample size. Often, however, that is not feasible. Alternatively, the analyst should consider using a more powerful test.

In general, parametric statistics are more powerful than their nonparametric counterparts. Figure 2 shows the sample sizes necessary for different magnitudes of two commonly used correlation coefficients, one parametric (Pearson's product moment correlation) and one nonparametric (Spearman's rank correlation) 6. As can be seen, for a specified level of power, Spearman's correlation always requires a larger sample size than Pearson's coefficient (approximately 20% larger for strong relationships). In general, for *large samples*, to achieve the same power as the Spearman correlation, a test using Pearson's coefficient would require only approximately 91% of the former's sample size [SC88]. This is called the asymptotic relative efficiency (ARE) [Gib71].

\_

<sup>&</sup>lt;sup>6</sup> The values in this table are based on the tables provided in [KT87] and [Coh88]. The calculations of sample sizes assume that the assumptions of the tests are met. Where there are analogous tables in [Coh88], the sample size values are only slightly different from [KT87] (approximately ±2 difference).

	Power = 90%			Power = 80%		
Corr.	Pearson	Spearman	% Difference	Pearson	Spearman	% Difference
0.1	854	1013	84%	618	733	84%
0.2	212	250	85%	154	183	84%
0.3	93	107	87%	68	79	86%
0.4	51	62	82%	38	46	83%
0.5	32	39	82%	24	30	80%
0.6	21	26	81%	16	20	80%
0.7	15	19	79%	12	15	80%

Figure 2: Minimal sample sizes required for Pearson's and Spearman's correlations for two levels of power (90% and 80%) at one tailed alpha = 0.05.

Therefore, in selecting a test to determine the statistical significance of a relationship, the analyst is more likely to be successful if s/he uses a parametric test. Of course, the assumptions of the particular test and the extent to which a particular set of data violate them should be considered when selecting a test.

## 3.4.3 Invalid Theory

The approach that we have presented in this paper for empirically validating measures of internal product attributes makes three assumptions:

- 1. that the internal attribute  $A_1$  is related to the external attribute  $A_2$  (i.e., that we can take the existence of this relationship in the real world for granted)
- 2. that measure  $X_1$  measures the internal attribute  $A_1$
- 3. that measure  $X_2$  measures the external attribute  $A_2$

Therefore, if the above assumptions are satisfied and if the analyst finds a relationship between  $X_1$  and  $X_2$ , then s/he has validated  $X_1$ . If assumption 1 is satisfied, then the analyst can be confident that the relationship is not spurious. The analyst can ensure that assumption 2 is met by theoretically validating  $X_1$  as described earlier in this paper. A similar procedure may be followed for ensuring that assumption 3 is met.

If the analyst does not find a relationship between  $X_1$  and  $X_2$ , then s/he should consider questioning assumption 1. One possible reason for not finding a relationship between the measured variables is that the hypothesized relationship between the attributes  $A_1$  and  $A_2$  is incorrect.

### 3.4.4 Unreliable Measures

In some cases, measures of internal attributes are not fully automated and hence they involve a level of subjectivity. A good example of this is the Function Point measure of the functionality attribute. An important consideration for such measures is their reliability. Reliability is concerned with the extent to which a measure is repeatable and consistent. For example, whether two independent raters will produce the same Function Point count for the same system is a question of reliability.

Less than perfect reliability of measured variables reduces the magnitude of their relationship, and hence reduces the possibility of finding the relationship statistically significant. If an estimate of the reliability of a measure is available, then one can correct the magnitude of the relationship for attenuation due to unreliability (for example, see [Nun78][AW91]).

If the expected relationship involves measures that are not perfectly reliable, then the analyst should consider the possibility that attenuation due to unreliability is contributing towards the lack of significance. A correction for attenuation is most useful in terms of validation when the reliability of the measure(s) is quite low.

## 3.5 Confirmation and Generalization of Empirical Validation Results

Assuming that an analyst has empirically validated the internal attribute measure, the next set of questions that need to be addressed are:

- a) Are the same results repeatable under similar conditions? How much can we believe the analyst's original result that the measure is valid? These questions are concerned with *confirming* the original empirical validation.
- b) Are the same results repeatable under different conditions? Would we get the same outcome in another project, set of projects, and/or organization(s)? These questions are concerned with *generalizing*<sup>7</sup> the original empirical validation.

Confirming the validity of a measure and establishing its generality involve replicating the original empirical validation. While replication of empirical studies in general is a requirement of a scientific discipline, it has not been practiced even mildly in software engineering. We discuss it here to emphasize its importance for the validation of measures and to encourage the practice amongst measurement researchers and practitioners.

There are degrees of replication, differentiated by the extent to which the conditions of the replicated validation are the same as those of the original validation. Along this continuum of "similarity" we distinguish amongst three types of replication, starting from the type where the conditions are *very similar* to the original validation, and ending with the type where the conditions are *very different* from the original validation. The former maximizes confirmatory power, while the latter maximizes generalizability. These are (this is based on the discussion in [LE93]):

a) **Hold-out sample.** This can be considered as the most basic form of replicating an empirical validation of a measure. Following this kind of approach, the analyst simply divides his/her sample into a test sample and a hold-out sample. The fraction of the hold-out sample can vary. If it is around half or one third of the sample, then the analyst uses the test sample to perform the original validation analysis, and then repeats the analysis using the hold-out sample. If the results converge then this is adds confirmatory power in that the original result is stable. However, since the conditions of the test sample and the hold-out sample would be very similar indeed, this approach would not add to our confidence of the generalizability of the original empirical validation results. An extension of this approach that is more applicable to small samples is to use N-fold

<sup>&</sup>lt;sup>7</sup> As a discipline, it is important for software engineering to develop general measures. However, the extent to which this can be achieved in practice remains an empirical question.

cross validation [B84]. If the sample is of size N, then this approach stipulates that the analysis be performed repeatedly for each n, n=1, ..., N, with n removed from the sample and using the remaining N-1 observations. When ordinary least squares regression is utilized for validation, for example, the PRESS (prediction sum of squares) criterion can be used to interpret the results of this approach [NWK90].

- b) Close replication. With close replication an analyst would attempt to repeat the actual empirical validation (i.e., collect a new set of data from another system or set of systems). However, the analyst would also try to keep as many of the other known conditions that may affect the outcomes the same or similar to those of the original study (e.g., the application domain, development methods and techniques, programming language, organization, programmer experience, etc.). If the results converge then this adds substantial confirmatory power to the original validation results. However, even though a different data set has been collected, this kind of replication does not provide much in the way of generalizability. This type of replication is best conducted early after an original internal attribute measure has been first validated, and demonstrates that the measure is valid under the same circumstances (i.e., the results of the original empirical validation are repeatable under the same conditions).
- c) **Differentiated replication.** With differentiated replication, the analyst starts to vary major conditions of the original empirical validation (such as the application domain and/or organization)<sup>8</sup>. S/he collects a new set of data and determines whether the replication results are the same as the original study results. If they are, then confidence in the generalizability of the measure has been increased. Of course, the more conditions that are varied the greater our confidence in the generalizability of the measure.

As members of a scientific discipline, it is responsible of software engineers to replicate empirical validation studies. This will increase our confidence in their application and also help us understand their limitations. For conducting replication validations, there are *internal* and *external* replications [BD+94]. The latter is conducted by the original analyst, and the former by an external agency. While ideally we would wish that internal replication be practiced more often, in the validation of measures it has not been so frequent. As a matter of fact, replications are infrequent even where the analyst would not have to collect new data, as in using a hold-out sample (however, see [BMB94] for an example where two internal replications of an empirical validation of high-level design metrics were reported). One pragmatic reason is the lack of funding for the collection of new data. External replication is even less frequently done, perhaps because replication research, in general, is seen as less prestigious than original research. Given this state of affairs, we would therefore encourage analysts to conduct such replications if we are to gain confidence in the empirical validity of internal product measures.

## 3.6 Comparison with Recent Work in the Literature

In [KPF95], the term "empirical validation" includes two kinds of validations. The authors distinguish between:

<sup>&</sup>lt;sup>8</sup> It should be noted, however, that changing some conditions may require modifications of the empirical relational system.

- a) Validating the measure, i.e., is the measure measuring accurately the attribute? Following this approach, measures can be compared to people's opinion and measures of associations can tell whether the measure is consistent with opinion.
- b) Validating the theories in which the measure takes part, i.e., are the expected relationships with measures of other attributes visible in the data? This is the approach that we have advocated in this paper.

Even though such a distinction is acceptable from a theoretical perspective, the former type of empirical validation does present some practical problems:

- a) People are not always capable of assessing product attributes such as complexity, coupling, etc. in a subjective way. In addition, they may be assessing different attributes without even realizing it. A good example of this difficulty is illustrated in the experiment of Gibson and Senn [GS89]. In that article, the authors asked experienced programmers to rank systems that the programmers had modified during the experiment based on their complexity. It was found that the different programmers produced substantially different rankings of the systems<sup>9</sup>.
- b) Opinion-based and measure-based rankings can be compared but it is unrealistic to expect people to provide (intuitively) distances and proportions between artifacts<sup>10</sup>. Therefore, it becomes difficult to validate interval and ratio-level measures by such direct estimation methods.

As a consequence, product measures can in practice only be experimentally validated by validating the theories in which they take place, e.g., validate a complexity measure by identifying an expected strong relationship between this measure and effort. In addition, if an attribute is not part of any theory, then defining a measure for it is not likely to be useful. Therefore, this paper focuses exclusively on this particular form of empirical validation since this is the one most likely to be used in practice<sup>11</sup>. However, we do not wish to broadly exclude validation procedures such as those suggested by [KPF95], only that we as a community do not yet know if they will produce meaningful results.

<sup>10</sup> This is our belief. However, we cannot claim for sure whether direct estimation of intervals and proportions is really difficult since we do not know of software engineering studies that actually attempted to do this. Furthermore, it should be noted that there are alternatives to direct estimation, for example, Thurnstone's method of comparative judgements can be used to construct interval scales of say complexity by asking programmers to make order judgements about

<sup>&</sup>lt;sup>9</sup> These results do not justify, however, the broad negative statements made by the authors of that article about subjective metrics in general. Complexity is such an abstract concept that it is unreasonable to expect all programmers to interpret it in the same way. The authors themselves indicate that the programmers seemed not to be able to distinguish between system complexity and maintenance task complexity. Perhaps if the criterion for the ranking was more precisely defined, then more consistent answers would have been obtained.

pairs of programs [AY79]. This kind of approach, however, has also not been used in software engineering.

Fenton and Kitchenham [FK90] criticise the commonly used empirical validation procedure whereby the analyst correlates the internal product attribute measure with any 'interesting measure' which happened to be available as data. We agree with this criticism and our approach does not advocate doing that. What we propose is basing empirical validation on existing software engineering theories and not on whatever data happens to be available. The exploratory study of a large set of attributes, and, consequently, the definition of a large number of metrics, may have dangerous consequences [CG93]. For instance, one may define a measure which turns out to be statistically well correlated to the external attribute of interest only by chance. The result obtained is of difficult and uncertain interpretation, and may lead to incorrect decisions.

## 4. Measurement Goals

Measurement does not occur in a vacuum, it should be driven by the particular measurement goals of the organization. In this section we discuss our validation methods within the more general context of goal directed measurement. One should always keep in mind that measurement is an expensive activity, which should be targeted at the achievement of business goals relevant to the organization in which it takes place. There is little point in measuring without a clearly defined context and goals: that is not likely to yield any useful and sensible results. Therefore, goal directed measurement provides: (a) guidance for the validation exercise, and (b) defines the scope for interpreting the results of the validation.

More precisely, the following elements of measurement goals influence theoretical and empirical validation:

- a) **Object of study.** Different objects of study (e.g., design vs. code) constitute the entities of different empirical relational systems. There might be differences in the nature of empirical relational systems between entities even when the same internal attribute is studied. For instance, the building of empirical relations for data flow complexity of code may take into account information that is not taken into account when building empirical relations for data flow complexity of design. In addition, different objects of study may be provided with different sets of attributes.
- b) **Quality focus.** Fenton classifies attributes as either internal or external. The quality focus is the external attribute of interest (or there can be more than one), for example, error-proneness of modules. Based on the external attribute(s) of interest, a set of relevant entities and internal attributes is identified. The assumption is that the identified internal attributes are related to the external attributes of interest in some predetermined way, which is basically our theory that serves as the basis for empirical validation.
- c) Environment in which the goal is defined. The empirical relational system and the theoretical basis for empirical validation embody intuition and knowledge that are specific to the people that belong to some environment, in which the defined goal is relevant. Therefore, the empirical relational system and the results of the empirical validation are applicable in that environment and may not be applicable elsewhere. One should always be very careful when reusing empirical relational systems (and the measures derived from them) and the results of empirical validations across environments. The conditions that affect the entities, the properties they exhibit, and the relationships amongst them may be different.
- d) **Viewpoint.** Depending on people's goals and role (e.g., design vs. implementation) in a software organization, different sets of entities (e.g., design vs. code artifacts) and different internal attributes may be selected (e.g., component coupling vs. control flow complexity).

The four factors mentioned above are four of the dimensions of GQM goals [B92, BR88]. Here is a summary of a template that may be used to define goals<sup>12</sup>:

Object of study: products, processes, resources

\_

<sup>&</sup>lt;sup>12</sup> The purpose dimension of GQM goals is most useful for interpreting the results of measurement.

*Purpose*: characterization, evaluation, prediction, improvement, ...

Quality focus: cost, correctness, defect removal, changes, reliability, ...

Viewpoint: user, customer, manager, developer, corporation, ...

*Environment*: people, resources, processes, ...

The following is an example of a GQM goal:

Object of study: C++ Classes

Purpose: prediction

Quality focus: likelihood of defect detection

Viewpoint: designer

Environment of Study: company X, OO systems developed in C++ in a given application domain

The GQM paradigm can be used even further as described in the references mentioned above. Starting from a goal, questions will be used to identify the internal attributes of interest and better characterize the external attribute. Based on these questions, suitable measures are derived for both internal and external attributes of interest. For instance, questions may be asked about the complexity and size (internal attributes) of the studied C++ classes, and about what is considered a defect (external attribute)—different environments have different definitions for defects. Measures should then be defined for complexity and size of C++ classes and for the number and criticality of uncovered defects.

# 5. Conclusion

In this paper, we have presented an approach to validate measures of internal product attributes which integrates some existing approaches to validation, measurement theory, and the GQM paradigm. This is extremely important in the context of software engineering measurement where ad-hoc approaches to measurement are still common. Since building empirical relational systems is a crucial part of measurement, more empirical studies and replicated experiments are needed for our community to build an empirical understanding of the phenomena we are studying.

From the discussion above, it is clear that both empirical and theoretical validations, as they are defined above, are necessary and complementary. We think that even though a particular internal product attribute measure is only used to assess a product and not to predict any of its attributes, this particular measure is implicitly or explicitly associated to some measure of an external quality attribute. Therefore, such assumptions needs to be empirically validated.

Furthermore, the two validation types are related. In selecting an external attribute measure as a dependent variable to validate the usefulness of an internal product attribute measure, one is usually guided by an assumed relationship between the attributes. Consequently, if the data analysis results do not support the relationship, and after ruling out serious methodological problems, then one would not know whether it is the assumed relationship(s) or the measurement assumptions that are incorrect, or both. It would therefore be prudent to provide evidence that the internal product attribute measure is measuring what it is purporting to measure prior to validating its usefulness. One way of doing so is to capture the measurement assumptions by defining an empirical relational system as described in Section 2.1. Furthermore, let us assume that we define a design complexity measure X, a product quality measure Y,

and that the data analysis results do support the relationship. In the case where it is not clear whether X measures design complexity, then the relationship may be spurious; and if it is not clear whether Y measures software quality, then the validation may be of no practical consequence.

It is also important to note that such validations are extremely difficult and one should not expect a single researcher to provide, within the context of one study, a complete and definitive validation. It is through replicated and iterative studies that confidence can be built over time.

# 6. References

- [AW91] L. Aiken and S. West: Multiple Regression: Testing and Interpreting Interactions, Sage Publications, 1991.
- [AY79] M. Allen and W. Yen: *Introduction to Measurement Theory*, Brooks/Cole Publishing Company, 1979.
- [AKD+81] F. Andrews, L. Klem, T. Davidson, P. O'Malley, and W. Rodgers: A Guide for Selecting Statistical Techniques for Analyzing Social Science Data, Institute for Social Research, University of Michigan, 1981.
- [BB81] J. Bailey and V. Basili: "A Meta-Model for Software Development Resource Expenditures." In *Proceedings of the International Conference on Software Engineering*, pages 107-116, 1981.
- [Bas80] V. Basili: "Resource Models." In *Tutorial on Models and Metrics for Software Management and Engineering*, IEEE Computer Society Press, V. Basili (ed.), 1980.
- [B92] V. Basili: "Software Modeling and Measurement: The Goal/Question/Metric Paradigm." *Technical Report*, CS-TR-2956, University of Maryland, September 1992.
- [BBT94] V. Basili, L. Briand, W. Thomas: "Experience Domain Analysis for Software Reuse", In *Proceedings of the 19th NASA-GSFC SEL Software Engineering Workshop*, 1994.
- [BR88] V. Basili and D. Rombach: "The TAME Project: Towards Improvement Oriented Software Environments." In *IEEE Transactions on Software Engineering*, 14(6):758-773, June 1988.
- [BBT92] L. Briand, V. Basili, W. Thomas: "A Pattern Recognition Approach for Software Engineering Data Analysis", In *IEEE Transactions on Software Engineering*, 18(11):931-942, 1992.
- [BBT93] L. Briand, V. Basili and C. Hetmanski: "Developing Interpretable Models with Optimized Set Reduction for Identifying High Risk Software Components," *IEEE Trans. Software Eng.*, 19 (11), November, 1993.
- [BEM96] L. Briand, K. El Emam, and S. Morasca: "On the Application of Measurement Theory to Software Engineering." To appear in *Empirical Software Engineering: An International Journal*, 1(1), 1996.
- [BMB94] L. Briand, S. Morasca, and V. Basili: "Defining and Validating High-Level Design Metrics." *Technical Report*, CS-TR-3301, University of Maryland, November 1994. Submitted for publication.
- [BMB96] L. Briand, S. Morasca, and V. Basili: "Property Based Software Engineering Measurement." In *IEEE Transactions on Software Engineering*, 22(1), January 1996.

- [B84] L. Breiman, J. Friedman, R. Olshen, and C. Stone: Classification and Regression Trees, Wadsworth, 1984.
- [BD+94] A. Brooks, J. Daly, J. Miller, M. Roper, and M. Wood: "Replications Role in Experimental Computer Science". Technical Report EFoCS-5-94, Empirical Foundations of Computer Science, University of Strathclyde, 1994.
- [Coh65] J. Cohen: "Some Statistical Issues in Psychological Research." In *Handbook of Clinical Psychology*, B. Woleman (ed.), McGraw-Hill, 1965.
- [Coh88] J. Cohen: Statistical Power Analysis for the Behavioral Sciences, Lawrence Erlbaum Associates, 1988.
- [CC83] J. Cohen and P. Cohen: Applied Multiple Regression / Correlation Analysis for the Behavioral Sciences, Lawrence Erlbaum Associates, 1983.
- [CG93] R. Courtney and D. Gustafson: "Shotgun Correlations in Software Measures", *Software Engineering Journal*, 8(1):5-13, 1993.
- [DG84] W. Dillon and M. Goldstein: "Multivariate Analysis: Methods and Applications." Wiley & Sons, 1984.
- [F91] N. Fenton: Software Metrics: A Rigorous Approach, Chapman & Hall, 1991.
- [FK90] N. Fenton and B. Kitchenham: "Validating Software Measures." In Journal of Software Testing, Verification and Reliability, 1(2):27-42, 1990.
- [Gib71] J. Gibbons: Nonparametric Statistical Inference, McGraw-Hill, 1971.
- [GS89] V. Gibson and J. Senn: "System Strutture and Software Maintenance Performance". In *Communications of the ACM*, 32(3):347-358, March 1989.
- [HL89] D. Hosmer and S. Lemeshow: "Applied Logistic Regression.", Wiley-Interscience, 1989
- [J95] M. Jørgensen: "Experience with the Accuracy of Software Maintenance Task Effort Prediction Models," *IEEE Trans. Software Eng.*, 21 (8), August, 1995.
- [KPF95] B. Kitchenham, S. Pfleeger, and N. Fenton: "Towards a Framework for Software Measurement Validation." In *IEEE Transactions on Software Engineering*, 21(12), December 1995.
- [KT87] H. Kraemer and S. Thiemann: *How Many Subjects? Statistical Power Analysis in Research*, Sage Publications, 1987.
- [L91] K. B. Lakshmanan, S. Jayaprakash, and P. K. Sinha: "Properties of Control-Flow Complexity Measures," In *IEEE Transactions on Software Engineering*, vol. 17, no. 12, pp. 1289-1295, Dec. 1991.
- [LE93] R. Lindsay and A. Ehrenberg: "The Design of Replicated Studies". In *The American Statistician*, 47(3):217-228, 1993.
- [MT77] F. Mosteller and J. Tukey: *Data Analysis and Regression*, Addison-Wesley, 1977.
- [NWK90] J. Neter, W. Wasserman, and M. Kunter: Applied Linear Statistical Models, IRWIN, 1990.
- [Nun78] J. Nunnally: *Psychometric Theory*, McGraw-Hill, 1978.

- [P72] D. Parnas: "On the Criteria to be Used in Decomposing Systems into Modules.", *Communications of the ACM*, 14(1): 221-227, 1972.
- [R79] F. Roberts: Measurement Theory with Applications to Decisionmaking, Utility, and the Social Sciences, Addison-Wesley, 1979.
- [S92] N. Schneidewind: "Methodology for Validating Software Metrics." In IEEE Transactions on Software Engineering, 18(5):410-422, 1992.
- [SP88] R. Selby and A. Porter: "Learning from Examples: Generation and Evaluation of Decision Trees for Software Resource Analysis", *IEEE Trans. Software Eng.*, 14 (12), December, 1988.
- [SC88] S. Siegel and J. Castellan: Nonparametric Statistics for the Behavioral Sciences, McGraw Hill, 1988.
- [Ste46] S. Stevens: "On the Theory of Scales of Measurement." In Science, 103(2684):677-680, June 1946.
- [TZ92] J. Tian and M. V. Zelkowitz: "A Formal Program Complexity Model and Its Application," *J. Syst. Software*, vol. 17, pp. 253-266, 1992.
- [Tuk86a] J. Tukey: "Data Analysis and Behavioral Science or Learning to Bear the Quantitative Man's Burden by Shunning Badmandments." In *The Collected Works of John W. Tukey*, Vol. III, Wadsworth, 1986.
- [Tuk86b] J. Tukey: "The Future of Data Analysis." In *The Collected Works of John W. Tukey*, Vol. III, Wadsworth, 1986.
- [W88] E. Weyuker: "Evaluating Software Complexity Measures." In *IEEE Transactions on Software Engineering*, 14(9):1357-1365, 1988.
- [Z91] H. Zuse: Software Complexity: Measures and Methods, de Gruyter, 1991.