

- Welcome to **PS + DSA** Module 🌟
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Programming constructs  
Problem solving (efficient)

0-1 count of factors

12 → 1, 2, 3, 4, 6, 12

24 → 1, 2, 3, 4, 6, 8, 12, 24

10 → 1, 2, 5, 10

N, factors → 1 to N

```

int countFactors (int N) {
    int count = 0;

    for (int i = 1; i <= N; i++) {
        if (N % i == 0) {
            // i is a factor of N
            count++;
        }
    }

    return count;
}

```

N = 10

i → 1 2 3 4 5 6 7 8 9 10

count = ~~0~~ ~~1~~ ~~2~~ ~~3~~ 4

**iterations: N**

Execution time

→ value of  $N$

→ system configuration

Assumption

$10^8$  iterations per seconds

$N$	iteration( $N$ )	time
$10^8$	$10^8$	1 Sec
$10^9$	$10^9$	10 Sec
$10^{18}$	$10^{18}$	$10^{10}$ Sec $\approx 317 \text{ years}$

$$10^8 \text{ itr} \rightarrow 1 \text{ Sec}$$

$$1 \text{ itr} \rightarrow \frac{1}{10^8} \text{ sec}$$

$$10^9 \text{ itr} \rightarrow \frac{1}{10^8} \times 10^9$$

$$= 10 \text{ Sec}$$

$$1 \text{ itr} \rightarrow \frac{1}{10^8} \text{ Sec}$$

$$10^{18} \text{ itr} \rightarrow \frac{1}{10^8} \times 10^{18}$$

$$= 10^{10} \text{ Sec}$$

## improvisation

$i \times j = N$  (both  $i$  and  $j$  are factors of  $N$ )

$j = \frac{N}{i}$  (both  $i$  and  $N/i$  are factors of  $N$ )

$N = 24$

$i$	$N/i$
1	24
2	12
3	8
4	6
6	4
8	3
12	2
24	1

$$i \leq \frac{N}{i}$$

$$i \times i \leq N$$

$$i^2 \leq N$$

$$i \leq \sqrt{N}$$

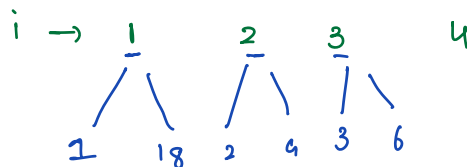
$N = 100$

$i$	$N/i$
1	100
2	50
4	25
5	20
10	10
20	5
25	4
50	2
100	1

Observation: a) All factors of  $N$  are present in first half.  
 b) we are in first half till  $i \leq \sqrt{N}$

$N = 18$

loop  $i: 1$  to  $\sqrt{N}$



```
int countFactors (int N) {
```

$N = 24$

```
    int count = 0;
```

$\sqrt{24} = 4$

```
    for (int i = 1; i <= sqrt(N); i++) {
```

```
        if (N % i == 0) {
```

```
            if (i == N/i) {
```

```
                count++;
```

```
            }
```

```
        else {
```

```
            // both i and N/i are factors of N
```

```
            count += 2;
```

```
        }
```

```
    }
```

```
    }
```

```
    return count;
```

```
}
```

i	count	
1	2	(1, 24)
2	4	(2, 12)
3	6	(3, 8)
4	8	(4, 6)
5	end of loop	

```
int countFactors (int N) {
```

```
    int count = 0;
```

```
    for (int i = 1; i <= sqrt(N); i++) {
```

```
        if (N % i == 0) {
```

```
            if (i == N/i) {
```

```
                count++;
```

```
            }
```

```
        else {
```

```
            // both i and N/i are factors of N
```

```
            count += 2;
```

```
        }
```

```
    }
```

```
}
```

```
return count;
```

```
}
```

$N = 36$

$\sqrt{36} = 6$

i	count	
1	2	1, 36
2	4	2, 18
3	6	3, 12
4	8	4, 9
5		
6	9	6, 6

```
int countFactors (int N) {
```

```
    int count = 0;
```

```
    for (int i = 1; i <=  $\sqrt{N}$ ; i++) {
```

```
        if (N % i == 0) {
```

```
            if (i == N/i) {
```

```
                count++;
```

```
            }
```

```
        } else {
```

```
            // both i and N/i are factors of N
```

```
            count += 2;
```

```
        }
```

```
    }
```

```
}
```

```
return count;
```

```
}
```

$N = 100$

$\sqrt{100} = 10$

i	count	i, N/i
1	2	1, 100
2	4	2, 50
3		
4	6	4, 25
5	8	5, 20
6		
7		
8		
9		
10	9	10, 10

iterations:  $\sqrt{N}$

N	iterations ( $\sqrt{N}$ )	time
$10^{18}$	$10^9$	10 sec

$10^8$  itr  $\rightarrow$  1 sec

$10^9$  itr  $\rightarrow \frac{1}{10^8} \times 10^9$   
= 10 sec

Q.2 Check whether given no. is prime or not.

Prime no.  $\rightarrow$  only two factors (1 and no. itself)

{ 10, 11, 23, 2, 25, 27, 31 }

$\rightarrow$  prime no. : 11 23 2 31

```
boolean isPrime(int N) {  
    |  
    if (countFactors(N) == 2) {  
        |  
        return true;  
    }  
    else {  
        |  
        return false;  
    }  
}
```

$\sqrt{N}$  iterations

```
int temp = (int) Math.sqrt(N);
```

$\hookrightarrow$   
 $\sqrt{N}$

Q-1 Reverse an array.

A = { 10 20 30 40 50 }

0      1      2      3      4

50      40      30      20      10

{ ~~10~~ ~~20~~ 30 ~~40~~ ~~50~~ }

0      1      2      3      4

S  
e

S	e
0	4
1	3
2	2

A = { 10 20 30 40 50 60 }

0      1      2      3      4      5

60      50      40      30      20      10

{ ~~10~~ ~~20~~ ~~30~~ ~~40~~ ~~50~~ ~~60~~ }

0      1      2      3      4      5

e      S

S	e
0	5
1	4
2	3
3	2

do swap till  $S < e$



```
void reverse (int [] A) {
```

```
    int n = A.length;
```

```
    int s = 0;
```

```
    int e = n-1;
```

```
    while (s < e) {
```

```
        // swap A[s] and A[e]
```

```
        int temp = A[s];
```

```
        A[s] = A[e];
```

```
        A[e] = temp;
```

```
        s++;
```

```
        e--;
```

```
    }
```

```
}
```

A =

	50	40		20	10
{	<del>10</del>	<del>20</del>	30	<del>40</del>	<del>50</del> }
	0	1	2	3	4

s  
e

A =

	10	40	10	10
{	<del>10</del>	<del>10</del>	<del>40</del>	<del>10</del> }
	0	1	2	3

e   s

Q-4 Reverse part of an Array.

A =

2	10	20	19	14	50	60	80	12
0		1	2	3	4	5	6	7

S = 2  
e = 5

3	10	20	60	50	14	14	80	12	3
0	1	2	3	4	5	6	7		

```
void reversePart (int[] A, int s, int e) {
```

```
while (s < e) {
```

11 swap  $A[s]$  and  $A[e]$

$$5 = 2$$

```
int temp = A[S];
```

$$e = 5$$
$$A[s] = A[e];$$

A[e] = temp;

$$A = \begin{matrix} & & & 7 & 6 & 4 & 1a \\ \begin{matrix} 3 \\ 0 \end{matrix} & 10 & 20 & \cancel{1a} & \cancel{4} & \cancel{8} & \cancel{7} & 133 \\ & & & 0 & 1 & 2 & 3 & 4 & 5 & 6 \end{matrix}$$
$$S \vdash \cdot$$

9- - ;

3

3

Q-6 Given an array, rotate it K times from last to first.

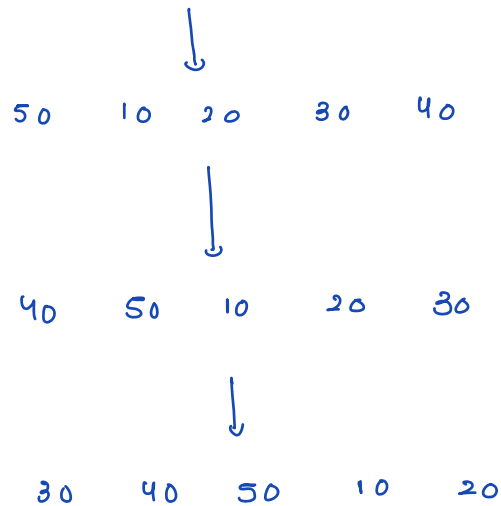
Google, Amazon

Note → i) don't create extra array

ii) do it efficient

A = 10 20 30 40 50

K = 3

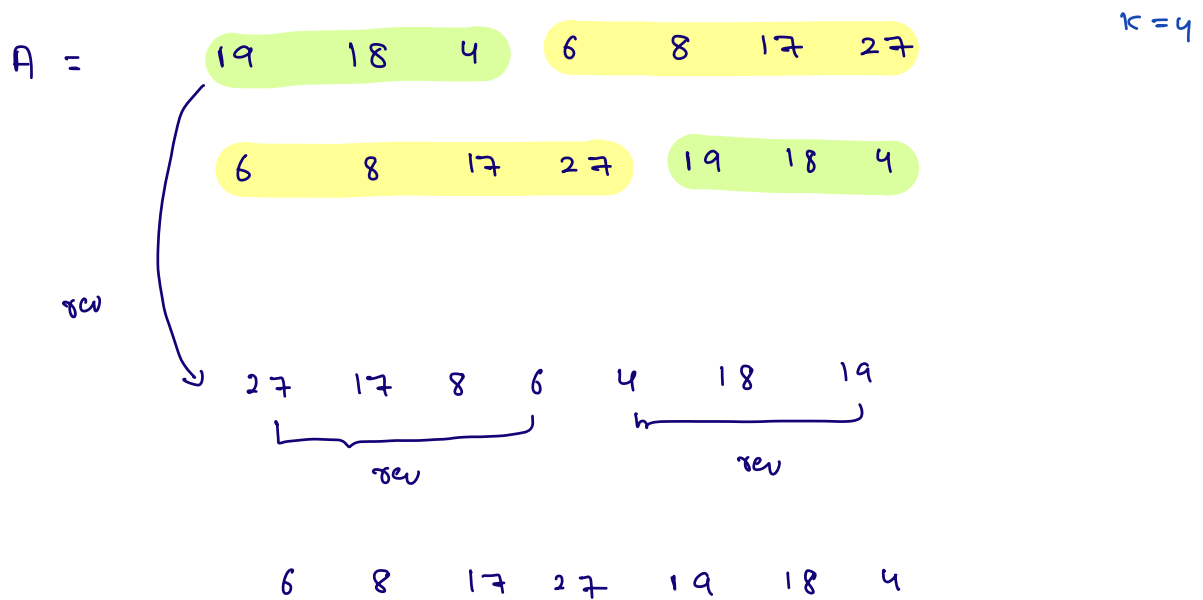
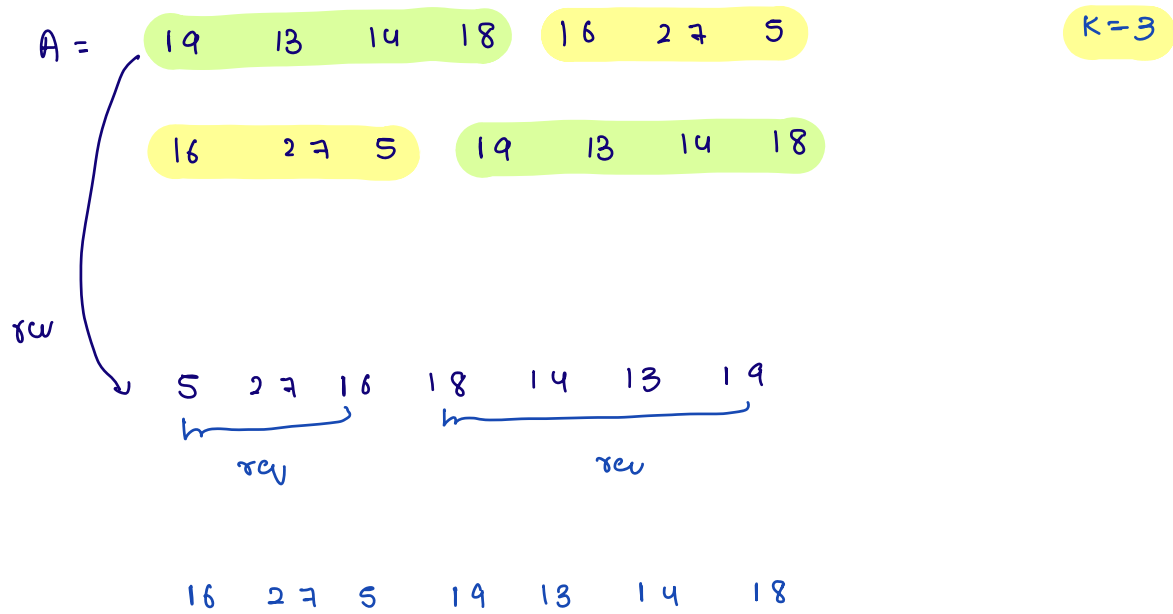


A =

19 18 16 48 36 44 39

K = 4

48 36 44 39 19 18 16



Obs:

- i) reverse complete array
- ii) reverse first k elements
- iii) reverse the remaining array.

k=4

```
void rotate (int[] A, int k) {
```

```
    int n = A.length;
```

```
    reversePart (A, 0, n-1);
```

```
    reversePart (A, 0, k-1);
```

```
    reversePart (A, k, n-1);
```

}

A =

10	20	30	19	14	16	18
0	1	2	3	4	5	6



19	14	16	19	10	20	30
<del>18</del>	<del>16</del>	<del>14</del>	<del>19</del>	<del>30</del>	<del>20</del>	<del>10</del>
0	1	2	3	4	5	6

19	14	16	18	10	20	30
----	----	----	----	----	----	----

k > A.length

```
void rotate (int[] A, int k) {
```

```
    int n = A.length;
```

```
    reversePart (A, 0, n-1); ✓
```

```
    reversePart (A, 0, k-1);
```

```
    reversePart (A, k, n-1);
```

}

k=12

A = 10 20 30 40 50

n=5

} Array index  
out of bound

10 20 30 40



40 10 20 30



30 40 10 20



20 30 40 10



10 20 30 40

$$K=4$$

$$n=4$$

$$n=5$$

$$K=12$$

$$nx: 2$$

$$n=6$$

$$K=27$$

$$nx: 3$$

```
void rotate (int[] A, int k) {
```

```
    int n = A.length;
```

```
    k = k % n;
```

```
    reversePart (A, 0, n-1);
```

```
    reversePart (A, 0, k-1);
```

```
    reversePart (A, k, n-1);
```

```
}
```

$n = 5$

$k = 3$

$k = 3 \% 5$   
 $= 3$

$n = 5$

$k = 29$

$k = 29 \% 5$   
 $= 4$

## log basics

$$\log_b a$$

(b power what is equals to a)

$$\log_b a = c$$

$$b^c = a$$

$$\log_2 8 = 3$$

$$\log_2 64 = 6$$

$$\log_{10} 10000 = 4$$

$$\log_3 81 = 4$$

$$\log_2 31 = \underline{4.954}$$

$\hookrightarrow \text{int} \Rightarrow 4$

$$\log_4 16 = 2$$

$$\log_3 27 = 3$$

\*\*\*

$$\text{i) } N = 2^k$$

$$k = \log_2 N$$

$$\text{ii) } \log_b b^N = N$$



## Problem Solving and DSA

- Time complexity
- Arrays : Prefix sum, subarrays, sliding window, 2D matrices.
- Bit manipulation
- Hashing
- Recursion
- Sorting
- Searching
- 2 pointer technique
- Strings
- Linked list
- Trees, BST, heaps
- Dynamic programming
- Graphs

52 classes

Divide by 5

$$12 \div 5 \rightarrow 2$$

$$\begin{array}{r} 2 \\ 5 \overline{) 12} \\ \underline{10} \\ 2 \end{array}$$

$$3 \div 5 \rightarrow 0$$

$$\begin{array}{r} 0 \\ 5 \overline{) 3} \end{array}$$

19	18	16	18	13	35	47
0	1	2	3	4	5	6

$$K = 5$$

print:  $n-K$  to  $n-1$   
last  $K$  values

print:  $0$  to  $n-K-1$   
first  $K$  values