



# Motion Planning | Potential Field Methods

## *Autonomous Mobile Robots*

**Martin Rufli – IBM Research GmbH**

Margarita Chli, Paul Furgale, Marco Hutter, Davide Scaramuzza, Roland Siegwart

# Potential Field methods | overview

- Methods produce a potential field whose gradient the robot follows
- They are characterized by
  - Being global, but at times remaining prone to local optima
  - Implicit incorporation of (basic) system models

# Local Potential Fields | working principle

- The method generates an attractive potential function centered at the goal and local repulsive potentials around obstacles

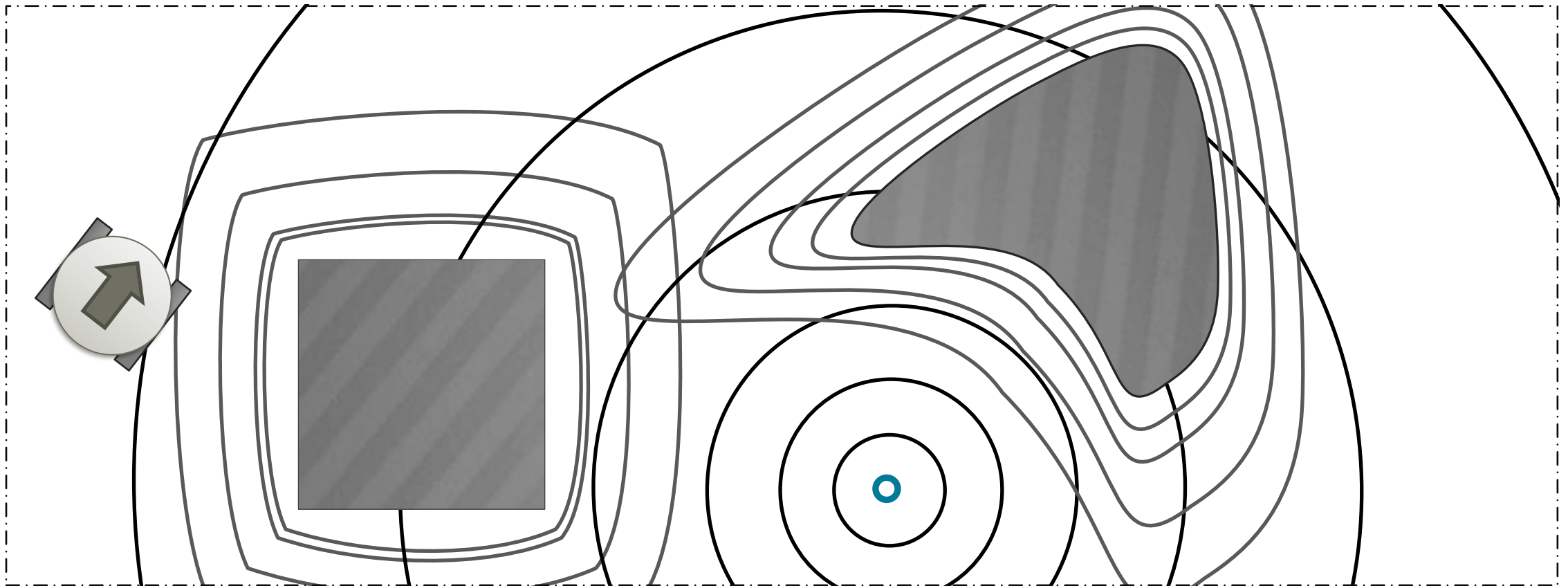
$$U_{\text{att}}(\mathbf{q}) = \frac{1}{2} k_{\text{att}} (\mathbf{q} - \mathbf{q}_{\text{goal}})^2$$

$$U_{\text{rep}}(\mathbf{q}) = \begin{cases} \frac{1}{2} k_{\text{rep}} \left( \frac{1}{\rho(\mathbf{q})} - \frac{1}{\rho_{\text{lim}}} \right)^2 & \text{if } \rho(\mathbf{q}) \leq \rho_{\text{lim}} \\ 0 & \text{otherwise} \end{cases}$$

- The robot follows the gradient (force vector) of the overall summed potential

# Local Potential Fields | working principle

- The method generates an attractive potential function centered at the goal and local repulsive potentials around obstacles



# Local Potential Fields | properties

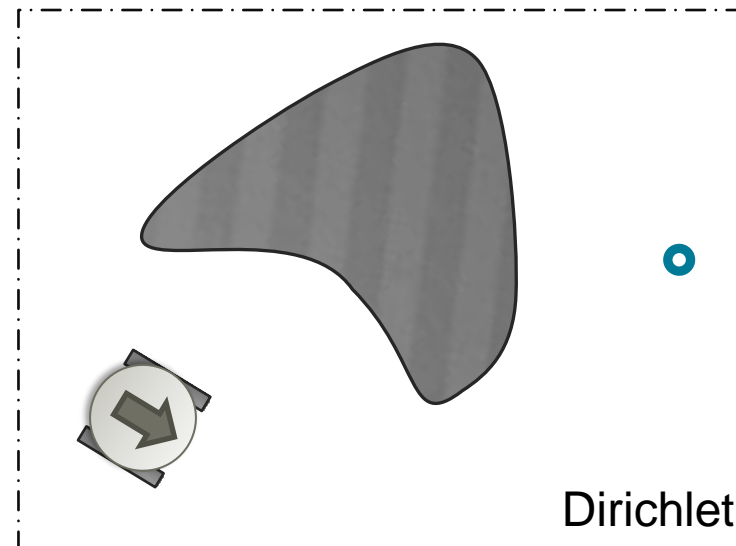
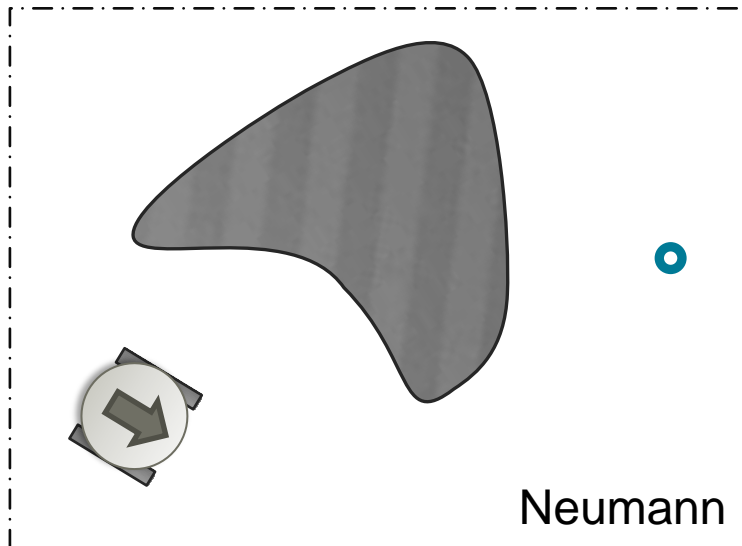
- Solutions form a control policy
- Solutions may be subject to local minima due to the localness of the repulsive potentials
- The formulation does not allow for the incorporation of agent dynamic constraints

# Harmonic Potential Fields | working principle

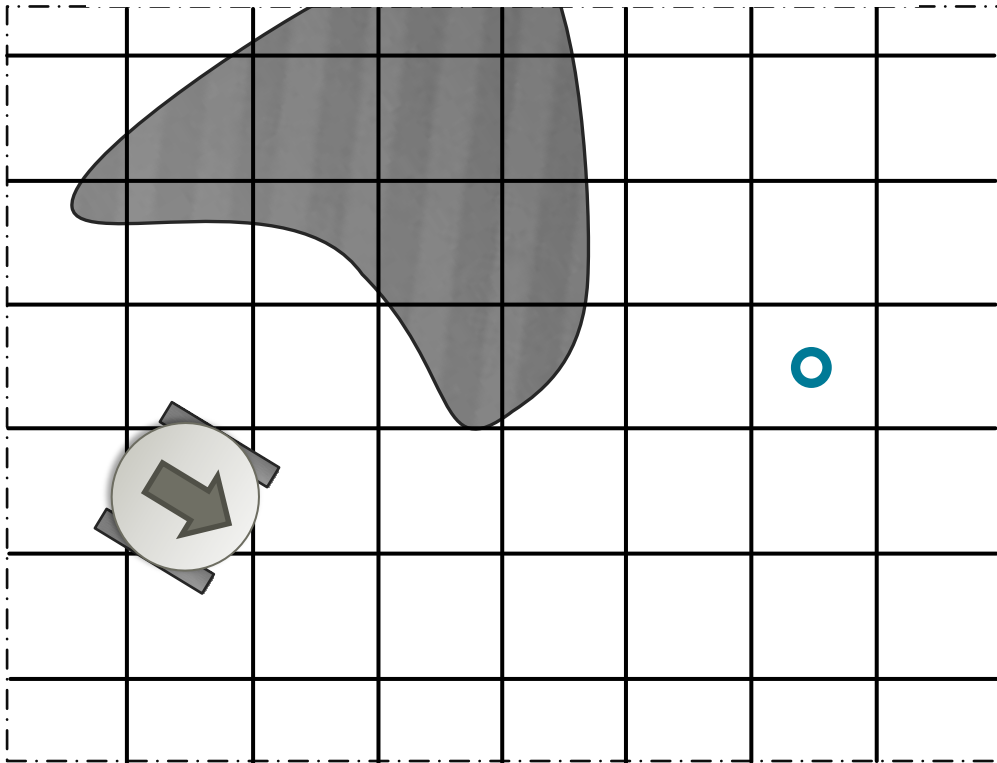
- Robot follows solution to the Laplace Equation  $\Delta U = \sum \frac{\partial^2 U}{\partial^2 q_i} = 0$
- Boundary conditions, any mixture of
  - Neumann: Equipotential lines lie orthogonal to obstacle boundaries
  - Dirichlet: Obstacle boundaries attain constant potential

# Harmonic Potential Fields | working principle

- Robot follows solution to the Laplace Equation  $\Delta U = \sum \frac{\partial^2 U}{\partial^2 q_i} = 0$
- Boundary conditions, any mixture of
  - Neumann: Equipotential lines lie orthogonal to obstacle boundaries
  - Dirichlet: Obstacle boundaries attain constant potential



# Harmonic Potential Fields | numeric solution



$$\Delta U = \sum \frac{\partial^2 U}{\partial^2 q_i} = 0$$

$$\nabla U(\mathbf{q})_i \approx \frac{U(\mathbf{q} + \delta \mathbf{e}_i) - U(\mathbf{q})}{\delta}$$

$$U^{k+1}(\mathbf{q}) = \frac{1}{2n} \sum_{i=1}^n (U^k(\mathbf{q} + \delta \mathbf{e}_i) + U^k(\mathbf{q} - \delta \mathbf{e}_i))$$



# Harmonic Potential Fields | properties

- Solutions form a control policy
- Solutions are free of local optima
- Closed-form solutions exist for simple object shapes only

# Potential Field methods | further reading

- Consideration of orientation constraints
  - R. A. Grupen, C. I. Connolly, K. X. Souccar, and W. P. Burleson: “Toward a Path Co-processor for Automated Vehicle Control”. In *Proceedings of the IEEE Symposium on Intelligent Vehicles*, 1995.
- Approximate integration of agent dynamic constraints
  - A. A. Masoud. Kinodynamic Motion Planning: “A Novel Type of Nonlinear, Passive Damping Forces and Advantages”. *IEEE Robotics & Automation Magazine*, 17(1):85–99, 2010.
  - C. Louste and A. Liegeois. Path planning for Non-holonomic Vehicles: “A Potential Viscous Fluid Method”. *Robotica*, 20:291–298, 2002.