

II. Data exploration & Statistical analyses

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Disease Eco-Evo Lab

In this course we will see:

- How to **explore your data**, verify your model assumptions
- Build simple (lm) and generalized (glm) **linear models**
- Perform simple **ANOVAs** (analyses of variance) and **post-hoc tests**
- How to perform **model comparison** (stepwise regression, using AIC)

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- How to perform **model comparison** (stepwise regression, using AIC)
- Plot your data using **ggplot2** and the **Hmisc** package
- Useful tips to organize your layout, change the legends, etc.
- Export your plot in **high resolution** (for publication / presentation...)

Mind the dogs !



The **Listen** Dog



The **Do** Dog

Is your data well organized?



| | A | B | C | D | E | F | G | H | I | J |
|----|----------|-------------|---------|-----------|-----------------|----------|-----------|----------|-------------|---|
| 1 | Exposure | Food | Clone | Replicate | Total_offspring | Survived | Age_death | Infected | Spore_count | |
| 2 | Control | Scenedesmus | AMME_12 | 1 | 17 | 1 | 35 | 0 | 0 | |
| 3 | Control | Scenedesmus | AMME_12 | 2 | 11 | 1 | 35 | 0 | 0 | |
| 4 | Control | Scenedesmus | AMME_12 | 3 | 13 | 1 | 35 | 0 | 0 | |
| 5 | Control | Scenedesmus | AMME_12 | 4 | 12 | 1 | 35 | 0 | 0 | |
| 6 | Control | Scenedesmus | AMME_12 | 5 | 19 | 1 | 35 | 0 | 0 | |
| 7 | Control | Scenedesmus | AMME_12 | 6 | 16 | 1 | 35 | 0 | 0 | |
| 8 | Control | Scenedesmus | AMME_12 | 7 | 12 | 1 | 35 | 0 | 0 | |
| 9 | Control | Scenedesmus | AMME_12 | 8 | 2 | 0 | 7 | 0 | 0 | |
| 10 | Control | Scenedesmus | AMME_12 | 9 | 9 | 1 | 35 | 0 | 0 | |
| 11 | Control | Scenedesmus | AMME_12 | 10 | 11 | 1 | 35 | 0 | 0 | |
| 12 | Control | Scenedesmus | AMME_12 | 11 | 12 | 1 | 35 | 0 | 0 | |
| 13 | Control | Scenedesmus | AMME_12 | 12 | 9 | 1 | 35 | 0 | 0 | |
| 14 | Control | Scenedesmus | AMME_12 | 13 | 11 | 1 | 35 | 0 | 0 | |
| 15 | Control | Scenedesmus | AMME_12 | 14 | 11 | 1 | 35 | 0 | 0 | |
| 16 | Control | Scenedesmus | AMME_12 | 15 | 13 | 1 | 35 | 0 | 0 | |
| 17 | Control | Scenedesmus | AMME_12 | 16 | 14 | 1 | 35 | 0 | 0 | |
| 18 | Control | Scenedesmus | AMME_12 | 17 | 17 | 1 | 35 | 0 | 0 | |
| 19 | Control | Scenedesmus | AMME_12 | 18 | 18 | 1 | 35 | 0 | 0 | |
| 20 | Control | Scenedesmus | AMME_12 | 19 | 6 | 0 | 18 | 0 | 0 | |
| 21 | Control | Scenedesmus | AMME_12 | 20 | 13 | 1 | 35 | 0 | 0 | |
| 22 | Control | Scenedesmus | MUGG_23 | 1 | 12 | 1 | 35 | 0 | 0 | |
| 23 | Control | Scenedesmus | MUGG_23 | 2 | 4 | 0 | 6 | 0 | 0 | |

What you control

What you measure

Is your data well organized?



| | A | B | C | D | E | F | G | H | I | J |
|----|----------|-------------|---------|-----------|-----------------|----------|-----------|----------|-------------|---|
| 1 | Exposure | Food | Clone | Replicate | Total_offspring | Survived | Age_death | Infected | Spore_count | |
| 2 | Control | Scenedesmus | AMME_12 | 1 | 17 | 1 | 35 | 0 | 0 | |
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| 4 | Control | Scenedesmus | AMME_12 | 3 | 13 | 1 | 35 | 0 | 0 | |
| 5 | Control | Scenedesmus | AMME_12 | 4 | 12 | 1 | 35 | 0 | 0 | |
| 6 | Control | Scenedesmus | AMME_12 | 5 | 19 | 1 | 35 | 0 | 0 | |
| 7 | Control | Scenedesmus | AMME_12 | 6 | 16 | 1 | 35 | 0 | 0 | |
| 8 | Control | Scenedesmus | AMME_12 | 7 | 12 | 1 | 35 | 0 | 0 | |
| 9 | Control | Scenedesmus | AMME_12 | 8 | 2 | 0 | 7 | 0 | 0 | |
| 10 | Control | Scenedesmus | AMME_12 | 9 | 9 | 1 | 35 | 0 | 0 | |
| 11 | Control | Scenedesmus | AMME_12 | 10 | 11 | 1 | 35 | 0 | 0 | |
| 12 | Control | Scenedesmus | AMME_12 | 11 | 12 | 1 | 35 | 0 | 0 | |
| 13 | Control | Scenedesmus | AMME_12 | 12 | 9 | 1 | 35 | 0 | 0 | |
| 14 | Control | Scenedesmus | AMME_12 | 13 | 11 | 1 | 35 | 0 | 0 | |
| 15 | Control | Scenedesmus | AMME_12 | 14 | 11 | 1 | 35 | 0 | 0 | |
| 16 | Control | Scenedesmus | AMME_12 | 15 | 13 | 1 | 35 | 0 | 0 | |
| 17 | Control | Scenedesmus | AMME_12 | 16 | 14 | 1 | 35 | 0 | 0 | |
| 18 | Control | Scenedesmus | AMME_12 | 17 | 17 | 1 | 35 | 0 | 0 | |
| 19 | Control | Scenedesmus | AMME_12 | 18 | 18 | 1 | 35 | 0 | 0 | |
| 20 | Control | Scenedesmus | AMME_12 | 19 | 6 | 0 | 18 | 0 | 0 | |
| 21 | Control | Scenedesmus | AMME_12 | 20 | 13 | 1 | 35 | 0 | 0 | |
| 22 | Control | Scenedesmus | MUGG_23 | 1 | 12 | 1 | 35 | 0 | 0 | |
| 23 | Control | Scenedesmus | MUGG_23 | 2 | 4 | 0 | 6 | 0 | 0 | |

Explanatory variables
(Factors)

Response variables
(Continuous, Binomial...)

Export your data safely (as .csv)

1138 | fx Σ = 72984

| | A | B | C | D | E | F | G | H | I | J | K |
|----|----------|-------------|---------|-----------|-----------------|----------|-----------|----------|-------------|---|---|
| 1 | Exposure | Food | Clone | Replicate | Total_offspring | Survived | Age_death | Infected | Spore_count | | |
| 2 | Control | Scenedesmus | AMME_12 | 1 | 17 | 1 | 35 | 0 | 0 | | |
| 3 | Control | Scenedesmus | AMME_12 | 2 | | | | | | | |
| 4 | Control | Scenedesmus | AMME_12 | 3 | | | | | | | |
| 5 | Control | Scenedesmus | AMME_12 | 4 | | | | | | | |
| 6 | Control | Scenedesmus | AMME_12 | 5 | | | | | | | |
| 7 | Control | Scenedesmus | AMME_12 | 6 | | | | | | | |
| 8 | Control | Scenedesmus | AMME_12 | 7 | | | | | | | |
| 9 | Control | Scenedesmus | AMME_12 | 8 | | | | | | | |
| 10 | Control | Scenedesmus | AMME_12 | 9 | | | | | | | |
| 11 | Control | Scenedesmus | AMME_12 | 10 | | | | | | | |
| 12 | Control | Scenedesmus | AMME_12 | 11 | | | | | | | |
| 13 | Control | Scenedesmus | AMME_12 | 12 | | | | | | | |
| 14 | Control | Scenedesmus | AMME_12 | 13 | | | | | | | |
| 15 | Control | Scenedesmus | AMME_12 | 14 | | | | | | | |
| 16 | Control | Scenedesmus | AMME_12 | 15 | | | | | | | |
| 17 | Control | Scenedesmus | AMME_12 | 16 | | | | | | | |
| 18 | Control | Scenedesmus | AMME_12 | 17 | 17 | 1 | 35 | 0 | 0 | | |
| 19 | Control | Scenedesmus | AMME_12 | 18 | 18 | 1 | 35 | 0 | 0 | | |
| 20 | Control | Scenedesmus | AMME_12 | 19 | 6 | 0 | 18 | 0 | 0 | | |
| 21 | Control | Scenedesmus | AMME_12 | 20 | 13 | 1 | 35 | 0 | 0 | | |
| 22 | Control | Scenedesmus | MUGG_23 | 1 | 12 | 1 | 35 | 0 | 0 | | |
| 23 | Control | Scenedesmus | MUGG_23 | 2 | 4 | 0 | 6 | 0 | 0 | | |

Export Text File

Field Options

Character set: Western Europe (Windows-1252/WinLatin 1)

Field delimiter: ;

String delimiter: "

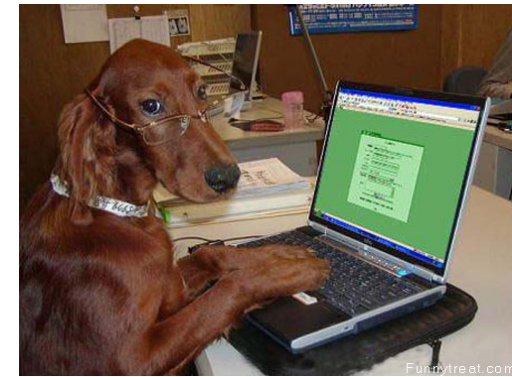
☒ Save cell content as shown

☐ Save cell formulae instead of calculated values

☒ Quote all text cells

☐ Fixed column width

Help OK Cancel



The purpose of statistical analyses



- You need an objective, non-biased tool to confirm (or disprove) the differences that you THINK you can see on your plots
- Otherwise, the goal is basically the same as plotting your data: you want to use **explanatory variables** (your x-axis, facet, colours...) to explain **differences in your response variable** (your y-axis)
- Therefore, if you know what kind of plot you want to make out of your data, then **you already know which statistical analyses you want to run !**

“Your hypothesis, is your plot, is your model”

Kate Laskowski, ca. 2019

Factors and levels



- In this course we will only focus on explanatory variables that take the form of **Factors** (as opposed to continuous variables)

| Factor | Dose |
|---------------|----------------|
| Factor levels | - No pesticide |
| | - Low dose |
| | - High Dose |
| | |

3

| Variable | Dose |
|----------|------|
| Values | 0 |
| | ... |
| | 1.57 |
| | ... |
| | 5.43 |
| | ... |
| | 9.67 |
| | ... |

∞

Factors and levels

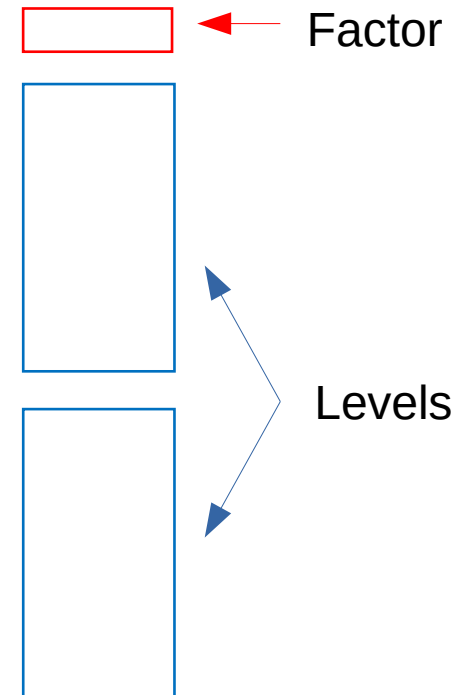


- In laboratory experiments, you often apply **treatments** to your organisms of interest
- For instance, you could expose your organism to **different diets**, or incubate them at different **temperatures**
- If you organized your data correctly, then remember that your **factors should be placed as header** (either *Food*, or *Temperature*), which can contain **several levels** (groups of rows with the same name)

Factors and levels



| | A | B | C | D | E | F | G | H | I | J |
|----|----------|-------------|---------|-----------|-----------------|----------|-----------|----------|-------------|---|
| 1 | Exposure | Food | Clone | Replicate | Total_offspring | Survived | Age_death | Infected | Spore_count | |
| 2 | Control | Scenedesmus | AMME_12 | 1 | 17 | 1 | 35 | 0 | 0 | |
| 3 | Control | Scenedesmus | AMME_12 | 2 | 11 | 1 | 35 | 0 | 0 | |
| 4 | Control | Scenedesmus | AMME_12 | 3 | 13 | 1 | 35 | 0 | 0 | |
| 5 | Control | Scenedesmus | AMME_12 | 4 | 12 | 1 | 35 | 0 | 0 | |
| 6 | Control | Scenedesmus | AMME_12 | 5 | 19 | 1 | 35 | 0 | 0 | |
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| 8 | Control | Scenedesmus | AMME_12 | 7 | 12 | 1 | 35 | 0 | 0 | |
| 9 | Control | Scenedesmus | AMME_12 | 8 | 2 | 0 | 7 | 0 | 0 | |
| 10 | Control | Scenedesmus | AMME_12 | 9 | 9 | 1 | 35 | 0 | 0 | |
| 11 | Control | Scenedesmus | AMME_12 | 10 | 11 | 1 | 35 | 0 | 0 | |
| 12 | Control | Scenedesmus | MUGG_23 | 1 | 12 | 1 | 35 | 0 | 0 | |
| 13 | Control | Scenedesmus | MUGG_23 | 2 | 4 | 0 | 6 | 0 | 0 | |
| 14 | Control | Scenedesmus | MUGG_23 | 3 | 11 | 1 | 35 | 0 | 0 | |
| 15 | Control | Scenedesmus | MUGG_23 | 4 | 9 | 1 | 35 | 0 | 0 | |
| 16 | Control | Scenedesmus | MUGG_23 | 5 | 12 | 1 | 35 | 0 | 0 | |
| 17 | Control | Scenedesmus | MUGG_23 | 6 | 13 | 1 | 35 | 0 | 0 | |
| 18 | Control | Scenedesmus | MUGG_23 | 7 | 6 | 0 | 12 | 0 | 0 | |
| 19 | Control | Scenedesmus | MUGG_23 | 8 | 12 | 1 | 35 | 0 | 0 | |
| 20 | Control | Scenedesmus | MUGG_23 | 9 | 9 | 1 | 35 | 0 | 0 | |
| 21 | Control | Scenedesmus | MUGG_23 | 10 | 9 | 1 | 35 | 0 | 0 | |
| 22 | Control | Microcystis | AMME_12 | 1 | 2 | 0 | 28 | 0 | 0 | |
| 23 | Control | Microcystis | AMME_12 | 2 | 2 | 1 | 25 | 0 | 0 | |



ANOVA vs. t-test



- t-tests can be performed when you want to **compare the mean of only two groups:**

(example: one factor, two levels → the '**pills**' group and the '**placebo**' group)

- ANOVAS should be performed when you want to **compare the means of at least three groups:**

(example 1: one factor, three levels → the '**pills**', '**placebo**' and '**control**' group)

One-Way ANOVA

(example 2: two factors, two levels → '**pills**' or '**placebo**' X '**sleep**' or '**no sleep**') |

Two-Way ANOVA

ANOVA: the principles



- Like other classical statistical tests, we calculate a test statistic (the F-ratio) with which we can obtain **the probability of obtaining the data assuming the null hypothesis** (the P-value).
- A significant P-value (usually taken as $P < 0.05$) suggests that **at least one group mean is significantly different from the others**.

Null hypothesis: all population means are equal

Alternative hypothesis: at least one population mean is different from the rest.

ANOVA: the principles



- ANOVA separates the variation in the dataset into 2 parts: **between-group** and **within-group**.

(NB: These variations are called the **sums of squares**)

- The **F-ratio** is then calculated as:

$$\frac{\text{Mean between-group SS}}{\text{Mean within-group SS}}$$

→ If the average difference between groups is **similar to that within groups**, the **F ratio is about 1**.

→ As the average difference between groups becomes **greater than that within groups**, the **F ratio becomes larger than 1**.

Linear models



- In order to perform an analysis of variance (ANOVA), you first need to **fit a linear model to your data**.
- Basically, your data becomes presented as a **formula** that resembles a mathematical function:

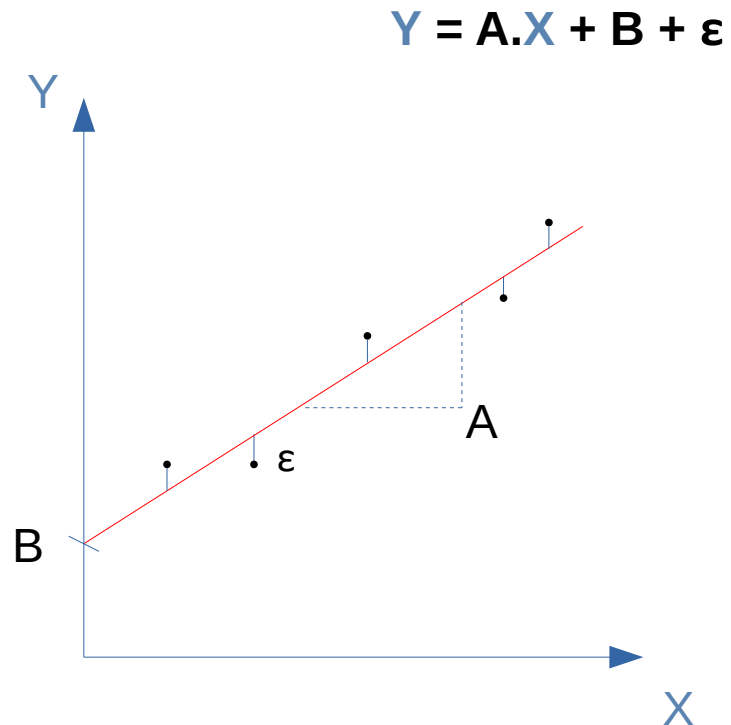
$$Y = A.X + (B) + \epsilon$$

- **Y** is a matrix containing a set of measurements on each of the **dependent variables**
- **X** is your design matrix (observations on each of the **independent variables**)
- **A** is a matrix containing parameters, determines the **slope** of your plot
- **B** determines the **intercept** of your plot (when different from 0)
- **ϵ** is the error matrix, containing the **residuals**

Linear models



- In order to perform an analysis of variance (ANOVA), you first need to **fit a linear model to your data**.
- Basically, your data becomes presented as a **formula** that resembles a mathematical function:





Please progress forward to Step 3 !

Post-hoc tests



- The information that you get from an ANOVA is often incomplete: at least one group mean is significantly different from the others !
- For instance, you could be working with a factor that has **more than two levels** (Treatments: T1 to T4) and 'treatment' comes out as significant in your ANOVA. In that case, **you still don't know if all treatments are different from one another**, or if maybe only one is bad for the health, while the other three are comparable !
- In that case, you want to follow your ANOVA by **post-hoc tests**, which occur 'after' your main analysis.

Post-hoc tests



- One common and popular method of post-hoc analysis is **Tukey's HSD test** ('Honestly Significant Difference'). Tukey's test **compares the means of all treatments to the mean of every other treatment**.
- In general, HSD is preferred when you want to make all the possible comparisons between a large set of means (**six or more means**) and is considered the best available method when confidence intervals are desired, or **if sample sizes are unequal**.

Tukey's HSD Post Hoc

The **HSD** is the least amount that means must vary from each other to be significantly different

$$HSD = q \sqrt{\frac{MS_w}{n_k}} \quad HSD = 4.05 \sqrt{\frac{1.20}{5}} = 1.98$$

q = constant (STUDENTIZED RANGE q TABLE)
 MS_w = mean square within
 n_k = number in each category (n for one condition)

| Means |
|--------------|
| $M_1 = 1.00$ |
| $M_2 = 1.40$ |
| $M_3 = 3.60$ |
| $M_4 = 4.20$ |

The minimum difference between means must be **1.98** for significance.

Slide 40

TODD DANIEL

Post-hoc tests



- There are other ways to perform post-hoc tests, all of which should be able to be performed in R (either with base functions or via specific packages). For instance:

Fisher's LSD (Least Significant Difference): This test is the most liberal of all Post Hoc tests. The critical t for significance is unaffected by the number of groups. This test is generally not considered appropriate if you have more than 3 means.

Dunn's t-test: In general, this test should be used when the number of comparisons you are making exceeds the number of degrees of freedom you have between groups (e.g. $K-1$). This test is extremely conservative and rapidly reduces power as the number of comparisons being made increase.



Please progress forward to Step 6 !

Generalized linear models



- The ‘simple’ linear model that we’ve been using so far is actually a specific case of a broader class of linear models, which are called ‘**generalized**’ (because they are not limited to normally distributed data, and can be used in many other cases).
- In ‘generalized’ linear models (or GLMs), each outcome (Y) of the dependent variables is assumed to be generated from a particular distribution in an exponential **family**, that includes the normal (gaussian), as well as **non-normal probability distributions**.
- GLMs always contain a ‘**link function**’, which provides the relationship between the linear predictor and the mean of the distribution function.

| Distribution | Support of distribution | Typical uses | Link name | Link function, $\mathbf{X}\beta = g(\mu)$ | Mean function |
|--------------|----------------------------|--|-----------|--|-------------------------------|
| Normal | real: $(-\infty, +\infty)$ | Linear-response data | Identity | $\mathbf{X}\beta = \mu$ | $\mu = \mathbf{X}\beta$ |
| Poisson | integer: $0, 1, 2, \dots$ | count of occurrences in fixed amount of time/space | Log | $\mathbf{X}\beta = \ln(\mu)$ | $\mu = \exp(\mathbf{X}\beta)$ |

Generalized linear models



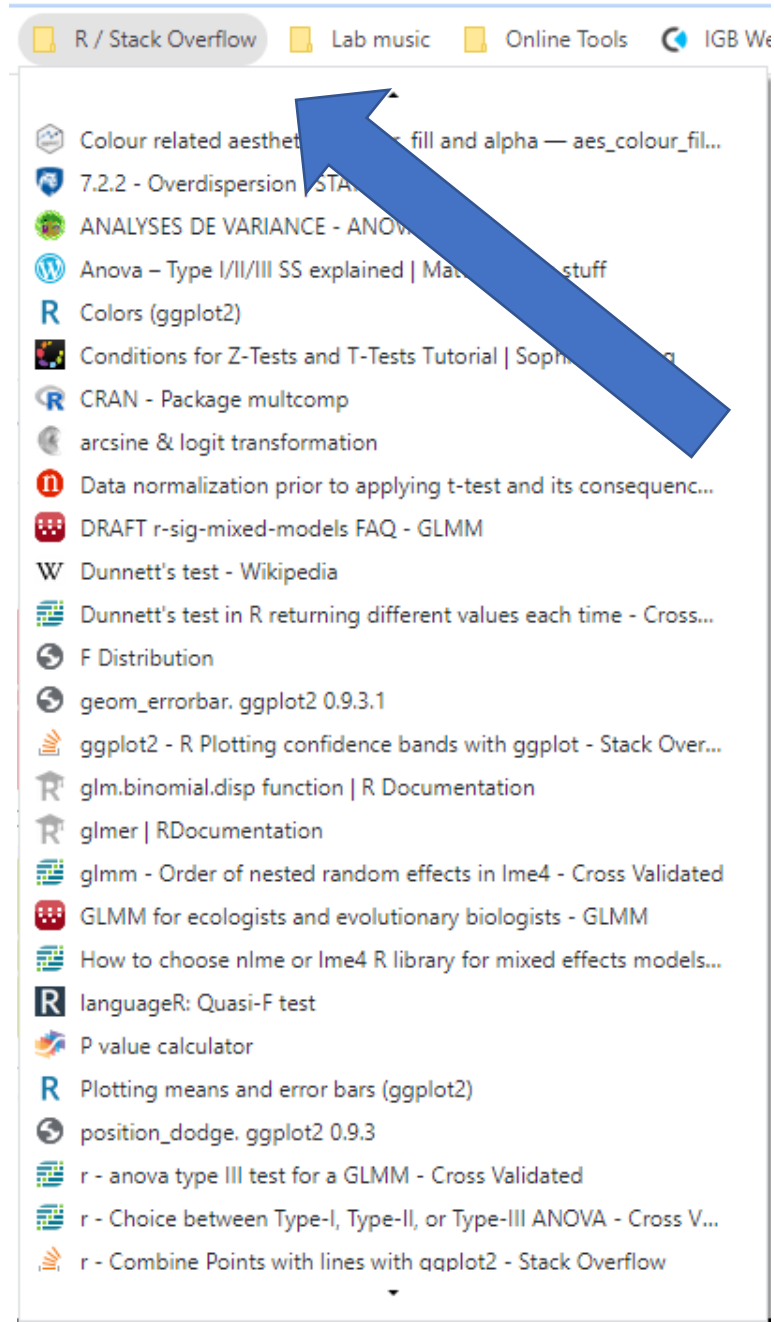
Generalized linear models are fit using the `glm()` function. The form of the `glm` function is

```
glm(formula, family=family(link=linkfunction), data=)
```

| Family | Default Link Function |
|---------------|-----------------------|
| gaussian | (link = "identity") |
| binomial | (link = "logit") |
| Gamma | (link = "inverse") |
| poisson | (link = "log") |
| quasibinomial | (link = "logit") |
| quasipoisson | (link = "log") |

Useful tips:

- Stack Overflow is your friend !
- If you found a page helpful, **save it** under a safe directory !



This way, you won't have to look for it ever again !

Stack Overflow & distraction !

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1 Answer

active oldest votes

1

In your initial model summary, `Estimate` is showing the estimated difference in mean for each group relative to the mean of the "listen" group (40.615). The "read2" group, has the largest shift (+20.885) away from the "listen" group is called significant with `p = .0340` when only these 4 comparisons are calculated.

Since `TUKEYHSD` is performing all pairwise comparisons for the group means (not just to reference level "listen" anymore), it is also performing p-value adjustments to account for all of these extra tests. Reason being, if you performed 20 comparisons on random data you'd expect one (1/20 or .05) to be called significant with `p < .05` simply because of doing that many tests. With the p-value adjustment factored in, your originally significant comparison between "listen - read2" no longer qualifies as significant.

But the larger difference between "watch2 - read2" (-32.3), which wasn't tested in the original model summary, is large enough to be considered significant with `p = .03688` even after doing all of the extra comparison adjusting.

Hope that helps, you can read more about the multiple comparisson problem [here](#) . And see `? p.adjust` for R's implementation of the most popular methods.

share improve this answer

answered Jan 8 '17 at 1:51

Nate

7,830 ● 1 ● 24 ● 33

1 R-Backtesting of a Model

Hot Network Questions

Count unique features of points inside polygon in QGIS 3.10

Could corroded or incorrectly soldered battery teminals cause parasitic drain?

Is there anything that can create a fire that burns underwater?

Macroeconomics for Mathematicians

Three statements that contradict each other

Would a 50 mph aircraft holding a ground pattern in a 20 mph cross wind risk stalling by abruptly rolling away from a crosswind?

As a contractor, how do I ask my employer for a new laptop?

Latex vs Groff for mathematics formatting

Double deck vs wide body airliner, why would anyone build a double deck one?

Layoffs are coming at my company. I want to volunteer instead of a co-worker. Problem is, I am not supposed to know

What is this unusual structure inside this banana?

Symbol `\perp` with a shorter horizontal line to be