Let's solve the given problem step by step.

### Given Data:

The table provides class intervals for weight (in kg) and the number of students in each class.

Weight (kg)	93-97	98-102	103-107	108-112	113-117	118-122	123-127	128-132
No. of students (f)	3	5	12	17	14	6	3	1

## **Step 1: Find the Mean**

The formula for the mean in grouped data is:

$$\bar{X} = \frac{\sum f_i x_i}{\sum f_i}$$

Where:

- $f_i$  is the frequency (number of students)
- $x_i$  is the midpoint of each class, calculated as:

$$x_i = \frac{\text{Lower Bound} + \text{Upper Bound}}{2}$$

## Compute midpoints $(x_i)$ :

Weight (kg)	Frequency $(f_i)$	Midpoint $(x_i)$	$f_i x_i$
93 - 97	3	$\frac{93+97}{2} = 95$	$3 \times 95 = 285$
98 - 102	5	$\frac{98+102}{2} = 100$	$5 \times 100 = 500$
103 - 107	12	$\frac{103+107}{2} = 105$	$12 \times 105 = 1260$
108 - 112	17	$\frac{108+112}{2} = 110$	$17 \times 110 = 1870$
113 - 117	14	$\frac{113+117}{2} = 115$	$14 \times 115 = 1610$
118 - 122	6	$\frac{118+122}{2} = 120$	$6 \times 120 = 720$
123 - 127	3	$\frac{123+127}{2} = 125$	$3 \times 125 = 375$
128 - 132	1	$\frac{128+132}{2} = 130$	$1 \times 130 = 130$

Summing up the values:

$$\sum f_i = 3 + 5 + 12 + 17 + 14 + 6 + 3 + 1 = 61$$

$$\sum f_i x_i = 285 + 500 + 1260 + 1870 + 1610 + 720 + 375 + 130 = 6750$$

Now, calculate the mean:

$$\bar{X} = \frac{6750}{61} = 110.66$$

## **Step 2: Find the Median**

The median is the value that divides the dataset into two equal parts. The formula for the median in grouped data is:

$$Median = L + (\frac{\frac{N}{2} - CF}{f}) \times h$$

Where:

- L = Lower boundary of the median class
- N = Total frequency = 61
- CF = Cumulative frequency before the median class
- f = Frequency of the median class
- h = Class width

## Finding the median class:

$$\frac{N}{2} = \frac{61}{2} = 30.5$$

We now calculate the cumulative frequencies (CF):

Weight (kg)	Frequency $(f_i)$	Cumulative Frequency (CF)
93 - 97	3	3
98 - 102	5	3 + 5 = 8
103 - 107	12	8 + 12 = 20
108 - 112	17	20 + 17 = 37
113 - 117	14	37 + 14 = 51
118 - 122	6	51 + 6 = 57
123 - 127	3	57 + 3 = 60
128 - 132	1	60 + 1 = 61

Since 30.5 lies in the class 108 - 112, this is our median class.

## Using the formula:

- L = 108
- CF = 20 (cumulative frequency before median class)
- f = 17 (frequency of median class)
- h = 5 (class width)

Median = 
$$108 + (\frac{30.5 - 20}{17}) \times 5$$
  
=  $108 + (\frac{10.5}{17}) \times 5$   
=  $108 + (0.6176 \times 5)$   
=  $108 + 3.09$   
=  $111.09$ 

## **Step 3: Find the Mode**

The mode is the class with the highest frequency. The formula for the mode in grouped data is:

Mode = 
$$L + (\frac{f_1 - f_0}{2f_1 - f_0 - f_2}) \times h$$

Where:

- L = Lower boundary of modal class
- $f_1$  = Frequency of modal class
- $f_0$  = Frequency before modal class
- $f_2$  = Frequency after modal class
- h = Class width

The modal class is 108 - 112 because it has the highest frequency ( $f_1 = 17$ ).

Using the formula:

- L = 108
- $f_1 = 17$
- $f_0 = 12$  (previous class frequency)
- $f_2 = 14$  (next class frequency)
- h = 5

Mode = 
$$108 + (\frac{17 - 12}{(2 \times 17) - 12 - 14}) \times 5$$
  
=  $108 + (\frac{5}{34 - 26}) \times 5$   
=  $108 + (\frac{5}{8}) \times 5$   
=  $108 + 3.125$   
=  $111.13$ 

## **Final Answers:**

- Mean = 110.66
- Median = 111.09
- Mode = 111.13

Thus, the values of mean, median, and mode are approximately 110.66, 111.09, and 111.13, respectively.

Let me know if you need further clarification!

## **Given Data:**

The table provides the class intervals for plant heights and the number of plants in each class.

Heights of plants (cm)	1-5	6-10	11-15	16-20	21-25
No. of plants (f)	7	10	16	32	24

## **Step 1: Find the Mean**

The formula for the mean in grouped data is:

$$\bar{X} = \frac{\sum f_i x_i}{\sum f_i}$$

Where:

- $f_i$  is the frequency (number of plants in each class)
- $x_i$  is the midpoint of each class, calculated as:

$$x_i = \frac{\text{Lower Bound} + \text{Upper Bound}}{2}$$

## Compute midpoints ( $x_i$ ):

Heights (cm)	Frequency ( $f_i$ )	Midpoint $(x_i)$	$f_i x_i$
1 - 5	7	$\frac{1+5}{2} = 3$	$7 \times 3 = 21$
6 - 10	10	$\frac{6+10}{2} = 8$	$10 \times 8 = 80$
11 - 15	16	$\frac{11+15}{2} = 13$	$16 \times 13 = 208$
16 - 20	32	$\frac{16+20}{2} = 18$	$32 \times 18 = 576$
21 - 25	24	$\frac{21+25}{2} = 23$	$24 \times 23 = 552$

Summing up the values:

$$\sum f_i = 7 + 10 + 16 + 32 + 24 = 89$$

$$\sum f_i x_i = 21 + 80 + 208 + 576 + 552 = 1437$$

Now, calculate the mean:

$$\bar{X} = \frac{1437}{89} = 16.14$$

## **Step 2: Find the Median**

The median is the value that divides the dataset into two equal parts. The formula for the median in grouped data is:

$$Median = L + (\frac{\frac{N}{2} - CF}{f}) \times h$$

Where:

• L = Lower boundary of the median class

• N = Total frequency = 89

• CF = Cumulative frequency before the median class

• f = Frequency of the median class

• h = Class width

### Finding the median class:

$$\frac{N}{2} = \frac{89}{2} = 44.5$$

We now calculate the cumulative frequencies (CF):

Heights (cm)	Frequency ( $f_i$ )	Cumulative Frequency (CF)
1 - 5	7	7
6 - 10	10	7 + 10 = 17
11 - 15	16	17 + 16 = 33
16 - 20	32	33 + 32 = 65
21 - 25	24	65 + 24 = 89

Since 44.5 lies in the class 16 - 20, this is our median class.

## Using the formula:

- L = 16
- CF = 33 (cumulative frequency before median class)
- f = 32 (frequency of median class)
- h = 5 (class width)

Median = 
$$16 + (\frac{44.5 - 33}{32}) \times 5$$
  
=  $16 + (\frac{11.5}{32}) \times 5$   
=  $16 + (0.359 \times 5)$   
=  $16 + 1.80$   
=  $17.80$ 

## **Step 3: Find the Mode**

The mode is the class with the highest frequency. The formula for the mode in grouped data is:

Mode = 
$$L + (\frac{f_1 - f_0}{2f_1 - f_0 - f_2}) \times h$$

Where:

• L = Lower boundary of modal class

- $f_1$  = Frequency of modal class
- $f_0$  = Frequency before modal class
- $f_2$  = Frequency after modal class
- h = Class width

The **modal class** is **16 - 20** because it has the highest frequency ( $f_1 = 32$ ).

Using the formula:

- *L* = 16
- $f_1 = 32$
- $f_0 = 16$  (previous class frequency)
- $f_2 = 24$  (next class frequency)
- h = 5

Mode = 
$$16 + (\frac{32 - 16}{(2 \times 32) - 16 - 24}) \times 5$$
  
=  $16 + (\frac{16}{64 - 40}) \times 5$   
=  $16 + (\frac{16}{24}) \times 5$   
=  $16 + (0.667 \times 5)$   
=  $16 + 3.33$   
=  $19.33$ 

## **Final Answers:**

- Mean = 16.14
- Median = 17.80
- Mode = 19.33

Thus, the values of mean, median, and mode are approximately 16.14, 17.80, and 19.33, respectively.

Let me know if you need further clarification!

solve above problem with full explanation as plain text

Let's solve the problem step by step.

Age in years	5-15	15-25	25-35	35-45	45-55
No. of patients $(f)$	23	11	14	15	13

## **Step 1: Find the Mean**

The formula for the mean in grouped data is:

$$\bar{X} = \frac{\sum f_i x_i}{\sum f_i}$$

Where:

- ullet  $f_i$  is the frequency (number of patients in each class)
- $x_i$  is the midpoint of each class, calculated as:

$$x_i = \frac{\text{Lower Bound} + \text{Upper Bound}}{2}$$

### Compute midpoints ( $x_i$ ):

Age group (years)	Frequency $(f_i)$	Midpoint $(x_i)$	$f_i x_i$
5 - 15	23	$\frac{5+15}{2} = 10$	$23 \times 10 = 230$
15 - 25	11	$\frac{15+25}{2} = 20$	$11 \times 20 = 220$
25 - 35	14	$\frac{25+35}{2} = 30$	$14 \times 30 = 420$
35 - 45	15	$\frac{35+45}{2} = 40$	$15 \times 40 = 600$
45 - 55	13	$\frac{45+55}{2} = 50$	$13 \times 50 = 650$

Summing up the values:

$$\sum f_i = 23 + 11 + 14 + 15 + 13 = 76$$

$$\sum f_i x_i = 230 + 220 + 420 + 600 + 650 = 2120$$

Now, calculate the mean:

$$\bar{X} = \frac{2120}{76} = 27.89$$

## **Step 2: Find the Median**

The median is the value that divides the dataset into two equal parts. The formula for the median in grouped data is:

$$Median = L + (\frac{\frac{N}{2} - CF}{f}) \times h$$

Where:

- $\bullet$  L = Lower boundary of the median class
- N = Total frequency = 76
- CF = Cumulative frequency before the median class
- f = Frequency of the median class

• h = Class width

## Finding the median class:

$$\frac{N}{2} = \frac{76}{2} = 38$$

We now calculate the **cumulative frequencies (CF)**:

Age group (years)	Frequency $(f_i)$	Cumulative Frequency (CF)
5 - 15	23	23
15 - 25	11	23 + 11 = 34
25 - 35	14	34 + 14 = 48
35 - 45	15	48 + 15 = 63
45 - 55	13	63 + 13 = 76

Since 38 lies in the class 25 - 35, this is our median class.

## Using the formula:

- L = 25
- CF = 34 (cumulative frequency before median class)
- f = 14 (frequency of median class)
- h = 10 (class width)

Median = 
$$25 + (\frac{38 - 34}{14}) \times 10$$
  
=  $25 + (\frac{4}{14}) \times 10$   
=  $25 + (0.286 \times 10)$   
=  $25 + 2.86$   
=  $27.86$ 

## **Step 3: Find the Mode**

The mode is the class with the highest frequency. The formula for the mode in grouped data is:

Mode = 
$$L + (\frac{f_1 - f_0}{2f_1 - f_0 - f_2}) \times h$$

Where:

- L = Lower boundary of modal class
- $f_1$  = Frequency of modal class
- $f_0$  = Frequency before modal class
- $f_2$  = Frequency after modal class
- h = Class width

The modal class is 5 - 15 because it has the highest frequency ( $f_1 = 23$ ).

Using the formula:

• *L* = 5

- $f_1 = 23$
- $f_0 = 0$  (since there is no previous class)
- $f_2 = 11$  (next class frequency)
- h = 10

Mode = 
$$5 + (\frac{23 - 0}{(2 \times 23) - 0 - 11}) \times 10$$
  
=  $5 + (\frac{23}{46 - 11}) \times 10$   
=  $5 + (\frac{23}{35}) \times 10$   
=  $5 + (0.657 \times 10)$   
=  $5 + 6.57$   
=  $11.57$ 

## **Final Answers:**

- Mean = 27.89
- Median = 27.86
- Mode = 11.57

Thus, the values of mean, median, and mode are approximately 27.89, 27.86, and 11.57, respectively.

Let me know if you need further clarification!

solve above problem with full explanation as plain text

Let's solve the given problem step by step.

## **Given Data:**

Class Intervals	0-10	10-20	20-30	30-40	40-50
Frequency (f)	3	5	4	8	2

## **Step 1: Find the Mean**

The formula for the mean in grouped data is:

$$\bar{X} = \frac{\sum f_i x_i}{\sum f_i}$$

Where:

- ullet  $f_i$  is the frequency (number of observations in each class)
- $x_i$  is the midpoint of each class, calculated as:

$$x_i = \frac{\text{Lower Bound} + \text{Upper Bound}}{2}$$

### Compute midpoints ( $x_i$ ):

Class Interval	Frequency ( $f_i$ )	Midpoint $(x_i)$	$f_i x_i$
0 - 10	3	$\frac{0+10}{2}=5$	$3\times 5=15$
10 - 20	5	$\frac{10+20}{2} = 15$	$5 \times 15 = 75$
20 - 30	4	$\frac{20+30}{2} = 25$	$4 \times 25 = 100$
30 - 40	8	$\frac{30+40}{2} = 35$	$8 \times 35 = 280$
40 - 50	2	$\frac{40+50}{2} = 45$	$2 \times 45 = 90$

Summing up the values:

$$\sum f_i = 3 + 5 + 4 + 8 + 2 = 22$$

$$\sum f_i x_i = 15 + 75 + 100 + 280 + 90 = 560$$

Now, calculate the mean:

$$\bar{X} = \frac{560}{22} = 25.45$$

## **Step 2: Find the Median**

The median is the value that divides the dataset into two equal parts. The formula for the median in grouped data is:

$$Median = L + (\frac{\frac{N}{2} - CF}{f}) \times h$$

Where:

- L = Lower boundary of the median class
- N = Total frequency = 22
- ullet CF = Cumulative frequency before the median class
- f = Frequency of the median class
- h = Class width

### Finding the median class:

$$\frac{N}{2} = \frac{22}{2} = 11$$

We now calculate the cumulative frequencies (CF):

Class Interval	Frequency $(f_i)$	Cumulative Frequency (CF)
0 - 10	3	3

Class Interval	Frequency $(f_i)$	Cumulative Frequency (CF)
10 - 20	5	3 + 5 = 8
20 - 30	4	8 + 4 = 12
30 - 40	8	12 + 8 = 20
40 - 50	2	20 + 2 = 22

Since 11 lies in the class 20 - 30, this is our median class.

## Using the formula:

- L = 20
- CF = 8 (cumulative frequency before median class)
- f = 4 (frequency of median class)
- h = 10 (class width)

Median = 
$$20 + (\frac{11 - 8}{4}) \times 10$$
  
=  $20 + (\frac{3}{4}) \times 10$   
=  $20 + (0.75 \times 10)$   
=  $20 + 7.5$   
=  $27.5$ 

## **Final Answers:**

- Mean = 25.45
- Median = 27.5

Thus, the values of mean and median are 25.45 and 27.5, respectively.

Let me know if you need further clarification!

solve above problem with full explanation as plain text

Let's solve the problem step by step.

## **Given Data:**

Classes	0-100	100-200	200-300	300-400	400-500	500-600	600-700
Frequency (f)	23	6	67	3	5	9	10

## **Step 1: Formula for Geometric Mean**

The Geometric Mean (GM) for grouped data is given by:

$$GM = \operatorname{antilog}\left(\frac{\sum f \log x}{\sum f}\right)$$

Where:

- *x* is the **midpoint** of each class interval.
- *f* is the **frequency** of each class.
- $\sum f$  is the total frequency.
- $\sum f \log x$  is the summation of the product of frequency and log of midpoint values.

## Step 2: Compute Midpoints (x)

The midpoint for each class is calculated as:

$$x = \frac{\text{Lower Bound} + \text{Upper Bound}}{2}$$

Classes	Frequency (f)	Midpoint (x)
0 - 100	23	$\frac{0+100}{2} = 50$
100 - 200	6	$\frac{100+200}{2} = 150$
200 - 300	67	$\frac{200+300}{2} = 250$
300 - 400	3	$\frac{300+400}{2} = 350$
400 - 500	5	$\frac{400+500}{2} = 450$
500 - 600	9	$\frac{500+600}{2} = 550$
600 - 700	10	$\frac{600+700}{2} = 650$

## **Step 3: Compute** $\log x$

Now, we calculate  $\log x$  (logarithm base 10 of midpoints) and multiply by frequency ( $f \log x$ ).

Classes	Frequency (f)	Midpoint (x)	$\log x$	$f \log x$
0 - 100	23	50	1.6990	$23 \times 1.6990 = 39.077$
100 - 200	6	150	2.1761	$6 \times 2.1761 = 13.057$
200 - 300	67	250	2.3979	$67 \times 2.3979 = 160.723$
300 - 400	3	350	2.5441	$3 \times 2.5441 = 7.632$
400 - 500	5	450	2.6532	$5 \times 2.6532 = 13.266$
500 - 600	9	550	2.7404	$9 \times 2.7404 = 24.664$
600 - 700	10	650	2.8129	$10 \times 2.8129 = 28.129$

## **Step 4: Compute Geometric Mean**

## Summing up the values

$$\sum f = 23 + 6 + 67 + 3 + 5 + 9 + 10 = 123$$

$$\sum f \log x = 39.077 + 13.057 + 160.723 + 7.632 + 13.266 + 24.664 + 28.129 = 286.548$$

Now, applying the formula:

$$GM = \operatorname{antilog}\left(\frac{286.548}{123}\right)$$

$$GM = antilog(2.3304)$$

Using antilog:

$$GM \approx 213.95$$

## **Final Answer:**

The Geometric Mean (GM) for the given data is 213.95.

This is the complete step-by-step solution. Let me know if you need further clarifications!



solve above problems with full explanation as plain text

## (a) Compare and contrast 'Range' and 'Standard Deviation' as a measure of dispersion.

Dispersion refers to the extent to which data values deviate from the central value (mean, median, mode). Two important measures of dispersion are Range and Standard Deviation.

## **Comparison Table:**

Feature	Range	Standard Deviation
Definition	The difference between the maximum and minimum values in a dataset.	Measures the average deviation of values from the mean.
Formula	Range = Max Value – Min Value	$\sigma = \sqrt{\frac{\sum (x - \bar{x})^2}{N}}$
Ease of Calculation	Very simple to calculate.	More complex, involves squaring deviations from the mean.
Data Consideration	Considers only the two extreme values.	Considers all data points.
Sensitivity to Outliers	Highly sensitive to extreme values.	Less affected by extreme values due to squaring deviations.
Use Case	Used for quick estimates of dispersion.	Used when a detailed measure of spread is needed.

#### **Conclusion:**

- Range is a simple and quick measure but ignores most of the data.
- Standard Deviation provides a more comprehensive measure of dispersion by considering all
  values.

# (b) What is an average? Explain the geometric mean and state its merits and demerits.

### **Definition of Average:**

An average is a single value representing the central tendency of a dataset. Common types of averages include:

- Arithmetic Mean (AM)
- Geometric Mean (GM)
- Median
- Mode

#### Geometric Mean (GM):

The **Geometric Mean** is used to find the average of values that are multiplied together. It is particularly useful for ratios, percentages, and exponential growth.

#### Formula for Geometric Mean:

For a dataset  $x_1, x_2, x_3, ..., x_n$ :

$$GM = (x_1 \times x_2 \times x_3 \times ... \times x_n)^{\frac{1}{n}}$$

For grouped data:

$$GM = \operatorname{antilog}\left(\frac{\sum f \log x}{\sum f}\right)$$

where:

- x = midpoints of class intervals
- f = frequencies

### **Merits of Geometric Mean:**

- 1. More Accurate for Growth Rates: Used for financial, economic, and population growth calculations.
- 2. **Less Affected by Extreme Values:** Unlike the arithmetic mean, GM does not overemphasize high or low values.
- 3. Useful for Ratios and Percentages: Particularly helpful in index numbers, investment returns, etc.
- 4. Mathematically Sound: GM always gives a positive value.

#### **Demerits of Geometric Mean:**

- 1. Complex Calculation: Requires logarithmic calculations, making it difficult by hand.
- 2. Cannot Handle Negative or Zero Values: GM is undefined if any value is zero or negative.
- 3. Difficult to Interpret: Unlike AM, it is not always intuitive.

#### **Conclusion:**

- The **Geometric Mean** is useful for growth-related calculations but is more complex compared to the arithmetic mean.
- Range and Standard Deviation measure dispersion but differ in how they handle data points.

Let me know if you need further clarifications!

solve above problems with full explanation as plain text

### (a) Important Functions of Statistics:

Statistics is a branch of mathematics that deals with data collection, analysis, interpretation, and presentation. The important functions of statistics include:

#### 1. Data Collection and Organization

• Helps in systematic collection and classification of data for analysis.

#### 2. Summarization of Data

 Provides concise representation of large data sets using measures like mean, median, mode, etc.

### 3. Comparison and Interpretation

• Helps compare different data sets and derive meaningful conclusions.

### 4. Prediction and Forecasting

• Assists in making future predictions using statistical models (e.g., population growth, sales forecasting).

### 5. Decision Making

• Used in business, economics, and research to make informed decisions based on data.

### 6. Understanding Relationships

• Determines correlations and dependencies between different variables.

### 7. Quality Control

• Used in industries to maintain and improve product quality through techniques like Six Sigma.

#### 8. Policy Formulation

 Governments and organizations use statistics for planning and policymaking in health, education, and economy.

### (b) Measures of Central Tendency and Their Merits & Demerits

### **Measures of Central Tendency:**

Central tendency refers to the central or typical value in a dataset. The three main measures are:

1. Mean (Arithmetic Mean)

- It is the sum of all observations divided by the number of observations.
- Formula:

$$Mean(\overline{x}) = \frac{\sum x}{n}$$

- Merits:
  - Simple and easy to calculate.
  - Considers all values in the dataset.
  - Suitable for further mathematical analysis.
- Demerits:
  - Affected by extreme values (outliers).
  - Not suitable for skewed distributions.

#### 2. Median

- It is the middle value when data is arranged in ascending or descending order.
- Formula:
  - If *n* is odd:

$$Median = \left(\frac{n+1}{2}\right)^{th} value$$

• If *n* is even:

Median = 
$$\frac{\left(\frac{n}{2}\right)^{th} \text{ value} + \left(\frac{n}{2} + 1\right)^{th} \text{ value}}{2}$$

- Merits:
  - Not affected by extreme values.
  - Useful for skewed distributions.
- Demerits:
  - Ignores all values except the middle one.
  - Cannot be used for further mathematical calculations.

### 3. Mode

- The mode is the most frequently occurring value in a dataset.
- Merits:
  - Easy to identify in discrete data.
  - Useful in qualitative data analysis.
- Demerits:
  - May not be unique (bimodal or multimodal data).
  - Not suitable for mathematical calculations.

### **Conclusion:**

- The choice of central tendency measure depends on the type and distribution of data.
- Mean is best for normal data, Median is ideal for skewed data, and Mode is useful for categorical data.

Let me know if you need more details!