YGAMMAS: Improving Mathematical Reasoning in Vision Language Models Through Synthetic Data Generation

Ramgopal Venkateswaran, Shubhra Mishra {ram1998, shubhra}@stanford.edu

Background

- MATHVISTA: Created a finegrained-benchmark for mathematical reasoning in VLMs
- **GSM8K/MATH:** Presented benchmarks for mathematical reasoning in LLMs for K-8 and high-school-level reasoning, respectvely
- Textbooks Are All You Need: demonstrated the importance of high-quality data by training Phi-1 using synthetic textbook-quality data

Problem Statement

Improving VLMs for math-problem solving tasks requires us to be able to generate synthetic high-quality training data without using VLMs in the loop, and then finetuning them with computationally efficient methods.

Contributions

- We propose GAMMAS: a pipeline to Generate Advanced Multi-modal Mathematical And Synthetic data. Overall, we generate 860 training samples and a validation set of size 200, comprising questions that test visual reasoning using bar charts and line plots.
- We finetune InternLM-XComposer2-VL-1.8B, using our generated training data
- We evaluate its performance both with the MATHVISTA "testmini" dataset and our own validation set. Within MATHVISTA, we investigate the performance improvement on not just line plot and bar chart based questions, but also on other related categories to understand the transfer learning capabilities of the model.

Evaluating Our Fine-Tuned Models

- Input: a mathematical question with a relevant image and multiple choice answers (letters and yes/no questions)
- Output: a multiple choice answer
- Evaluation metric: accuracy on various subsections of testmini (TestM) and our own validation set (GVal)
 - TestM-B: testmini bar chart questions
 - TestM-L: testmini line chart questions
 - TestM-B: testmini non-bar-and-line-chart questions
 - GVal-B: bar chart questions in the validation set we create
 - GVal-L: line chart questions in the validation set we create

Dataset & Methods

GAMMAS: Generating Advanced Multi-modal Mathematical and Synthetic Data

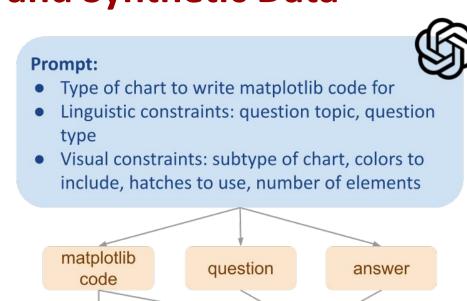


Figure Type	Precision (%)	Recall (%)
Bar Chart	100.0	85.2
Line Plot	95.2	93.1

Table 1: Precision and recall analysis of LLM-as-a-judge on our generated data.

• Generate 1060 filtered samples (860 train, 200 test)

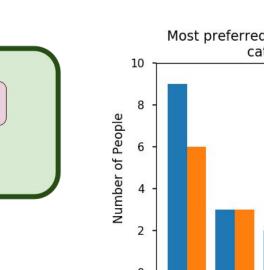
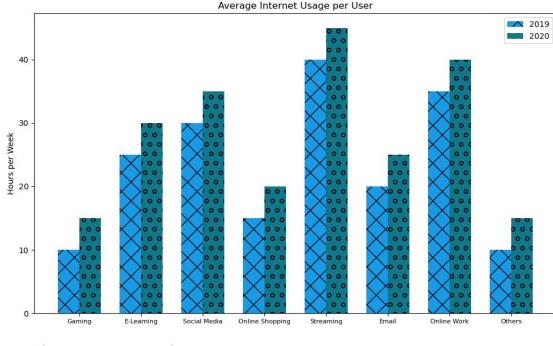


Figure 2: Example Bar Chart from MATHVISTA. Associated question: How many people like the least preferred object in the whole chart?



question, answer

fine-tuning sample generated using

Figure 1: GAMMAS

Figure 3: Example Bar Chart Generated Using GAMMAS. Associated question: According to the bar chart, what was the percentage increase in hours spent by users on Online Shopping from 2019 to 2020?

pity pity spray saint

Fine-tuning

- We use LoRA and DoRA to finetune the language model (LM) component of InternLM-XComposer2-VL-1.8B
- We jointly fully fine-tune the vision encoder (ViT)
- We do not finetune the sampler which connects ViT and LM.
- LoRA
 - Fixes existing weights and learns an additional low-rank update matrix
 - Reduces GPU memory by only propagating gradients through matrices with a rank r << the ranks of the dens weight matrix
- DoRA
 - Adds an extra parameter *m* to tune the magnitude of the weight matrices
 - Increases memory consumption during training, but does not affect inference cost

Experiments & Analysis

- Training for all experiments was done on a single L4 GPU. We tuned the following hyperparameters:
 - r, the rank of the low-rank matrix in LoRA and DoRA
 - Learning rate: values ranging from 2e-4 to 8e-6
 - Adam optimizer, cosine learning rate schedule with weight decay of 0.1
 - Categories of figures that we train on
 - Whether or not we randomize options for MCQs
 - Whether or not we use filtered data from LLM-as-a-judge
 - Whether or not we modify the vision encoder

Model	GVal-B	TestM-B	TestM-L	TestM-O	Model	GVal-L	TestM-B	TestM-L	TestM-O
Baseline	50.0	64.5	58.3	50.7	Baseline	49.4	64.5	58.3	50.7
LoRA (r = 2)	64.1	-	-	-	LoRA (32)	57.1	64.9	62.5	53.8
LoRA (r = 8)	59.4	-	-					0_10	00.0
LoRA (r = 32)	67.2	61.3	58.3	54.4	Table 3:	Only Train	ning on Syn	thetic Line	Charts
Ablate ViT	60.9	61.3	58.3	55.5		,	0 /		

Dascinic	77.7	04.5	30.3	30.7
LoRA (32)	57.1	64.9	62.5	53.8
Table 2	Only Trai	ning on Syn	thatic Lina	Charte

Table2: Only Training on Synthetic Bar Charts

Model	GVal-B/L	TestM-B	TestM-L	TestM-O
Baseline	50.0/49.4	64.5	58.3	50.7
LoRA (32)	68.8/63.6	67.7	70.8	54.2
DoRA (32)	71.9/58.4	71.0	70.8	54.6

Table 4: Training on Both Synthetic Bar and Line Charts

15 -		- synthetic line
5 -		- table
Second t-SNE		- line plot
-10 -	100	- scatter plot
-15 - -20 -	42	- bar chart
	-20 -10 0 10 20 30	geometry diag
	Figure 2: t-SNE	

GAMMAS generates more challenging and diverse data than the current leading benchmark

- Baseline models consistently perform worse on GVal than they do on TestM
- This trend also generally holds for fine-tuned models, despite finetuning having also been done on data generated using GAMMAS

Data diversity improves model performance

Models finetuned using only line- or bar-charts tend to either degrade in performance on TestM, or not improve at the level that models finetuned with both charts do

Impact of Vision vs. Language

Tuning ViT together with LM improves performance on validation sets compared to tuning just LM; performance on TestM datasets is comparable for both. Two reasons could be: 1) overfitting 2) difficulty of GAMMAS

Conclusions & Future Work

- We present GAMMAS: a novel pipeline to generate synthetic multi-modal data for math problem-solving, which we use to finetune a small VLM using PeFT techniques, showing up to 17.2% improvement on math problem solving tasks
- In the future, not only do we wish to expand this work to additional tasks, but also explore techniques like ReFT, and measure the impact of fine-tuning the sampler as well